

**A STUDY OF SHOT PEENING EFFECTS ON
FRETTING FATIGUE**

APPENDICES SUBMITTED BY

RACHEL ELIZABETH EDWARDS

IN PARTIAL FULFILMENT OF THE REQUIREMENTS FOR THE
DEGREE OF

DOCTOR OF PHILOSOPHY



THE UNIVERSITY OF SHEFFIELD

DEPARTMENT OF MECHANICAL ENGINEERING

JULY 2008

APPENDIX A

PROGRAMME: FRETTING TESTS

The normal pressure was maintained at a constant value during these tests, whilst the axial load was cyclic with a stress ratio of -1 and a sinusoidal waveform of 20 Hz.

A.1 UNPEENED

Table A.1a: The normal load conditions for the fretting fatigue tests on unpeened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Bridge set (no.)	Normal stress (MPa)	Normal load (kN)	1/2 normal load (kN)	Axial stress (MPa)	Axial load (kN)
106	2	10	0.203	0.102	70	11.2
105	2	20	0.406	0.203	70	11.2
56	3	40	0.813	0.406	70	11.2
59	5	60	1.219	0.610	70	11.2
109	5	80	1.626	0.813	70	11.2
104	5	100	2.032	1.016	70	11.2

Table A.1b: The normal load conditions for the fretting fatigue tests on unpeened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Bridge set (no.)	Normal stress (MPa)	Normal load (kN)	1/2 normal load (kN)	Axial stress (MPa)	Axial load (kN)
8	1	10	0.203	0.102	100	16
2	1	10	0.203	0.102	100	16
11	1	20	0.406	0.203	100	16
103	4	20	0.406	0.203	100	16
16	1	40	0.813	0.406	100	16
9	1	40	0.813	0.406	100	16
10	1	60	1.219	0.610	100	16
6	1	60	1.219	0.610	100	16
18	1	80	1.626	0.813	100	16
5	1	80	1.626	0.813	100	16
19	1	100	2.032	1.016	100	16
20	1	100	2.032	1.016	100	16

Table A.1c: The normal load conditions for the fretting fatigue tests on unpeened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 125 MPa.

Specimen (no.)	Bridge set (no.)	Normal stress (MPa)	Normal load (kN)	1/2 normal load (kN)	Axial stress (MPa)	Axial load (kN)
39	2	10	0.203	0.102	125	20
40	1	20	0.406	0.203	125	20
38	1	40	0.813	0.406	125	20
37	1	60	1.219	0.610	125	20
100	5	80	1.626	0.813	125	20
102	3	80	1.626	0.813	125	20
101	2	100	2.032	1.016	125	20
108	3	100	2.032	1.016	125	20

A.2 PEENED

Table A.2a: The normal load conditions for the fretting fatigue tests on peened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Bridge set (no.)	Normal stress (MPa)	Normal load (kN)	1/2 normal load (kN)	Axial stress (MPa)	Axial load (kN)
9P	8	10	0.203	0.102	70	11.2
2P	8	60	1.219	0.610	70	11.2
5P	7	100	2.032	1.016	70	11.2

Table A.2b: The normal load conditions for the fretting fatigue tests on peened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Bridge set (no.)	Normal stress (MPa)	Normal load (kN)	1/2 normal load (kN)	Axial stress (MPa)	Axial load (kN)
6P	7	10	0.203	0.102	100	16
8P	8	60	1.219	0.610	100	16
4P	8	100	2.032	1.016	100	16

Table A.2c: The normal load conditions for the fretting fatigue tests on peened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 125 MPa.

Specimen (no.)	Bridge set (no.)	Normal stress (MPa)	Normal load (kN)	1/2 normal load (kN)	Axial stress (MPa)	Axial load (kN)
3P	7	10	0.203	0.102	125	20
10P	7	40	0.813	0.406	125	20
1P	7	100	2.032	1.016	125	20

APPENDIX B

PROGRAM: CYCLIC DATA ANALYSIS

This Visual Basic program post processes data collected by the Rubicon data logging system to evaluate the maximum, minimum and average values for each fatigue cycle.

B.1 INSTRUCTIONS

Click 'Open File' and select all files.

Navigate to and open the required ASC file.

Choose 'Delimited' and select both the 'Tab' and 'Space' options.

Click 'Finish'.

There should be no empty columns.

Click 'Save As' and save the file.

Click the 'Process Calculations' button on the toolbar (calculator image).

Follow the instructions onscreen to complete the process.

B.2 FORMS

Time Interval ✕

Enter the time interval between data sets
(hint: enter a value less than the actual value)

250

Calculate Values ✕

Enable all choices

Time is in column: First Row of Data:

Cycles are in column: Row containing headings:

Enter the column number to calculate values from: Enter the number of columns you wish to process:

Multiple Columns

Enter Column Numbers ✕

Enter column number: 1

3

B.3 VISUAL BASIC CODE

Option Explicit

```
Dim gDataSets() As Integer
Dim gAverages() As Double
Dim gMaximums() As Double
Dim gMinimums() As Double
```

```
Dim gFinalDataRow, gTimeColumn, gCycleColumn, gTimeInterval,
    gNumberOfDataSets, gFirstDataRow As Integer
```

```
Global gColumnNumberList() As Integer
Global gFormTimeIntervalFlag, gFormCalculateFlag, gMultiColumnFlag,
    gFormGetColumnsFlag As Boolean
Global gColumnNumber, gHeadingRow, gColumnLoopNumber As Integer
```

Public Sub FindFinalDataPoint()

```
Dim DataRow As Integer
Dim LastDataFound As Boolean
```

```
DataRow = gFirstDataRow - 1
LastDataFound = False
```

```
If Cells(gFirstDataRow, gTimeColumn) = "" Then
    MsgBox ("No data found in first row")
End
End If
```

```
Do
```

```
    DataRow = DataRow + 1
```

```
    If Cells(DataRow + 1, gTimeColumn) - Cells(DataRow, gTimeColumn) >
gTimeInterval Then
```

```
        If Cells(DataRow + 1, gCycleColumn) = Cells(DataRow, gCycleColumn) Then
```

```
            gFinalDataRow = DataRow
```

```
            LastDataFound = True
```

```
        End If
```

```
        ElseIf Cells(DataRow + 1, gTimeColumn) = "" Then
```

```
            gFinalDataRow = DataRow
```

```
            LastDataFound = True
```

```
        End If
```

```
    Loop While LastDataFound = False
```

```
End Sub
```

Public Sub AverageCalculations()

```
ReDim gAverages(gNumberOfDataSets) As Double
Dim DataRow, DataRowStart, DataRowEnd, DataSet As Integer
Dim Sum As Double

For DataSet = 1 To gNumberOfDataSets
    DataRowStart = gDataSets((DataSet * 2) - 1)
    DataRowEnd = gDataSets(DataSet * 2)
    Sum = 0
    For DataRow = DataRowStart To DataRowEnd
        Sum = Sum + Cells(DataRow, gColumnNumber)
    Next
    gAverages(DataSet) = Sum / (DataRowEnd - DataRowStart + 1)
Next

End Sub
```

Public Sub FindDataSets()

```
ReDim gDataSets(1 To 2) As Integer
Dim DataRow, DataRowStart As Integer

DataRow = gFirstDataRow - 1
DataRowStart = DataRow + 1
gNumberOfDataSets = 1

Do
    DataRow = DataRow + 1
    If Cells(DataRow + 1, gTimeColumn) - Cells(DataRow, gTimeColumn) >
gTimeInterval Then
        gDataSets((gNumberOfDataSets * 2) - 1) = DataRowStart
        gDataSets(gNumberOfDataSets * 2) = DataRow
        If DataRow <> gFinalDataRow Then
            gNumberOfDataSets = gNumberOfDataSets + 1
            ReDim Preserve gDataSets(1 To (gNumberOfDataSets * 2)) As Integer
            DataRowStart = DataRow + 1
        End If
        ElseIf Cells(DataRow + 1, gTimeColumn) = "" Then
            gDataSets((gNumberOfDataSets * 2) - 1) = DataRowStart
            gDataSets(gNumberOfDataSets * 2) = DataRow
        End If
    Loop While DataRow <> gFinalDataRow

    If Cells(gDataSets((gNumberOfDataSets * 2) - 1), gCycleColumn) =
Cells(gDataSets(gNumberOfDataSets * 2), gCycleColumn) Then
        gNumberOfDataSets = gNumberOfDataSets - 1
    End If

    If gNumberOfDataSets = 0 Then
        MsgBox ("No valid data sets exist")
    End
End If

End Sub
```


Public Sub MaximumCalculations()

```
ReDim gMaximums(gNumberOfDataSets) As Double
Dim DataRow, DataRowStart, DataRowEnd, DataSet As Integer
Dim MaximumValue As Double
```

```
For DataSet = 1 To gNumberOfDataSets
    DataRowStart = gDataSets((DataSet * 2) - 1)
    DataRowEnd = gDataSets(DataSet * 2)
    MaximumValue = Cells(DataRowStart, gColumnNumber)
    For DataRow = DataRowStart To DataRowEnd
        If Cells(DataRow, gColumnNumber) > MaximumValue Then
            MaximumValue = Cells(DataRow, gColumnNumber)
        End If
    Next
    gMaximums(DataSet) = MaximumValue
Next
```

End Sub

Public Sub MinimumCalculations()

```
ReDim gMinimums(gNumberOfDataSets) As Double
Dim DataRow, DataRowStart, DataRowEnd, DataSet As Integer
Dim MinimumValue As Double
```

```
For DataSet = 1 To gNumberOfDataSets
    DataRowStart = gDataSets((DataSet * 2) - 1)
    DataRowEnd = gDataSets(DataSet * 2)
    MinimumValue = Cells(DataRowStart, gColumnNumber)
    For DataRow = DataRowStart To DataRowEnd
        If Cells(DataRow, gColumnNumber) < MinimumValue Then
            MinimumValue = Cells(DataRow, gColumnNumber)
        End If
    Next
    gMinimums(DataSet) = MinimumValue
Next
```

End Sub

Public Sub ProcessCalculations()

```
If ActiveWorkbook.Name = "MaxMinAvg.xls" Then
    MsgBox ("Sorry, Calculations not valid on this workbook.")
    Exit Sub
End If
If ActiveSheet.Name = "Calculations Sheet" Then
    MsgBox ("Sorry, calculations not valid on this sheet. Select correct sheet and try
again.")
    Sheets(2).Select
    Exit Sub
End If
frmTimeInterval.Show
If gFormTimeIntervalFlag = True Then
    MsgBox ("Operation Cancelled")
    End
End If
frmCalculate.Show
If gFormCalculateFlag = True Then
    MsgBox ("Operation Cancelled")
    End
End If
gTimeColumn = Int(frmCalculate.txtTimeColumn.Text)
gCycleColumn = Int(frmCalculate.txtCycleColumn.Text)
gTimeInterval = Int(frmTimeInterval.txtTimeInterval.Text)
gFirstDataRow = Int(frmCalculate.txtFirstDataRow.Text)
gHeadingRow = Int(frmCalculate.txtHeadingRow.Text)
If gMultiColumnFlag = True Then
    ReDim gColumnNumberList(Int(frmCalculate.txtNumberOfColumns.Text))
    For gColumnLoopNumber = 1 To Int(frmCalculate.txtNumberOfColumns.Text)
        frmGetColumns.Show
        If gFormGetColumnsFlag = True Then
            MsgBox ("Operation Cancelled")
            End
        End If
    Next
    For gColumnLoopNumber = 1 To Int(frmCalculate.txtNumberOfColumns.Text)
        gColumnNumber = gColumnNumberList(gColumnLoopNumber)
        frmPleaseWait.Show
    Next
End If
If gMultiColumnFlag = False Then
    gColumnLoopNumber = 1
    gColumnNumber = Int(frmCalculate.txtColumnNumber.Text)
    frmPleaseWait.Show
End If
End Sub
```

Public Sub WriteData()

```
Dim DataSet, CalculationCount, FirstColumn As Integer  
Dim NewSheetFlag As Boolean
```

```
NewSheetFlag = False
```

```
If Worksheets.count = 1 Then  
    Sheets.Add  
    ActiveSheet.Name = "Calculations Sheet"  
    Columns(1).Hidden = True  
    NewSheetFlag = True  
    Cells(1, 1) = 0
```

```
End If
```

```
If NewSheetFlag = False Then  
    Sheets("Calculations Sheet").Select  
End If
```

```
CalculationCount = Cells(1, 1)  
FirstColumn = (CalculationCount * 9) + 2
```

```
Range(Cells(1, FirstColumn), Cells(1, FirstColumn + 7)).Select  
With Selection
```

```
    .HorizontalAlignment = xlCenter  
    .VerticalAlignment = xlBottom  
    .WrapText = False  
    .Orientation = 0  
    .AddIndent = False  
    .ShrinkToFit = False  
    .MergeCells = False
```

```
End With
```

```
Selection.Merge
```

```
Cells(1, FirstColumn) = "Calculations for column number" + Str(gColumnNumber) +  
". Title: " + Worksheets(2).Cells(gHeadingRow, gColumnNumber)
```

```
Range(Cells(3, FirstColumn), Cells(4, FirstColumn + 7)).Select  
Selection.HorizontalAlignment = xlCenter
```

```
Cells(3, FirstColumn) = "Data"
```

```
Cells(4, FirstColumn) = "Set"
```

```
Cells(3, FirstColumn + 1) = "Time"
```

```
Cells(4, FirstColumn + 1) = "Start"
```

```
Cells(3, FirstColumn + 2) = "Time"
```

```
Cells(4, FirstColumn + 2) = "End"
```

```
Cells(3, FirstColumn + 3) = "Cycle"
```

```
Cells(4, FirstColumn + 3) = "Start"
```

```
Cells(3, FirstColumn + 4) = "Cycle"
```

```
Cells(4, FirstColumn + 4) = "End"
```

```
Cells(3, FirstColumn + 5) = "Average"
```

```
Cells(4, FirstColumn + 5) = "Value"
```

```
Cells(3, FirstColumn + 6) = "Maximum"
```

```
Cells(4, FirstColumn + 6) = "Value"
```

```
Cells(3, FirstColumn + 7) = "Minimum"
```

```
Cells(4, FirstColumn + 7) = "Value"
```

```

For DataSet = 1 To gNumberOfDataSets
    Cells(DataSet + 4, FirstColumn) = DataSet
    Cells(DataSet + 4, FirstColumn + 1) = Worksheets(2).Cells(gDataSets((DataSet *
2) - 1), gTimeColumn)
    Cells(DataSet + 4, FirstColumn + 2) = Worksheets(2).Cells(gDataSets((DataSet *
2)), gTimeColumn)
    Cells(DataSet + 4, FirstColumn + 3) = Worksheets(2).Cells(gDataSets((DataSet *
2) - 1), gCycleColumn)
    Cells(DataSet + 4, FirstColumn + 4) = Worksheets(2).Cells(gDataSets((DataSet *
2)), gCycleColumn)
    Cells(DataSet + 4, FirstColumn + 5) = gAverages(DataSet)
    Cells(DataSet + 4, FirstColumn + 6) = gMaximums(DataSet)
    Cells(DataSet + 4, FirstColumn + 7) = gMinimums(DataSet)
Next
Cells(2, FirstColumn).Select
Cells(1, 1) = CalculationCount + 1

End Sub

```

APPENDIX C

PROGRAMME: EVOLUTION OF FRETTING SCARS

Interrupted fretting fatigue tests were conducted at three normal pressures, 10 MPa, 40 MPa or 60 MPa, and 100 MPa, these being the minimum previously applied, the maximum previously applied and that which yielded the shortest life for each axial stress in the fretting fatigue test programme. Fretting scars at a tenth, quarter, half and three quarters of the total fretting fatigue lives found previously were produced.

C.1 UNPEENED

Table C.1a: The normal load conditions and cycles administered for the scar development tests on unpeened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Bridges		Normal stress (MPa)	1/2 normal load (kN)	Axial stress (MPa)	Life expectancy (no.)	Life proportion (no.)	Cycles administered (no.)	Timing expected (hr)
	Top (no.)	Bottom (no.)							
43	R1	R2	10	0.102	70	3,733,888	1/10	373,389	5.19
49	J3	J4	10	0.102	70	3,733,888	1/4	933,472	12.96
51	R3	R4	10	0.102	70	3,733,888	1/2	1,866,944	25.93
66	G1	G2	10	0.102	70	3,733,888	3/4	2,800,416	38.89
69	H1	H2	60	0.610	70	886,320	1/10	88,632	1.23
68	O1	O2	60	0.610	70	886,320	1/4	221,580	3.08
53	K1	K2	60	0.610	70	886,320	1/2	443,160	6.16
63	P1	P2	60	0.610	70	886,320	3/4	664,740	9.23
64	L3	L4	100	1.016	70	1,741,888	1/10	174,189	2.42
61	L1	L2	100	1.016	70	1,741,888	1/4	435,472	6.05
70	I1	I2	100	1.016	70	1,741,888	1/2	870,944	12.10
50	N3	N4	100	1.016	70	1,741,888	3/4	1,306,416	18.14

Table C.1b: The normal load conditions and cycles administered for the scar development tests on unpeened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Bridges		Normal stress (MPa)	1/2 normal load (kN)	Axial stress (MPa)	Life expectancy (no.)	Life proportion (no.)	Cycles administered (no.)	Timing expected (hr)
	Top (no.)	Bottom (no.)							
26	D2	D1	10	0.102	100	298,836	1/10	29,884	0.83
23	E2	E1	10	0.102	100	298,836	1/4	74,709	2.08
24	A4	A3	10	0.102	100	298,836	1/2	149,418	4.15
25	C4	C3	10	0.102	100	298,836	3/4	224,127	6.23
31	A2	A1	40	0.406	100	193,561	1/10	19,356	0.27
28	B4	B3	40	0.406	100	193,561	1/4	48,390	0.67
29	C2	C1	40	0.406	100	193,561	1/2	96,781	2.69
30	B2	B1	40	0.406	100	193,561	3/4	145,171	4.03
32	D4	D3	100	1.016	100	479,201	1/10	47,920	1.33
33	F2	F1	100	1.016	100	479,201	1/4	119,800	3.33
34	F4	F3	100	1.016	100	479,201	1/2	239,601	6.66
35	E4	E3	100	1.016	100	479,201	3/4	359,401	9.98

Table C.1c: The normal load conditions and cycles administered for the scar development tests on unpeened aluminium alloy 2024 T351 in contact with aluminium alloy 2024 T351 and subjected to an axial stress amplitude of 125 MPa.

Specimen (no.)	Bridges		Normal stress (MPa)	1/2 normal load (kN)	Axial stress (MPa)	Life expectancy (no.)	Life proportion (no.)	Cycles administered (no.)	Timing expected (hr)
	Top (no.)	Bottom (no.)							
42	K3	K4	10	0.102	125	546,587	1/10	54,659	0.76
45	I3	I4	10	0.102	125	546,587	1/4	136,647	1.90
46	M1	M2	10	0.102	125	546,587	1/2	273,294	3.80
48	J1	J2	10	0.102	125	546,587	3/4	409,940	5.69
67	Q3	Q4	60	0.610	125	83,704	1/10	8,370	0.12
52	P3	P4	60	0.610	125	83,704	1/4	20,926	0.29
47	O3	O4	60	0.610	125	83,704	1/2	41,852	0.58
60	N1	N2	60	0.610	125	83,704	3/4	62,778	0.87
65	G3	G4	100	1.016	125	145,848	1/10	14,585	0.20
44	H3	H4	100	1.016	125	145,848	1/4	36,462	0.51
62	Q1	Q2	100	1.016	125	145,848	1/2	72,924	1.01
71	M3	M4	100	1.016	125	145,848	3/4	109,386	1.52

C.2 PEENED

Table C.2a: The normal load conditions and cycles administered for the scar development tests on peened aluminium alloy 2024 T351 in contact with aluminium alloy 2024-T351 and subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Bridges		Normal stress (MPa)	1/2 normal load (kN)	Axial stress (MPa)	Life expectancy (no.)	Life proportion (no.)	Cycles administered (no.)	Timing expected (hr)
	Top (no.)	Bottom (no.)							
15P	T3	T4	10	0.102	70	6,131,072	1/10	613,107	8.52
27P	Z3	Z4	10	0.102	70	6,131,072	1/4	1,532,768	21.29
16P	X1	X2	10	0.102	70	4,579,328	1/2	2,289,664	31.80
20P	W1	W2	10	0.102	70	6,131,072	3/4	4,598,304	63.87
32P	AC1	AC2	60	0.610	70	4,579,328	1/10	457,933	6.36
18P	V1	V2	60	0.610	70	4,579,328	1/4	1,144,832	15.90
14P	T1	T2	60	0.610	70	6,131,072	1/2	3,065,536	42.58
17P	Y1	Y2	60	0.610	70	4,579,328	3/4	3,434,496	47.70
43P	AH3	AH4	100	1.016	70	5,000,000	1/10	500,000	6.94
19P	V3	V4	100	1.016	70	5,000,000	1/4	1,250,000	17.36
26P	Z1	Z2	100	1.016	70	5,000,000	1/2	2,500,000	34.72
28P	AA1	AA2	100	1.016	70	5,000,000	3/4	3,750,000	52.08

Table C.2b: The normal load conditions and cycles administered for the scar development tests on peened aluminium alloy 2024 T351 in contact with aluminium alloy 2024-T351 and subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Bridges		Normal stress (MPa)	1/2 normal load (kN)	Axial stress (MPa)	Life expectancy (no.)	Life proportion (no.)	Cycles administered (no.)	Timing expected (hr)
	Top (no.)	Bottom (no.)							
45P	AI3	AI4	10	0.102	100	5,000,000	1/10	500,000	6.94
22P	X1	X2	10	0.102	100	5,000,000	1/4	1,250,000	17.36
12P	S1	S2	10	0.102	100	5,000,000	1/2	2,500,000	34.72
17P	U3	U4	40	0.406	100	1,976,448	1/10	197,645	2.75
49P	AJ1	AJ2	40	0.406	100	1,976,448	1/4	494,112	6.86
34P	AD1	AD2	40	0.406	100	1,976,448	2/4	988,224	13.73
29P	AA3	AA4	40	0.406	100	1,976,448	3/4	1,482,336	20.59
16P	U1	U2	100	1.016	100	1,330,816	1/10	133,082	1.85
30P	AB1	AB2	100	1.016	100	1,330,816	1/4	332,704	4.62
39P	AF3	AF4	100	1.016	100	1,330,816	2/4	665,408	9.24
24P	Y1	Y2	100	1.016	100	1,330,816	3/4	998,112	13.86

Table C.2c: The normal load conditions and cycles administered for the scar development tests on peened aluminium alloy 2024 T351 in contact with aluminium alloy 2024-T351 and subjected to an axial stress amplitude of 125 MPa.

Specimen (no.)	Bridges		Normal stress (MPa)	1/2 normal load (kN)	Axial stress (MPa)	Life expectancy (no.)	Life proportion (no.)	Cycles administered (no.)	Timing expected (hr)
	Top (no.)	Bottom (no.)							
38P	AF1	AF2	10	0.102	125	1,786,240	1/10	178,624	2.48
44P	AI1	AI2	10	0.102	125	1,786,240	1/4	446,560	6.20
13P	S3	S4	10	0.102	125	1,786,240	2/4	893,120	12.40
13P	S3	S4	10	0.102	125	1,786,240	3/4	1,339,680	18.61
33P	AC3	AC4	60	0.610	125	1,129,792	1/10	112,979	1.57
42P	AH1	AH2	60	0.610	125	1,129,792	1/4	282,448	3.92
23P	X3	X4	60	0.610	125	1,129,792	2/4	564,896	7.85
40P	AG1	AG2	60	0.610	125	1,129,792	3/4	847,344	11.77
36P	AE1	AE2	100	1.016	125	434,432	1/10	43,443	0.60
37P	AE3	AE4	100	1.016	125	434,432	1/4	108,608	1.51
21P	W3	W4	100	1.016	125	434,432	2/4	217,216	3.02
25P	Y3	Y4	100	1.016	125	434,432	3/4	325,824	4.53

APPENDIX D

PROGRAM: SCAR DATA ANALYSIS

This Visual Basic program, written by Miss S. Scorey, post processes data collected by the UBM data logging system. First, the profiles are levelled about a centre line, then these are smoothed. The maximum notch depth found, the length of that notch and the height of the highest peaks either side of that notch are evaluated. These values are collated together with plots of the profiles and close ups of the areas of interest. The means and medians for every combination of load and proportion of life are saved to a separate file.

D.1 VISUAL BASIC CODE

Option Explicit

'This module contains the code that manipulates each PR file found in a given location.

Sub ConvertPRFiles()

'Opens up each PR file found in a given location.

'Deletes rows 1 and 2 if data starts on row 3 and saves as an excel file.

```
Dim MyPath As String
Dim MyName As String
Dim i As Integer
Dim IsPeened As Boolean
Dim PeenedStr As String
Dim MyMPa As String
```

```
IsPeened = False
MyMPa = "\70 MPa"
```

```
PeenedStr = "Unpeened"
If IsPeened = True Then PeenedStr = "Peened"
```

```
Application.DisplayAlerts = False
```

'MyPath will need to be modified if the locations of the files changes.

'Set MyPath to be the top folder (should contain the folders Unpeened and Peened and the file Template.xls).

```
MyPath = "C:\Documents and Settings\Rachel Edwards\My Documents\My  
PhD\Unpeened\Levelled" & PeenedStr & MyMPa
```

```
With Application.FileSearch
```

```
  .NewSearch
```

```
  .LookIn = MyPath & "\PR files"
```

```
  .SearchSubFolders = False
```

```
  .FileType = msoFileTypeAllFiles
```

```
  .Execute
```

```
  For i = 1 To .FoundFiles.Count
```

```
    Application.Workbooks.Open (.FoundFiles(i))
```

```
    MyName = Mid(ActiveWorkbook.Name, 1, 6) & ".xls"
```

```
    If IsPeened = True Then MyName = Mid(ActiveWorkbook.Name, 1, 7) & ".xls"
```

```
    If Mid(Cells(1, 1).Value, 1, 1) = "P" Then
```

```
      Rows(1).Delete
```

```
      Rows(1).Delete
```

```
    End If
```

```
    ActiveWorkbook.SaveAs (MyPath & "\XLS files\" & MyName)
```

```
    ActiveWorkbook.Close
```

```
  Next
```

```
End With
```

```
Application.DisplayAlerts = True
```

```
End Sub
```

Option Explicit

'This module contains the code that levels the data.

Sub LevelData()

```
Dim i As Integer
Dim j As Integer
Dim k As Integer
Dim xArr(2801) As Integer
Dim yArr(2801) As Single
Dim MyPath As String
Dim MyPath1 As String
Dim MyPath2 As String
Dim SavePath As String
Dim MyName1 As String
Dim MyName2 As String
Dim MyMPa As String
Dim MyS As Single
Dim MyI As Single
Dim WkBkA As Workbook
Dim WkBkB As Workbook
Dim AvgDf As Single
Dim MaxDf As Single
```

```
MyMPa = "70 MPa"
```

'MyPath will need to be modified if the location of the files changes.

'Set MyPath to be the top folder (should contain the folders Unpeened and Peened and the file Template.xls).

```
MyPath = "C:\Documents and Settings\Rachel Edwards\My Documents\My PhD\Surface  
Roughness"
```

```
MyPath1 = MyPath & "\Raw data\Unpeened\" & MyMPa
```

```
MyPath2 = MyPath & "\Levelled data\Unpeened\" & MyMPa & "\XLS files"
```

```
SavePath = MyPath1 & "\Levelled\"
```

```
ThisWorkbook.Sheets("Diffs").Cells(1, 1).Value = "File"
```

```
ThisWorkbook.Sheets("Diffs").Cells(1, 2).Value = "AvgAbsDf"
```

```
ThisWorkbook.Sheets("Diffs").Cells(1, 3).Value = "MaxAbsDf"
```

```
Application.DisplayAlerts = False
```

```
With Application.FileSearch
```

'Find all the files in the folder MyPath1.

```
.NewSearch  
.LookIn = MyPath1  
.SearchSubFolders = False  
.Execute
```

'For each of the files found.

```
For j = 1 To .FoundFiles.Count
```

'Open the workbook.

```
Application.Workbooks.Open (.FoundFiles(j))
```

'Create the levelled data file name.

```
MyName1 = Mid(ActiveWorkbook.Name, 1, 5) & "LS" & ".xls"  
MyName2 = Mid(ActiveWorkbook.Name, 1, 5) & "L" & ".xls"  
ActiveWorkbook.SaveAs (SavePath & MyName1)
```

'Put each data point and its corresponding row in the worksheet, into arrays. yArr and xArr, respectively.

```
For i = 1 To 2801  
    xArr(i) = i  
    yArr(i) = Cells(i, 1)  
Next
```

'Use the LinEst function to find the slope and the intercept of the data as a function of the row that its in (i.e. the 'error' as a function of its position in the data).

```
MyS = Excel.WorksheetFunction.Index(Excel.WorksheetFunction.LinEst(yArr, xArr),  
1)  
Myl = Excel.WorksheetFunction.Index(Excel.WorksheetFunction.LinEst(yArr, xArr),  
2)
```

'Remove the error component from the data by subtracting $y = mx + c$ from each value (where m is the slope MyS, c is the intercept Myl and x is the row).

```
For i = 1 To 2801  
    Cells(i, 2).Value = Cells(i, 1).Value - (MyS * i + Myl)  
Next
```

'Standardise the data by shifting all values up or down by the average amount the values differ from zero.

```
For i = 1 To 2801  
    Cells(i, 3).Value = Cells(i, 2).Value -  
Excel.WorksheetFunction.Average(Range(Cells(1, 2), Cells(2801, 2)))  
Next
```

'Remove the original data and the non-standardised data.

```
Columns(1).Select  
Selection.Delete  
Columns(1).Select  
Selection.Delete
```

'Format the data to three decimal places (and set precision to match).

```
Selection.NumberFormat = "0.000"  
ActiveWorkbook.PrecisionAsDisplayed = True
```

'Save and close the levelled data.

```
ActiveWorkbook.Save  
ThisWorkbook.Sheets("Diffs").Cells(j + 1, 1).Value = MyName1  
If Dir(MyPath2 & "\" & MyName2) <> "" Then  
    Set WkBkA = ActiveWorkbook  
    Application.Workbooks.Open (MyPath2 & "\" & MyName2)  
    Set WkBkB = ActiveWorkbook  
    Range(Cells(1, 1), Cells(2801, 1)).Select  
    If Mid(Cells(1, 1), 1, 1) = "P" Then Range(Cells(3, 1), Cells(2803, 1)).Select  
    Selection.Copy  
    WkBkA.Activate  
    Cells(1, 2).Select  
    ActiveSheet.Paste  
    For k = 1 To 2801  
        Cells(k, 3).Value = Abs(Cells(k, 2).Value - Cells(k, 1).Value)  
    Next  
    AvgDf = Excel.WorksheetFunction.Average(Range(Cells(1, 3), Cells(2801, 3)))  
    MaxDf = Excel.WorksheetFunction.Max(Range(Cells(1, 3), Cells(2801, 3)))  
    ThisWorkbook.Sheets("Diffs").Cells(j + 1, 2).Value = AvgDf  
    ThisWorkbook.Sheets("Diffs").Cells(j + 1, 3).Value = MaxDf  
    WkBkB.Close  
End If  
ActiveWorkbook.Close  
Next  
End With  
Application.DisplayAlerts = True  
  
End Sub
```

Option Explicit

'This module contains the code that performs the analysis of the data.

Sub Analysis()

Private IsPeened As String

Dim GetSD As Variant
Dim MySD As String
Dim MyPath As String
Dim NewPath As String
Dim ResPath As String
Dim MyFileName As String
Dim i As Integer
Dim j As Integer
Dim k As Integer
Dim kArray(2801) As Single
Dim WA As Workbook
Dim WB As Workbook
Dim TempFile As String
Dim Pressure As Integer

'Set IsPeened to either 'Unpeened' or 'Peened' to run the analysis for the unpeened or peened data.

IsPeened = "Unpeened"

'MyPath will need to be modified if the location of the files changes.

'Set MyPath to be the top folder (should contain the folders Unpeened and Peened and the file Template.xls).

MyPath = "C:\Documents and Settings\Rachel Edwards\My Documents\My PhD\Surface Roughness\"

'Find the template file.

TempFile = MyPath & "Template.xls"

'Turn off alerts.

Application.DisplayAlerts = False

'Find out what value of SD to use.

GetSD = InputBox("Please enter the smoothing constant (SD):" & vbCrLf & "NB: this must be an integer in the range 0-100.", "Smoothing constant", "20")

'If the input box is left blank, then end.

If GetSD = "" Then Exit Sub

'Convert the text in the input box to an integer number.

MySD = Int(GetSD)

For i = 1 To 3

'For each Pressure value.

 Select Case i

 Case 1

 Pressure = 70

 Case 2

 Pressure = 100

 Case 3

 Pressure = 125

 End Select

'Set NewPath to look in the correct folder (i.e. Unpeened or Peened, then the Pressure for this loop).

 NewPath = MyPath & IsPeened & "\" & Pressure & " MPa"

'Set ResPath to the file path where results files are to be saved.

 ResPath = NewPath & "\Results~" & MySD & "\"

'If the folder named ResPath doesn't exist, create it.

 If Len(Dir(ResPath, vbDirectory)) = 0 Then MkDir (ResPath)

 With Application.FileSearch

'Find all the files in the folder 'XLS files' in NewPath.

 .NewSearch

 .LookIn = NewPath & "XLS files"

 .SearchSubFolders = False

 .Execute

'For each of the files found.

 For j = 1 To .FoundFiles.Count

'Open the workbook.

 Application.Workbooks.Open (.FoundFiles(j))

'Give the currently open workbook a 'codename' WA, so it can be referenced easily in the code.

```
Set WA = ActiveWorkbook
```

'Create the results file name, based on the letter 'R', plus the original file name, plus the current value of pressure.

```
MyFileName = "R" & Mid(WA.Name, 1, 7) & MySD & ".xls"
```

```
If IsPeened = "Unpeened" Then MyFileName = "R" & Mid(WA.Name, 1, 6) &  
MySD & ".xls"
```

'Open the template file (identified earlier as TempFile).

```
Application.Workbooks.Open (TempFile)
```

'Give the template file a 'codename' WB, so it can be referenced easily in the code.

```
Set WB = ActiveWorkbook
```

'Save the template using the file name created earlier.

```
WB.SaveAs (ResPath & MyFileName)
```

'Enter the value of SD into the results file.

```
Sheets("data").Select  
Cells(1, 5).Value = MySD
```

'Copy the data from the original file.

```
WA.Activate  
Range(Cells(1, 1), Cells(2801, 1)).Select  
Selection.Copy
```

'Paste into the results file.

```
WB.Activate  
Cells(243, 2).Select  
ActiveSheet.Paste
```

'If the file is measured from the right hand side of the block, invert the results.

```
If Mid(WA.Name, Len(WA.Name) - 6, 1) = "R" Then  
  For k = 0 To 2800  
    kArray(k) = Cells(k + 243, 2).Value  
  Next  
  For k = 0 To 2800  
    Cells(k + 243, 2).Value = kArray(2800 - k)  
  Next  
End If
```

'Close the original data file.

```
WA.Close
```


'Find the depth, width, minimum, maximum, etc.

Call FindValues

'Transfer the values from the results file to this file.

Call TransferValues(Pressure)

'Close the results file.

WB.Close

'Save this workbook.

ThisWorkbook.Save

Next
End With

Next

End Sub

Sub FindValues()

```
Dim i As Integer  
Dim j As Integer  
Dim k As Integer  
Dim xMin As Single  
Dim xMax As Single  
Dim jMin As Integer  
Dim jMax As Integer  
Dim max As Single
```

'Find the scar depth, and the row containing the deepest part of the scar.

```
j = 243
```

'Set max to equal the deepest part of the scar.

```
max = Cells(243, 3).Value  
For i = 244 To 3043
```

'If the value of cell(i,3) is less than max, set max equal to the value of cell(i,3).

```
    If max > Cells(i, 3).Value Then  
        max = Cells(i, 3).Value  
        j = i  
    End If  
Next
```

'j is the row number of the cell containing the deepest point of the scar and remains so for the rest of the subroutine.

'Set jMin to 636 rows (~1.27 mm) before the centre of the scar.

```
jMin = j - 636
```

'If jMin is less than the number of the first row of data, set jMin equal to the number of the first row of data (243).

```
If jMin < 243 Then jMin = 243
```

'Set jMax to 636 rows (~1.27 mm) after the centre of the scar.

```
jMax = j + 636
```

'If jMax is greater than the number of the first row of data, set jMax equal to the number of the first row of data (3043).

```
If jMax > 3043 Then jMax = 3043
```

'Change the named ranges ZoomX, ZoomR and ZoomS to contain only the data 636 rows either side of the deepest part of the scar.

```
ActiveWorkbook.Names.Add Name:="ZoomX", RefersToR1C1:="=data!R" & jMin & "C1:R" & jMax & "C1"
```

```
ActiveWorkbook.Names.Add Name:="ZoomR", RefersToR1C1:="=data!R" & jMin & "C2:R" & jMax & "C2"
```

```
ActiveWorkbook.Names.Add Name:="ZoomS", RefersToR1C1:="=data!R" & jMin & "C3:R" & jMax & "C3"
```

'Set the range of values to appear on the x-axis, based on the lowest and highest values of x (ie from the value of cell(jMin,1) to the value of cell(jMax,1)).

```
xMin = (Int(10 * Cells(jMin, 1).Value)) / 10
```

```
xMax = (Int(10 * Cells(jMax, 1).Value + 1)) / 10
```

'Set the x-axis on chart zoom to range from xMin to xMax.

```
Charts("zoom").Select  
  With ActiveChart.Axes(xlCategory)  
    .MinimumScale = xMin  
    .MaximumScale = xMax  
  End With
```

'Return to the data sheet.

```
Sheets("data").Select
```

'Enters the x position of the deepest part of the scar into cell (243,9).

```
Cells(243, 9).Value = Cells(j, 1).Value
```

'Enters the magnitude of the depth of the scar into cell (243,10).

```
Cells(243, 10).Value = Abs(max)
```

'Find the position of the start of the scar, (i.e. the last point before the scar where the data crosses the x-axis).

```
i = j  
Do Until Cells(i, 3).Value > 0#  
  i = i - 1  
  If i < 243 Then  
    Cells(244, 9).Value = "N/A"  
    Exit Do  
  End If  
Loop
```

'Enters the x position of the start of the scar into cell (244,9).

```
Cells(244, 9).Value = Cells(i, 1).Value
```

'Find the maximum height before the scar.

k = 243

max = Cells(243, 3).Value

'Starts 636 rows (~1.27mm) before deepest point of scar.

For i = jMin To j

 If max < Cells(i, 3).Value Then

 max = Cells(i, 3).Value

 k = i

 End If

Next

'Enters the x position of the maximum height before the scar into cell(247,9).

Cells(247, 9).Value = Cells(k, 1).Value

'Enters the magnitude of the maximum height before the scar into cell(247,10).

Cells(247, 10).Value = max

'Find the position of the end of the scar, (i.e. the first 'point after the scar where the data crosses the x-axis).

i = j

Do Until Cells(i, 3).Value > 0#

 i = i + 1

 If i > 3043 Then

 Cells(245, 9).Value = "N/A"

 Exit Do

 End If

Loop

'Enters the x position of the end of the scar into cell (245,9).

Cells(245, 9).Value = Cells(i, 1).Value

'Find the maximum height after the scar.

k = j

max = Cells(j, 3).Value

'Ends 636 rows (~1.27mm) after deepest point of scar.

For i = j To jMax

 If max < Cells(i, 3).Value Then

 max = Cells(i, 3).Value

 k = i

 End If

Next

Enters the x position of the maximum height after the scar into cell (248,9).

```
Cells(248, 9).Value = Cells(k, 1).Value
```

'Enters the magnitude of the maximum height before the scar into cell (248,10).

```
Cells(248, 10).Value = max
```

'Save the results workbook.

```
ActiveWorkbook.Save
```

```
End Sub
```

Sub TransferValues(Pressure As Integer)

'Transfer the values from the results file into the 'Results' sheet of this file.

```
Dim i As Integer  
Dim SheetB As Worksheet  
Dim WBName As String
```

'Set WBName equal to the first seven letters of the results file.

```
WBName = Mid(ActiveWorkbook.Name, 1, 7)
```

'Set SheetB equal to the data sheet in the active results file.

```
Set SheetB = ActiveWorkbook.Sheets("data")
```

'Activate this workbook and select the 'Results' sheet.

```
ThisWorkbook.Activate  
SheetB.Activate
```

'Find the first empty row on the sheet.

```
i = 2  
Do Until Cells(i, 1).Value = ""  
    i = i + 1  
Loop
```

'Add the value stored in WBName to the 1st cell.

```
Cells(i, 1).Value = WBName
```

'Add the specimen number to the 2nd cell (2nd, 3rd and 4th characters of WBName).

```
Cells(i, 2).Value = Mid(WBName, 2, 3)
```

'Add the Top/Bottom position to the 3rd cell.

```
Cells(i, 3).Value = "=Mid(RC[-2], 5, 1)"
```

'Add the Left/Middle/Right position to the 4th cell.

```
Cells(i, 4).Value = "=Mid(RC[-3], 6, 1)"
```

'Add the Front/Middle/Back position to the 5th cell.

```
Cells(i, 5).Value = "=Mid(RC[-4], 7, 1)"  
If IsPeened = "Unpeened" Then
```

'The values in cells 2 to 5 need to be modified if the file contains unpeened data.

```
Cells(i, 2).Value = Mid(WBName, 2, 2)
Cells(i, 3).Value = "=Mid(RC[-2], 4, 1)"
Cells(i, 4).Value = "=Mid(RC[-3], 5, 1)"
Cells(i, 5).Value = "=Mid(RC[-4], 6, 1)"
End If
```

'Lookup the values of Normal, Axial and L_Prop in the sheet 'Specimens', using the specimen number in cell 2.

```
Cells(i, 6).Value = "=vlookup(RC[-4], Specimens!SpecRange, 2,false)"
Cells(i, 7).Value = "=vlookup(RC[-5], Specimens!SpecRange, 3,false)"
Cells(i, 8).Value = "=vlookup(RC[-6], Specimens!SpecRange, 4,false)"
```

'Transfer the SD from the results file.

```
Cells(i, 9).Value = SheetB.Cells(1, 5).Value
```

'Transfer the Depth/Width/etc. values from the results file.

```
Cells(i, 10).Value = SheetB.Cells(243, 10).Value
Cells(i, 11).Value = SheetB.Cells(243, 9).Value
Cells(i, 12).Value = SheetB.Cells(244, 9).Value
Cells(i, 13).Value = SheetB.Cells(245, 9).Value
Cells(i, 14).Value = SheetB.Cells(246, 9).Value
Cells(i, 15).Value = SheetB.Cells(247, 9).Value
Cells(i, 16).Value = SheetB.Cells(247, 10).Value
```

'Calculate the total height of the maximum before the scar, by adding the height from 0 to the maximum scar depth.

```
Cells(i, 17).Value = Cells(i, 16).Value + Cells(i, 10).Value
Cells(i, 18).Value = SheetB.Cells(248, 9).Value
Cells(i, 19).Value = SheetB.Cells(248, 10).Value
```

'Calculate the total height of the maximum after the scar, by adding the height from 0 to the maximum scar depth.

```
Cells(i, 20).Value = Cells(i, 19).Value + Cells(i, 10).Value
```

End Sub

Sub CreateChartZoom(ScarMax As Integer)

```
,
ActiveWorkbook.Names.Add Name:="ZoomX", RefersToR1C1:="=data!R2" & j - 636 &
"C1:R" & j + 636 & "C1"
,
```

```
Sheets("chart").Copy Before:=Sheets("data")
ActiveChart.SetSourceData Source:=Sheets("data").Range("A253:C3033")
```

End Sub

APPENDIX E

RESULTS: FRETTING FATIGUE LIFE

Failure is defined as the fracture of the specimens, rather than the achievement of a given crack length.

E.1 UNPEENED

Table E.1a: The number of cycles to failure for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Cycles to failure (no.)
55	10	70	5,099,520
106	10	70	3,733,888
105	20	70	1,598,400
56	40	70	1,224,704
59	60	70	886,320
109	80	70	1,033,504
54	100	70	3,273,088
104	100	70	1,741,888
107	100	70	1,253,056

Table E.1b: The number of cycles to failure for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Cycles to failure (no.)
8	10	100	316,952
2	10	100	321,077
11	20	100	377,392
16	40	100	176,027
9	40	100	229,077
10	60	100	252,756
6	60	100	134,366
18	80	100	364,468
5	80	100	204,560
19	100	100	553,971
20	100	100	404,431

Table E.1c: The number of cycles to failure for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 125 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Cycles to failure (no.)
39	10	125	546,587
40	20	125	327,497
38	40	125	83,867
37	60	125	133,992
100	80	125	176,427
102	80	125	91,600
101	100	125	137,632
108	100	125	145,848

E.2 PEENED

Table E.2a: The number of cycles to failure for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Cycles to failure (no.)
9P	10	70	6,131,072+
2P	60	70	4,579,328 G
5P	100	70	5,000,000+

Table E.2b: The number of cycles to failure for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Cycles to failure (no.)
2P	10	100	5,000,000+
8P	40	100	1,976,448
4P	100	100	1,330,816

Table E.2c: The number of cycles to failure for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 125 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Cycles to failure (no.)
3P	10	125	1,786,240 P
10P	60	125	1,129,792
1P	100	125	434,432 G

- + Test stopped before failure in the fretting test section.
- G Test stopped due to failure not in the fretting test section, but in the grips.
- P Test stopped due to failure not in the fretting test section, but in a locating pin.

APPENDIX F

RESULTS: FRICTION DATA

These friction parameters were taken from hysteresis loops plotted for every test which can be found in Appendix H. The coefficient of friction is a ratio of the friction force and half of the normal load, definition of which can be found in Section 4.2.2.2.

F.1 UNPEENED

Table F.1a: The friction forces, amplitudes and coefficients for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 70 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Friction force max. (kN)		Friction force min. (kN)		Friction amplitude (kN)			Friction coefficient (μ)		
			Top	Bottom	Top	Bottom	Top	Bottom	Average	Top	Bottom	Average
106	10	70	0.147	0.148	-0.098	-0.073	0.122	0.111	0.117	1.204	1.089	1.147
105	20	70	0.503	0.555	-0.233	-0.058	0.368	0.306	0.337	1.810	1.508	1.659
56	40	70	0.478	0.594	-0.393	-0.310	0.435	0.452	0.444	1.070	1.112	1.091
59	60	70	0.374	0.348	-0.366	-0.357	0.370	0.353	0.361	0.607	0.578	0.593
109	80	70	0.688	1.624	-0.512	-1.174	0.600	1.399	0.999	0.738	1.721	1.230
104	100	70	0.471	0.601	-0.478	-0.336	0.475	0.468	0.471	0.467	0.461	0.464

Table F.1b: The friction forces, amplitudes and coefficients for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 100 MPa.

Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Friction force max. (kN)		Friction force min. (kN)		Friction amplitude (kN)			Friction coefficient (μ)		
			Top	Bottom	Top	Bottom	Top	Bottom	Average	Top	Bottom	Average
8	10	100	0.166	0.316	-0.072	-0.132	0.119	0.224	0.171	1.169	2.207	1.688
2	10	100	0.207	0.232	-0.081	-0.157	0.144	0.194	0.169	1.421	1.914	1.667
11	20	100	0.299	0.383	-0.126	-0.253	0.212	0.318	0.265	1.045	1.564	1.304
16	40	100	0.432	0.490	-0.293	-0.377	0.363	0.433	0.398	0.893	1.067	0.980
9	40	100	0.559	0.626	-0.412	-0.462	0.486	0.544	0.515	1.195	1.339	1.267
10	60	100	0.416	0.526	-0.324	-0.424	0.370	0.475	0.422	0.607	0.779	0.693
6	60	100	0.640	0.468	-0.409	-0.301	0.524	0.385	0.454	0.860	0.631	0.746
18	80	100	0.280	0.599	-0.336	-0.400	0.308	0.500	0.404	0.379	0.615	0.497
5	80	100	0.638	0.555	-0.506	-0.456	0.572	0.505	0.539	0.704	0.622	0.663
19	100	100	0.533	0.714	-0.545	-0.534	0.539	0.624	0.582	0.531	0.614	0.572
20	100	100	0.488	0.673	-0.576	-0.610	0.532	0.642	0.587	0.524	0.632	0.578

Table F.1c: The friction forces, amplitudes and coefficients for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to an axial stress amplitude of 125 MPa.

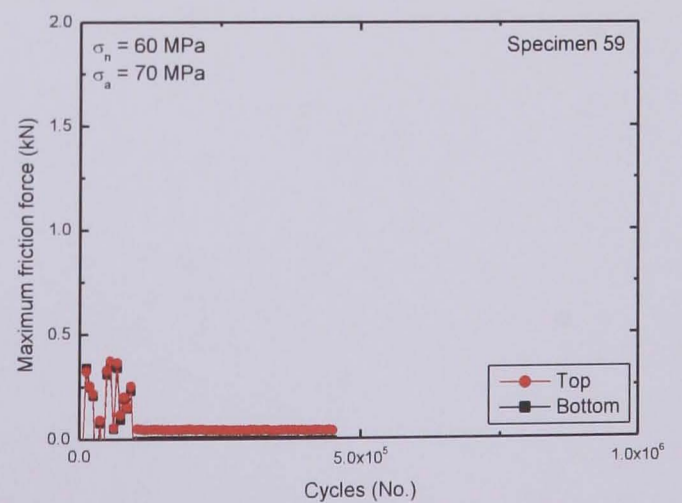
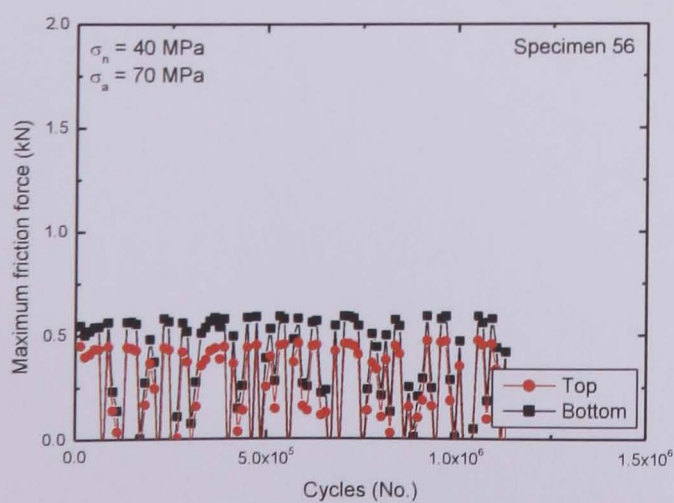
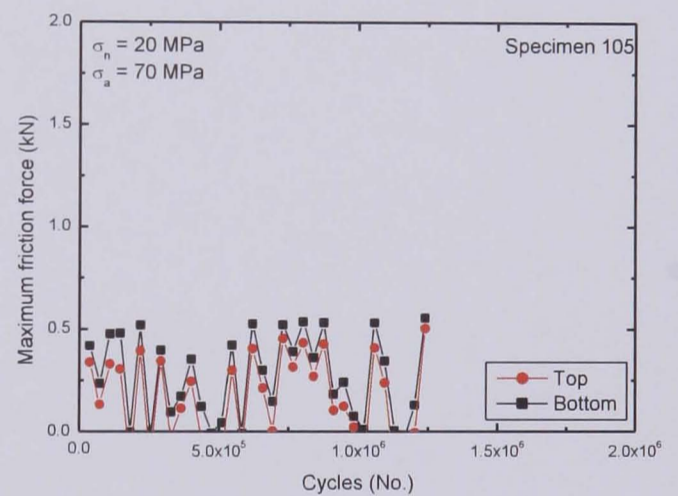
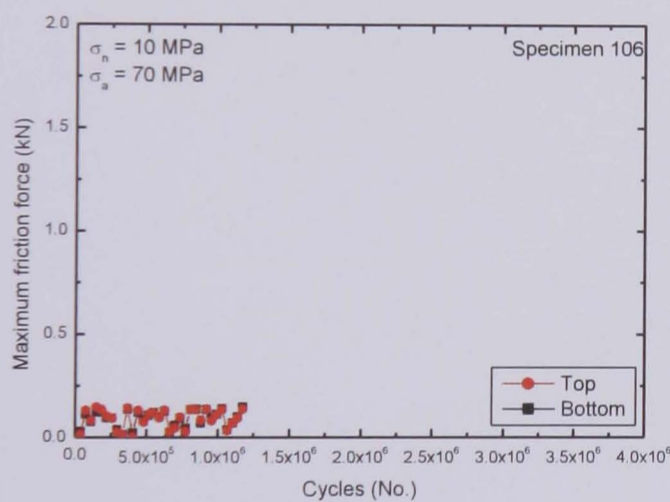
Specimen (no.)	Normal stress (MPa)	Axial stress (MPa)	Friction force max. (kN)		Friction force min. (kN)		Friction amplitude (kN)			Friction coefficient (μ)		
			Top	Bottom	Top	Bottom	Top	Bottom	Average	Top	Bottom	Average
39	10	125	0.234	0.752	-0.139	-0.082	0.186	0.417	0.302	1.834	4.106	2.970
40	20	125	0.412	0.556	-0.280	-0.159	0.346	0.357	0.352	1.703	1.759	1.731
38	40	125	0.933	0.763	-0.469	-0.433	0.701	0.598	0.650	1.725	1.472	1.598
37	60	125	0.951	0.971	-0.596	-0.456	0.774	0.714	0.744	1.269	1.171	1.220
100	80	125	0.803	0.954	-0.476	-0.510	0.639	0.732	0.685	0.787	0.900	0.843
101	100	125	1.143	1.281	-0.729	-0.614	0.936	0.947	0.942	0.921	0.932	0.927

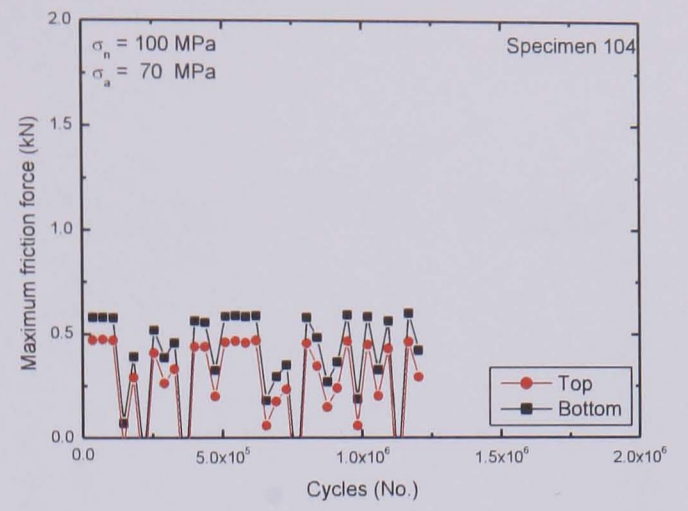
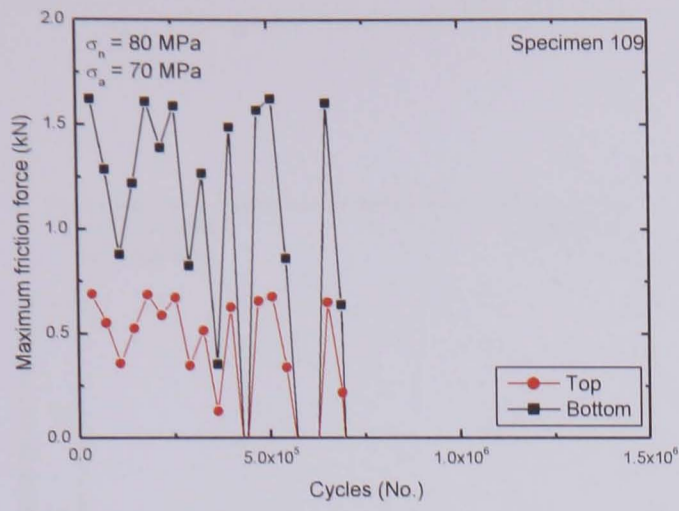
APPENDIX G

RESULTS: EVOLUTION OF MAXIMUM FRICTION VALUES

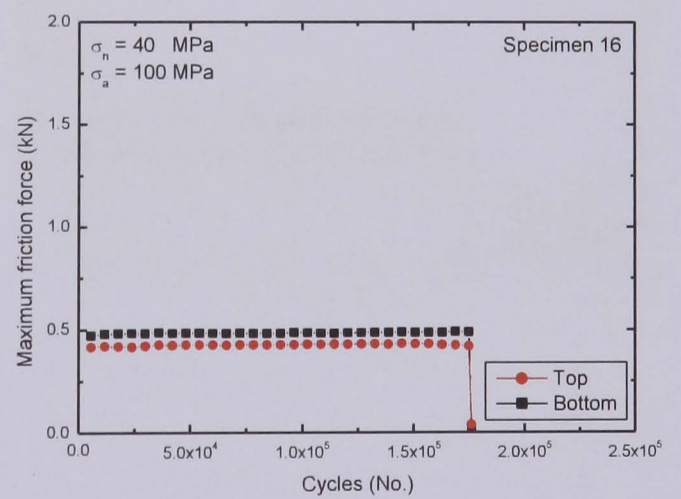
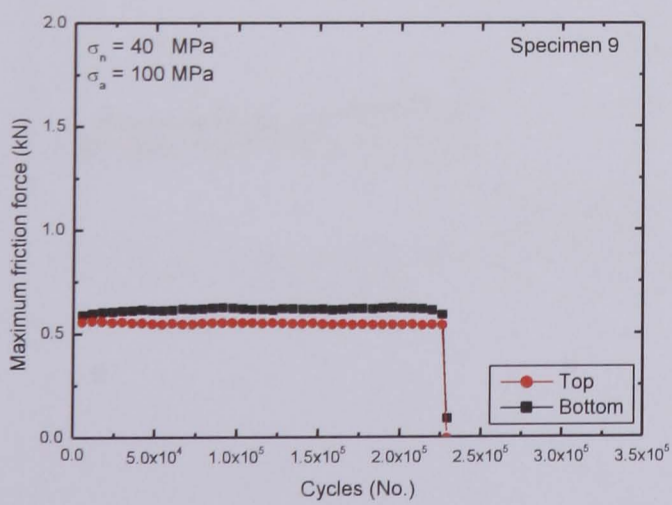
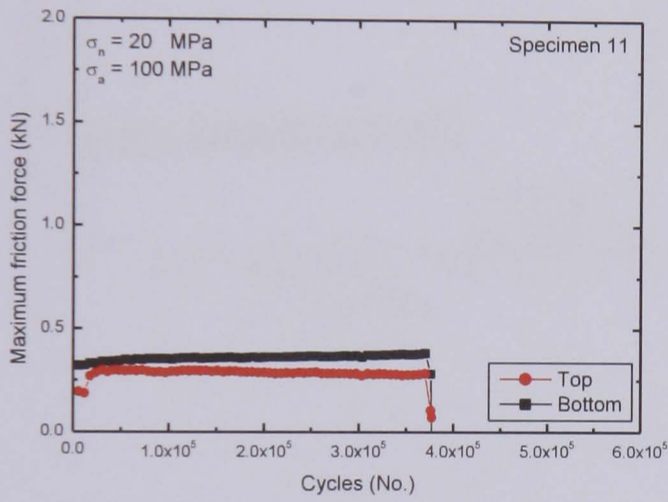
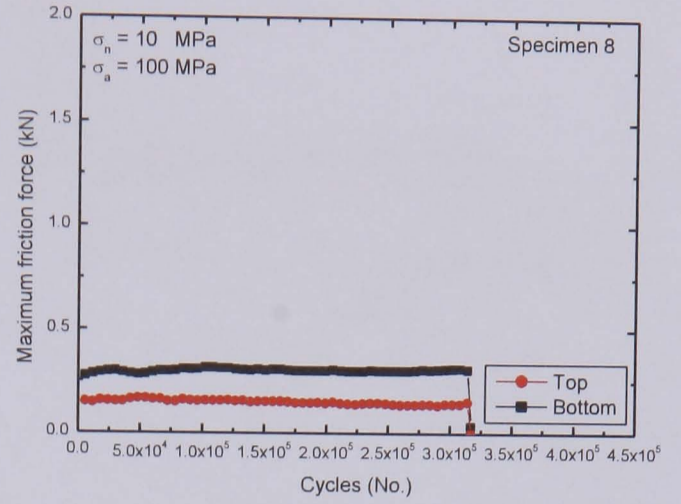
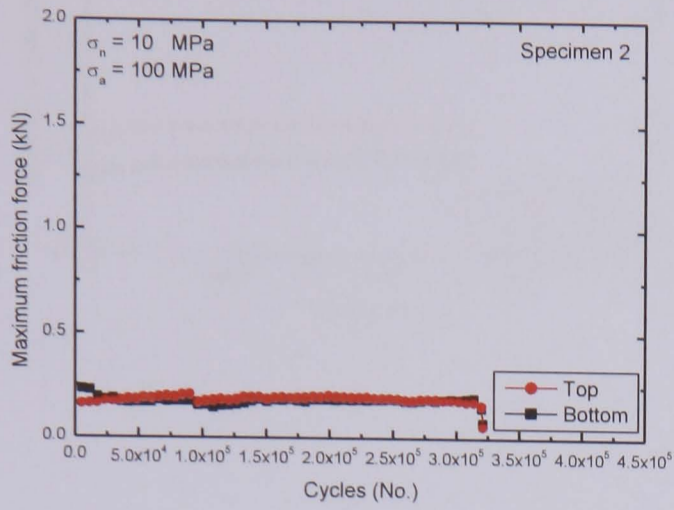
The evolution of the maximum friction force recorded over the life of every unpeened specimen, traced for both the top and bottom fretting pad.

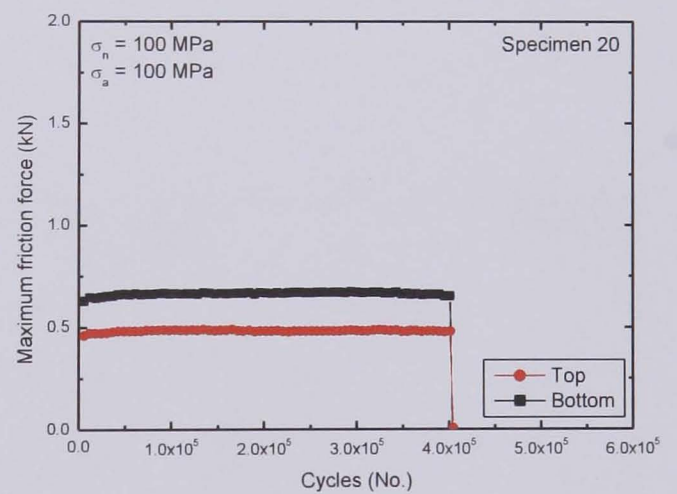
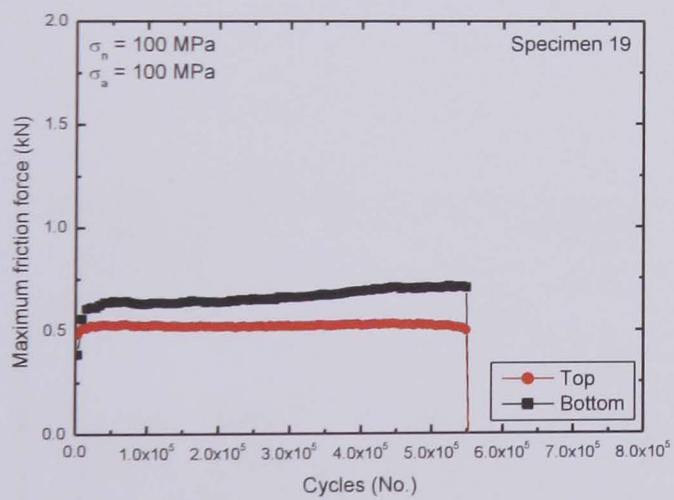
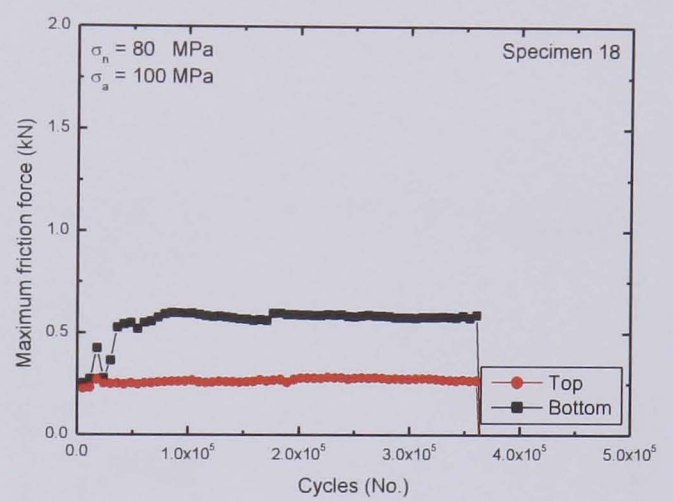
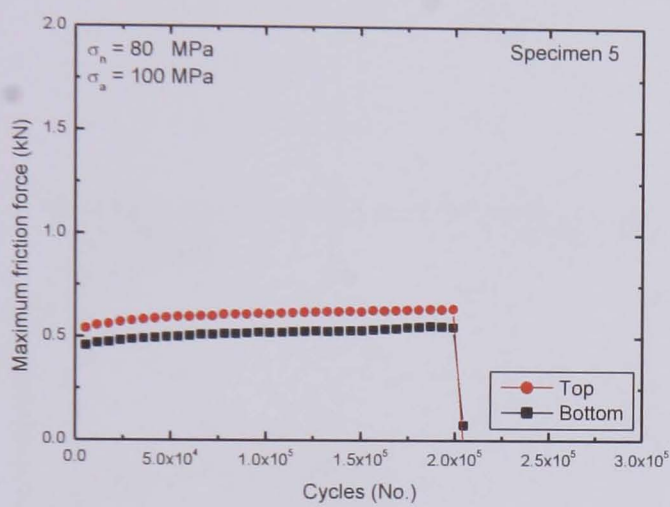
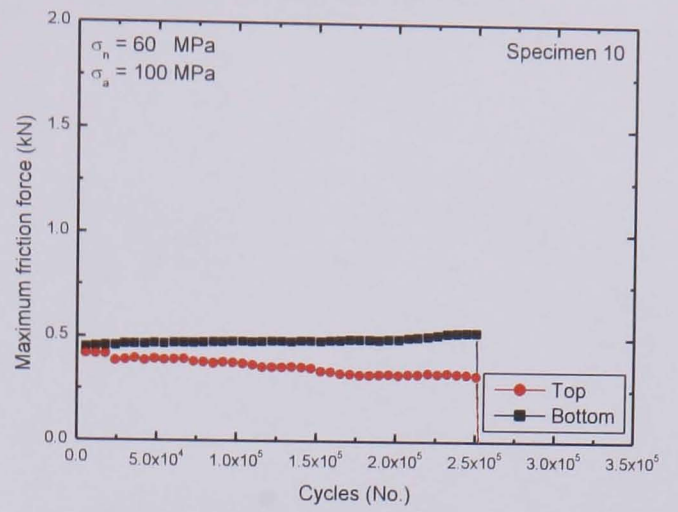
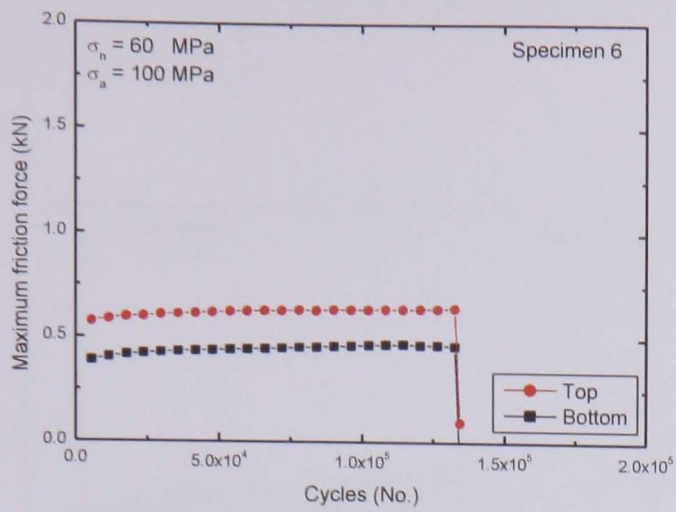
G.1 FRICTION MAXIMUM: $\sigma_a = 70$ MPa unpeened



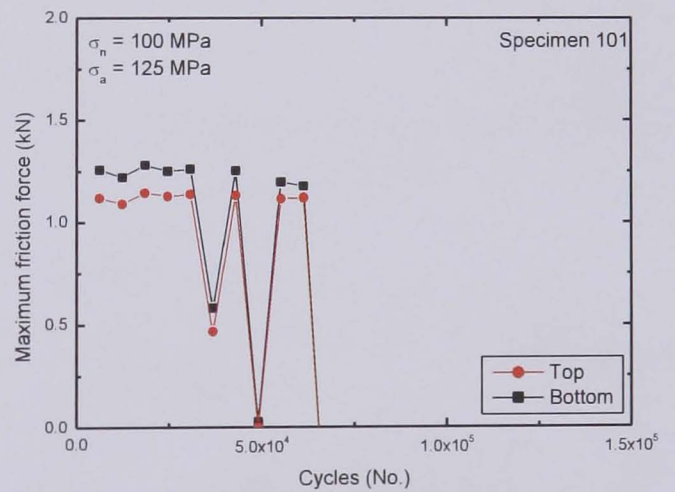
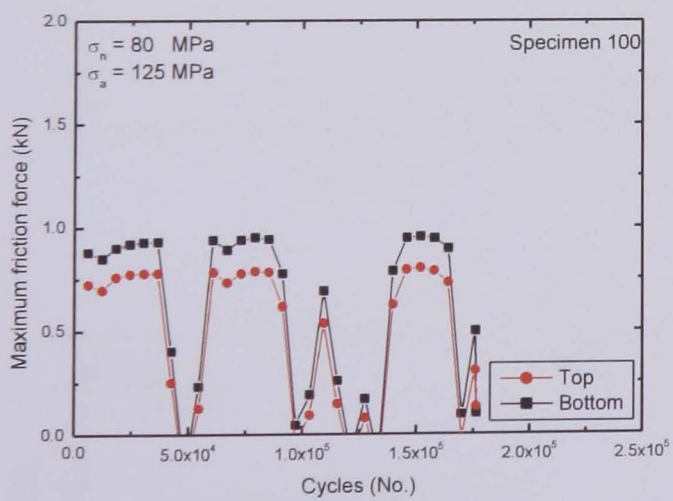
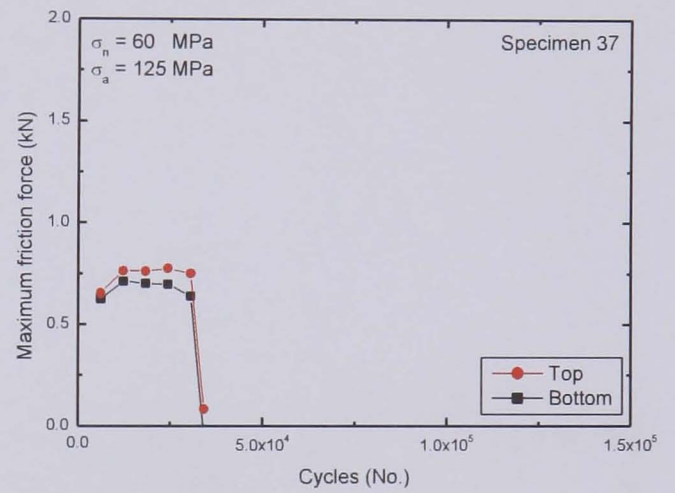
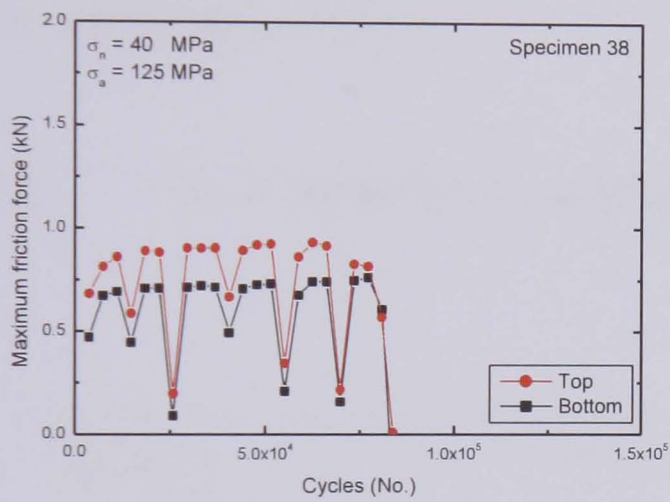
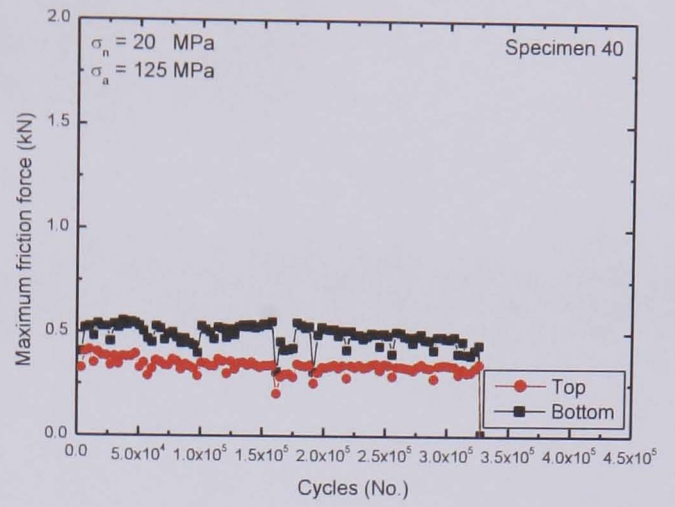
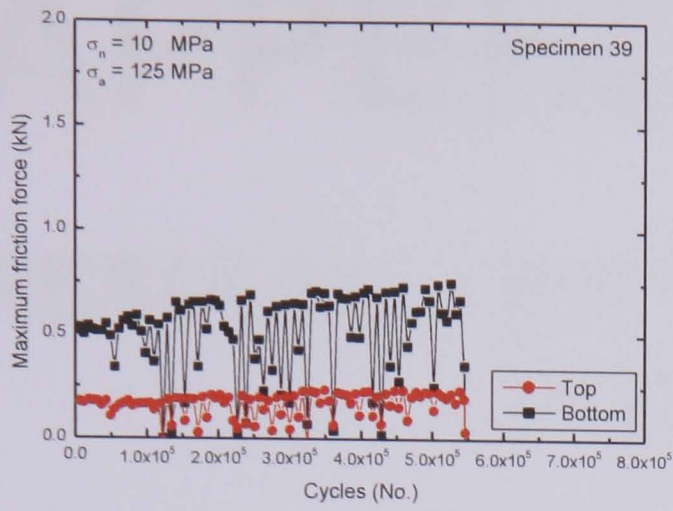


G.2 FRICTION MAXIMUM: $\sigma_a = 100$ MPa unpeened





G.3 FRICTION MAXIMUM: $\sigma_a = 125$ MPa unpeened

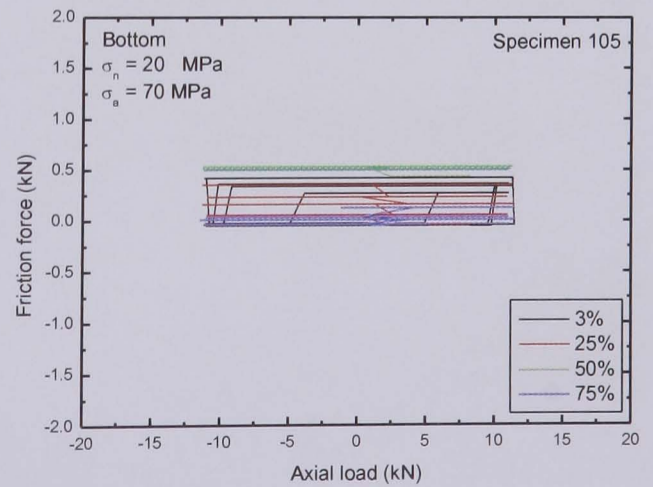
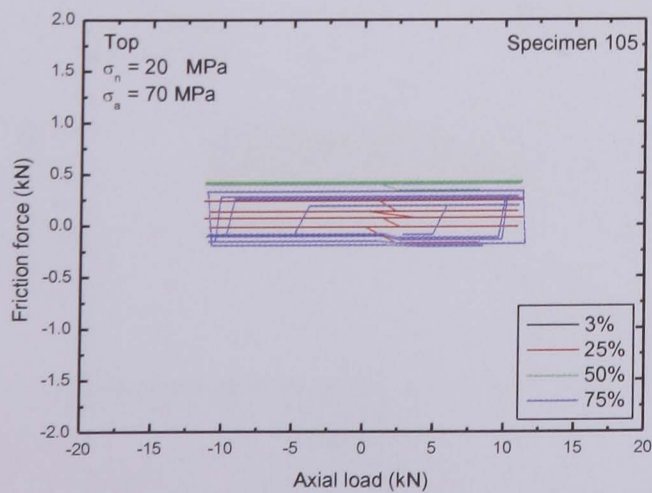
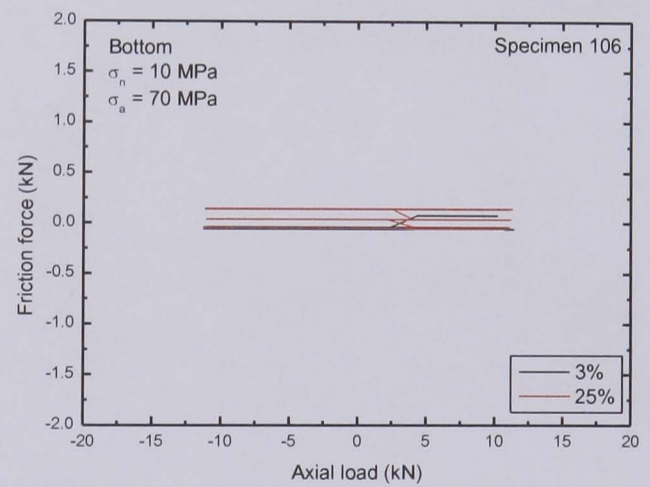
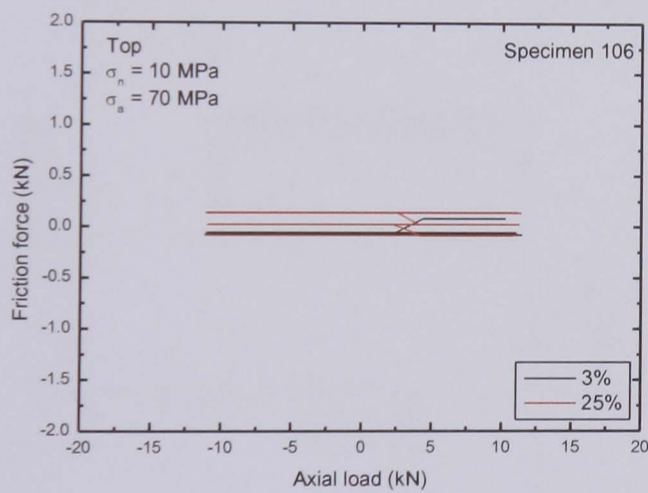


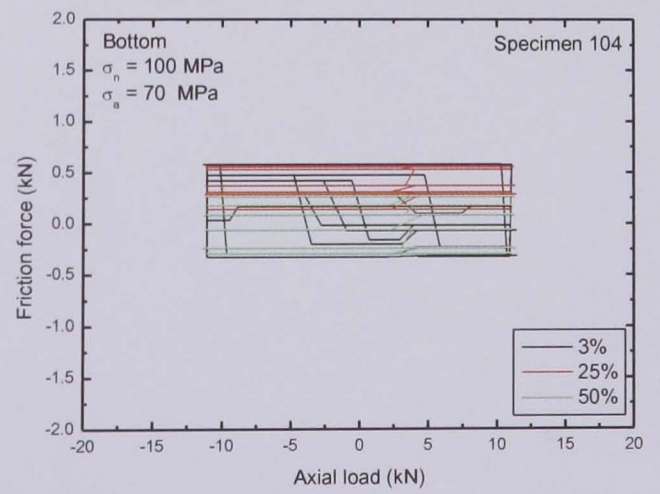
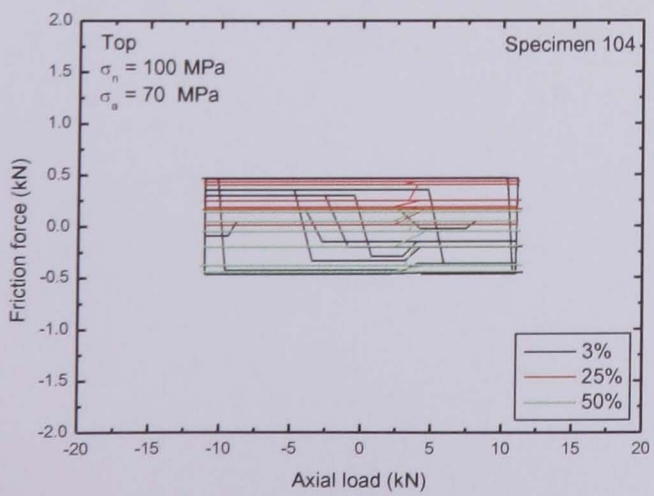
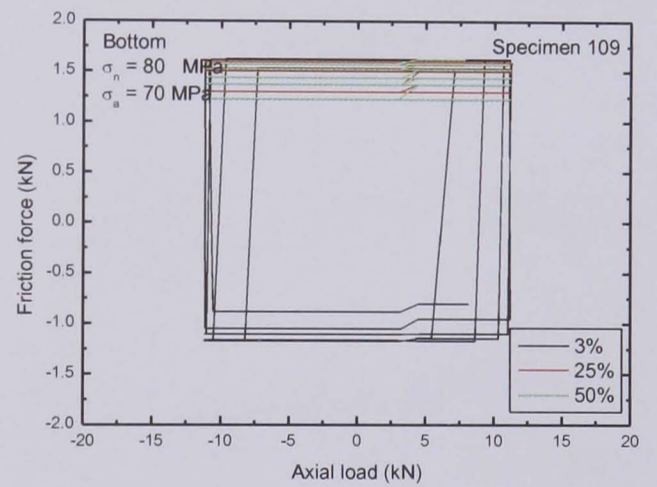
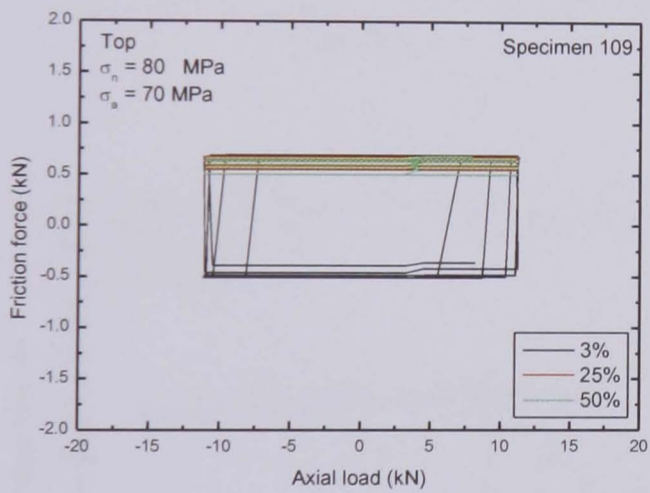
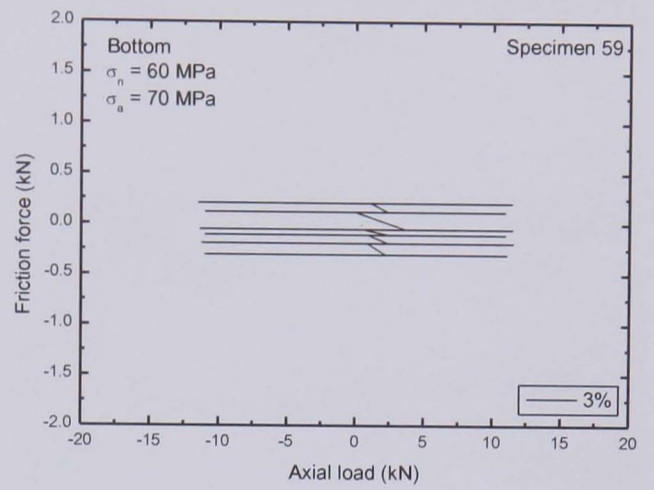
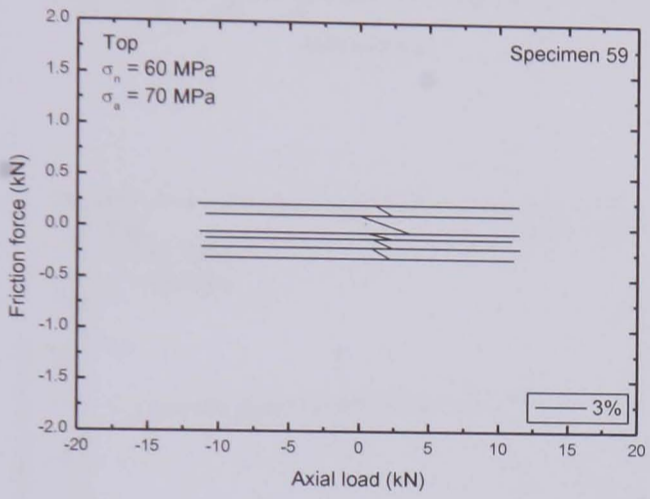
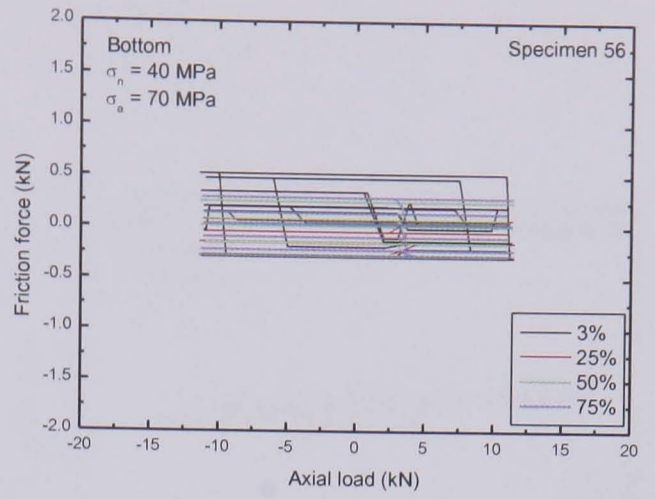
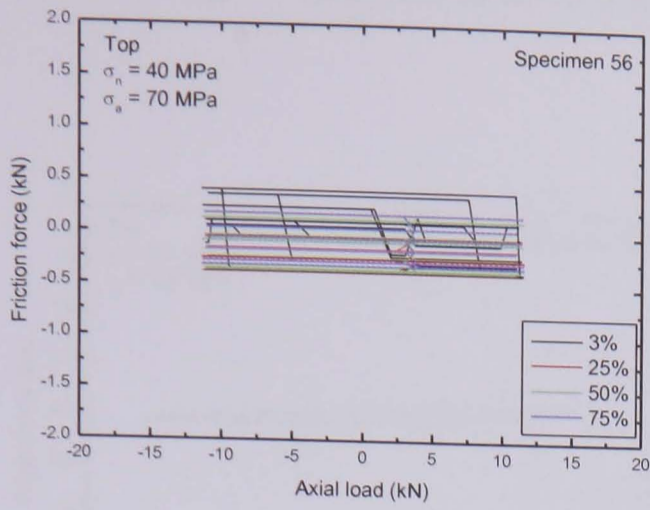
APPENDIX H

RESULTS: FRICTION HYSTERESIS LOOPS

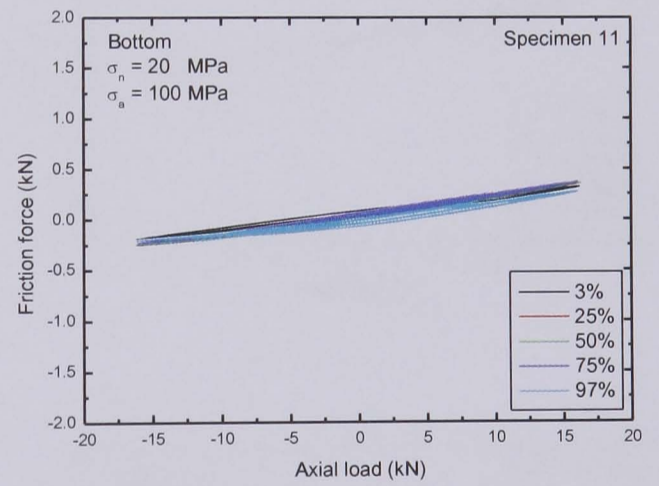
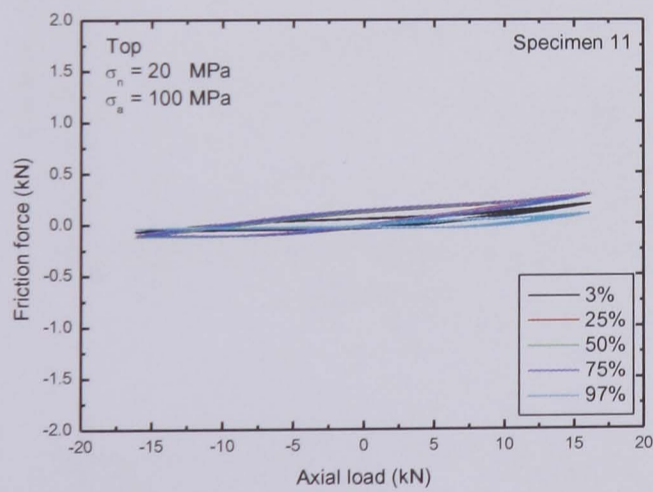
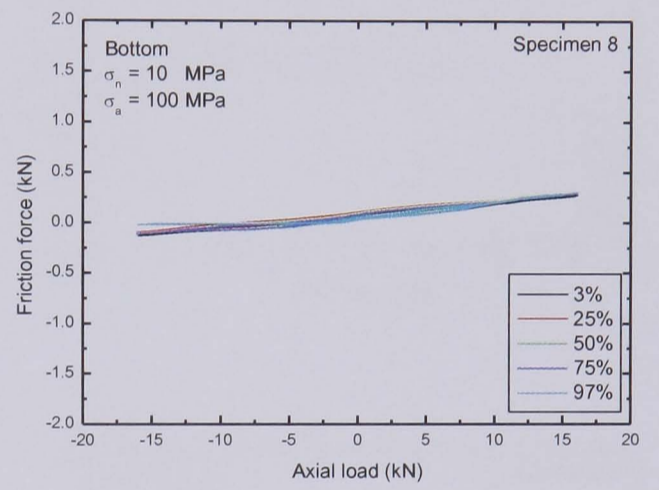
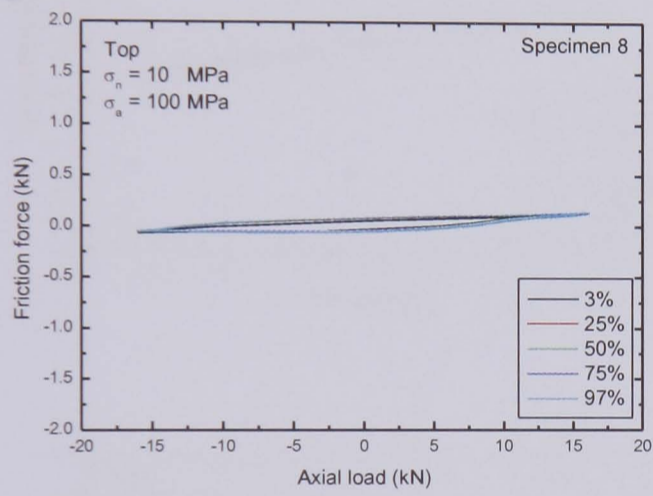
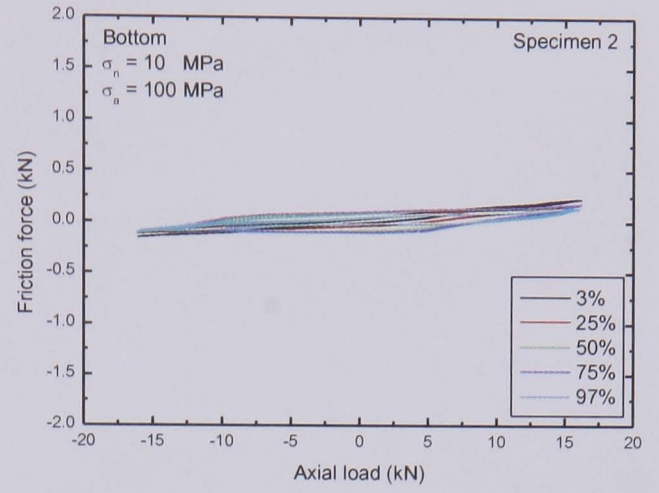
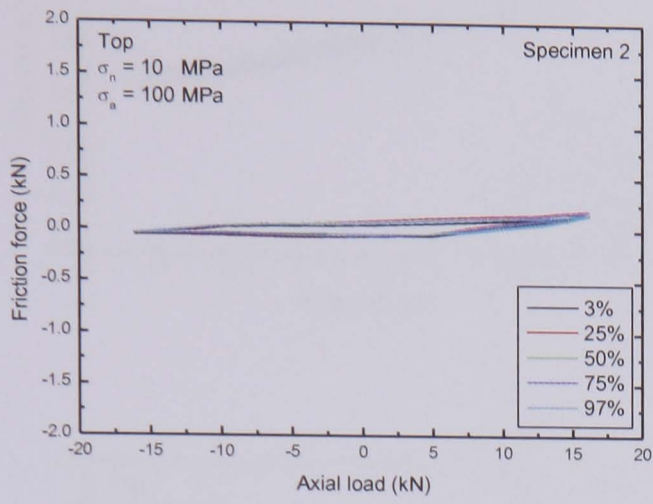
All hysteresis loops plotted for every test, including those that were distorted by the data logging system.

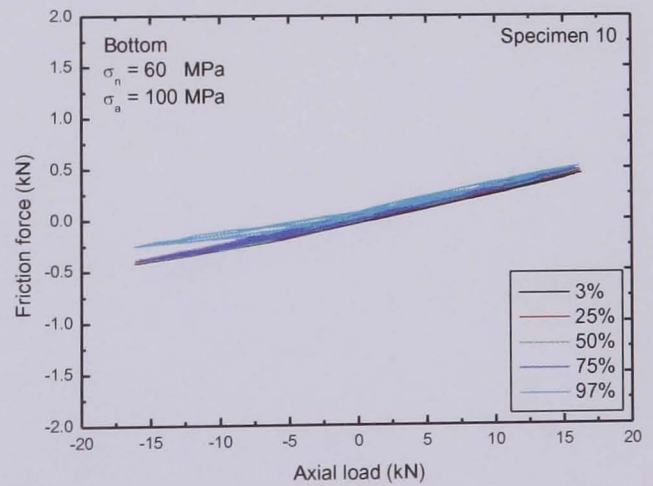
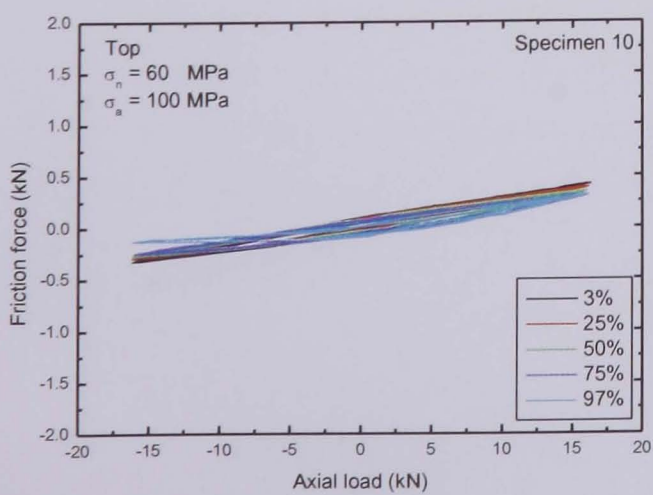
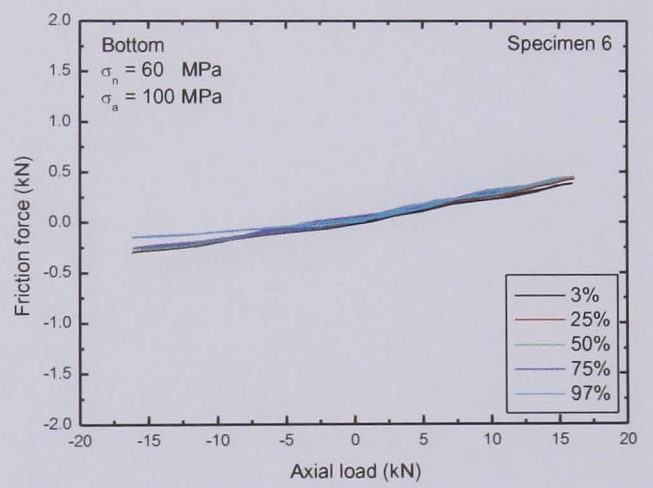
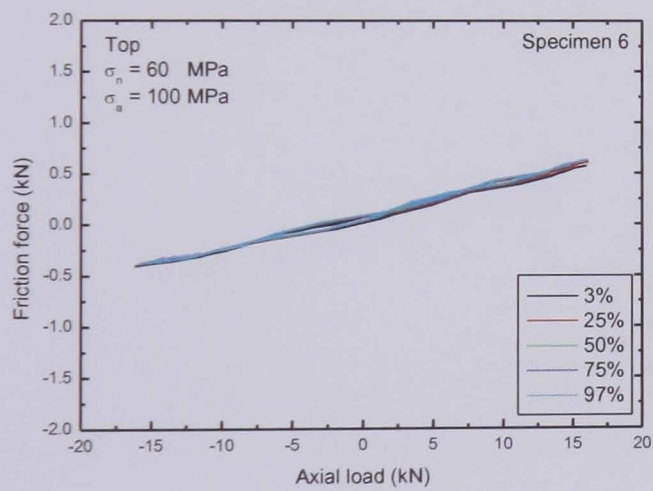
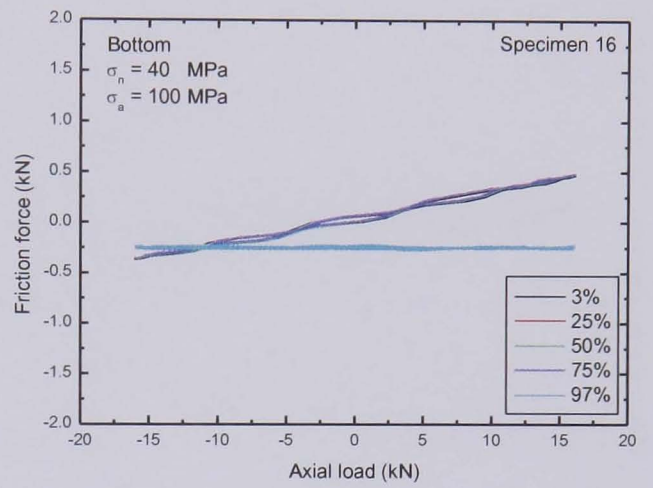
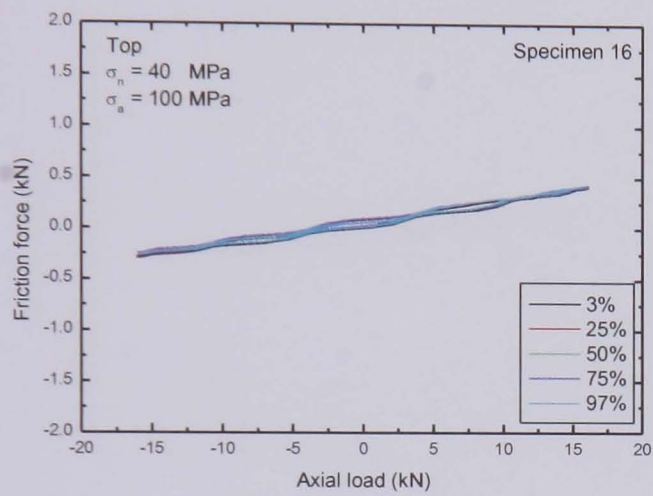
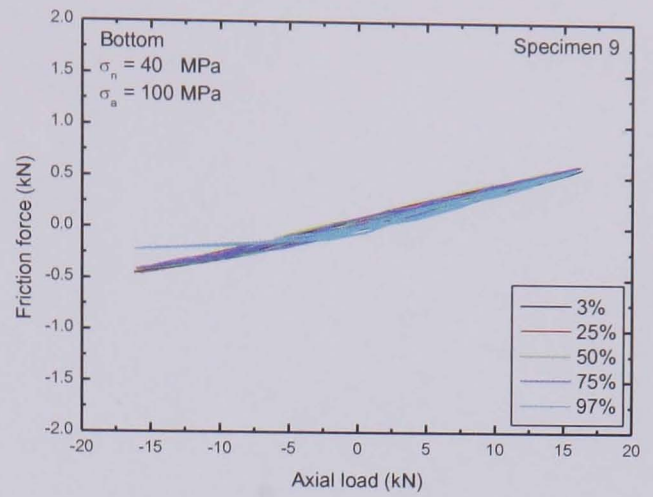
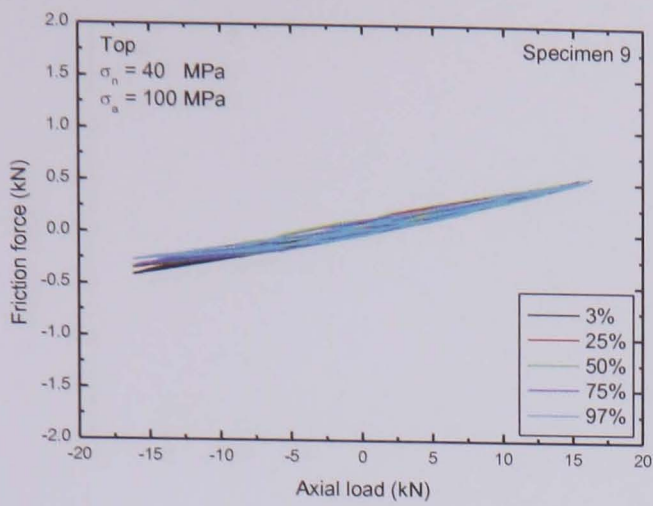
H.1 $\sigma_a = 70$ MPa unpeened

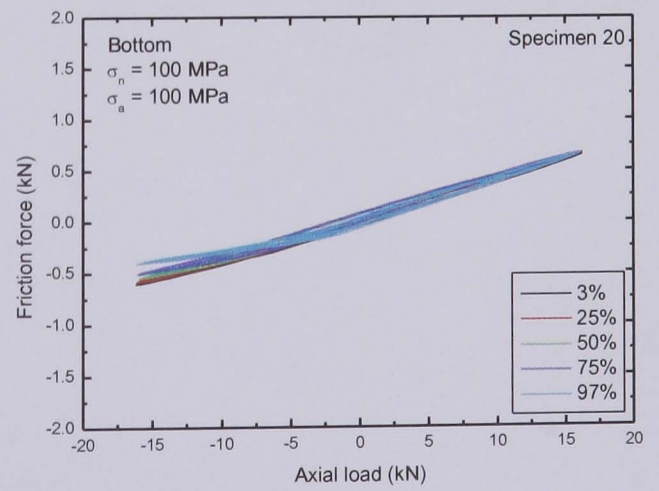
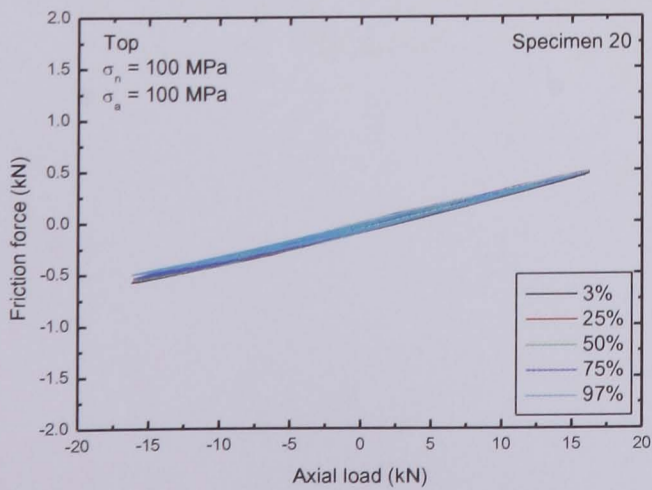
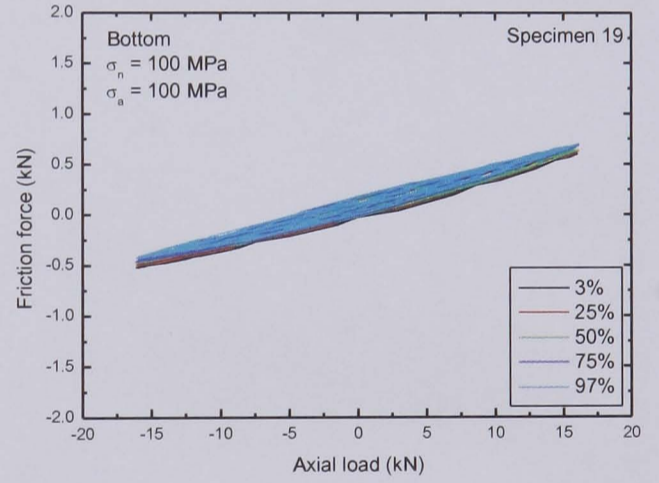
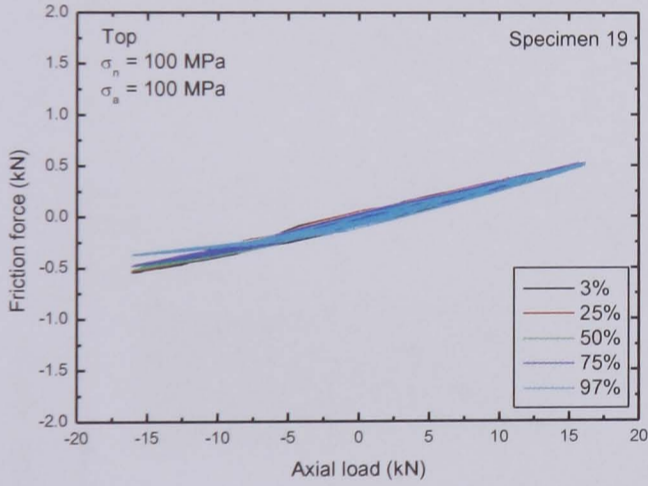
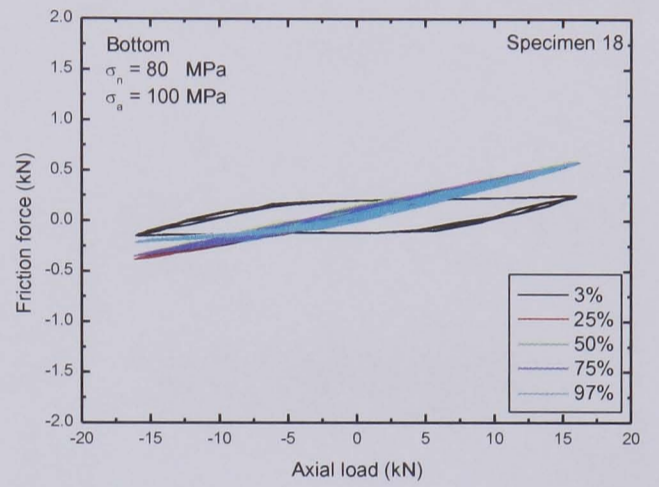
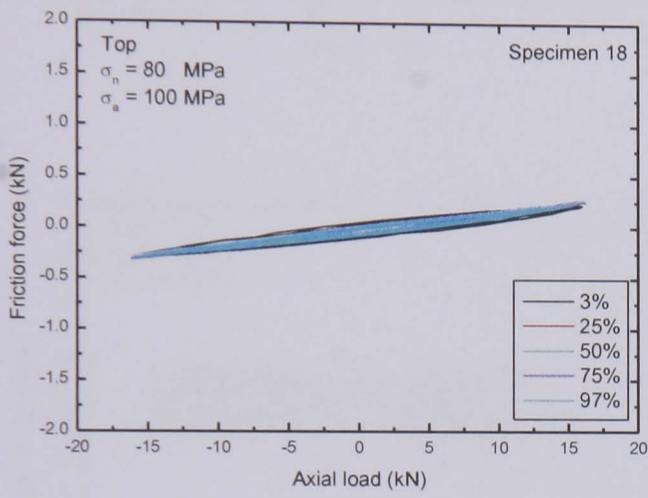
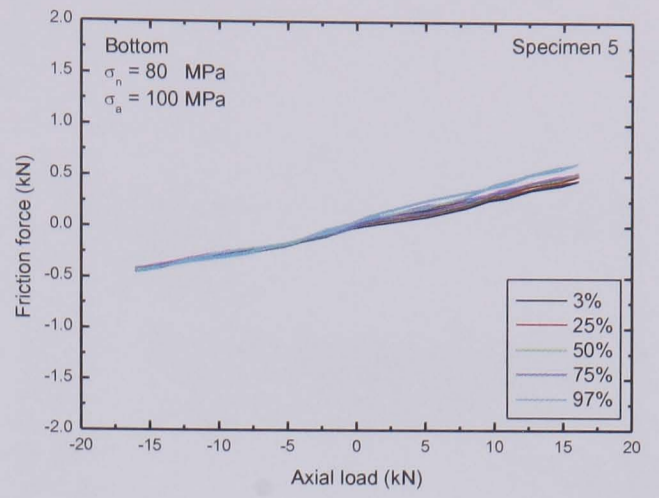
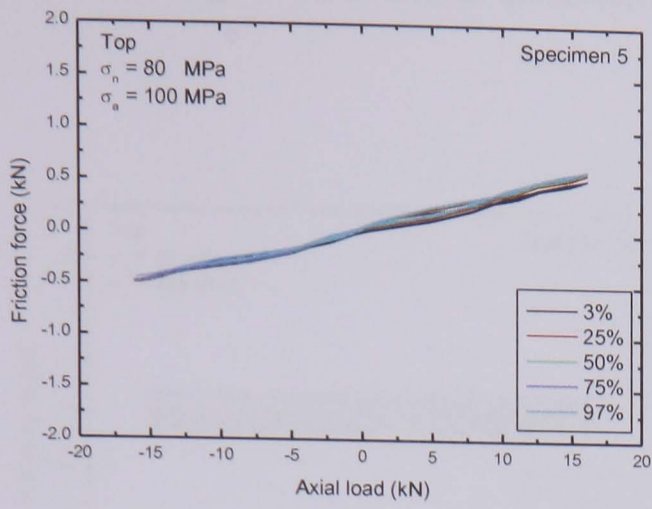




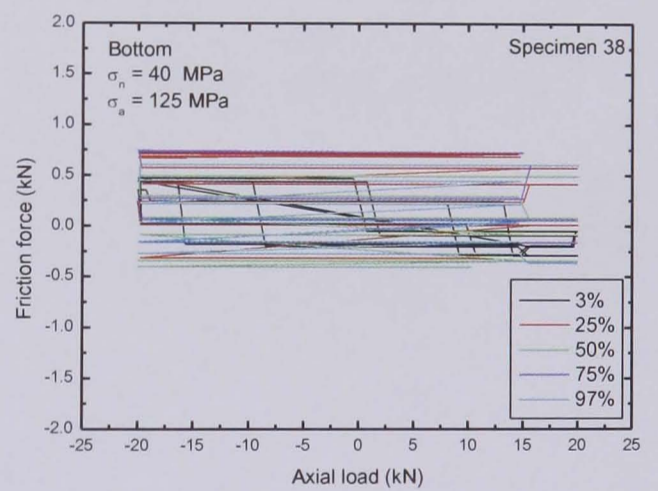
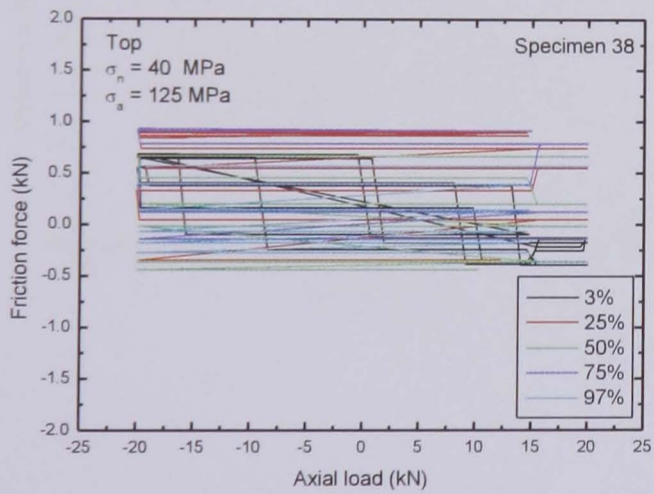
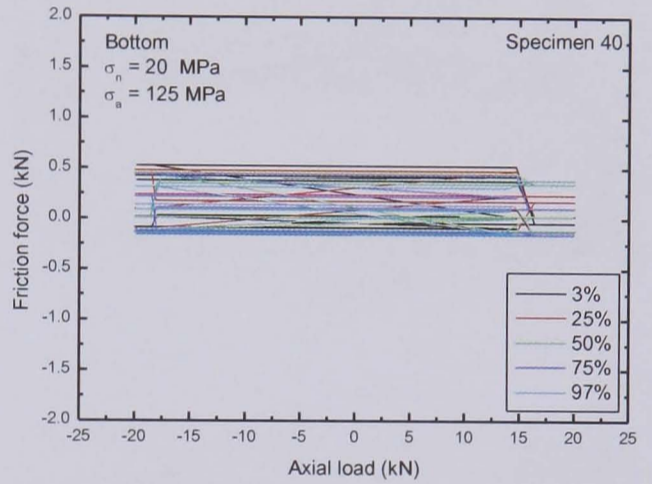
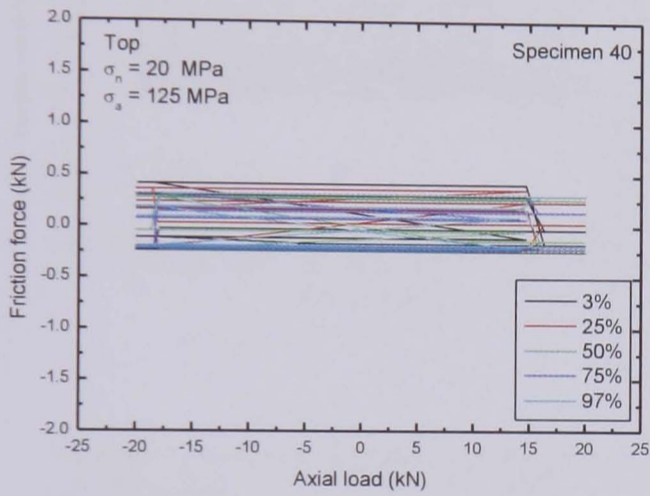
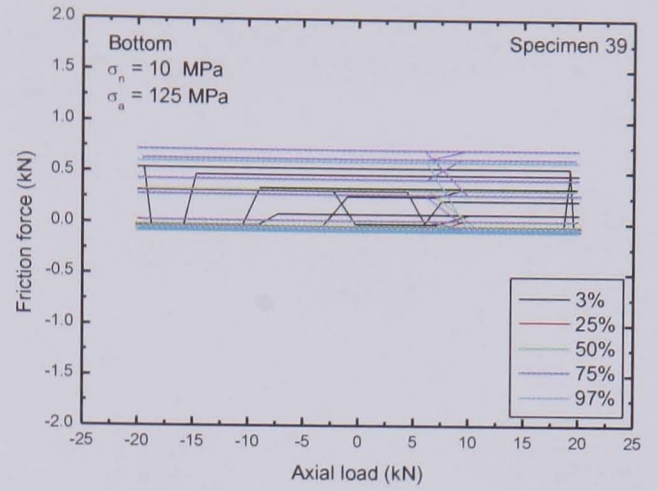
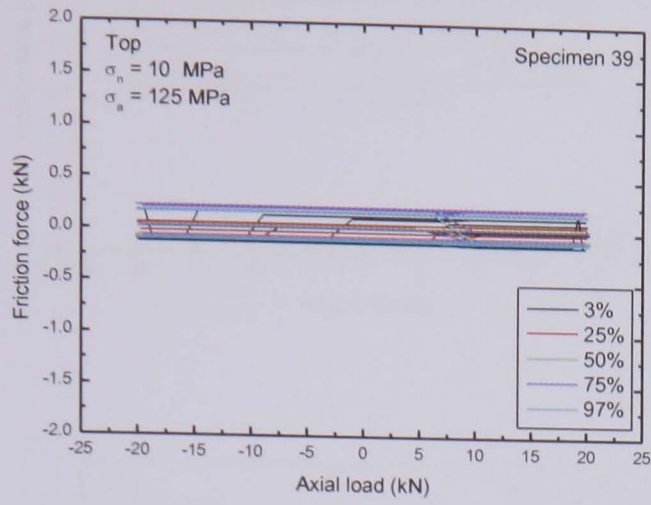
H.2 $\sigma_a = 100$ MPa unpeened

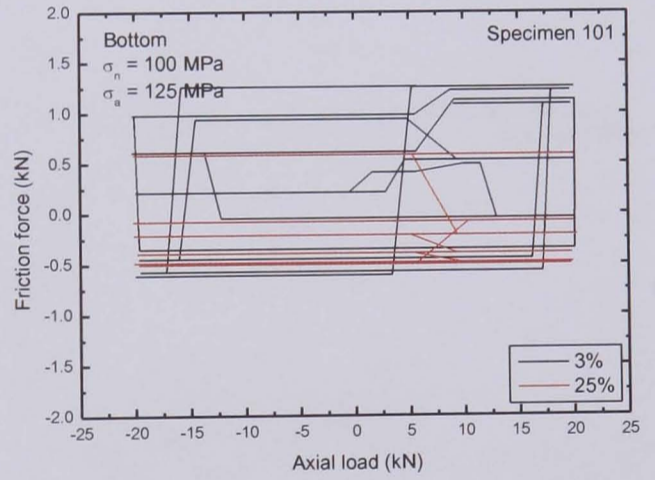
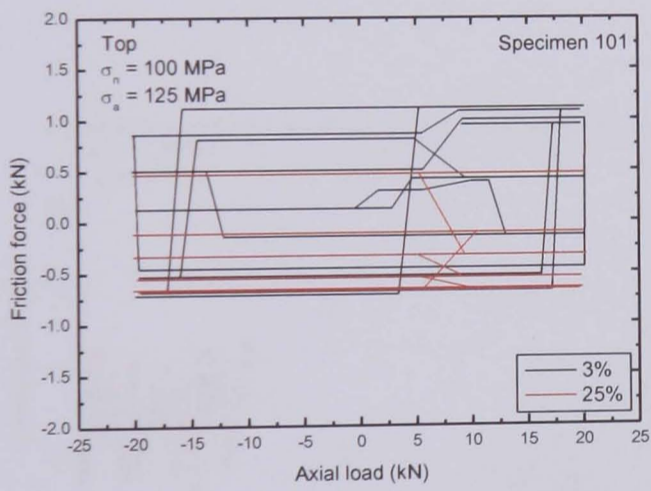
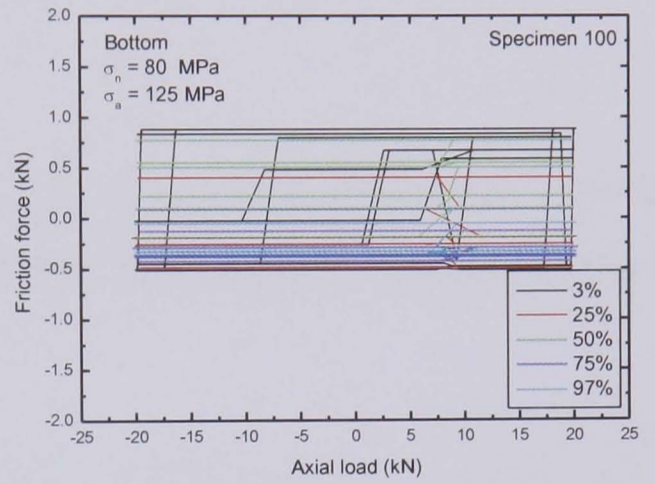
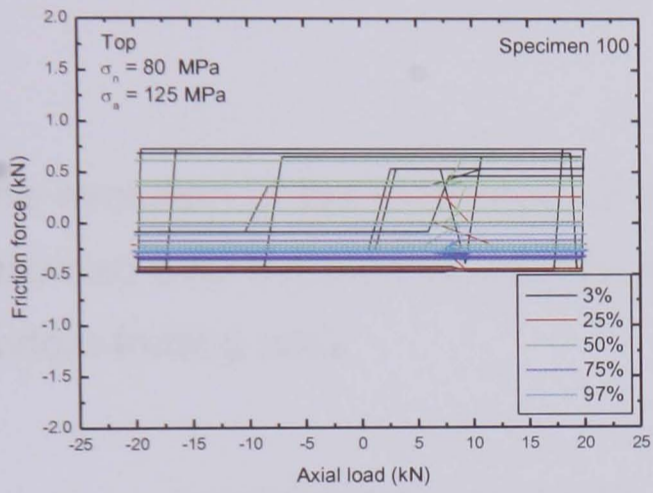
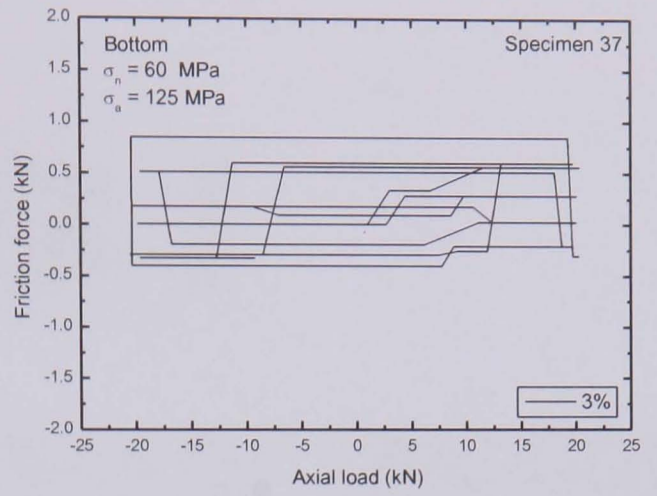
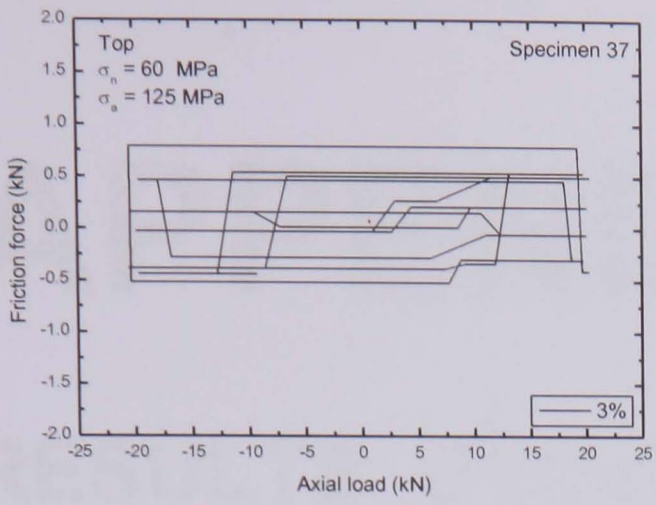






H.3 $\sigma_a = 125$ MPa unpeened



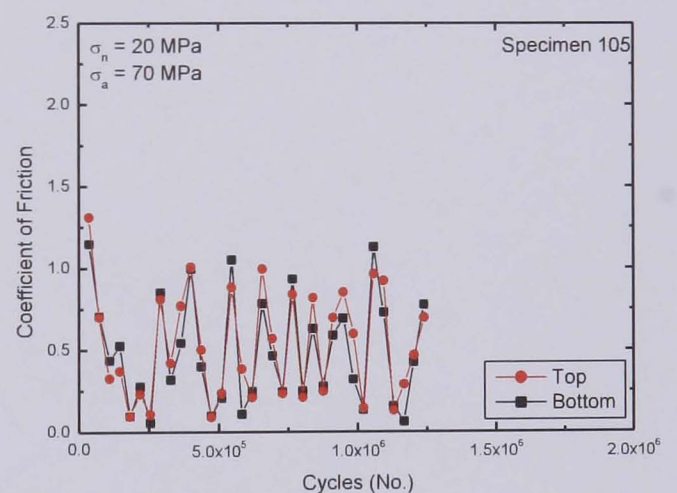
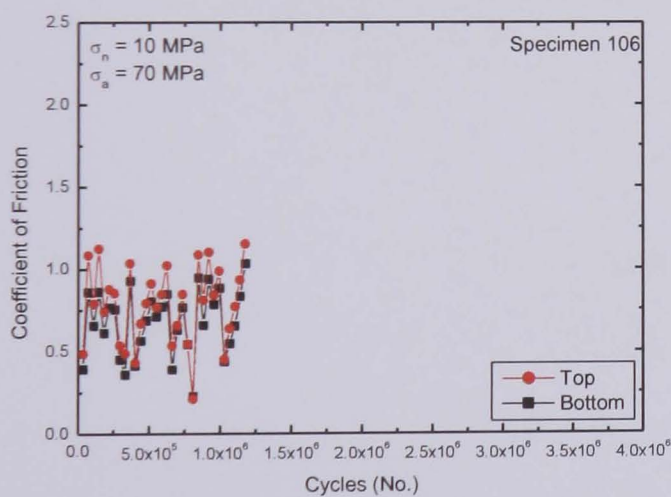


APPENDIX I

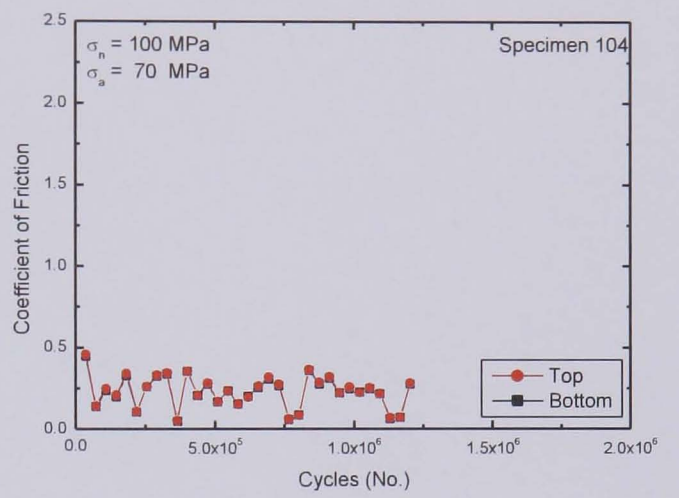
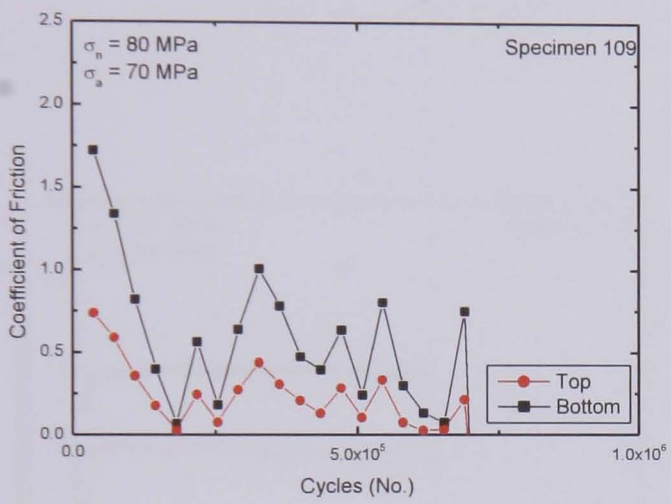
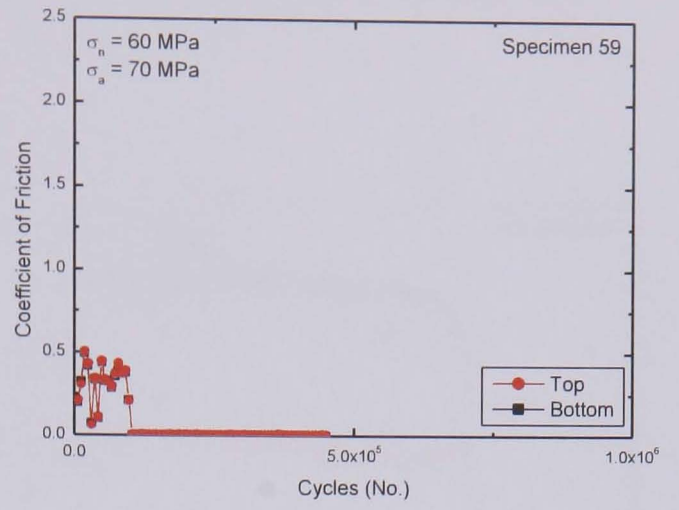
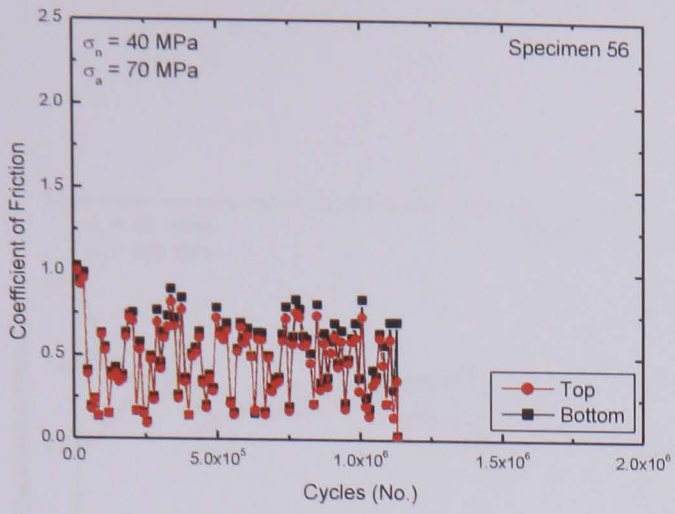
RESULTS: EVOLUTION OF FRICTION COEFFICIENT VALUES

The evolution of the coefficient of friction calculated from the friction force data recorded over the life of every unpeened specimen, traced for both the top and bottom fretting pad.

I.1 FRICTION COEFFICIENT: $\sigma_a = 70$ MPa unpeened

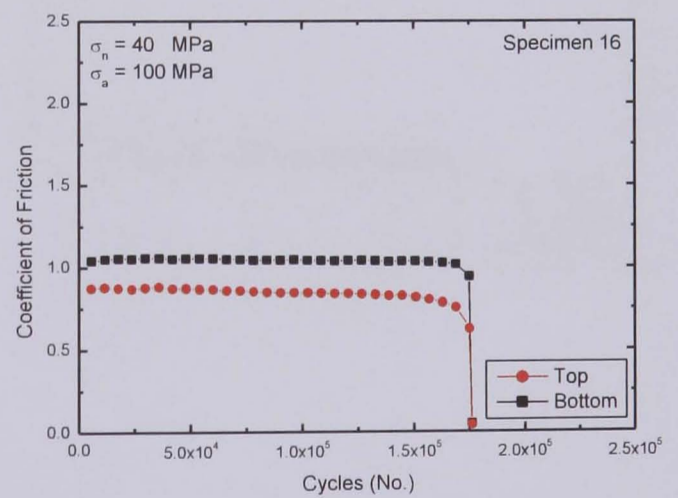
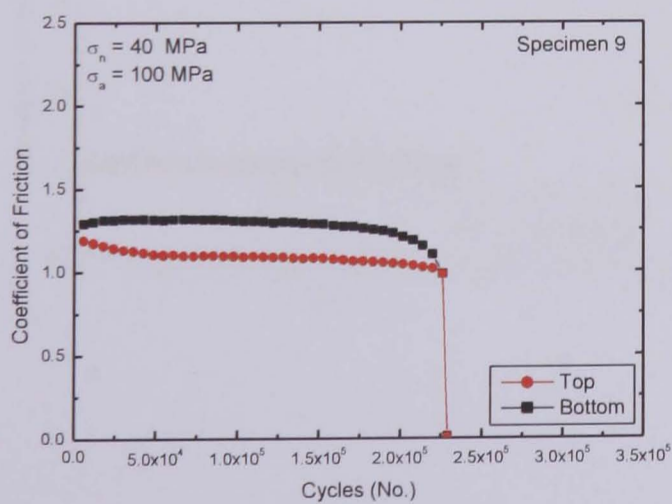
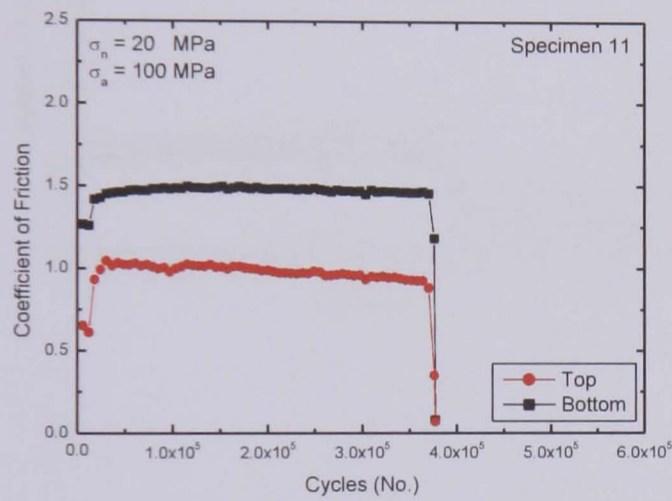
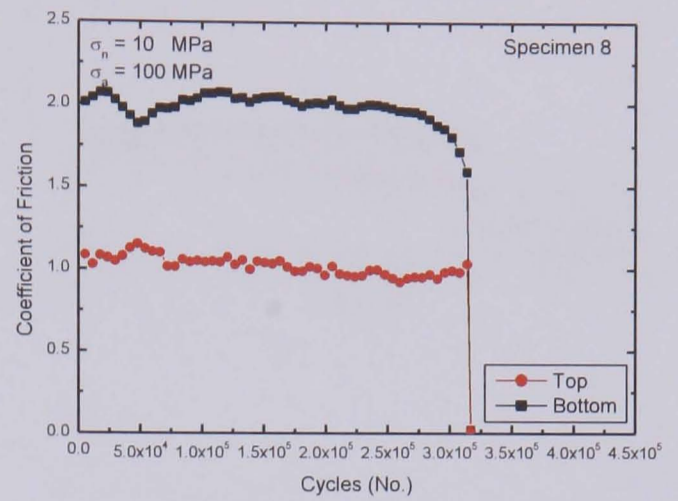
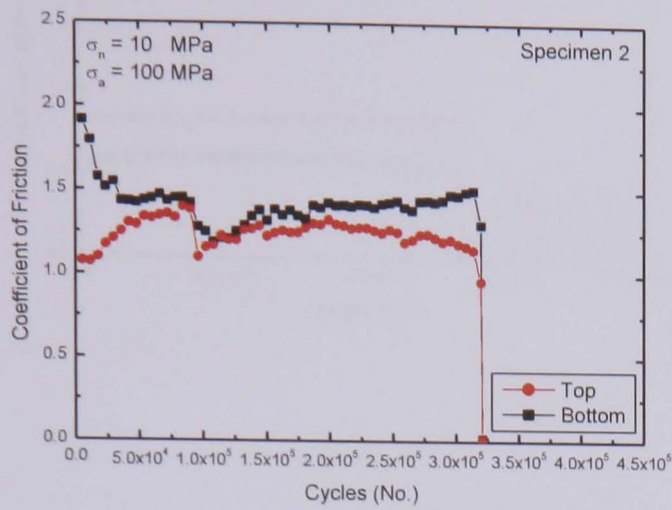


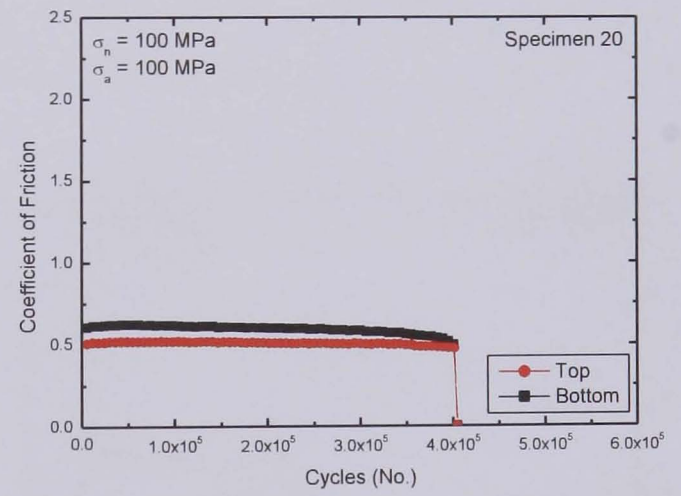
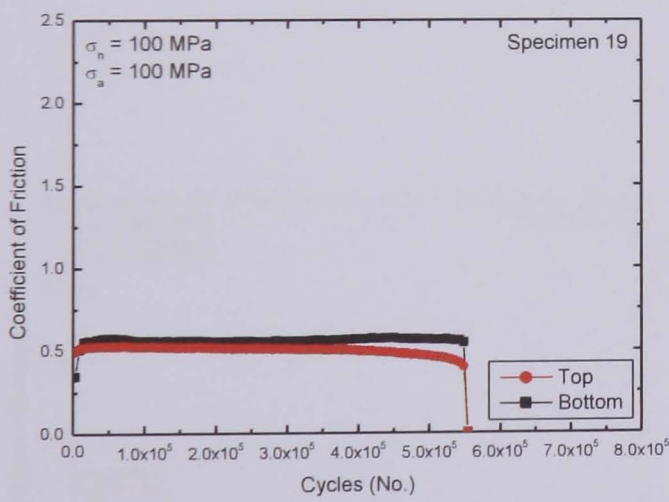
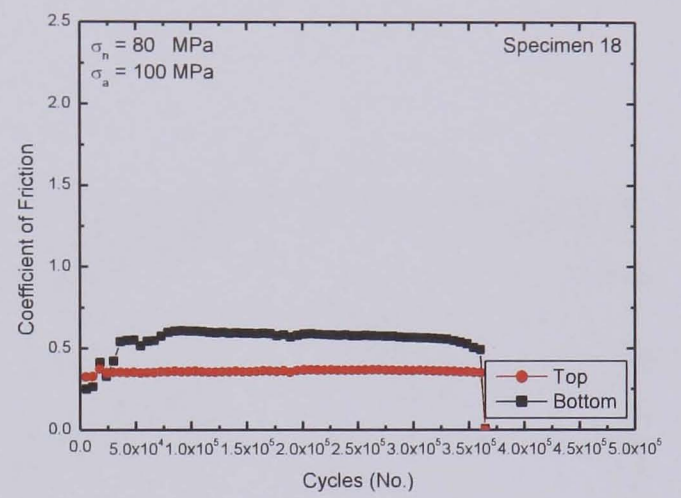
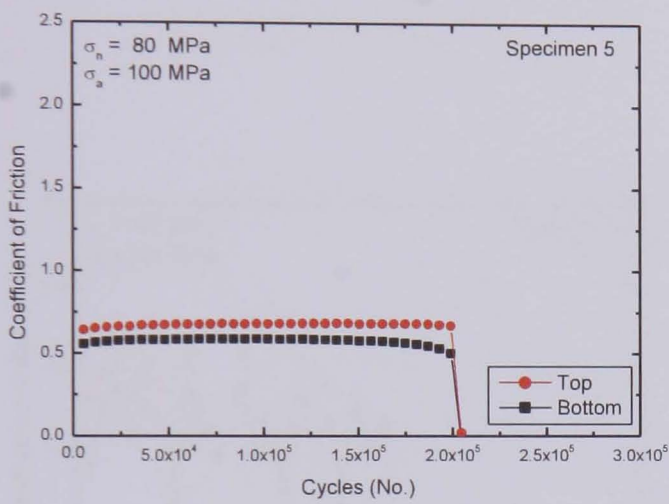
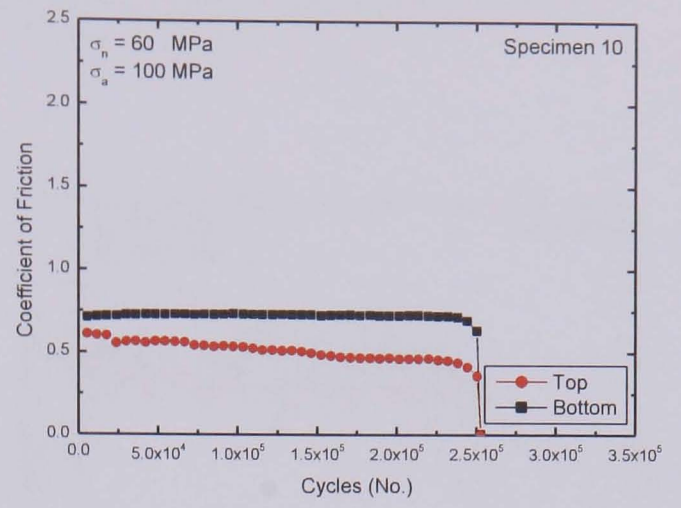
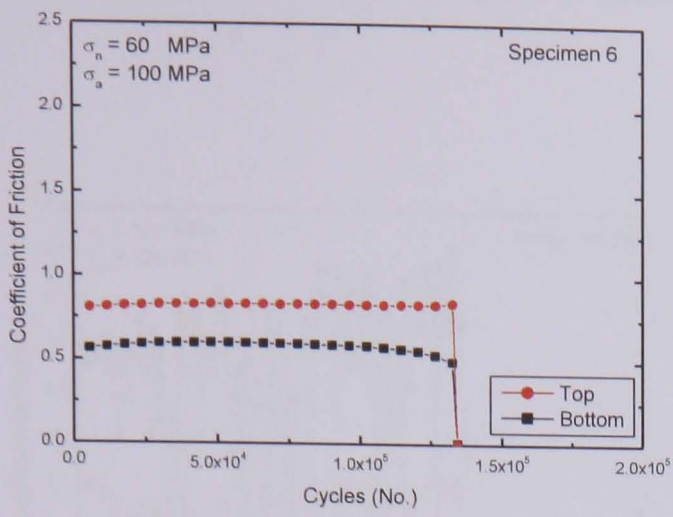
1.2 FRICTION COEFFICIENT



I.2

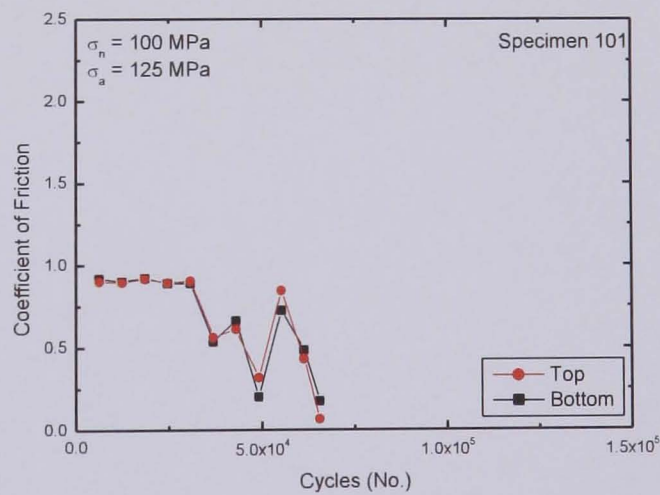
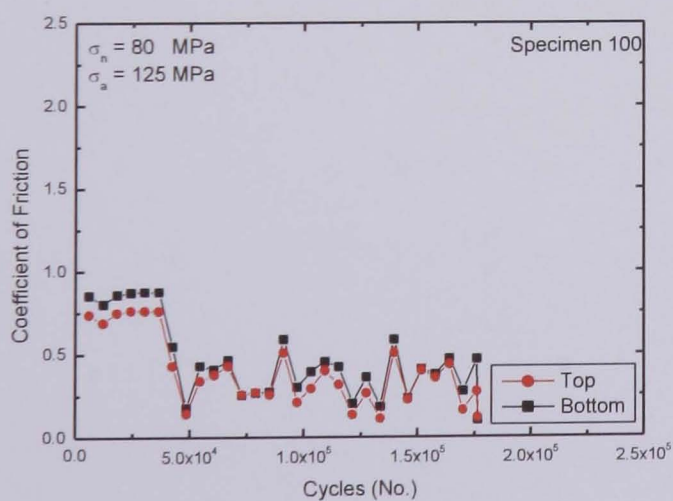
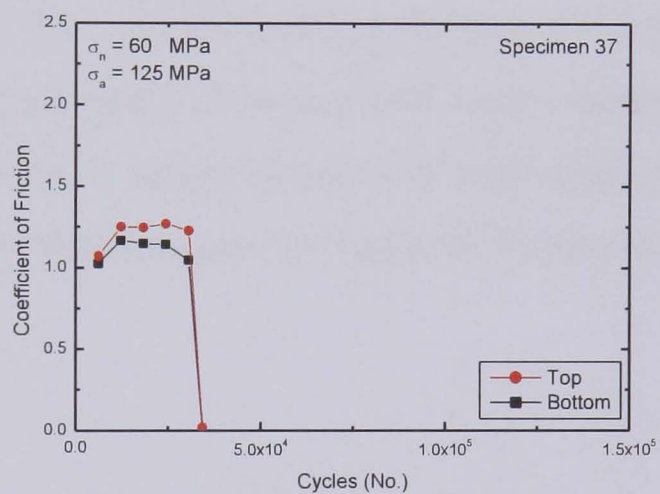
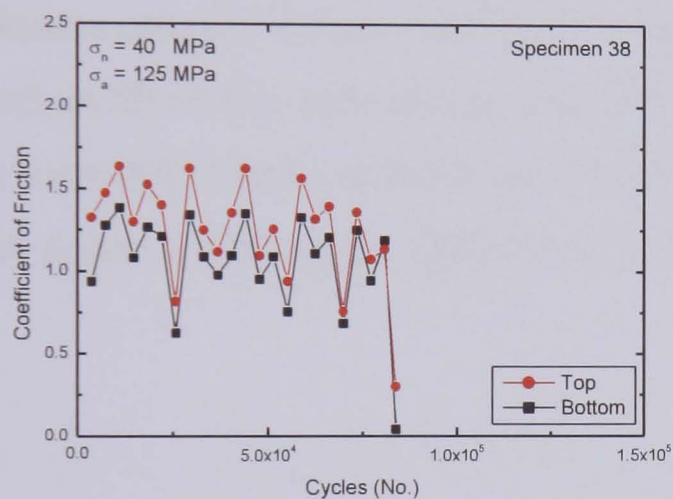
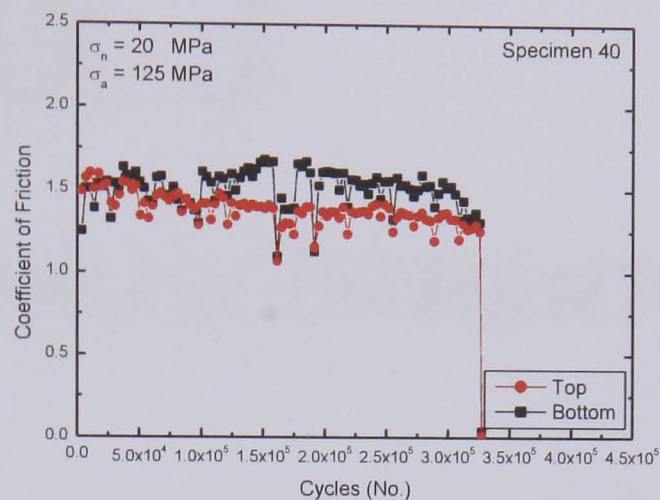
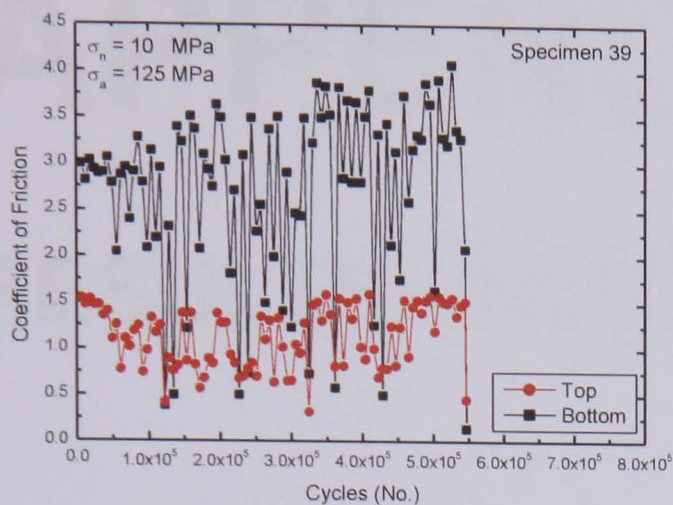
FRICITION COEFFICIENT: $\sigma_a = 100$ MPa unpeened





I.3

FRICITION COEFFICIENT: $\sigma_a = 125$ MPa unpeened



APPENDIX J

RESULTS: SCAR MEASUREMENTS

J.1 UNPEENED: $\sigma_a = 70 \text{ MPa}$

Measurements determined from traces of the fretting scars including: the depth and width of the scar about a base line, the height of peaks that were observed to form either side of the scar, the total peak to valley depth, the total width and the angle of the notch. Definitions of these features can be found in Figure 4.44.

Table J.1a: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 10 MPa and an axial stress amplitude of 70 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
43	10%	Bottom	Left	Back	1.887	0.230	6.255	7.905	9.793	0.928	178
43	10%	Bottom	Left	Front	1.464		0.429	-0.234	1.892	1.905	
43	10%	Bottom	Left	Middle	2.895		-1.034	-1.224	1.860	5.598	
43	10%	Bottom	Right	Back	1.269	0.516	0.784	0.326	2.054	1.509	179
43	10%	Bottom	Right	Front	2.304	1.294	0.756	1.071	3.375	4.760	180
43	10%	Bottom	Right	Middle	1.539		-0.844	0.520	2.059	0.622	
43	10%	Top	Left	Back	3.446		-0.762	15.251	18.697	2.915	
43	10%	Top	Left	Front	0.813		0.455	-0.630	1.269	0.412	
43	10%	Top	Left	Middle	2.817	0.206	7.173	1.000	9.991	0.830	177
43	10%	Top	Right	Back	0.993	0.204	0.807	3.625	4.619	0.906	179
43	10%	Top	Right	Front	1.646	1.429	1.930	0.068	3.576	1.847	180
43	10%	Top	Right	Middle	1.542	0.418	1.227	1.539	3.082	0.956	179
49	25%	Bottom	Left	Back	1.560	1.937	1.143	3.948	5.509	2.543	180
49	25%	Bottom	Left	Front	1.683		0.963	-0.793	2.646	0.618	
49	25%	Bottom	Left	Middle	1.936		0.340	-1.110	2.276	1.130	
49	25%	Bottom	Right	Back	1.266	0.826	0.664	0.956	2.222	2.335	180
49	25%	Bottom	Right	Front	1.718		0.595	-0.369	2.314	1.184	
49	25%	Bottom	Right	Middle	1.905		-1.145	6.003	7.907	0.854	
49	25%	Top	Left	Back	1.216	0.456	1.422	0.876	2.638	1.268	179
49	25%	Top	Left	Front	2.048	1.797	1.979	0.459	4.027	2.211	180
49	25%	Top	Left	Middle	2.740	0.208	1.347	0.952	4.087	0.358	177
49	25%	Top	Right	Back	1.864	0.204	1.199	0.807	3.063	1.278	178
49	25%	Top	Right	Front	2.651	0.310	0.783	2.152	4.803	1.168	178
49	25%	Top	Right	Middle	1.616	1.188	1.499	0.736	3.115	1.839	180
51	50%	Bottom	Left	Back	1.900	2.101	0.062	12.802	14.702	2.961	180
51	50%	Bottom	Left	Front	1.479	0.966	0.921	0.881	2.400	5.104	180
51	50%	Bottom	Left	Middle	1.051	0.792	2.110	1.711	3.161	0.944	180
51	50%	Bottom	Right	Back	3.689	0.414	2.134	1.580	5.823	0.716	178
51	50%	Bottom	Right	Front	2.330		-0.272	7.912	10.242	1.507	
51	50%	Bottom	Right	Middle	2.298	1.212	0.323	7.085	9.383	1.651	180
51	50%	Top	Left	Back	2.385	1.238	0.807	0.855	3.240	2.391	180
51	50%	Top	Left	Front	4.449	0.180	1.527	7.848	12.297	1.122	174
51	50%	Top	Left	Middle	9.538	0.320	11.641	9.524	21.179	0.720	173
51	50%	Top	Right	Back	3.704	0.514	1.110	5.598	9.302	1.421	178
51	50%	Top	Right	Front	1.206	0.920	2.449	0.250	3.655	1.533	180
51	50%	Top	Right	Middle	1.840	0.846	0.922	2.317	4.157	1.238	180
66	75%	Bottom	Left	Back	2.477	0.152	0.610	2.033	4.510	1.549	176
66	75%	Bottom	Left	Front	19.374	1.899	11.902	9.159	31.276	2.919	178
66	75%	Bottom	Left	Middle	20.521	1.641	6.450	3.708	26.971	3.141	177
66	75%	Top	Left	Back	2.971	3.019	1.115	-0.500	4.086	3.533	180
66	75%	Top	Left	Front	41.437	0.382	11.282	16.338	57.775	0.924	156
66	75%	Top	Left	Middle	12.316	0.436	12.362	2.075	24.678	1.463	174
Minimum:					0.813	0.152	-1.145	-1.224	1.269	0.358	156
Maximum:					41.437	3.019	12.362	16.338	57.775	5.598	180

Table J.1b: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 60 MPa and an axial stress amplitude of 70 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
69	10%	Bottom	Left	Back	1.044		-0.635	0.542	1.586	1.240	
69	10%	Bottom	Left	Front	1.445	1.867	0.480	-0.268	1.925	1.415	180
69	10%	Bottom	Left	Middle	1.879	0.788	0.530	0.367	2.409	1.769	179
69	10%	Bottom	Right	Back	1.432	1.008	0.694	0.674	2.126	1.601	180
69	10%	Bottom	Right	Front	2.483	0.632	1.403	7.438	9.921	0.974	179
69	10%	Bottom	Right	Middle	1.133	0.466	1.288	0.879	2.421	0.716	179
69	10%	Top	Left	Back	1.998	0.958	1.184	0.420	3.182	1.687	180
69	10%	Top	Left	Front	1.953	0.570	0.358	0.394	2.347	0.738	179
69	10%	Top	Left	Middle	1.351	1.268	1.262	0.300	2.614	2.459	180
69	10%	Top	Right	Back	1.581	1.851	1.710	-0.066	3.290	1.993	180
69	10%	Top	Right	Front	3.117	0.598	1.186	1.736	4.853	2.013	179
69	10%	Top	Right	Middle	1.683	1.010	0.303	0.909	2.592	1.224	180
68	25%	Bottom	Left	Back	1.989		-0.876	0.817	2.806	1.411	
68	25%	Bottom	Left	Front	1.033	1.030	2.562	1.031	3.595	1.713	180
68	25%	Bottom	Left	Middle	1.258	1.471	1.386	1.416	2.674	2.185	180
68	25%	Bottom	Right	Back	1.605	0.896	0.672	1.491	3.096	1.729	180
68	25%	Bottom	Right	Front	1.281	0.798	0.483	1.112	2.394	1.346	180
68	25%	Bottom	Right	Middle	1.235	1.090	0.374	0.726	1.962	2.065	180
68	25%	Top	Left	Back	1.371	0.714	0.989	0.148	2.359	1.493	180
68	25%	Top	Left	Front	2.489	2.261	0.659	1.011	3.500	4.336	180
68	25%	Top	Left	Middle	1.630		-0.902	0.972	2.603	0.700	
68	25%	Top	Right	Back	1.396	1.739	0.806	1.268	2.663	2.543	180
68	25%	Top	Right	Front	0.837		0.692	-0.118	1.529	1.895	
68	25%	Top	Right	Middle	0.814	0.572	0.146	0.967	1.781	1.054	180
53	50%	Bottom	Left	Back	1.977	1.314	0.935	0.367	2.913	2.501	180
53	50%	Bottom	Left	Front	1.551	1.136	1.809	1.028	3.359	1.971	180
53	50%	Bottom	Left	Middle	1.211	1.296	1.765	0.500	2.976	1.557	180
53	50%	Bottom	Right	Back	1.356	0.200	0.843	4.717	6.073	1.485	178
53	50%	Bottom	Right	Front	1.712	0.368	0.351	0.740	2.452	0.460	179
53	50%	Bottom	Right	Middle	1.295		1.496	-0.306	2.791	1.941	
53	50%	Top	Left	Back	0.830		0.705	-0.075	1.536	1.104	
53	50%	Top	Left	Front	1.210	0.536	1.130	2.161	3.371	1.240	179
53	50%	Top	Left	Middle	1.651	0.220	0.961	1.537	3.188	1.427	178
53	50%	Top	Right	Back	1.217	2.043	1.962	0.001	3.179	2.113	180
53	50%	Top	Right	Front	3.832	1.246	2.149	0.413	5.981	1.859	179
53	50%	Top	Right	Middle	3.212	1.709	1.311	-0.134	4.524	1.885	180
63	75%	Bottom	Left	Back	0.949	0.924	0.542	1.185	2.134	1.873	180
63	75%	Bottom	Left	Front	1.279	0.496	1.908	0.682	3.187	2.351	179
63	75%	Bottom	Left	Middle	1.211	0.500	0.842	1.103	2.314	1.755	179
63	75%	Bottom	Right	Back	1.294		0.573	0.039	1.472	1.268	
63	75%	Bottom	Right	Front	1.476		-0.611	1.433	2.909	0.836	
63	75%	Bottom	Right	Middle	1.645	0.272	1.440	1.252	3.085	1.773	179
63	75%	Top	Left	Back	6.462	0.180	3.665	6.969	13.431	0.490	172
63	75%	Top	Left	Front	1.137	1.088	0.414	1.097	2.234	1.443	180
63	75%	Top	Left	Middle	2.220	0.438	0.816	0.910	3.129	1.767	179
63	75%	Top	Right	Back	2.414	1.228	0.757	3.849	6.262	1.869	180
63	75%	Top	Right	Front	1.985		1.066	-0.007	3.051	0.276	
63	75%	Top	Right	Middle	2.602	0.746	1.895	0.452	4.496	1.304	179
Minimum:					0.814	0.180	-0.902	-0.306	1.472	0.276	172
Maximum:					6.462	2.261	3.665	7.438	13.431	4.336	180

Table J.1c: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024-T351 bridge in contact with an aluminium alloy 2024-T351 specimen subjected to a normal pressure of 100 MPa an axial stress amplitude of 70 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
64	10%	Bottom	Left	Back	5.394	0.202	7.330	1.250	12.724	0.340	174
64	10%	Bottom	Left	Front	1.287	0.796	0.909	1.303	2.590	1.296	180
64	10%	Bottom	Left	Middle	1.783	1.166	0.961	0.244	2.744	1.981	180
64	10%	Bottom	Right	Back	2.806	0.108	2.188	2.235	5.041	0.466	174
64	10%	Bottom	Right	Front	1.840	1.092	1.905	1.319	3.745	1.687	180
64	10%	Bottom	Right	Middle	1.021	0.978	0.518	0.539	1.560	1.871	180
64	10%	Top	Left	Back	1.019	0.276	0.440	0.359	1.459	1.607	179
64	10%	Top	Left	Front	0.996	1.813	0.364	0.570	1.566	4.216	180
64	10%	Top	Left	Middle	1.924		1.760	-0.335	3.684	1.188	
64	10%	Top	Right	Back	1.100	1.595	1.395	0.539	2.496	2.313	180
64	10%	Top	Right	Front	2.040	1.398	1.311	0.679	3.351	2.301	180
64	10%	Top	Right	Middle	1.450	0.330	1.417	0.493	2.867	1.340	179
61	25%	Bottom	Left	Back	1.806		-0.978	1.339	3.145	1.421	
61	25%	Bottom	Left	Front	1.642	1.368	0.839	0.722	2.481	1.897	180
61	25%	Bottom	Left	Middle	1.667	0.760	1.400	0.865	3.067	1.407	179
61	25%	Bottom	Right	Back	2.018		1.198	-0.001	3.216	1.398	
61	25%	Bottom	Right	Front	1.275		0.729	-0.328	2.005	1.372	
61	25%	Bottom	Right	Middle	1.248	0.588	0.618	2.102	3.350	4.336	180
61	25%	Top	Left	Back	2.969	0.610	0.043	1.743	4.712	1.372	179
61	25%	Top	Left	Front	1.208	1.290	0.331	0.588	1.796	4.011	180
61	25%	Top	Left	Middle	1.426	0.528	0.825	1.363	2.789	1.086	179
61	25%	Top	Right	Back	1.397	0.466	0.545	1.289	2.686	1.084	179
61	25%	Top	Right	Front	1.526	0.412	1.662	1.803	3.329	1.132	179
61	25%	Top	Right	Middle	1.652		-0.932	1.082	2.734	1.094	
70	50%	Bottom	Left	Back	1.419	0.668	0.958	1.483	2.902	1.587	180
70	50%	Bottom	Left	Front	1.328	1.471	0.922	0.220	2.251	3.579	180
70	50%	Bottom	Left	Middle	1.461		1.384	-0.280	2.844	1.188	
70	50%	Bottom	Right	Back	1.065	1.172	0.551	0.710	1.775	2.219	180
70	50%	Bottom	Right	Front	3.969	1.362	2.182	2.033	6.151	2.041	179
70	50%	Bottom	Right	Middle	1.765	0.426	1.326	2.192	3.957	1.236	179
70	50%	Top	Left	Back	2.174	1.368	0.762	0.399	2.936	3.551	180
70	50%	Top	Left	Front	1.564	1.575	0.114	1.083	2.646	1.723	180
70	50%	Top	Left	Middle	1.202		-0.645	0.694	1.896	1.298	
70	50%	Top	Right	Back	1.803	1.332	0.948	0.552	2.751	4.404	180
70	50%	Top	Right	Front	1.070	0.382	0.877	0.434	1.947	1.877	179
70	50%	Top	Right	Middle	2.208	1.020	0.938	0.348	3.146	1.162	180
50	75%	Bottom	Left	Back	1.760	0.948	1.042	0.196	2.802	1.775	180
50	75%	Bottom	Left	Front	1.775	1.128	0.854	0.629	2.629	2.125	180
50	75%	Bottom	Left	Middle	1.690	0.706	0.459	0.215	2.149	0.834	179
50	75%	Bottom	Right	Back	1.342	1.002	0.931	0.455	2.273	1.739	180
50	75%	Bottom	Right	Front	1.051	0.668	0.626	0.421	1.678	1.132	180
50	75%	Bottom	Right	Middle	0.990	0.686	0.625	1.635	2.626	1.238	180
50	75%	Top	Left	Back	1.430	0.652	0.365	0.055	1.794	1.497	179
50	75%	Top	Left	Front	1.215	0.966	0.426	0.058	1.641	1.431	180
50	75%	Top	Left	Middle	1.974	0.656	1.240	0.344	3.214	1.843	179
50	75%	Top	Right	Back	2.047	0.420	1.384	0.172	3.431	0.828	179
50	75%	Top	Right	Front	2.517	1.561	6.797	-0.101	9.315	0.750	180
50	75%	Top	Right	Middle	1.196	1.651	0.784	0.599	1.980	1.907	180
Minimum:					0.990	0.108	-0.978	-0.335	1.459	0.340	174
Maximum:					5.394	1.813	7.330	2.235	12.724	4.404	180

J.2 UNPEENED: $\sigma_a = 100 \text{ MPa}$

Table J.2a: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024-T351 bridge in contact with an aluminium alloy 2024-T351 specimen subjected to a normal pressure of 10 MPa and an axial stress amplitude of 100 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
26	10%	Bottom	Left	Back	0.866		-0.265	0.324	1.190	0.954	
26	10%	Bottom	Left	Front	2.401	1.048	2.736	0.024	5.137	1.396	179
26	10%	Bottom	Left	Middle	2.708	0.216	1.730	0.641	4.439	1.485	177
26	10%	Bottom	Right	Back	1.506	1.571	0.776	0.957	2.462	2.277	180
26	10%	Bottom	Right	Front	2.182	1.288	1.210	1.932	4.114	1.951	180
26	10%	Bottom	Right	Middle	1.378	0.698	0.635	2.826	4.205	4.852	180
26	10%	Top	Left	Back	1.531		1.859	-0.131	3.390	1.443	
26	10%	Top	Left	Front	1.497	1.719	0.795	0.929	2.426	3.875	180
26	10%	Top	Left	Middle	2.024	1.178	1.866	0.285	3.889	1.631	180
26	10%	Top	Right	Back	1.171	1.018	1.055	0.558	2.227	2.319	180
26	10%	Top	Right	Front	2.164		-1.218	0.821	2.985	1.499	
26	10%	Top	Right	Middle	3.003	0.182	4.019	1.089	7.022	0.726	176
23	25%	Bottom	Left	Back	0.864	0.882	0.601	0.161	1.465	3.825	180
23	25%	Bottom	Left	Front	7.907	0.814	1.788	3.593	11.500	1.114	178
23	25%	Bottom	Left	Middle	2.084	1.012	0.268	0.368	2.451	1.382	180
23	25%	Bottom	Right	Back	1.047	0.426	1.046	0.796	2.093	0.844	179
23	25%	Bottom	Right	Front	2.240	0.806	0.637	2.775	5.015	2.067	179
23	25%	Bottom	Right	Middle	1.308	1.216	0.579	0.551	1.887	2.029	180
23	25%	Top	Left	Back	1.457	0.556	7.458	0.562	8.915	0.734	179
23	25%	Top	Left	Front	1.848		5.206	-0.079	7.054	2.177	
23	25%	Top	Left	Middle	2.316	0.892	0.935	4.638	6.955	1.533	179
23	25%	Top	Right	Back	2.656		1.679	-0.205	4.335	1.987	
23	25%	Top	Right	Front	9.369	0.398	1.497	10.482	19.851	0.558	175
23	25%	Top	Right	Middle	3.045	0.100	4.782	13.351	16.396	0.310	173
24	50%	Bottom	Left	Back	3.010	1.002	5.318	2.808	8.329	1.663	179
24	50%	Bottom	Left	Front	5.407	0.852	2.018	7.497	12.904	1.747	179
24	50%	Bottom	Left	Middle	3.490	1.368	1.979	0.440	5.470	3.265	179
24	50%	Bottom	Right	Back	0.919	0.552	0.527	0.938	1.857	1.411	180
24	50%	Bottom	Right	Front	4.755	0.676	2.105	11.749	16.504	0.922	178
24	50%	Bottom	Right	Middle	2.261	0.562	8.087	0.131	10.347	1.593	179
24	50%	Top	Left	Back	1.790	0.538	2.096	1.947	3.886	0.904	179
24	50%	Top	Left	Front	1.793	1.258	1.511	2.853	4.647	2.325	180
24	50%	Top	Left	Middle	13.232	0.576	7.445	1.892	20.677	1.435	175
24	50%	Top	Right	Back	1.486	0.300	0.612	1.785	3.271	1.052	179
24	50%	Top	Right	Front	0.947	0.242	0.037	1.727	2.674	0.462	179
24	50%	Top	Right	Middle	2.715	1.098	0.966	3.084	5.799	2.393	179
25	75%	Bottom	Left	Back	1.933		-0.139	1.369	3.302	1.314	
25	75%	Bottom	Left	Front	5.760	1.078	2.596	2.239	8.357	1.535	179
25	75%	Bottom	Left	Middle	17.464	1.220	7.665	2.872	25.128	1.380	177
25	75%	Bottom	Right	Back	5.071	0.600	4.773	1.376	9.844	1.555	178
25	75%	Bottom	Right	Front	7.376	1.236	2.821	5.816	13.193	1.815	179
25	75%	Bottom	Right	Middle	8.320	1.068	17.436	1.699	25.756	1.493	178
25	75%	Top	Left	Back	1.503	0.560	0.830	3.277	4.780	1.148	179
25	75%	Top	Left	Front	14.538	0.248	5.641	8.704	23.242	1.050	167
25	75%	Top	Left	Middle	10.791	0.194	5.196	14.171	24.961	1.370	167
25	75%	Top	Right	Back	1.465	0.832	0.719	0.455	2.184	1.120	180
25	75%	Top	Right	Front	3.012		15.695	-1.737	18.707	1.749	
25	75%	Top	Right	Middle	1.917	0.858	1.179	0.523	3.097	1.122	179
Minimum:					0.864	0.100	-1.218	-1.737	1.190	0.310	167
Maximum:					17.464	1.719	17.436	14.171	25.756	4.852	180

Table J.2b: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 40 MPa and an axial stress amplitude of 100 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
31	10%	Bottom	Left	Back	4.664	0.358	1.083	5.356	10.020	0.618	177
31	10%	Bottom	Left	Front	3.500	1.120	1.616	3.396	6.896	1.621	179
31	10%	Bottom	Left	Middle	4.605	0.158	0.694	2.000	6.605	0.896	173
31	10%	Bottom	Right	Back	2.559	0.126	1.273	5.030	7.588	0.826	175
31	10%	Bottom	Right	Front	1.421	0.356	0.678	0.553	2.099	1.465	179
31	10%	Bottom	Right	Middle	1.557	0.428	0.815	0.786	2.371	1.172	179
31	10%	Top	Left	Back	2.960	2.617	1.884	-0.035	4.844	1.443	180
31	10%	Top	Left	Front	2.582	0.282	6.581	1.183	9.163	0.422	178
31	10%	Top	Left	Middle	1.654	0.274	0.072	1.042	2.696	1.441	179
31	10%	Top	Right	Back	1.844	1.673	0.304	2.320	4.165	2.525	180
31	10%	Top	Right	Front	1.459	1.469	4.370	0.017	5.829	2.375	180
31	10%	Top	Right	Middle	1.019		-0.456	0.804	1.823	1.070	
28	25%	Bottom	Left	Back	3.182		5.409	-0.869	8.591	1.162	
28	25%	Bottom	Left	Front	2.403	2.079	2.005	-0.110	4.408	1.503	180
28	25%	Bottom	Left	Middle	2.104	0.174	0.286	1.923	4.027	1.403	177
28	25%	Bottom	Right	Back	2.694	1.204	4.462	1.966	7.156	1.755	179
28	25%	Bottom	Right	Front	4.391	0.270	2.118	3.239	7.630	0.964	176
28	25%	Bottom	Right	Middle	1.225	1.154	1.039	1.034	2.263	1.603	180
28	25%	Top	Left	Back	4.837	0.950	3.260	0.006	8.097	1.681	179
28	25%	Top	Left	Front	1.931	0.438	1.205	0.503	3.136	0.880	179
28	25%	Top	Left	Middle	7.940	1.102	2.147	9.806	17.746	1.621	178
28	25%	Top	Right	Back	1.455	0.740	0.736	1.207	2.662	2.109	180
28	25%	Top	Right	Front	2.042	1.561	0.721	1.248	3.290	4.093	180
28	25%	Top	Right	Middle	10.597	0.370	3.003	5.424	16.020	1.252	173
29	50%	Bottom	Left	Back	4.817	0.580	3.546	6.997	11.813	1.178	178
29	50%	Bottom	Left	Front	1.827	0.208	0.604	2.290	4.117	0.392	178
29	50%	Bottom	Left	Middle	4.499	0.148	7.920	8.924	13.423	0.938	173
29	50%	Bottom	Right	Back	10.948	0.524	5.129	1.398	16.077	1.034	175
29	50%	Bottom	Right	Front	1.330	1.118	0.570	2.068	3.398	2.149	180
29	50%	Bottom	Right	Middle	2.717	0.170	5.014	0.858	7.731	0.318	176
29	50%	Top	Left	Back	2.294	0.684	2.528	0.969	4.822	1.455	179
29	50%	Top	Left	Front	1.385	0.768	0.430	1.036	2.421	1.531	180
29	50%	Top	Left	Middle	1.676	1.030	1.973	0.992	3.649	1.549	180
29	50%	Top	Right	Back	1.847	1.581	0.146	0.416	2.263	1.901	180
29	50%	Top	Right	Front	1.382	1.425	3.516	0.500	4.898	1.813	180
29	50%	Top	Right	Middle	2.848	0.394	6.305	6.164	9.152	0.570	178
30	75%	Bottom	Left	Back	2.471	1.214	0.671	1.030	3.501	1.701	180
30	75%	Bottom	Left	Front	3.584	0.292	2.011	2.246	5.830	0.428	177
30	75%	Bottom	Left	Middle	2.698		13.665	-0.501	16.362	1.262	
30	75%	Bottom	Right	Back	1.058	0.670	0.981	1.305	2.363	1.831	180
30	75%	Bottom	Right	Front	2.548	1.487	-0.167	2.544	5.092	3.977	180
30	75%	Bottom	Right	Middle	1.294	0.848	0.355	0.405	1.699	1.138	180
30	75%	Top	Left	Back	6.181	0.532	3.216	0.256	9.396	1.162	177
30	75%	Top	Left	Front	2.961	0.140	1.559	4.107	7.069	0.456	175
30	75%	Top	Left	Middle	2.388	1.947	1.804	0.257	4.192	2.397	180
30	75%	Top	Right	Back	2.093	2.113	1.317	0.028	3.410	2.275	180
30	75%	Top	Right	Front	1.296	2.473	0.788	0.491	2.083	4.087	180
30	75%	Top	Right	Middle	1.175	0.462	0.747	0.455	1.922	1.633	179
Minimum:					1.019	0.126	-0.456	-0.869	1.699	0.318	173
Maximum:					10.948	2.617	13.665	9.806	17.746	4.093	180

Table J.2c: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 100 MPa an axial stress amplitude of 100 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
32	10%	Bottom	Left	Back	1.470		3.398	-0.268	4.868	1.801	
32	10%	Bottom	Left	Front	3.655	1.014	5.535	7.886	11.541	1.338	179
32	10%	Bottom	Left	Middle	3.264		1.015	-3.078	4.278	0.148	
32	10%	Bottom	Right	Back	1.478	0.452	0.271	4.116	5.594	1.419	179
32	10%	Bottom	Right	Front	1.246	1.010	1.720	0.191	2.966	1.903	180
32	10%	Bottom	Right	Middle	2.507	0.946	3.807	1.072	6.314	1.286	179
32	10%	Top	Left	Back	1.649	0.230	0.754	2.516	4.165	0.986	178
32	10%	Top	Left	Front	1.106	0.260	1.374	1.036	2.480	1.571	179
32	10%	Top	Left	Middle	2.285	0.848	1.527	1.623	3.908	1.439	179
32	10%	Top	Right	Back	1.869	1.182	0.581	5.392	7.261	3.491	180
32	10%	Top	Right	Front	2.019	0.918	4.830	2.799	6.849	1.338	179
32	10%	Top	Right	Middle	1.820	0.562	1.846	0.213	3.666	0.668	179
33	25%	Bottom	Left	Back	1.291	0.642	1.461	0.468	2.752	0.792	180
33	25%	Bottom	Left	Front	5.336	1.148	3.130	2.766	8.466	1.346	179
33	25%	Bottom	Left	Middle	3.264	1.026	14.774	5.014	18.038	1.284	179
33	25%	Bottom	Right	Back	1.125	0.792	0.763	0.869	1.994	1.302	180
33	25%	Bottom	Right	Front	2.083	0.848	1.442	2.535	4.618	1.338	179
33	25%	Bottom	Right	Middle	5.747	0.744	9.321	5.962	15.068	1.160	178
33	25%	Top	Left	Back	1.824		-0.917	1.474	3.298	1.374	
33	25%	Top	Left	Front	2.142	0.742	1.229	4.449	6.592	2.243	179
33	25%	Top	Left	Middle	1.531	0.152	1.098	2.814	4.345	1.212	178
33	25%	Top	Right	Back	2.297		1.337	-0.555	3.634	1.619	
33	25%	Top	Right	Front	3.720	0.262	1.539	1.206	5.259	1.082	177
33	25%	Top	Right	Middle	7.015	0.218	1.703	9.122	16.137	0.694	173
34	50%	Bottom	Left	Back	1.431	1.086	0.928	0.756	2.359	1.755	180
34	50%	Bottom	Left	Front	2.433	0.854	1.209	0.687	3.643	1.903	179
34	50%	Bottom	Left	Middle	0.951		-0.426	1.441	2.392	1.557	
34	50%	Bottom	Right	Back	5.407	0.174	2.625	15.015	20.422	0.856	173
34	50%	Bottom	Right	Front	1.396		0.580	-0.485	1.976	1.298	
34	50%	Bottom	Right	Middle	1.888	2.001	1.113	-0.357	3.001	1.861	180
34	50%	Top	Left	Back	0.901	0.548	0.344	0.618	1.519	1.386	180
34	50%	Top	Left	Front	2.049		-0.208	1.866	3.915	1.192	
34	50%	Top	Left	Middle	1.709		6.219	-0.374	7.928	1.701	
34	50%	Top	Right	Back	1.873	0.374	0.092	0.335	2.208	0.454	179
34	50%	Top	Right	Front	6.117	0.174	3.629	0.904	9.746	1.052	172
34	50%	Top	Right	Middle	1.354		-0.465	0.423	1.777	1.264	
35	75%	Bottom	Left	Back	5.189	1.597	0.798	6.171	11.361	1.983	179
35	75%	Bottom	Left	Front	4.267	1.507	1.786	6.497	10.764	2.217	179
35	75%	Bottom	Left	Middle	5.310	1.455	1.204	4.966	10.275	2.079	179
35	75%	Bottom	Right	Back	1.703	0.550	1.905	0.712	3.608	0.978	179
35	75%	Bottom	Right	Front	2.817	1.070	1.528	4.134	6.951	2.331	179
35	75%	Bottom	Right	Middle	1.410		0.051	-0.367	1.461	5.598	
35	75%	Top	Left	Back	2.400	1.166	0.867	1.433	3.833	2.215	180
35	75%	Top	Left	Front	3.236	1.691	-0.056	4.354	7.591	1.246	180
35	75%	Top	Left	Middle	2.185		-1.216	1.549	3.734	0.802	
35	75%	Top	Right	Back	1.427	0.590	0.311	0.413	1.839	1.903	179
35	75%	Top	Right	Front	2.164	0.644	4.790	0.552	6.954	1.072	179
35	75%	Top	Right	Middle	3.659	0.682	4.514	0.327	8.173	0.812	179
Minimum:					0.901	0.152	-1.216	-3.078	1.461	0.148	172
Maximum:					7.015	2.001	14.774	15.015	20.422	5.598	180

J.3 UNPEENED: $\sigma_a = 125 \text{ MPa}$

Table J.3a: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 10 MPa and an axial stress amplitude of 125 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
42	10%	Bottom	Left	Back	1.203	0.514	0.547	0.978	2.180	1.575	179
42	10%	Bottom	Left	Front	4.513	0.530	2.589	4.121	8.634	1.511	178
42	10%	Bottom	Left	Middle	23.630	0.372	7.930	6.843	31.560	0.678	166
42	10%	Bottom	Right	Back	1.404	1.026	0.456	0.338	1.859	4.802	180
42	10%	Bottom	Right	Front	3.738	3.361	1.813	-1.224	5.551	3.063	180
42	10%	Bottom	Right	Middle	1.604	0.716	1.351	0.980	2.955	2.199	179
42	10%	Top	Left	Back	2.037	1.565	1.532	4.349	6.386	2.325	180
42	10%	Top	Left	Front	2.701	2.189	0.181	9.910	12.612	2.891	180
42	10%	Top	Left	Middle	15.770	0.494	6.452	3.071	22.222	0.934	173
42	10%	Top	Right	Back	1.010	0.414	0.816	2.378	3.388	1.895	179
42	10%	Top	Right	Front	1.479	1.605	1.286	-0.108	2.765	1.511	180
42	10%	Top	Right	Middle	0.755	1.036	0.529	0.106	1.284	2.445	180
45	25%	Bottom	Left	Back	1.419	0.366	0.472	2.127	3.546	0.586	179
45	25%	Bottom	Left	Front	2.282	1.731	5.399	0.896	7.681	1.947	180
45	25%	Bottom	Left	Middle	13.482	0.648	5.541	5.985	19.466	0.896	175
45	25%	Bottom	Right	Back	2.598	0.476	1.316	6.097	8.695	1.318	179
45	25%	Bottom	Right	Front	2.202		-0.007	-1.211	2.195	1.226	
45	25%	Bottom	Right	Middle	1.165	0.574	1.122	0.110	2.287	1.400	180
45	25%	Top	Left	Back	2.572		2.010	-1.205	4.582	1.238	
45	25%	Top	Left	Front	4.781		26.787	-2.128	31.568	1.749	
45	25%	Top	Left	Middle	15.280	0.742	12.218	2.034	27.498	0.958	175
45	25%	Top	Right	Back	1.577	0.892	0.952	1.564	3.141	2.011	180
45	25%	Top	Right	Front	1.887		0.256	-0.462	2.143	0.682	
45	25%	Top	Right	Middle	1.003	1.667	0.306	0.500	1.504	3.819	180
46	50%	Bottom	Left	Back	3.545	0.434	1.265	7.415	10.960	1.116	178
46	50%	Bottom	Left	Front	1.020	0.868	0.578	0.810	1.830	2.199	180
46	50%	Bottom	Left	Middle	6.104	0.336	5.239	6.859	12.963	1.004	176
46	50%	Bottom	Right	Back	8.995	1.813	0.870	5.645	14.640	2.901	179
46	50%	Bottom	Right	Front	0.761	0.522	0.895	0.283	1.656	1.803	180
46	50%	Bottom	Right	Middle	1.053	1.032	0.617	0.071	1.670	2.385	180
46	50%	Top	Left	Back	1.266		0.688	-0.569	1.953	1.036	
46	50%	Top	Left	Front	1.580	0.438	0.291	0.707	2.287	1.487	179
46	50%	Top	Left	Middle	0.966	0.494	0.363	0.556	1.522	1.587	180
46	50%	Top	Right	Back	1.276	1.645	1.119	4.523	5.799	2.447	180
46	50%	Top	Right	Front	1.068	0.554	0.624	2.371	3.438	1.403	180
46	50%	Top	Right	Middle	1.793	0.350	0.725	1.856	3.648	1.555	179
48	75%	Bottom	Left	Back	3.269	0.748	1.164	4.265	7.534	1.058	179
48	75%	Bottom	Left	Front	10.515	0.400	1.243	14.455	24.970	0.750	174
48	75%	Bottom	Left	Middle	9.323	0.534	1.709	7.160	16.483	1.032	176
48	75%	Bottom	Right	Back	1.886	1.228	0.509	0.339	2.395	3.037	180
48	75%	Bottom	Right	Front	4.698		-0.619	-2.045	4.079	5.598	
48	75%	Bottom	Right	Middle	2.466	0.672	1.004	8.406	10.872	0.854	179
48	75%	Top	Left	Back	2.110	0.242	4.567	3.203	6.677	0.642	178
48	75%	Top	Left	Front	3.521		-1.840	1.588	5.108	1.555	
48	75%	Top	Left	Middle	2.877	1.376	5.244	0.118	8.120	2.277	180
48	75%	Top	Right	Back	3.322	1.925	-0.016	4.525	7.847	0.990	180
48	75%	Top	Right	Front	5.092		-1.751	-2.285	3.342	5.598	
48	75%	Top	Right	Middle	3.157	0.098	4.395	4.338	7.552	0.232	173
Minimum:					0.755	0.098	-1.840	-2.285	1.284	0.232	166
Maximum:					23.630	3.361	26.787	14.455	31.568	5.598	180

Table J.3b: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 60 MPa and an axial stress amplitude of 125 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
67	10%	Bottom	Left	Back	3.038		2.344	-1.680	5.382	1.350	
67	10%	Bottom	Left	Front	1.476	1.427	1.375	0.838	2.851	2.481	180
67	10%	Bottom	Left	Middle	1.077	0.384	0.471	0.747	1.824	0.996	179
67	10%	Bottom	Right	Back	1.370	1.366	1.452	0.157	2.822	2.071	180
67	10%	Bottom	Right	Front	1.940	0.232	1.908	1.389	3.848	0.356	178
67	10%	Bottom	Right	Middle	1.222	0.814	0.593	4.128	5.350	2.101	180
67	10%	Top	Left	Back	1.669	2.055	1.158	0.521	2.827	2.509	180
67	10%	Top	Left	Front	1.263	0.708	0.757	0.197	2.021	1.449	180
67	10%	Top	Left	Middle	1.271	0.748	1.508	0.808	2.779	1.849	180
67	10%	Top	Right	Back	1.799	2.355	0.102	1.025	2.824	4.544	180
67	10%	Top	Right	Front	3.109	1.156	4.875	2.245	7.984	1.435	179
67	10%	Top	Right	Middle	1.438	0.368	1.314	0.545	2.751	1.613	179
52	25%	Bottom	Left	Back	1.296		-0.603	0.123	1.419	1.352	
52	25%	Bottom	Left	Front	1.332	0.514	0.547	1.138	2.470	2.083	179
52	25%	Bottom	Left	Middle	0.969	1.040	0.207	0.508	1.477	1.939	180
52	25%	Bottom	Right	Back	2.107	1.771	-0.183	1.403	3.511	1.250	180
52	25%	Bottom	Right	Front	3.454	2.701	1.367	-0.110	4.821	3.943	180
52	25%	Bottom	Right	Middle	1.313	1.086	0.704	0.252	2.017	1.617	180
52	25%	Top	Left	Back	2.430	0.202	3.596	4.635	7.064	0.664	177
52	25%	Top	Left	Front	0.648	0.666	0.479	0.083	1.127	1.276	180
52	25%	Top	Left	Middle	1.055	0.082	3.398	3.470	4.525	0.624	177
52	25%	Top	Right	Back	14.921	0.664	6.656	5.616	21.577	1.595	175
52	25%	Top	Right	Front	1.332	1.411	2.051	0.409	3.383	1.683	180
52	25%	Top	Right	Middle	2.162		0.685	-0.623	2.847	0.978	
47	50%	Bottom	Left	Back	1.098	0.634	0.725	1.093	2.191	1.513	180
47	50%	Bottom	Left	Front	8.781	0.224	9.978	3.351	18.759	1.376	171
47	50%	Bottom	Left	Middle	2.280	0.154	3.750	3.942	6.222	0.798	177
47	50%	Bottom	Right	Back	0.931		0.695	-0.366	1.626	1.308	
47	50%	Bottom	Right	Front	2.175	0.180	4.467	2.762	6.643	0.356	177
47	50%	Bottom	Right	Middle	5.458	0.336	3.499	1.347	8.956	0.566	176
47	50%	Top	Left	Back	1.414	0.098	1.921	1.357	3.335	0.246	177
47	50%	Top	Left	Front	0.841	1.042	0.486	0.172	1.327	1.449	180
47	50%	Top	Left	Middle	1.105	1.553	0.888	0.208	1.993	1.947	180
47	50%	Top	Right	Back	2.648		1.810	-0.459	4.458	1.715	
47	50%	Top	Right	Front	2.095	1.649	-0.138	6.900	8.995	2.825	180
47	50%	Top	Right	Middle	6.821	0.124	10.166	8.703	16.987	0.320	167
60	75%	Bottom	Left	Back	1.512		-0.680	0.055	1.567	1.455	
60	75%	Bottom	Left	Front	1.816	1.102	6.309	0.562	8.125	1.531	180
60	75%	Bottom	Left	Middle	1.433		-0.387	0.885	2.318	1.018	
60	75%	Bottom	Right	Back	1.791	1.553	1.004	0.407	2.795	2.481	180
60	75%	Bottom	Right	Front	1.423	1.252	1.772	0.922	3.195	1.907	180
60	75%	Bottom	Right	Middle	0.727	0.522	0.290	1.070	1.796	1.623	180
60	75%	Top	Left	Back	7.292	0.558	3.209	4.512	11.804	0.928	177
60	75%	Top	Left	Front	2.924	1.248	0.868	7.256	10.180	1.671	179
60	75%	Top	Left	Middle	1.618	1.507	1.244	0.360	2.863	1.943	180
60	75%	Top	Right	Back	3.106	0.388	0.521	12.388	15.494	1.086	178
60	75%	Top	Right	Front	3.003	1.771	1.560	6.988	9.991	2.433	180
60	75%	Top	Right	Middle	2.490	1.675	1.157	0.851	3.647	2.217	180
Minimum:					0.648	0.082	-0.680	-1.680	1.127	0.246	167
Maximum:					14.921	2.701	10.166	12.388	21.577	4.544	180

Table J.3c: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with an aluminium alloy 2024 T351 specimen subjected to a normal pressure of 100 MPa an axial stress amplitude of 125 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
65	10%	Bottom	Left	Back	2.537		-1.193	1.130	3.667	1.449	
65	10%	Bottom	Left	Front	2.079		1.217	-1.127	3.296	0.794	
65	10%	Bottom	Left	Middle	2.736	3.133	1.300	-0.620	4.036	3.873	180
65	10%	Bottom	Right	Back	1.691		-0.703	0.868	2.559	1.082	
65	10%	Bottom	Right	Front	2.114	1.593	3.783	-0.052	5.897	1.749	180
65	10%	Bottom	Right	Middle	5.662	0.328	4.099	3.238	9.761	0.888	176
65	10%	Top	Left	Back	1.960		1.199	-1.047	3.159	1.016	
65	10%	Top	Left	Front	0.972	1.072	0.482	0.580	1.552	2.353	180
65	10%	Top	Left	Middle	1.156		-0.001	1.476	2.633	1.423	
65	10%	Top	Right	Back	3.157	2.627	1.077	-1.402	4.233	2.375	180
65	10%	Top	Right	Front	3.086		-1.442	0.845	3.931	1.216	
65	10%	Top	Right	Middle	1.446	1.096	0.290	0.565	2.011	1.579	180
44	25%	Bottom	Left	Back	0.797	0.302	0.440	1.035	1.831	0.430	179
44	25%	Bottom	Left	Front	6.425	0.402	4.031	2.846	10.456	0.934	176
44	25%	Bottom	Left	Middle	1.287		-0.347	0.842	2.129	0.962	
44	25%	Bottom	Right	Back	1.805	0.600	1.328	0.410	3.133	1.779	179
44	25%	Bottom	Right	Front	1.430		-0.799	1.127	2.558	1.230	
44	25%	Bottom	Right	Middle	1.663	2.641	-0.034	0.941	2.604	2.041	180
44	25%	Top	Left	Back	6.379	0.370	0.755	5.031	11.410	1.545	176
44	25%	Top	Left	Front	1.464	1.985	0.602	1.803	3.267	3.473	180
44	25%	Top	Left	Middle	1.543	1.619	0.213	0.739	2.282	3.547	180
44	25%	Top	Right	Back	1.040		0.066	-0.191	1.106	1.302	
44	25%	Top	Right	Front	2.172		0.573	-0.640	2.745	1.234	
44	25%	Top	Right	Middle	1.725		0.805	-0.760	2.530	1.539	
62	50%	Bottom	Left	Back	1.652	0.506	2.099	0.523	3.751	0.738	179
62	50%	Bottom	Left	Front	3.017	1.967	1.622	2.348	5.365	2.291	180
62	50%	Bottom	Left	Middle	3.969	0.476	2.853	3.310	7.280	0.918	178
62	50%	Bottom	Right	Back	1.386	1.270	3.125	1.174	4.510	1.835	180
62	50%	Bottom	Right	Front	1.355	1.220	0.456	2.121	3.477	3.615	180
62	50%	Bottom	Right	Middle	1.900		-1.300	1.866	3.766	1.314	
62	50%	Top	Left	Back	4.035	0.988	3.016	0.447	7.051	1.394	179
62	50%	Top	Left	Front	2.112	0.988	0.498	1.029	3.141	4.149	180
62	50%	Top	Left	Middle	6.084	0.886	0.840	4.733	10.817	1.338	178
62	50%	Top	Right	Back	1.908	1.609	3.899	0.048	5.807	2.049	180
62	50%	Top	Right	Front	5.681	0.462	3.632	14.864	20.545	0.676	177
62	50%	Top	Right	Middle	3.193	0.142	6.895	3.297	10.088	0.452	175
71	75%	Bottom	Left	Back	1.950	1.128	1.002	2.851	4.801	2.699	180
71	75%	Bottom	Left	Front	2.599	0.688	2.009	11.141	13.740	1.294	179
71	75%	Bottom	Left	Middle	1.607		-0.305	0.822	2.429	1.312	
71	75%	Bottom	Right	Back	1.959		-0.664	0.929	2.888	1.204	
71	75%	Bottom	Right	Front	1.951	0.258	3.904	2.328	5.856	0.918	178
71	75%	Bottom	Right	Middle	1.189	1.078	0.564	1.250	2.439	1.771	180
71	75%	Top	Left	Back	1.842	0.886	0.959	0.978	2.820	1.843	180
71	75%	Top	Left	Front	1.905	0.982	4.930	0.501	6.835	2.033	180
71	75%	Top	Left	Middle	2.630	0.132	2.627	3.981	6.610	0.312	175
71	75%	Top	Right	Back	4.337	0.930	2.777	0.569	7.114	1.364	179
71	75%	Top	Right	Front	1.909	0.472	0.628	1.817	3.726	1.473	179
71	75%	Top	Right	Middle	1.127		0.784	-0.075	1.910	1.439	
Minimum:					0.797	0.132	-1.442	-1.402	1.106	0.312	175
Maximum:					6.425	3.133	6.895	14.864	20.545	4.149	180

J.4 PEENED: $\sigma_a = 70$ MPa

Table J.4a: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 10 MPa and an axial stress amplitude of 70 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
15P	10%	Bottom	Left	Back	9.74	0.22	10.51	6.00	20.250	0.678	170
15P	10%	Bottom	Left	Front	8.18	0.36	5.62	11.84	20.015	1.423	175
15P	10%	Bottom	Left	Middle	10.603	0.680	8.012	6.525	18.615	0.924	176
15P	10%	Bottom	Right	Back	6.57	0.63	3.28	6.25	12.816	0.948	178
15P	10%	Bottom	Right	Front	14.20	0.39	7.16	3.16	21.356	0.542	172
15P	10%	Bottom	Right	Middle	9.208		-6.135	4.206	13.413	0.570	
15P	10%	Top	Left	Back	9.66	0.55	7.03	1.97	16.686	1.268	176
15P	10%	Top	Left	Front	9.92	0.23	7.76	8.45	18.369	0.688	170
15P	10%	Top	Left	Middle	9.692	0.198	26.921	2.524	36.613	1.186	169
15P	10%	Top	Right	Back	8.93	0.69	3.89	6.88	15.809	2.543	177
15P	10%	Top	Right	Front	9.45	0.31	6.18	5.10	15.629	2.129	173
15P	10%	Top	Right	Middle	8.517	0.602	2.109	5.454	13.971	1.473	177
27P	25%	Bottom	Left	Back	9.34	0.78	11.32	4.82	20.658	1.893	177
27P	25%	Bottom	Left	Front	13.21	0.28	7.86	9.42	22.630	0.932	169
27P	25%	Bottom	Left	Middle	10.844	0.452	8.394	5.830	19.238	1.256	175
27P	25%	Bottom	Right	Back	11.75	0.24	14.25	2.01	26.003	0.724	169
27P	25%	Bottom	Right	Front	8.41	0.50	10.31	5.26	18.718	1.134	176
27P	25%	Bottom	Right	Middle	8.086	0.218	9.391	2.949	17.478	1.591	172
27P	25%	Top	Left	Back	13.94	0.47	7.88	14.20	28.143	1.633	173
27P	25%	Top	Left	Front	8.73	0.28	6.40	5.18	15.127	0.506	173
27P	25%	Top	Left	Middle	12.860	0.488	13.861	7.368	26.722	1.312	174
27P	25%	Top	Right	Back	11.07	0.36	7.82	5.00	18.888	0.962	173
27P	25%	Top	Right	Front	11.09	0.50	9.98	7.79	21.063	1.210	175
27P	25%	Top	Right	Middle	17.696	0.674	6.872	8.296	25.992	1.455	174
20P	75%	Bottom	Left	Back	11.45	0.65	7.24	7.35	18.793	2.351	176
20P	75%	Bottom	Left	Front	8.21	0.26	9.07	8.46	17.286	0.460	173
20P	75%	Bottom	Left	Middle	11.787	0.356	8.600	13.456	25.244	0.604	172
20P	75%	Bottom	Right	Back	9.13	0.45	8.23	1.36	17.363	1.156	175
20P	75%	Bottom	Right	Front	9.06		-3.02	8.68	17.734	0.482	
20P	75%	Bottom	Right	Middle	11.429	0.472	5.046	6.023	17.452	1.701	174
20P	75%	Top	Left	Back	8.36	0.71	6.90	8.04	16.405	1.943	177
20P	75%	Top	Left	Front	12.27	0.47	9.50	1.67	21.775	1.224	174
20P	75%	Top	Left	Middle	9.060	0.668	4.367	7.237	16.297	1.198	177
20P	75%	Top	Right	Back	11.84	0.48	5.53	10.11	21.943	1.583	174
20P	75%	Top	Right	Front	8.70	0.24	9.96	9.30	18.659	1.244	172
20P	75%	Top	Right	Middle	12.018	0.300	6.090	9.332	21.349	1.919	171
Minimum:					6.57	0.20	-6.13	1.36	12.82	0.46	169
Maximum:					17.70	0.78	26.92	14.20	36.61	2.54	178

Table J.4b: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 60 MPa and an axial stress amplitude of 70 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
32P	10%	Bottom	Left	Back	12.59	0.94	5.60	12.41	24.994	1.947	177
32P	10%	Bottom	Left	Front	14.15	0.42	7.51	5.34	21.663	1.064	172
32P	10%	Bottom	Left	Middle	8.046	0.398	10.037	7.859	18.083	1.727	175
32P	10%	Bottom	Right	Back	8.08	0.32	2.42	5.20	13.284	1.421	174
32P	10%	Bottom	Right	Front	12.64	0.38	8.86	5.96	21.502	1.811	172
32P	10%	Bottom	Right	Middle	11.367	0.322	3.392	8.211	19.578	0.504	172
32P	10%	Top	Left	Back	7.86	0.20	4.67	4.83	12.693	1.258	171
32P	10%	Top	Left	Front	10.20		-0.13	4.37	14.573	1.000	
32P	10%	Top	Left	Middle	13.183	0.348	3.314	9.151	22.334	2.869	171
32P	10%	Top	Right	Back	9.62	0.64	10.43	3.96	20.043	1.128	177
32P	10%	Top	Right	Front	10.07	0.54	7.67	4.86	17.736	1.725	176
32P	10%	Top	Right	Middle	9.585	0.482	6.267	10.246	19.831	1.142	175
18P	25%	Bottom	Left	Back	10.98	0.35	16.60	7.53	27.582	2.313	173
18P	25%	Bottom	Left	Front	11.08	0.71	5.76	4.20	16.840	2.515	176
18P	25%	Bottom	Left	Middle	10.735	0.306	5.314	12.519	23.254	1.152	172
18P	25%	Bottom	Right	Back	13.20		11.18	-7.67	24.377	0.722	
18P	25%	Bottom	Right	Front	26.55		-14.62	57.03	83.576	1.156	
18P	25%	Bottom	Right	Middle	9.778	1.050	5.961	7.695	17.473	1.897	178
18P	25%	Top	Left	Back	8.32	0.49	6.04	10.05	18.368	1.010	176
18P	25%	Top	Left	Front	11.25	0.51	13.77	6.15	25.023	1.829	175
18P	25%	Top	Left	Middle	7.750	0.522	7.328	5.600	15.078	1.252	177
18P	25%	Top	Right	Back	9.40	0.39	10.67	6.09	20.065	1.531	174
18P	25%	Top	Right	Front	12.96	0.49	13.47	3.81	26.437	0.956	174
18P	25%	Top	Right	Middle	7.209		-2.650	8.234	15.442	0.414	
14P	50%	Bottom	Left	Back	4.77	0.67	4.58	7.61	12.375	1.549	178
14P	50%	Bottom	Left	Front	9.06	0.81	3.53	5.88	14.942	0.974	177
14P	50%	Bottom	Left	Middle	13.591	0.570	5.468	4.120	19.059	1.673	175
14P	50%	Bottom	Right	Back	9.95	0.58	5.41	3.98	15.359	1.296	176
14P	50%	Bottom	Right	Front	10.11	0.39	6.17	3.53	16.285	1.292	174
14P	50%	Bottom	Right	Middle	9.123	0.388	5.554	6.668	15.791	1.382	175
14P	50%	Top	Left	Back	8.76	0.41	10.04	6.41	18.794	0.800	175
14P	50%	Top	Left	Front	9.16	0.29	10.03	8.76	19.198	1.805	173
14P	50%	Top	Left	Middle	15.731	0.686	2.208	6.492	22.224	1.130	175
14P	50%	Top	Right	Back	11.10	0.48	7.77	9.71	20.810	1.140	175
14P	50%	Top	Right	Front	9.66	0.48	6.54	5.95	16.209	0.972	175
14P	50%	Top	Right	Middle	16.357	0.716	10.032	5.014	26.389	1.266	175
Minimum:					4.77	0.20	-14.62	-7.67	12.38	0.41	171
Maximum:					26.55	1.05	16.60	57.03	83.58	2.87	178

Table J.4c: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 100 MPa an axial stress amplitude of 70 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
43P	10%	Bottom	Left	Back	10.83	0.23	2.33	5.91	16.741	0.390	169
43P	10%	Bottom	Left	Front	9.44	0.39	5.00	9.51	18.944	1.272	175
43P	10%	Bottom	Left	Middle	13.128	0.582	7.504	6.599	20.632	1.755	175
43P	10%	Bottom	Right	Back	7.92	0.30	7.02	8.79	16.709	1.973	174
43P	10%	Bottom	Right	Front	8.36	0.32	7.47	6.05	15.829	1.056	174
43P	10%	Bottom	Right	Middle	9.511	0.396	5.281	9.687	19.199	0.796	174
43P	10%	Top	Left	Back	7.13	0.70	4.48	7.15	14.273	0.934	178
43P	10%	Top	Left	Front	8.97	0.20	7.87	7.24	16.843	1.703	170
43P	10%	Top	Left	Middle	7.668	0.244	7.082	5.943	14.751	1.421	173
43P	10%	Top	Right	Back	9.80	0.68	1.71	9.71	19.508	0.942	177
43P	10%	Top	Right	Front	9.27	0.25	7.25	7.11	16.522	2.391	172
43P	10%	Top	Right	Middle	9.487	0.236	10.790	8.471	20.277	0.498	171
19P	25%	Bottom	Left	Back	9.51	0.36	3.75	4.45	13.953	1.174	174
19P	25%	Bottom	Left	Front	16.21	0.32	10.28	5.22	26.491	0.826	168
19P	25%	Bottom	Left	Middle	8.716	0.610	11.330	5.831	20.046	1.747	177
19P	25%	Bottom	Right	Back	7.90	0.27	6.66	2.30	14.565	0.762	173
19P	25%	Bottom	Right	Front	9.09	0.49	8.88	7.84	17.972	1.709	176
19P	25%	Bottom	Right	Middle	11.211	0.938	12.669	5.235	23.880	1.543	177
19P	25%	Top	Left	Back	8.47	0.58	0.79	5.09	13.557	1.773	177
19P	25%	Top	Left	Front	11.79	0.28	4.91	8.21	20.001	0.530	170
19P	25%	Top	Left	Middle	8.732	0.244	6.152	11.377	20.109	1.585	172
19P	25%	Top	Right	Back	13.68	0.87	8.16	12.44	26.119	2.493	176
19P	25%	Top	Right	Front	12.08	0.42	12.97	8.60	25.050	1.304	173
19P	25%	Top	Right	Middle	9.179	0.274	4.076	7.477	16.656	1.044	172
26P	50%	Bottom	Left	Back	13.05	0.91	7.63	4.55	20.680	1.735	177
26P	50%	Bottom	Left	Front	8.96	0.52	3.04	5.97	14.937	0.850	176
26P	50%	Bottom	Left	Middle	18.218	0.530	7.209	4.961	25.427	1.895	172
26P	50%	Bottom	Right	Back	10.07	0.37	5.48	10.60	20.665	0.626	174
26P	50%	Bottom	Right	Front	8.02	0.53	7.93	5.45	15.956	1.809	177
26P	50%	Bottom	Right	Middle	12.988	0.276	6.415	4.278	19.403	0.758	169
26P	50%	Top	Left	Back	11.14	0.66	10.55	6.26	21.692	1.611	176
26P	50%	Top	Left	Front	7.25	0.45	10.54	4.86	17.794	0.880	176
26P	50%	Top	Left	Middle	10.811	0.576	5.198	6.103	16.915	2.357	176
26P	50%	Top	Right	Back	10.12	0.27	4.74	5.54	15.662	1.919	171
26P	50%	Top	Right	Front	9.81	0.36	6.00	7.70	17.511	0.606	174
26P	50%	Top	Right	Middle	6.710	0.420	8.404	3.024	15.115	1.437	176
28P	75%	Bottom	Left	Back	11.60	0.26	4.70	6.12	17.713	0.480	170
28P	75%	Bottom	Left	Front	10.82	0.52	6.36	6.68	17.501	1.587	175
28P	75%	Bottom	Left	Middle	9.455	0.688	10.777	6.784	20.232	1.565	177
28P	75%	Bottom	Right	Back	7.11	0.69	6.53	3.47	13.637	1.160	178
28P	75%	Bottom	Right	Front	12.01	0.53	4.31	7.38	19.385	1.380	175
28P	75%	Bottom	Right	Middle	17.388	0.332	10.585	5.949	27.972	1.773	168
28P	75%	Top	Left	Back	7.86	0.24	4.36	11.45	19.315	0.802	172
28P	75%	Top	Left	Front	11.27	0.41	6.19	7.23	18.500	1.018	174
28P	75%	Top	Left	Middle	10.616	0.666	1.884	9.470	20.086	1.342	176
28P	75%	Top	Right	Back	8.70	0.32	6.05	9.05	17.745	1.220	174
28P	75%	Top	Right	Front	12.61	1.07	4.62	9.79	22.402	1.783	177
28P	75%	Top	Right	Middle	10.228	0.510	7.424	5.872	17.652	1.220	175
Minimum:					6.71	0.20	0.79	2.30	13.56	0.39	168
Maximum:					18.22	1.07	12.97	12.44	27.97	2.49	178

J.5 PEENED: $\sigma_a = 100 \text{ MPa}$

Table J.5a: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 10 MPa and an axial stress amplitude of 100 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
45P	10%	Bottom	Left	Back	11.228	0.324	2.576	7.196	18.423	1.154	172
45P	10%	Bottom	Left	Front	9.585	0.260	7.121	5.634	16.707	0.530	172
45P	10%	Bottom	Left	Middle	9.232	0.322	4.825	10.963	20.195	0.608	173
45P	10%	Bottom	Right	Back	9.522	0.292	4.765	10.451	19.974	0.810	173
45P	10%	Bottom	Right	Front	10.315		5.612	-5.794	15.927	1.150	
45P	10%	Bottom	Right	Middle	8.901	0.446	10.092	4.103	18.993	0.720	175
45P	10%	Top	Left	Back	10.037	0.216	8.854	7.959	18.891	0.430	169
45P	10%	Top	Left	Front	20.058	0.740	7.775	8.778	28.836	1.643	174
45P	10%	Top	Left	Middle	7.042	0.368	9.475	8.098	16.516	1.463	176
45P	10%	Top	Right	Back	10.004	0.600	7.551	1.719	17.555	1.258	176
45P	10%	Top	Right	Front	9.507	0.356	4.885	6.634	16.141	0.956	174
45P	10%	Top	Right	Middle	9.529	0.386	6.800	4.832	16.329	1.142	174
22P	25%	Bottom	Left	Back	14.061	0.296	7.432	10.481	24.542	1.170	169
22P	25%	Bottom	Left	Front	11.348	0.272	12.818	11.635	24.165	0.940	170
22P	25%	Bottom	Left	Middle	11.071	0.306	6.472	5.945	17.543	1.545	172
22P	25%	Bottom	Right	Back	6.976	0.440	4.155	7.130	14.106	0.662	176
22P	25%	Bottom	Right	Front	8.877		12.036	-5.639	20.913	0.764	
22P	25%	Bottom	Right	Middle	14.781	0.364	8.719	7.228	23.501	1.675	171
22P	25%	Top	Left	Back	9.549	0.754	9.839	5.769	19.388	1.376	177
22P	25%	Top	Left	Front	8.936	0.412	7.334	10.772	19.708	1.869	175
22P	25%	Top	Left	Middle	13.908	0.558	3.834	8.315	22.223	1.549	174
22P	25%	Top	Right	Back	10.650		6.979	-1.029	17.629	1.114	
22P	25%	Top	Right	Front	9.393	0.564	8.405	0.965	17.798	1.164	176
22P	25%	Top	Right	Middle	9.333		5.489	-0.966	14.822	1.336	
12P	50%	Bottom	Left	Back	9.310	0.296	10.154	7.028	19.464	1.747	173
12P	50%	Bottom	Left	Front	10.069	0.470	8.908	7.273	18.977	1.038	175
12P	50%	Bottom	Left	Middle	7.620	0.416	6.196	4.293	13.815	1.108	176
12P	50%	Bottom	Right	Back	10.573	1.403	10.604	2.118	21.176	2.421	178
12P	50%	Bottom	Right	Front	7.173	0.970	4.217	8.499	15.672	1.585	178
12P	50%	Bottom	Right	Middle	10.666	0.234	4.759	7.570	18.236	0.542	170
12P	50%	Top	Left	Back	8.904	0.646	0.789	6.149	15.053	1.182	177
12P	50%	Top	Left	Front	14.435	0.792	6.663	3.733	21.098	0.968	176
12P	50%	Top	Left	Middle	7.298	0.230	12.253	4.575	19.551	1.631	173
12P	50%	Top	Right	Back	13.078	0.278	7.293	8.852	21.930	1.931	169
12P	50%	Top	Right	Front	12.096	0.246	6.706	7.641	19.737	1.605	169
12P	50%	Top	Right	Middle	9.766	0.258	4.316	7.121	16.887	1.717	171
Minimum:					6.98	0.22	0.79	-5.79	13.82	0.43	169
Maximum:					20.06	1.40	12.82	11.63	28.84	2.42	178

Table J.5b: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 40 MPa and an axial stress amplitude of 100 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
17P	10%	Bottom	Left	Back	17.381	0.582	8.658	8.358	26.039	1.411	173
17P	10%	Bottom	Left	Front	10.044	0.262	6.169	8.055	18.100	0.462	171
17P	10%	Bottom	Left	Middle	13.852	0.540	3.301	4.846	18.698	2.493	174
17P	10%	Bottom	Right	Back	11.392	0.548	6.464	11.138	22.529	1.819	175
17P	10%	Bottom	Right	Front	7.590		5.168	-4.556	12.757	0.938	
17P	10%	Bottom	Right	Middle	7.145	0.440	3.335	6.624	13.770	1.338	176
17P	10%	Top	Left	Back	11.491	0.424	7.273	5.195	18.764	0.688	174
17P	10%	Top	Left	Front	8.855	0.396	9.350	5.116	18.205	1.455	175
17P	10%	Top	Left	Middle	11.869	0.862	11.068	3.673	22.937	1.413	177
17P	10%	Top	Right	Back	9.130		10.731	-0.795	19.861	0.974	
17P	10%	Top	Right	Front	24.052	0.200	6.236	12.244	36.296	0.896	153
17P	10%	Top	Right	Middle	12.123	0.914	4.756	2.155	16.878	1.110	177
34P	50%	Bottom	Left	Back	10.422	0.236	6.415	5.481	16.837	1.977	170
34P	50%	Bottom	Left	Front	9.998	0.290	11.913	0.985	21.911	1.977	172
34P	50%	Bottom	Left	Middle	8.453	0.584	7.870	6.928	16.323	1.719	177
34P	50%	Bottom	Right	Back	9.697	0.324	5.390	10.138	19.835	0.984	173
34P	50%	Bottom	Right	Front	7.581	0.528	8.316	8.771	16.352	1.437	177
34P	50%	Bottom	Right	Middle	15.349	0.230	7.944	16.850	32.200	0.834	165
34P	50%	Top	Left	Back	8.844	0.700	6.027	8.607	17.450	1.597	177
34P	50%	Top	Left	Front	10.704		10.735	-0.455	21.439	0.998	
34P	50%	Top	Left	Middle	10.610	0.424	6.094	4.567	16.704	1.673	174
34P	50%	Top	Right	Back	11.559	0.356	12.766	4.058	24.326	2.469	173
34P	50%	Top	Right	Front	8.045	0.312	0.666	5.288	13.333	1.517	174
34P	50%	Top	Right	Middle	7.595	0.320	1.547	7.982	15.577	1.571	175
29P	75%	Bottom	Left	Back	9.233	0.410	6.405	6.405	15.638	1.681	175
29P	75%	Bottom	Left	Front	9.611	0.234	6.033	5.144	15.643	1.651	171
29P	75%	Bottom	Left	Middle	9.606	0.358	6.296	7.024	16.629	0.832	174
29P	75%	Bottom	Right	Back	14.257	0.226	7.740	9.710	23.966	0.652	166
29P	75%	Bottom	Right	Front	8.931	0.258	3.788	8.065	16.996	1.178	172
29P	75%	Bottom	Right	Middle	15.359	0.710	9.423	9.751	25.109	1.559	175
29P	75%	Top	Left	Back	9.003	0.236	6.358	4.008	15.362	1.222	171
29P	75%	Top	Left	Front	9.050	0.388	7.965	8.499	17.548	0.706	175
29P	75%	Top	Left	Middle	9.110	0.492	7.202	4.260	16.312	1.481	176
29P	75%	Top	Right	Back	8.994		-0.142	8.743	17.737	0.700	
29P	75%	Top	Right	Front	10.401	0.544	6.867	6.577	17.267	1.348	176
29P	75%	Top	Right	Middle	9.470	0.306	9.391	3.690	18.861	1.306	173
Minimum:					7.15	0.20	-0.14	-4.56	12.76	0.46	153
Maximum:					24.05	0.91	12.77	16.85	36.30	2.49	177

Table J.5c: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 100 MPa an axial stress amplitude of 100 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
16P	10%	Bottom	Left	Back	7.934		3.930	-4.410	11.864	0.574	
16P	10%	Bottom	Left	Front	12.872	0.400	6.646	3.143	19.518	1.731	173
16P	10%	Bottom	Left	Middle	6.835	0.354	9.056	4.223	15.891	0.712	176
16P	10%	Bottom	Right	Back	9.846	0.302	7.786	4.960	17.632	1.619	173
16P	10%	Bottom	Right	Front	8.541		8.649	-3.530	17.190	1.194	
16P	10%	Bottom	Right	Middle	7.308	0.598	5.031	8.223	15.531	2.087	177
16P	10%	Top	Left	Back	10.774	0.784	7.471	5.800	18.246	1.054	177
16P	10%	Top	Left	Front	11.133	0.266	9.456	5.417	20.590	1.142	170
16P	10%	Top	Left	Middle	14.168	0.462	9.138	10.204	24.372	1.198	173
16P	10%	Top	Right	Back	12.363	0.832	6.526	2.078	18.889	1.577	177
16P	10%	Top	Right	Front	11.507		-6.198	8.681	20.188	0.982	
16P	10%	Top	Right	Middle	10.197	0.650	10.520	0.145	20.717	0.798	176
39P	50%	Bottom	Left	Back	10.230	0.558	6.360	4.248	16.590	1.324	176
39P	50%	Bottom	Left	Front	8.464	0.276	6.704	5.250	15.169	1.134	173
39P	50%	Bottom	Left	Middle	9.074	0.580	2.786	6.255	15.329	1.378	176
39P	50%	Bottom	Right	Back	15.188	0.586	4.609	5.116	20.304	1.575	174
39P	50%	Bottom	Right	Front	11.824		3.143	-1.299	14.966	1.212	
39P	50%	Bottom	Right	Middle	9.347	0.414	2.099	7.502	16.849	1.411	175
39P	50%	Top	Left	Back	10.901	0.468	7.563	5.455	18.465	1.751	175
39P	50%	Top	Left	Front	10.237	0.962	9.617	5.219	19.854	1.751	178
39P	50%	Top	Left	Middle	11.638	0.424	7.369	4.720	19.007	2.309	174
39P	50%	Top	Right	Back	12.189	0.764	10.740	6.736	22.929	1.543	176
39P	50%	Top	Right	Front	6.817	1.332	7.662	8.755	15.572	2.101	179
39P	50%	Top	Right	Middle	10.938	0.260	4.695	7.551	18.489	1.499	170
24P	75%	Bottom	Left	Back	7.664	0.246	7.127	9.746	17.410	1.190	173
24P	75%	Bottom	Left	Front	14.649	0.362	9.169	6.830	23.818	1.248	171
24P	75%	Bottom	Left	Middle	8.282	0.560	8.430	5.748	16.712	1.985	177
24P	75%	Bottom	Right	Back	9.927	0.264	10.154	4.719	20.081	0.874	171
24P	75%	Bottom	Right	Front	10.609	0.496	3.470	6.263	16.871	1.869	175
24P	75%	Bottom	Right	Middle	7.348	0.422	7.464	3.832	14.813	0.994	176
24P	75%	Top	Left	Back	12.049	0.586	6.806	9.125	21.174	0.888	175
24P	75%	Top	Left	Front	12.024	0.626	5.756	4.219	17.781	1.501	176
24P	75%	Top	Left	Middle	9.745	0.744	5.644	4.088	15.389	1.797	177
24P	75%	Top	Right	Back	10.093		8.602	-3.688	18.695	1.579	
24P	75%	Top	Right	Front	9.470	0.632	6.082	7.551	17.020	1.813	177
24P	75%	Top	Right	Middle	7.976	0.204	5.989	6.448	14.424	0.484	171
Minimum:					6.82	0.20	-6.20	-4.41	11.86	0.48	170
Maximum:					15.19	1.33	10.74	10.20	24.37	2.31	179

J.6 PEENED: $\sigma_a = 125 \text{ MPa}$

Table J.6a: The scar depths, widths and peaks and calculated values h , l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 10 MPa and an axial stress amplitude of 125 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
38P	10%	Bottom	Left	Back	13.506	0.624	5.351	5.140	18.857	2.071	175
38P	10%	Bottom	Left	Front	9.089	0.538	6.396	5.561	15.485	2.023	176
38P	10%	Bottom	Left	Middle	7.835	0.558	6.595	7.976	15.811	1.344	177
38P	10%	Bottom	Right	Back	12.397	1.204	6.167	7.691	20.088	1.443	178
38P	10%	Bottom	Right	Front	11.692	0.662	3.833	11.367	23.059	1.725	176
38P	10%	Bottom	Right	Middle	8.760	0.596	3.780	7.686	16.446	1.821	177
38P	10%	Top	Left	Back	24.160		-0.685	35.639	59.799	1.757	
38P	10%	Top	Left	Front	41.631	0.680	14.819	6.736	56.450	1.653	166
38P	10%	Top	Left	Middle	15.417		43.243	-6.372	58.660	1.671	
38P	10%	Top	Right	Back	12.046	0.646	7.471	8.584	20.630	1.376	176
38P	10%	Top	Right	Front	9.477	0.632	1.185	4.413	13.890	1.721	177
38P	10%	Top	Right	Middle	8.039	0.578	2.962	4.465	12.504	1.443	177
13P	50%	Bottom	Left	Back	10.494	0.480	5.311	6.404	16.898	0.756	175
13P	50%	Bottom	Left	Front	22.423	1.326	9.737	15.163	37.586	1.767	176
13P	50%	Bottom	Left	Middle	8.019	0.314	6.432	0.803	14.451	0.488	174
13P	50%	Bottom	Right	Back	65.359	1.499	16.701	27.915	93.274	2.171	170
13P	50%	Bottom	Right	Front	94.749	1.627	20.292	29.870	124.619	2.019	167
13P	50%	Bottom	Right	Middle	51.182	0.596	15.665	8.804	66.847	1.833	161
13P	50%	Top	Left	Back	19.904	0.890	11.209	6.262	31.113	1.292	175
13P	50%	Top	Left	Front	10.443	0.720	10.116	4.560	20.559	0.954	177
13P	50%	Top	Left	Middle	22.495	0.992	6.213	7.132	29.626	3.663	175
13P	50%	Top	Right	Back	12.488	0.274	7.824	6.697	20.312	1.641	170
13P	50%	Top	Right	Front	9.179	0.408	6.053	13.339	22.518	1.008	175
13P	50%	Top	Right	Middle	7.380	0.664	10.306	6.185	17.686	2.051	177
Minimum:					7.38	0.27	-0.68	-6.37	12.50	0.49	161
Maximum:					94.75	1.63	43.24	35.64	124.62	3.66	178

Table J.6b: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 60 MPa and an axial stress amplitude of 125 MPa.

Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
33P	10%	Bottom	Left	Back	8.262	0.450	8.757	9.619	17.881	1.130	176
33P	10%	Bottom	Left	Front	9.333	0.290	10.953	3.618	20.286	1.070	173
33P	10%	Bottom	Left	Middle	10.768	0.742	4.175	3.887	14.944	2.091	177
33P	10%	Bottom	Right	Back	31.932	0.754	7.684	11.144	43.076	1.741	170
33P	10%	Bottom	Right	Front	11.087	1.603	-0.299	4.864	15.952	0.766	178
33P	10%	Bottom	Right	Middle	6.926	0.672	5.730	5.088	12.656	2.023	178
33P	10%	Top	Left	Back	17.270	0.412	11.481	17.305	34.576	1.342	170
33P	10%	Top	Left	Front	7.796	0.438	10.593	5.459	18.389	1.356	176
33P	10%	Top	Left	Middle	11.250	0.748	10.194	2.666	21.444	1.427	177
33P	10%	Top	Right	Back	17.983	0.750	6.147	6.768	24.751	2.167	175
33P	10%	Top	Right	Front	9.599	0.490	6.359	7.088	16.687	1.883	176
33P	10%	Top	Right	Middle	7.760	0.558	1.809	10.526	18.286	1.142	177
42P	25%	Bottom	Left	Back	9.209	0.442	0.383	9.519	18.728	0.754	175
42P	25%	Bottom	Left	Front	8.351	0.278	7.896	6.765	16.246	0.978	173
42P	25%	Bottom	Left	Middle	8.147	0.536	4.262	0.015	12.409	1.258	177
42P	25%	Bottom	Right	Back	17.338	1.380	1.902	23.649	40.987	1.697	177
42P	25%	Bottom	Right	Front	10.787	0.608	2.584	2.977	13.764	1.278	176
42P	25%	Bottom	Right	Middle	13.509	0.622	6.936	4.802	20.445	0.810	175
42P	25%	Top	Left	Back	9.037		4.506	-0.578	13.543	0.966	
42P	25%	Top	Left	Front	7.787	0.612	5.618	6.622	14.408	2.135	177
42P	25%	Top	Left	Middle	9.347	0.252	9.681	4.975	19.028	1.467	172
42P	25%	Top	Right	Back	12.775	0.434	6.444	4.486	19.220	1.465	173
42P	25%	Top	Right	Front	8.544	0.570	7.095	2.693	15.639	2.285	177
42P	25%	Top	Right	Middle	7.463		5.339	-4.242	12.803	0.564	
23P	50%	Bottom	Left	Back	9.557	0.416	9.152	8.831	18.709	1.236	175
23P	50%	Bottom	Left	Front	21.381		-2.389	49.700	71.081	1.254	
23P	50%	Bottom	Left	Middle	8.868	0.292	0.514	6.256	15.124	1.429	173
23P	50%	Bottom	Right	Back	7.084	0.180	3.084	6.213	13.297	1.242	171
23P	50%	Bottom	Right	Front	11.450	0.772	5.489	8.287	19.737	1.194	177
23P	50%	Bottom	Right	Middle	13.301	0.796	8.829	3.462	22.130	1.154	176
23P	50%	Top	Left	Back	10.378		-6.142	7.195	17.574	1.308	
23P	50%	Top	Left	Front	7.347	0.612	11.591	8.661	18.939	2.545	177
23P	50%	Top	Left	Middle	10.394	0.202	5.550	7.167	17.561	1.100	168
23P	50%	Top	Right	Back	10.017	0.512	2.305	6.160	16.177	0.702	176
23P	50%	Top	Right	Front	13.665	0.638	14.286	5.758	27.951	1.232	175
23P	50%	Top	Right	Middle	8.916	0.352	6.801	14.632	23.548	0.868	174
Minimum:					6.93	0.18	-6.14	-4.24	12.41	0.56	168
Maximum:					31.93	1.60	14.29	49.70	71.08	2.55	178

Table J.6c: The scar depths, widths and peaks and calculated values h, l and θ , for the fretting fatigue tests with an aluminium alloy 2024 T351 bridge in contact with a shot peened aluminium alloy 2024 T351 specimen subjected to a normal pressure of 100 MPa an axial stress amplitude of 125 MPa.

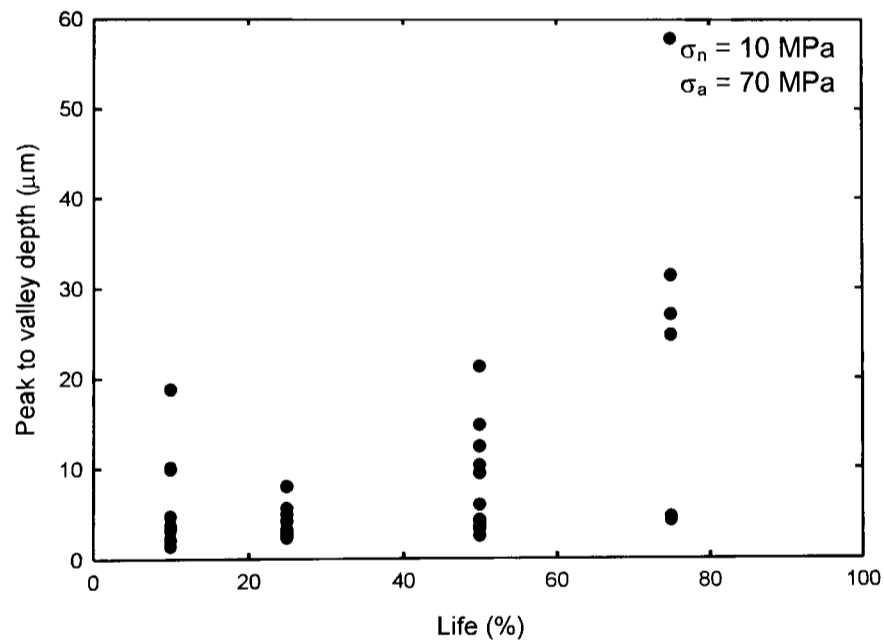
Specimen (no.)	Life proportion (%)	Scar		Trace	Depth (μm)	Width (mm)	Left peak (μm)	Right peak (μm)	h (μm)	l (mm)	θ ($^\circ$)
		T/B	L/R	F/M/B							
36P	10%	Bottom	Left	Back	12.032	0.998	4.559	2.146	16.591	3.475	177
36P	10%	Bottom	Left	Front	13.960	1.196	6.203	6.140	20.163	4.414	177
36P	10%	Bottom	Left	Middle	11.123	1.603	11.225	-1.455	22.349	1.949	178
36P	10%	Bottom	Right	Back	14.694	1.098	6.204	9.184	23.878	2.179	177
36P	10%	Bottom	Right	Front	11.169	0.422	5.166	5.671	16.840	1.196	174
36P	10%	Bottom	Right	Middle	12.920	0.714	9.844	9.931	22.851	1.547	176
36P	10%	Top	Left	Back	11.278	0.614	11.115	8.827	22.392	2.123	176
36P	10%	Top	Left	Front	8.805		-1.179	6.516	15.321	0.628	
36P	10%	Top	Left	Middle	9.547	0.536	6.836	4.193	16.383	2.239	176
36P	10%	Top	Right	Back	10.317		-1.192	11.137	21.454	0.530	
36P	10%	Top	Right	Front	7.162	0.610	3.484	4.677	11.839	1.417	177
36P	10%	Top	Right	Middle	9.836	0.238	4.463	6.237	16.074	0.402	171
37P	25%	Bottom	Left	Back	7.544	0.348	7.917	3.663	15.461	0.572	175
37P	25%	Bottom	Left	Front	13.352	0.830	10.826	6.707	24.178	1.619	176
37P	25%	Bottom	Left	Middle	7.222		6.151	-2.538	13.373	1.521	
37P	25%	Bottom	Right	Back	8.458	0.338	4.116	5.902	14.360	0.914	174
37P	25%	Bottom	Right	Front	9.871	0.334	7.729	4.919	17.600	1.599	173
37P	25%	Bottom	Right	Middle	7.311	0.766	7.387	6.620	14.698	2.467	178
37P	25%	Top	Left	Back	8.938		15.988	-2.160	24.926	1.228	
37P	25%	Top	Left	Front	11.276		6.705	-2.312	17.981	0.714	
37P	25%	Top	Left	Middle	8.111	0.258	4.141	5.720	13.831	1.330	173
37P	25%	Top	Right	Back	14.711	0.288	5.099	7.789	22.501	1.567	168
37P	25%	Top	Right	Front	9.983	0.280	6.336	6.582	16.566	0.694	172
37P	25%	Top	Right	Middle	9.638	0.278	6.528	8.513	18.151	1.292	172
21P	50%	Bottom	Left	Back	9.461	0.576	4.046	9.422	18.884	1.280	176
21P	50%	Bottom	Left	Front	7.823	0.528	8.367	9.319	17.142	1.537	177
21P	50%	Bottom	Left	Middle	10.545	0.316	1.399	4.593	15.138	0.906	172
21P	50%	Bottom	Right	Back	8.095	0.384	11.053	4.864	19.148	1.667	175
21P	50%	Bottom	Right	Front	8.053	0.646	6.936	9.257	17.310	1.122	177
21P	50%	Bottom	Right	Middle	7.936	0.262	7.782	8.103	16.038	0.490	173
21P	50%	Top	Left	Back	7.865	0.306	11.539	2.153	19.404	0.584	174
21P	50%	Top	Left	Front	7.580	0.402	6.440	6.338	14.020	0.882	176
21P	50%	Top	Left	Middle	11.353	0.374	6.132	6.547	17.900	0.728	173
21P	50%	Top	Right	Back	8.940	0.336	9.315	9.365	18.305	1.441	174
21P	50%	Top	Right	Front	9.673	0.280	5.116	2.811	14.789	1.517	172
21P	50%	Top	Right	Middle	10.668	0.316	1.848	10.896	21.564	1.348	172
Minimum:					7.16	0.24	-1.19	-2.54	11.84	0.40	168
Maximum:					14.71	1.60	15.99	11.14	24.93	4.41	178

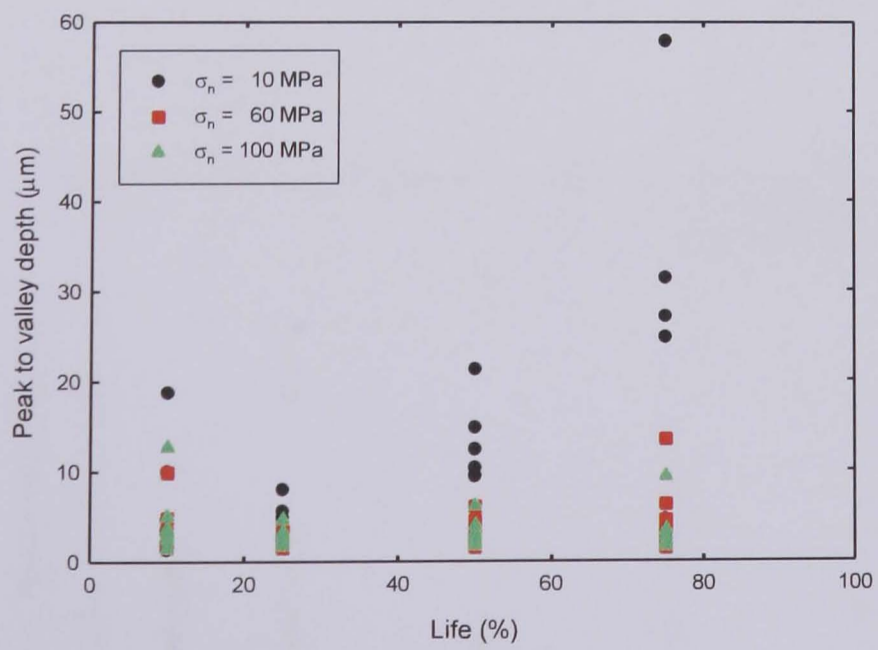
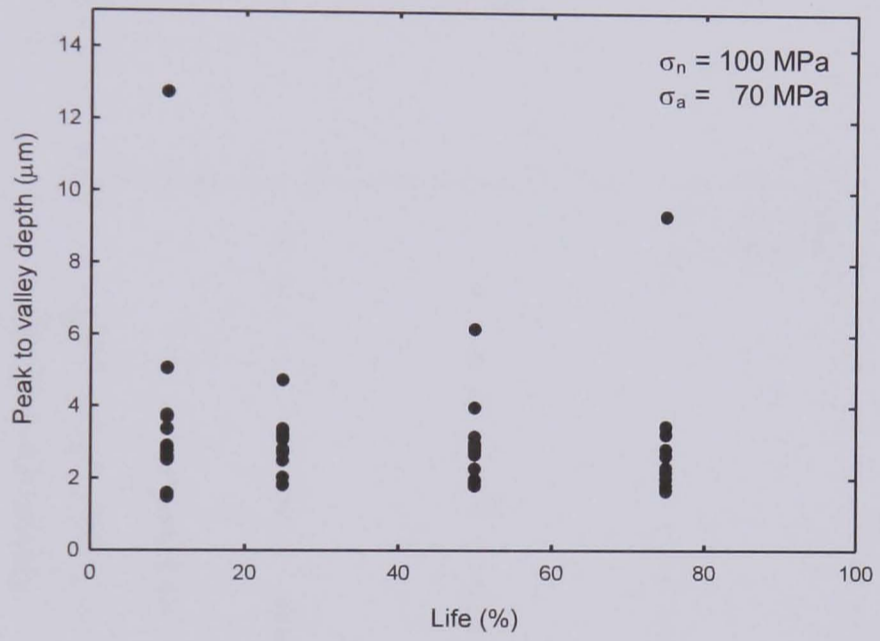
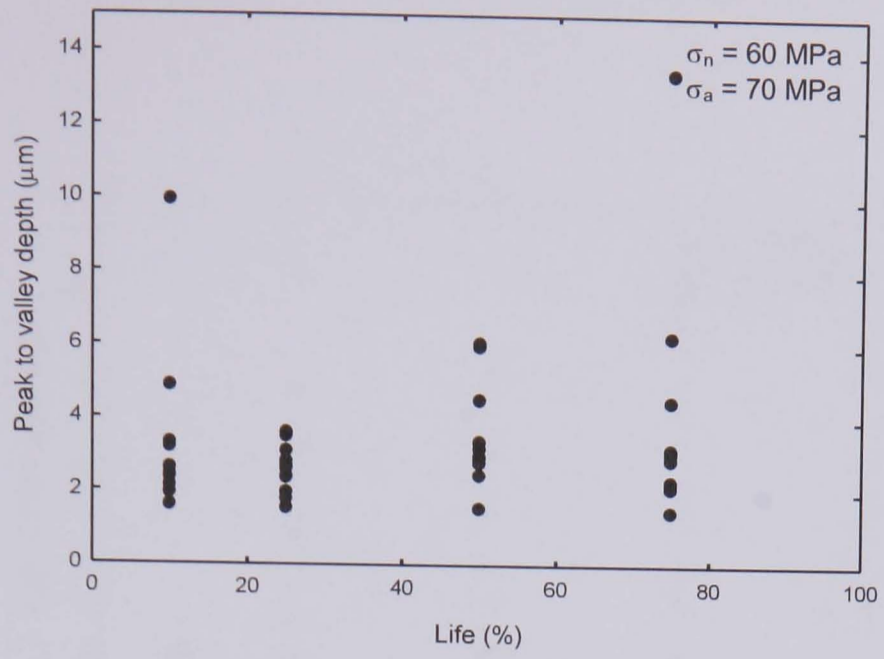
APPENDIX K

RESULTS: PEAK TO VALLEY DEPTH

Measurements of the total peak to valley depth, h , determined from traces of the fretting scars. A definition of this feature can be found in Figure 4.44.

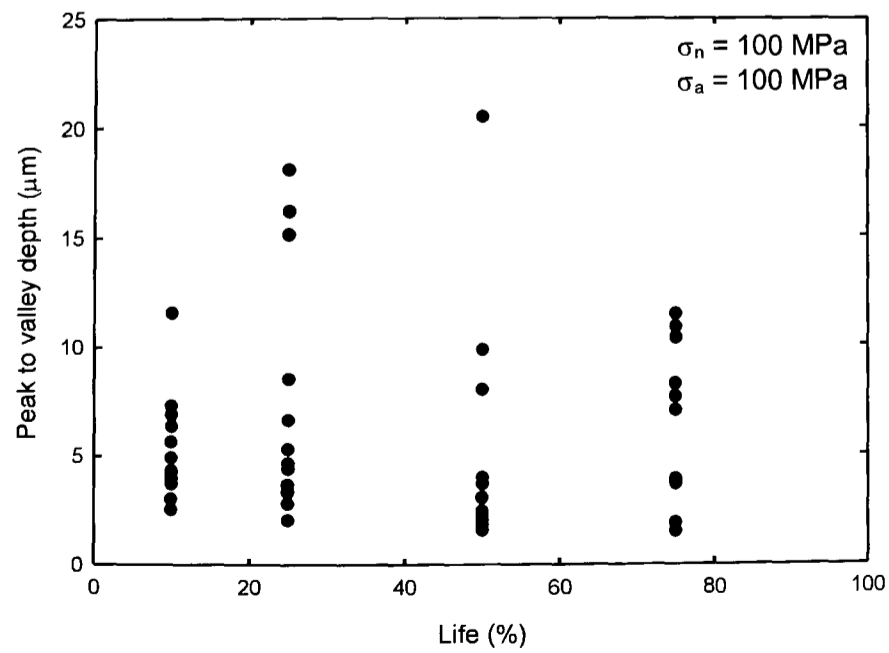
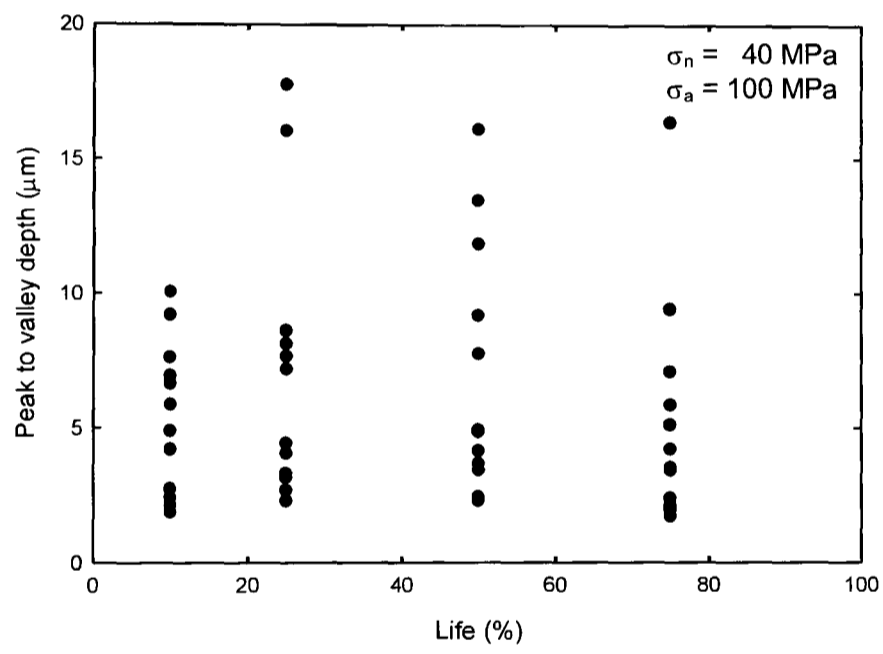
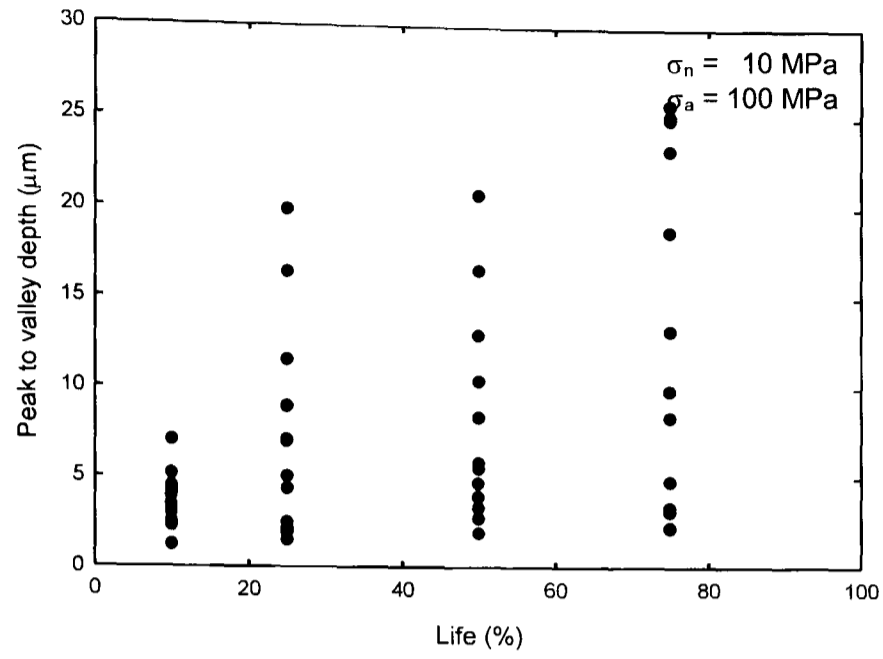
K.1 PEAK TO VALLEY DEPTH: $\sigma_a = 70$ MPa unpeened

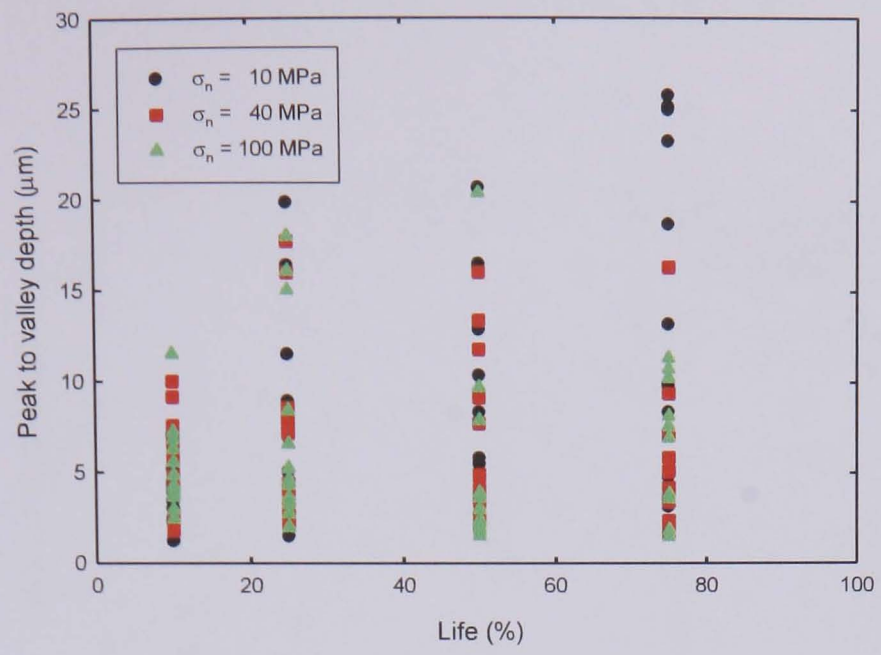




K.2

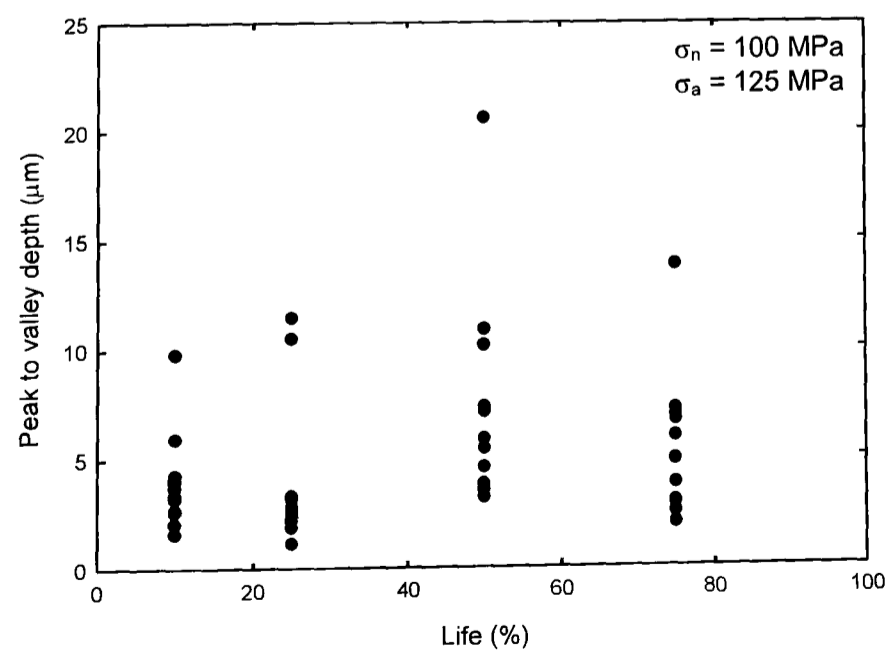
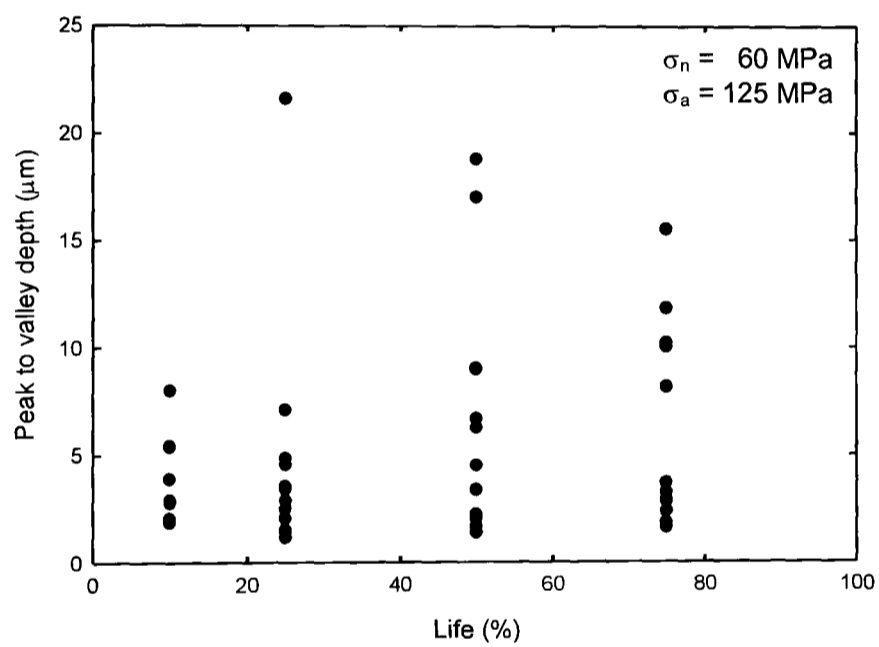
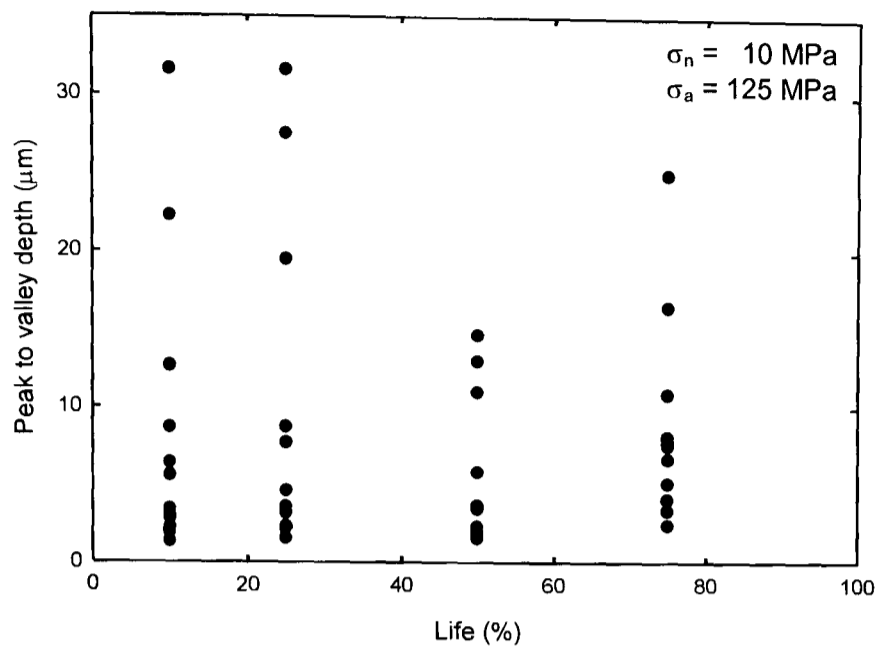
PEAK TO VALLEY DEPTH: $\sigma_a = 100$ MPa unpeened

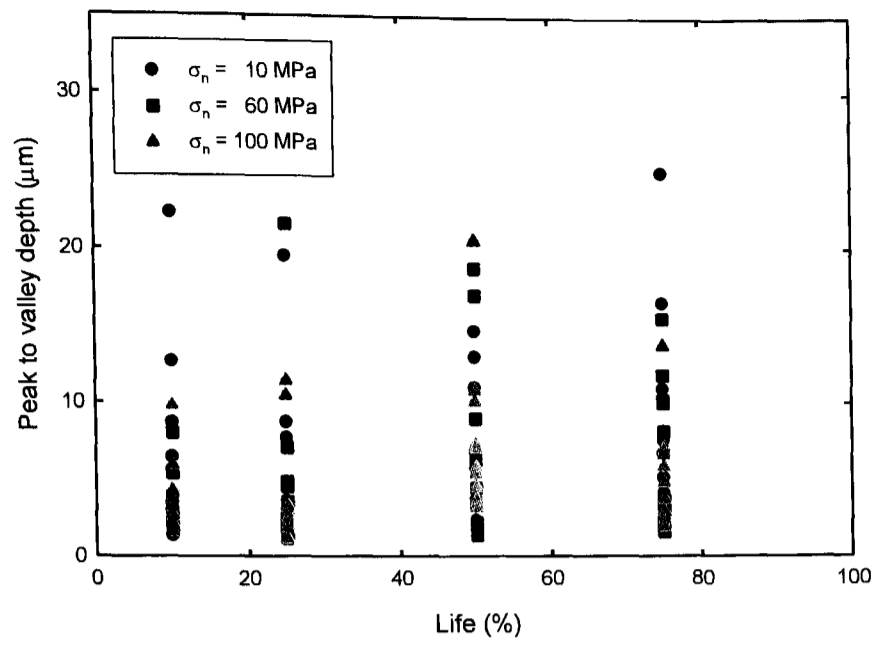




K.3

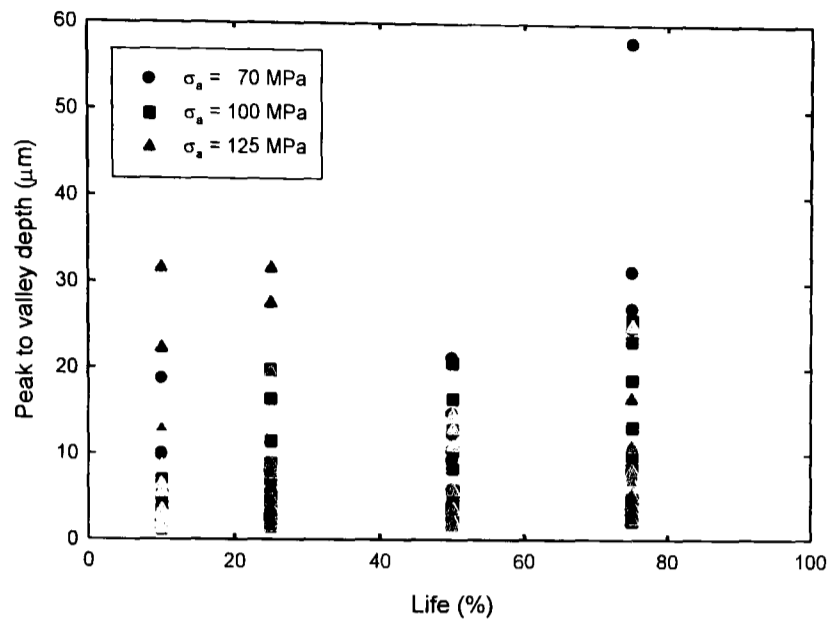
PEAK TO VALLEY DEPTH: $\sigma_a = 125$ MPa unpeened



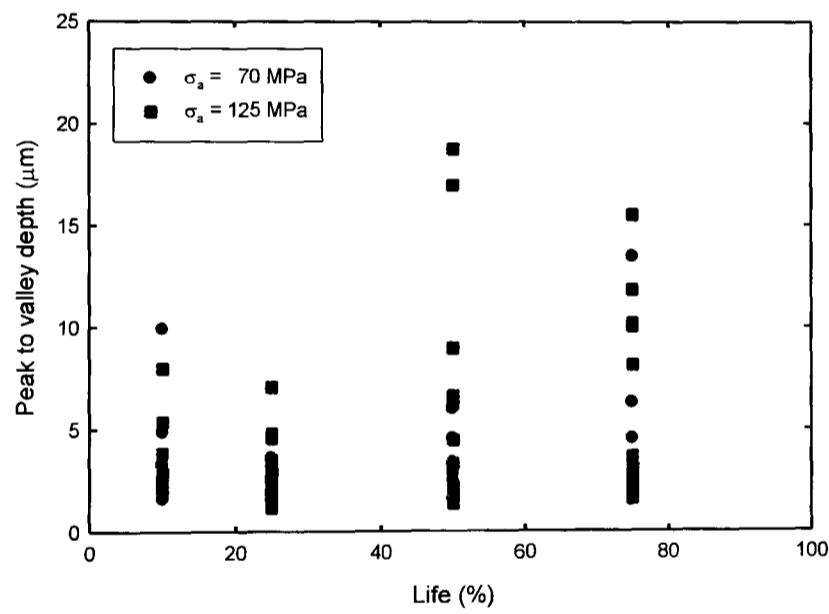


K.4 PEAK TO VALLEY DEPTH: Unpeened

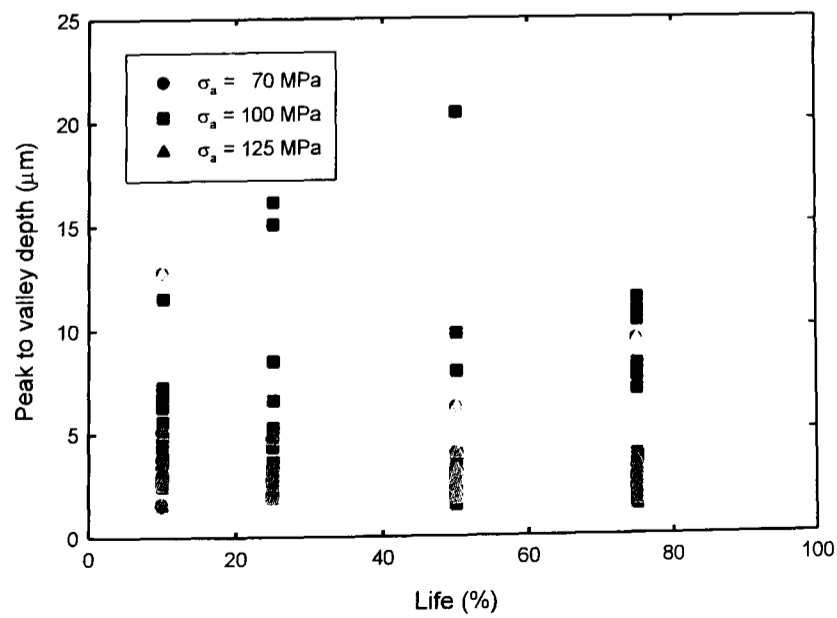
$\sigma_n = 10 \text{ MPa}$:



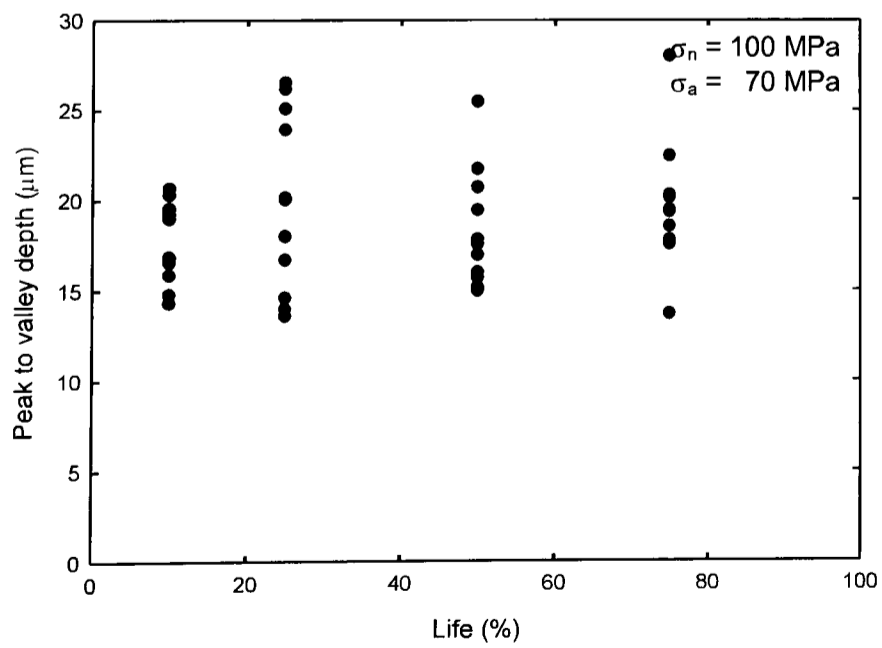
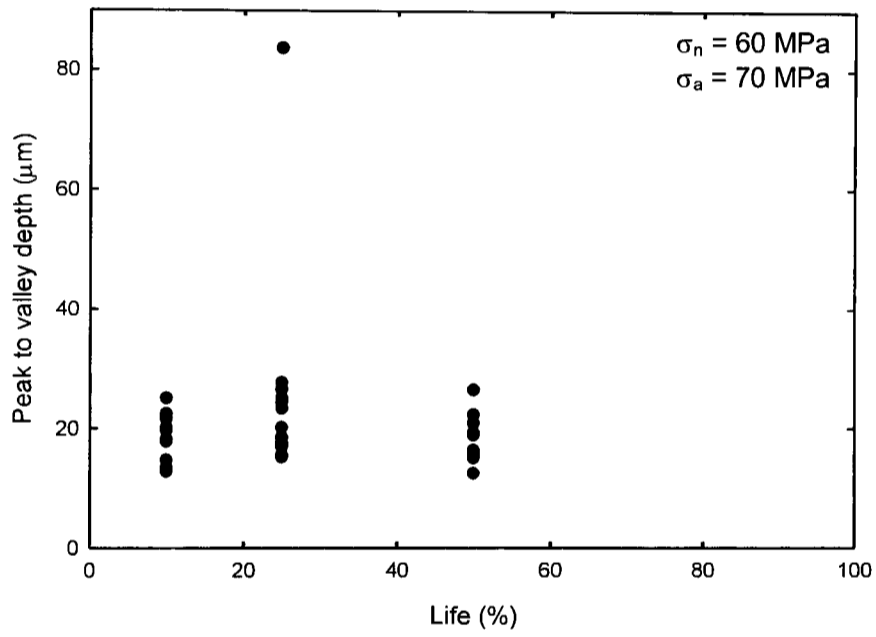
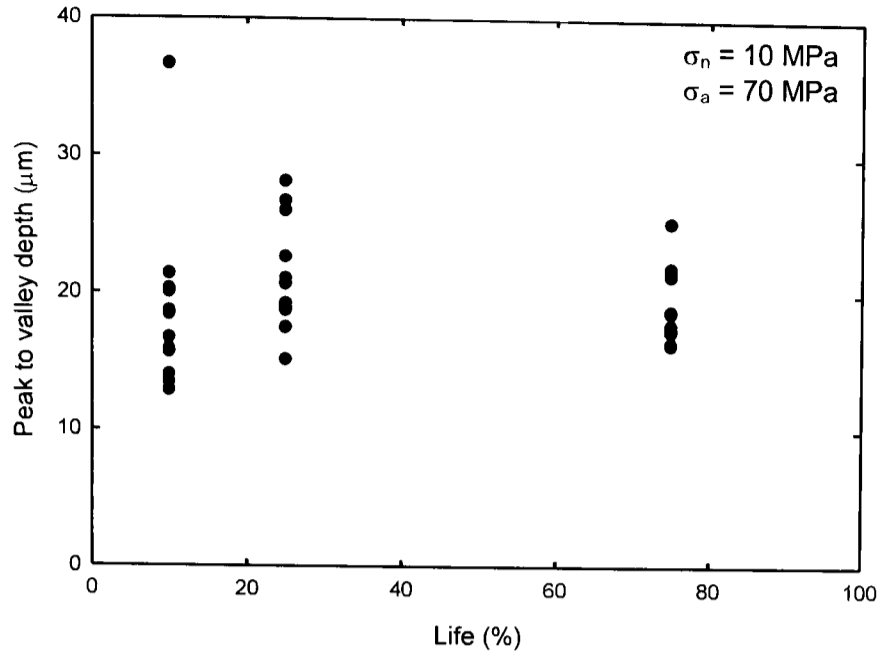
$\sigma_n = 60 \text{ MPa}$:

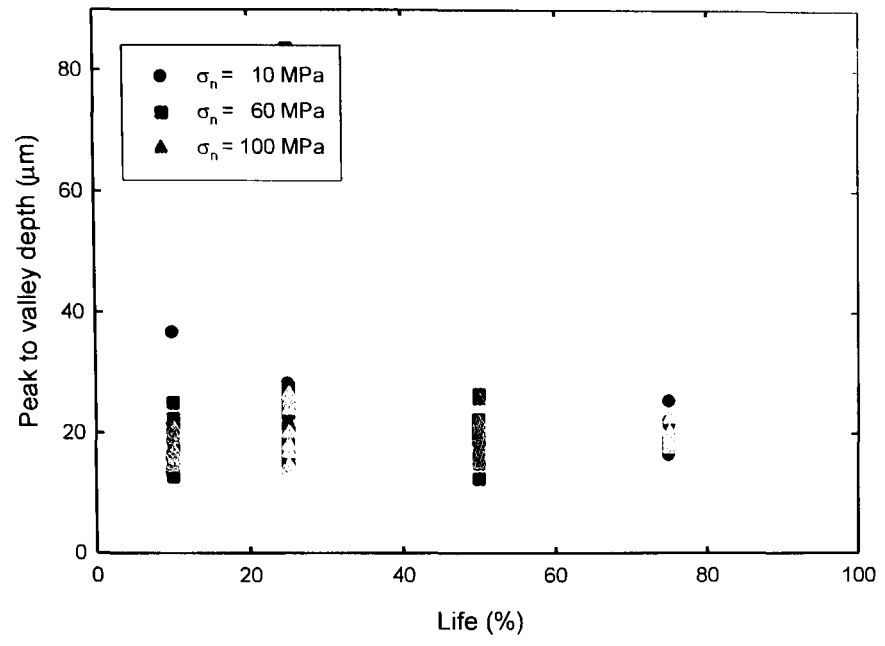


$\sigma_n = 100 \text{ MPa}$:



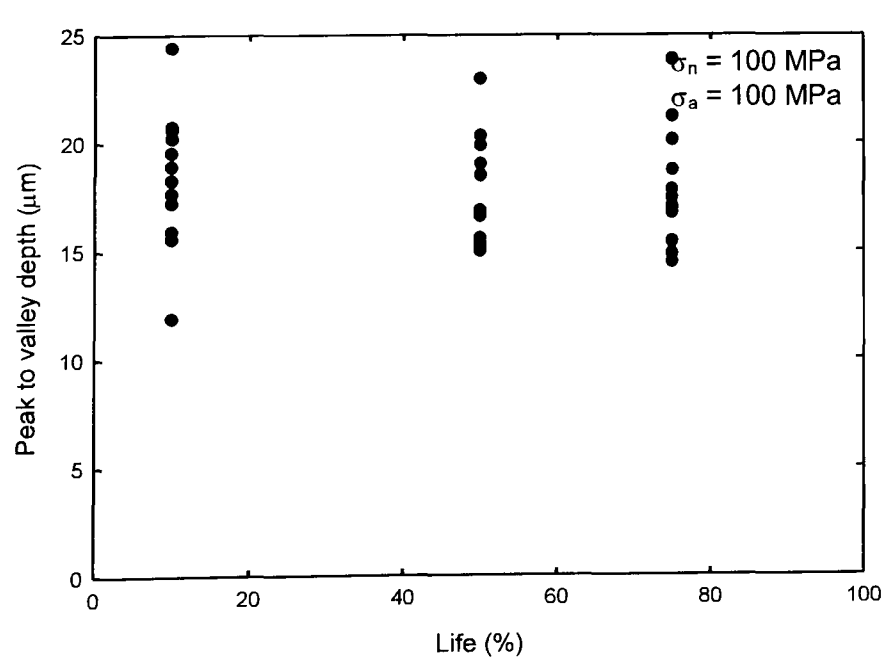
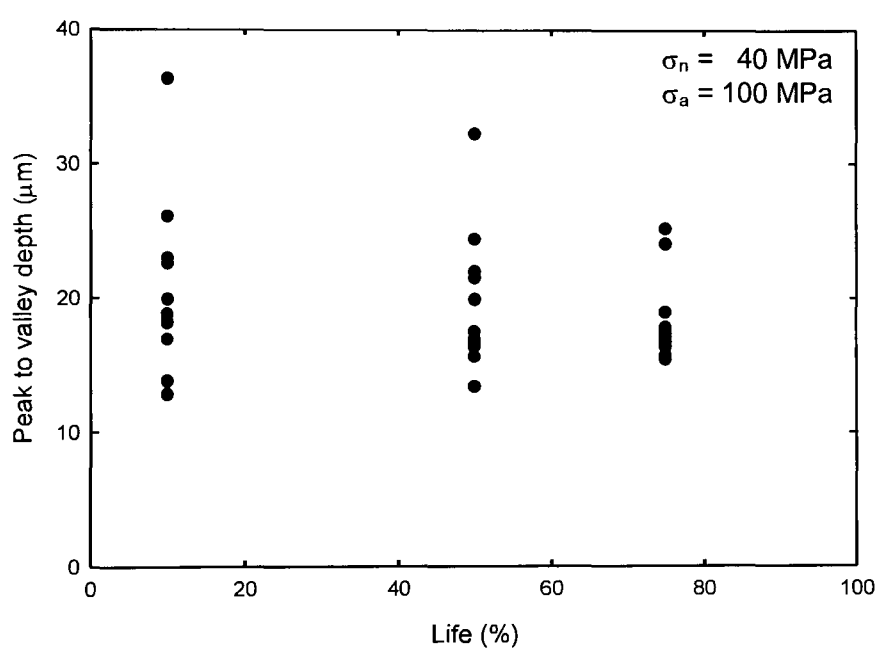
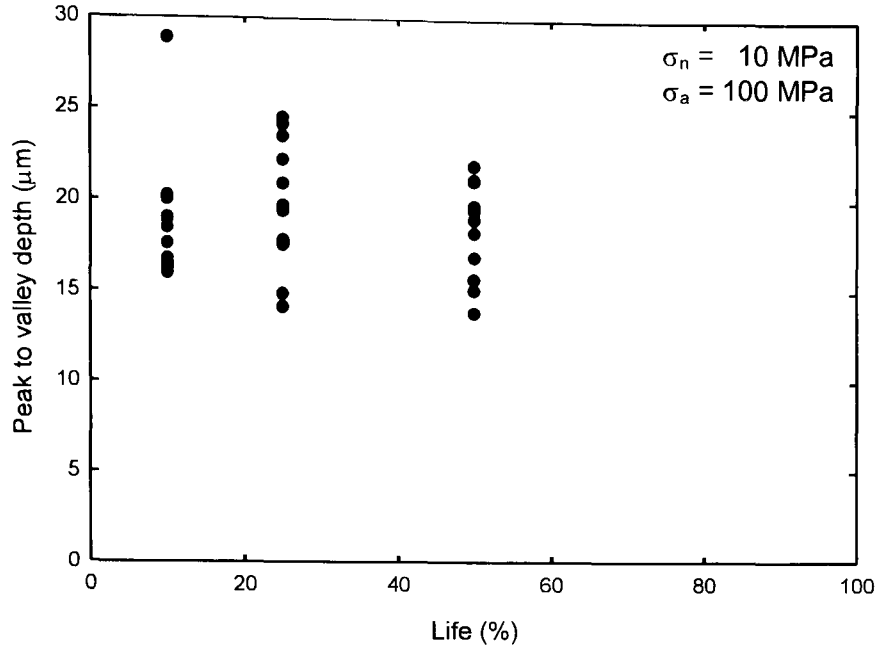
K.5 PEAK TO VALLEY DEPTH: $\sigma_a = 70$ MPa peened

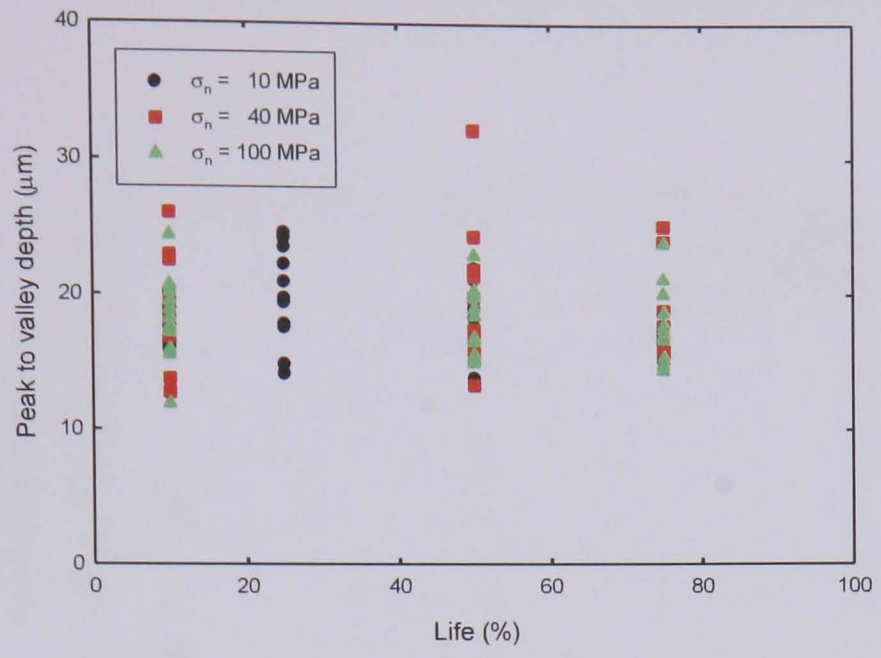




K.6

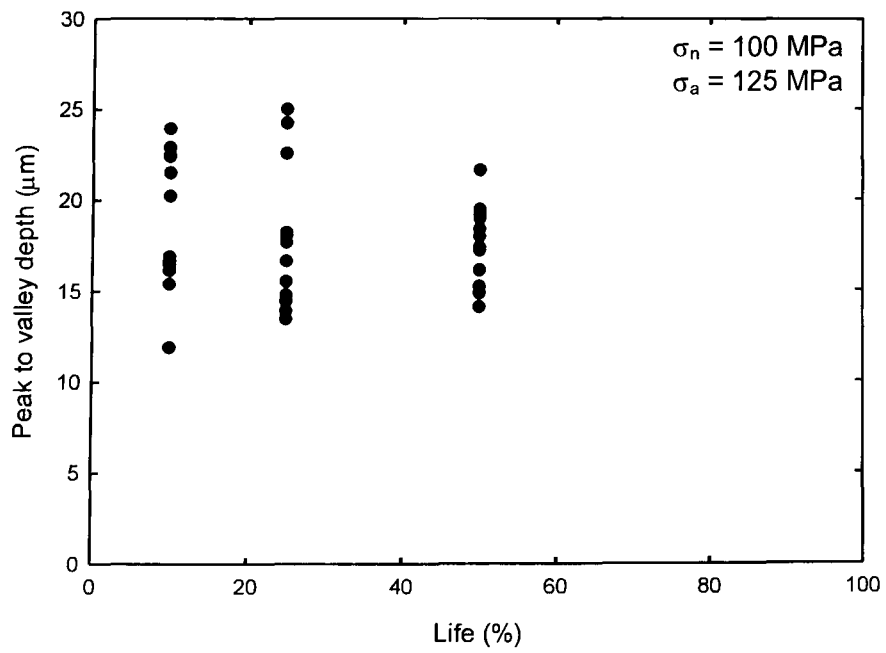
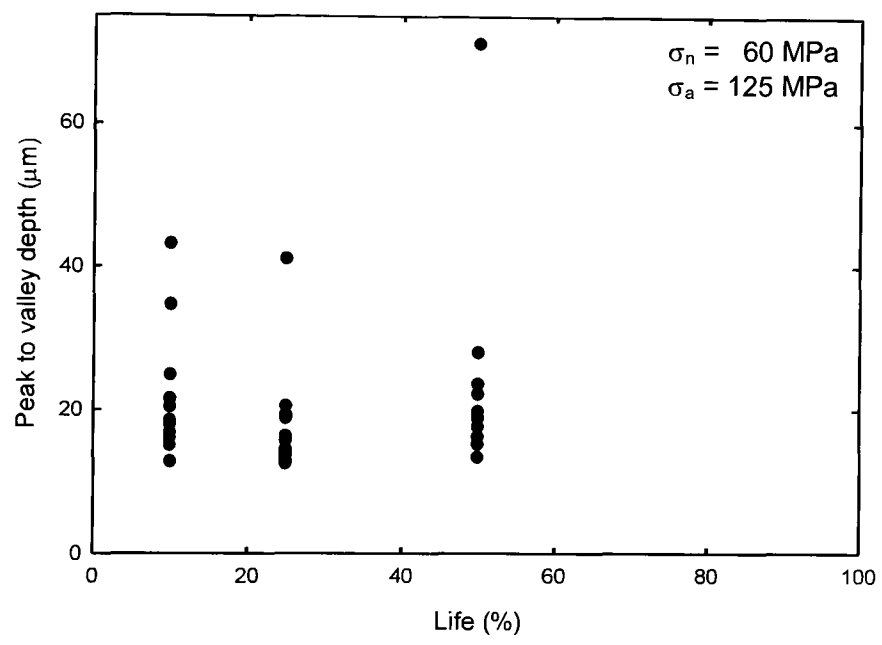
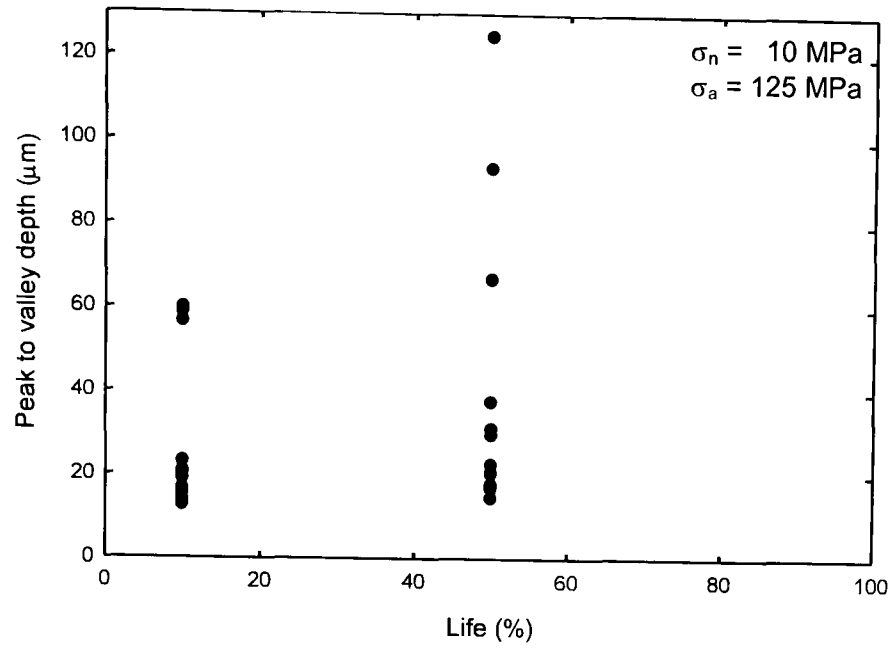
PEAK TO VALLEY DEPTH: $\sigma_a = 100$ MPa peened

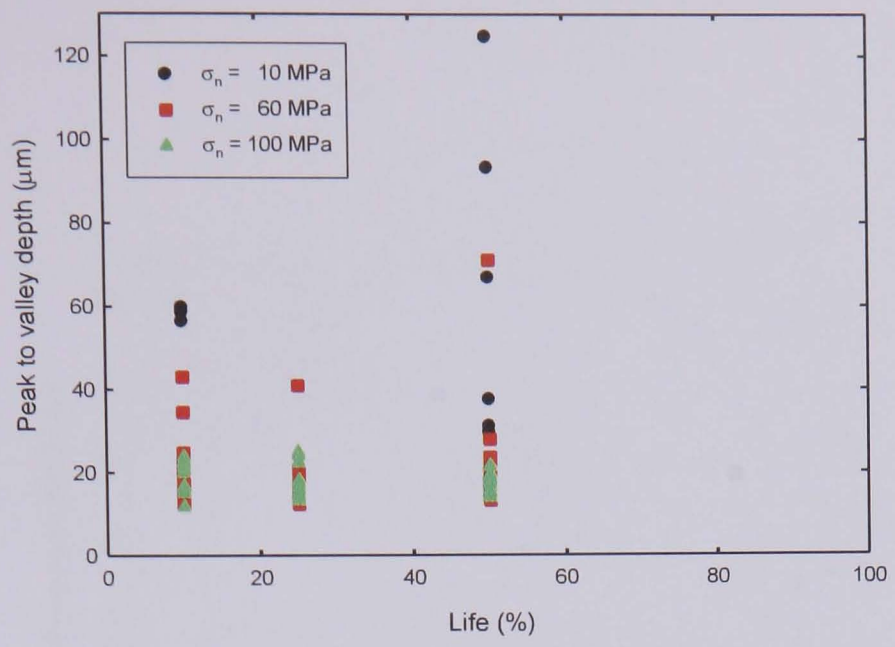




K.7

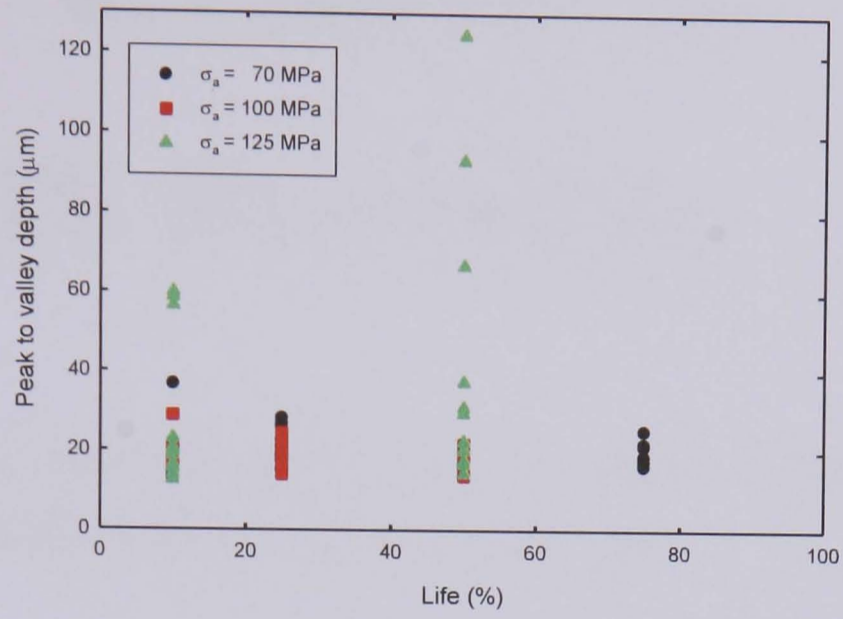
PEAK TO VALLEY DEPTH: $\sigma_a = 125$ MPa peened



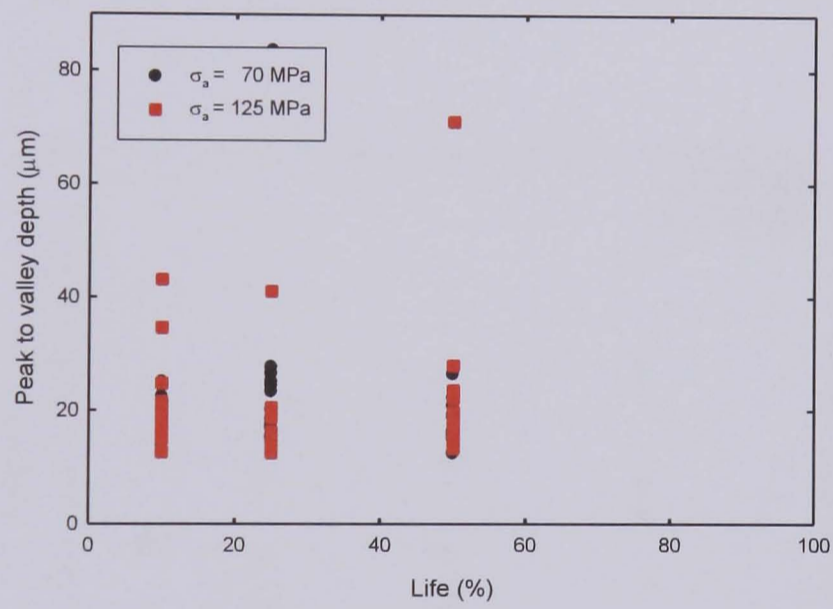


K.8 PEAK TO VALLEY DEPTH: Peened

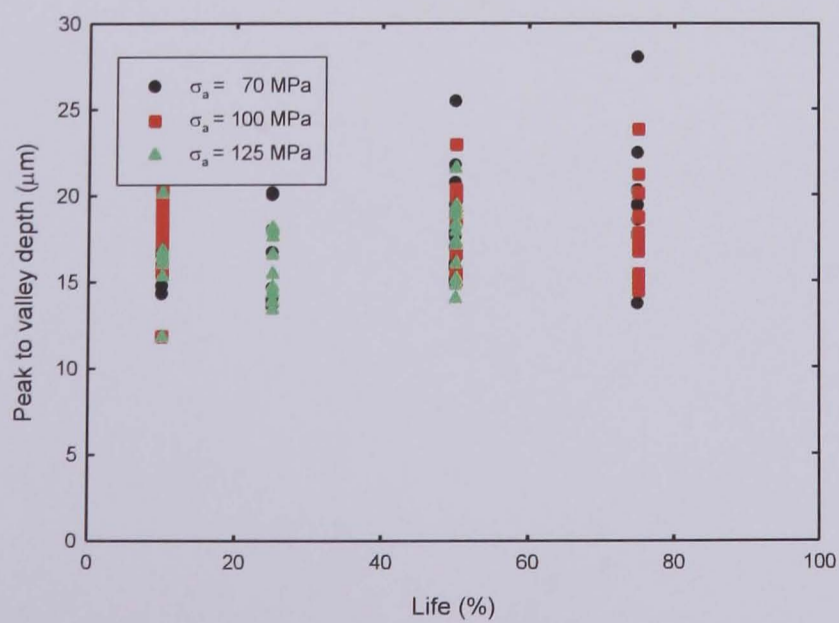
$\sigma_n = 10$ MPa:



$\sigma_n = 60$ MPa:



$\sigma_n = 100$ MPa:

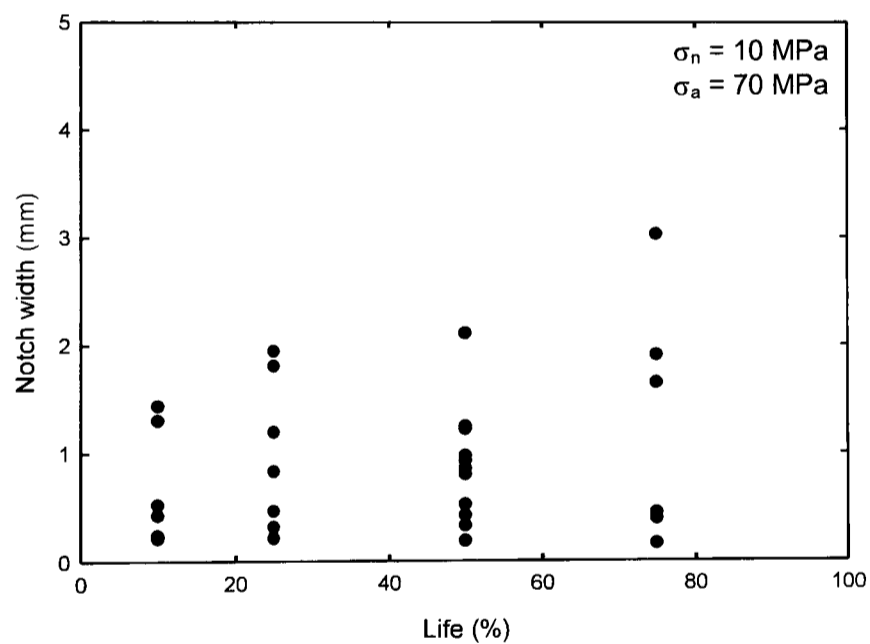


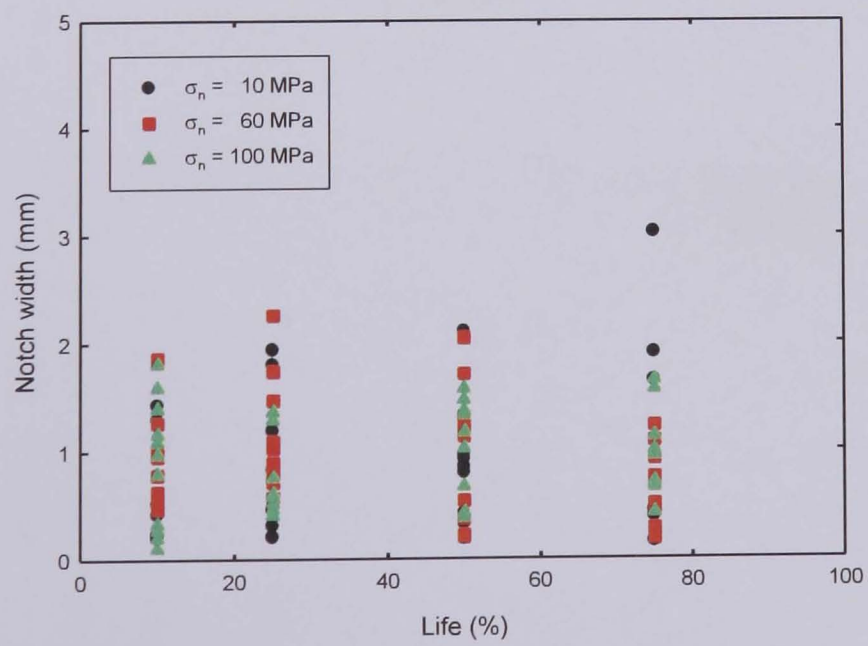
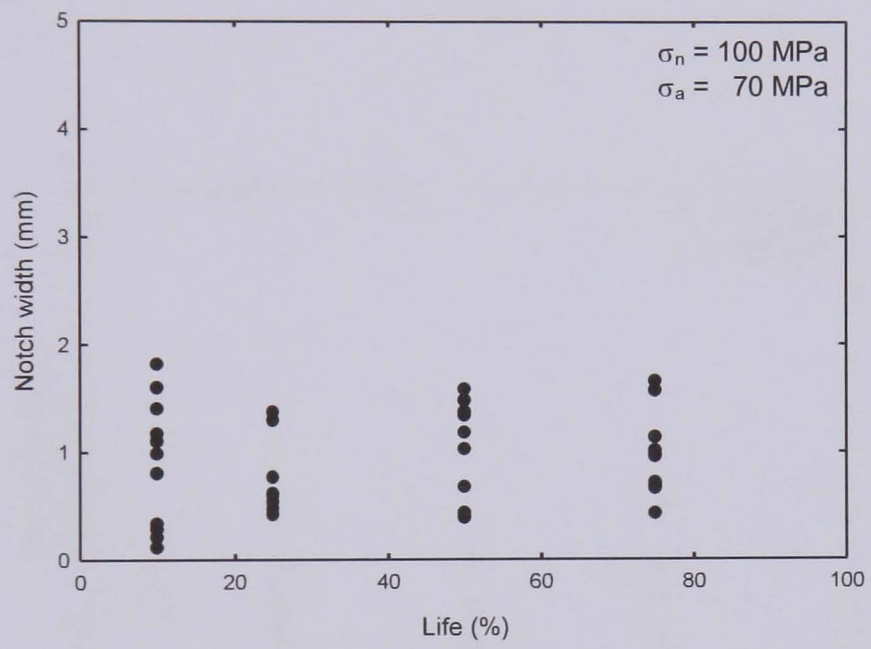
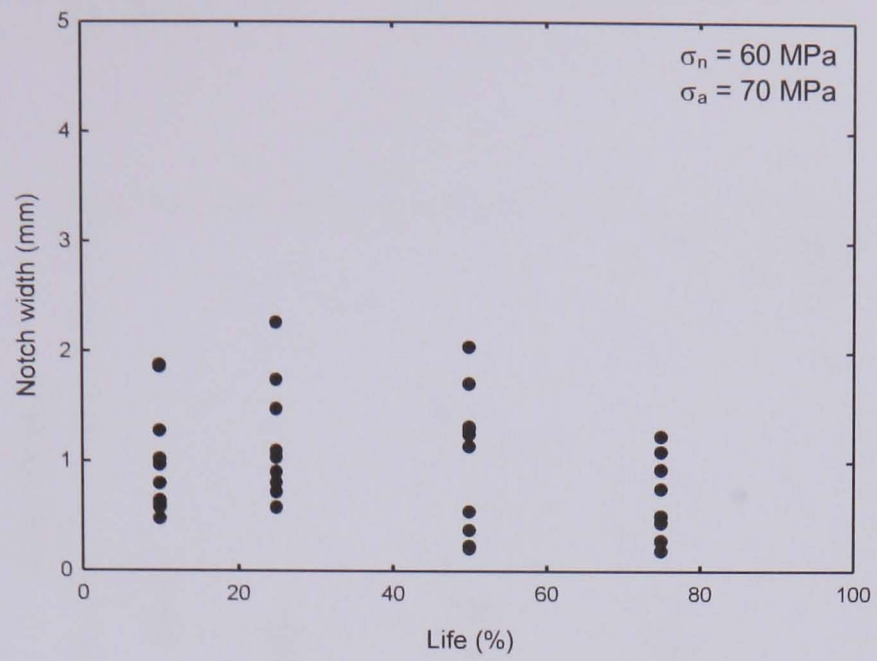
APPENDIX L

RESULTS: SCAR WIDTH

Measurements of width, w , determined from traces of the fretting scars. A definition of this feature can be found in Figure 4.44.

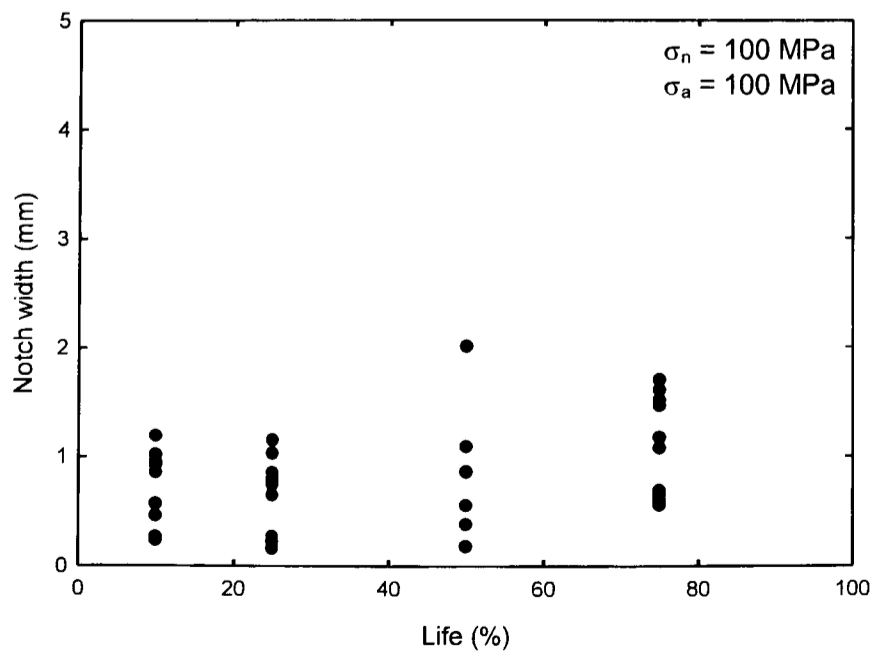
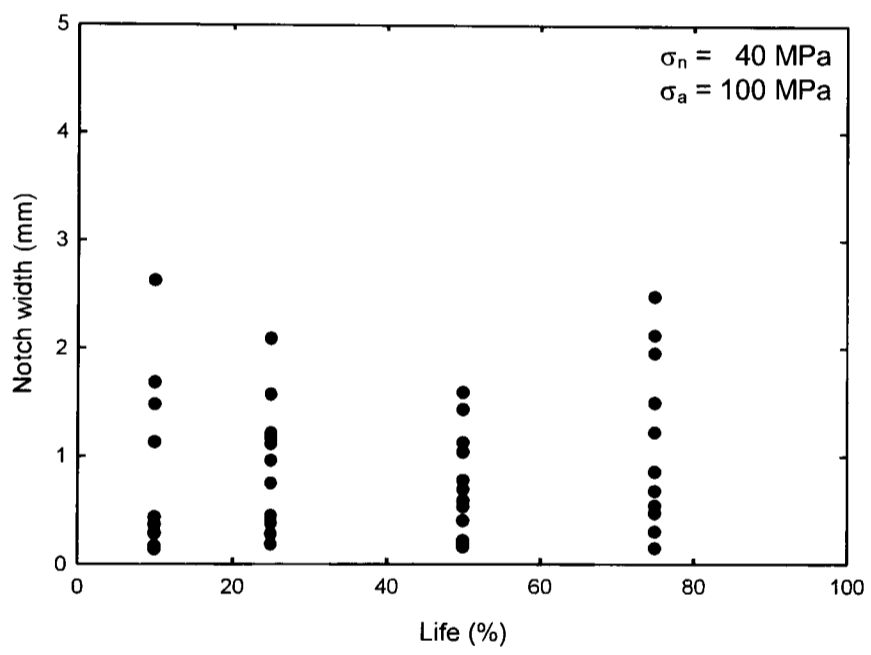
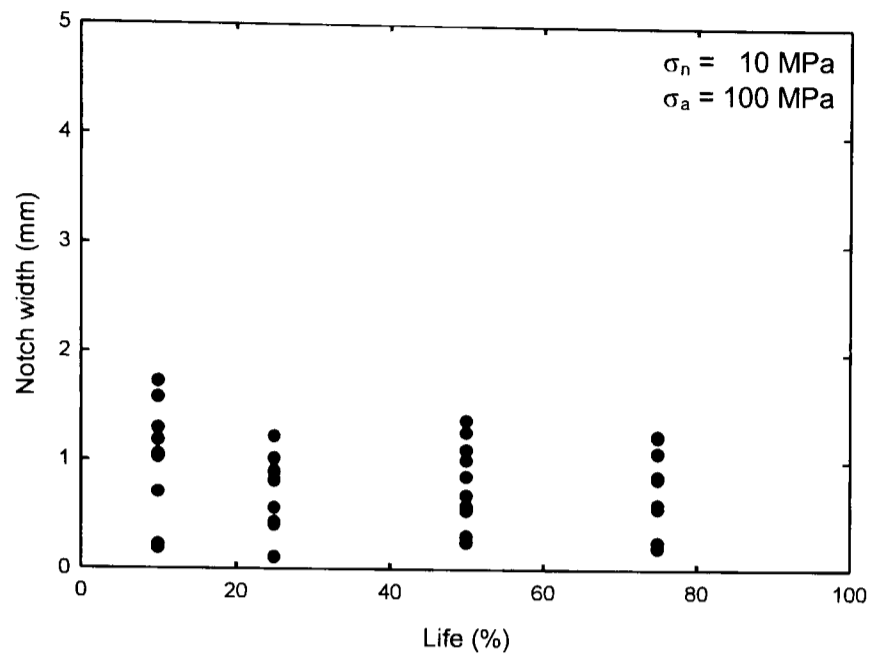
L.1 SCAR WIDTH: $\sigma_a = 70$ MPa unpeened

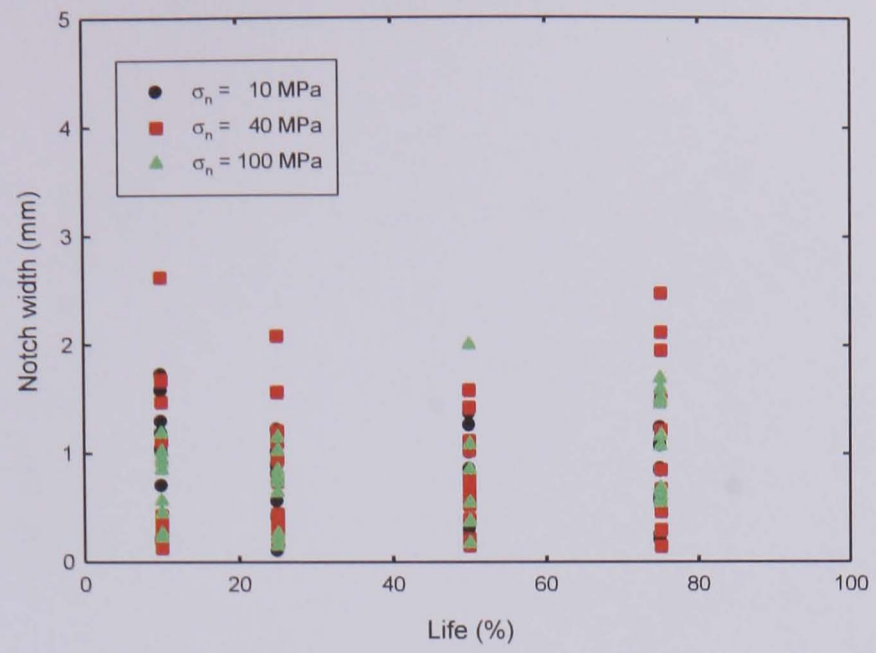




L.2

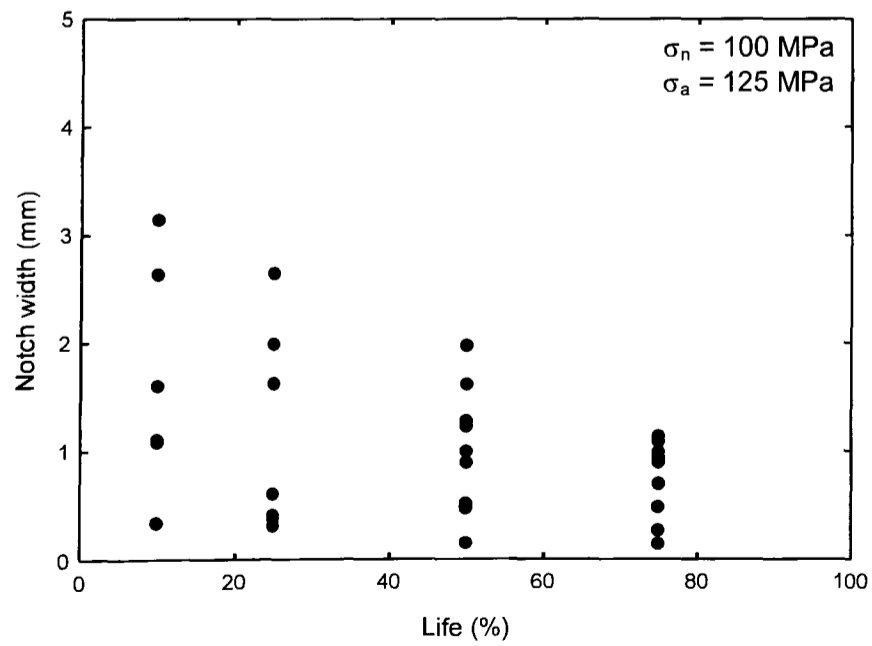
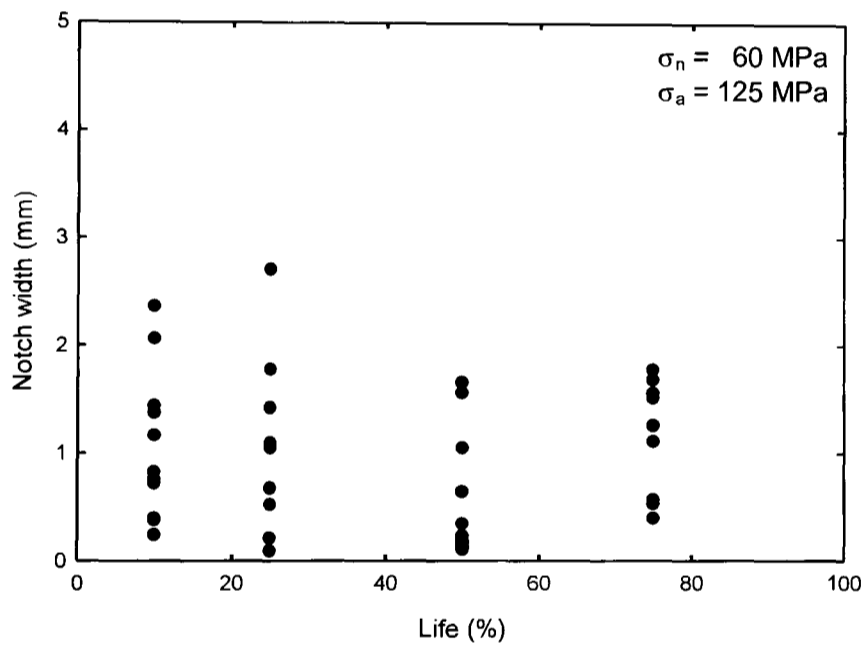
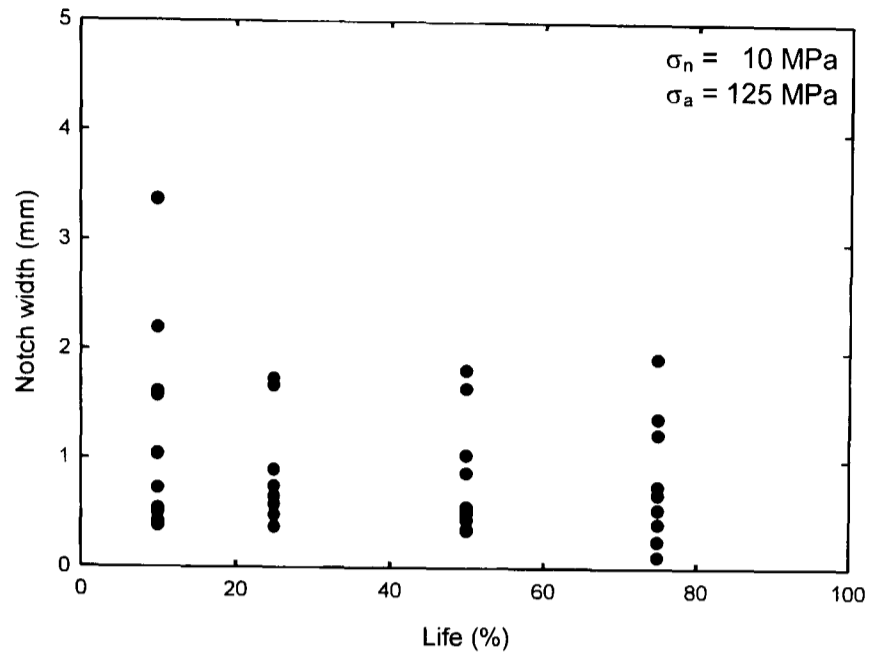
SCAR WIDTH: $\sigma_a = 100$ MPa unpeened

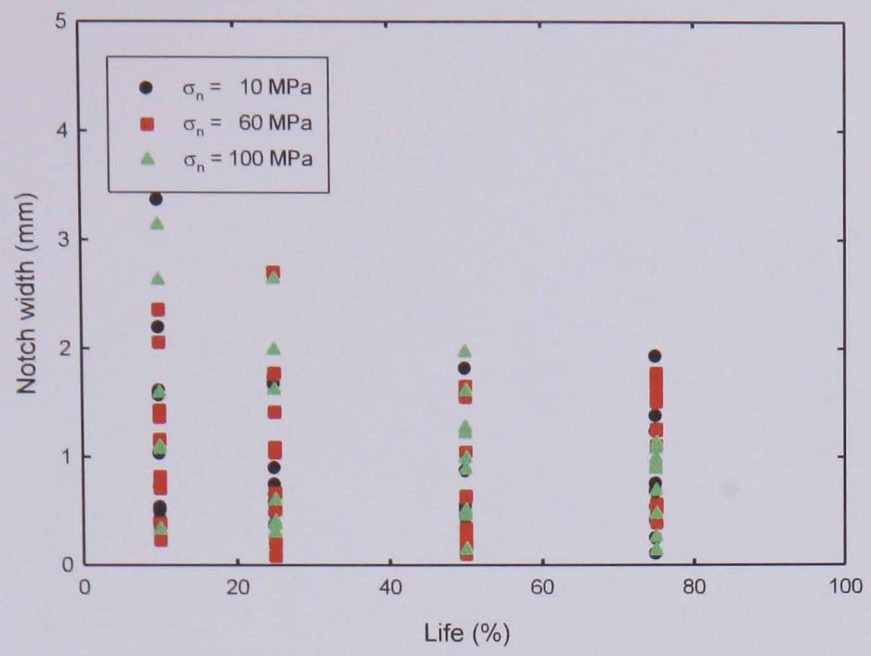




L.3

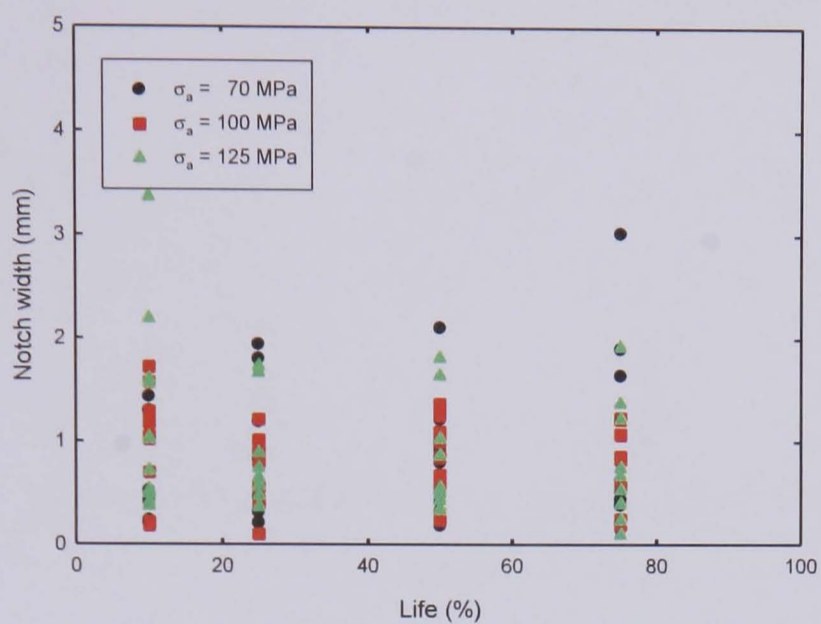
SCAR WIDTH: $\sigma_a = 125$ MPa unpeened



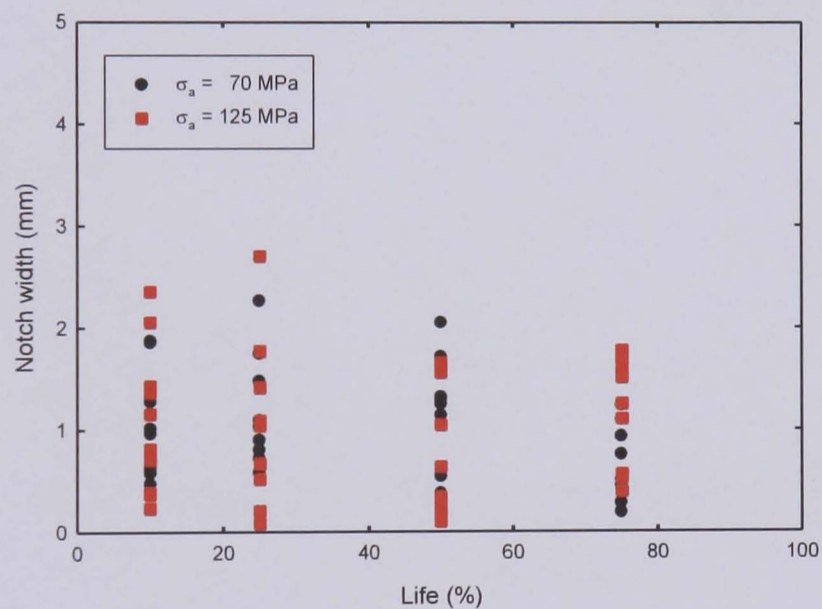


L.4 SCAR WIDTH: Unpeened

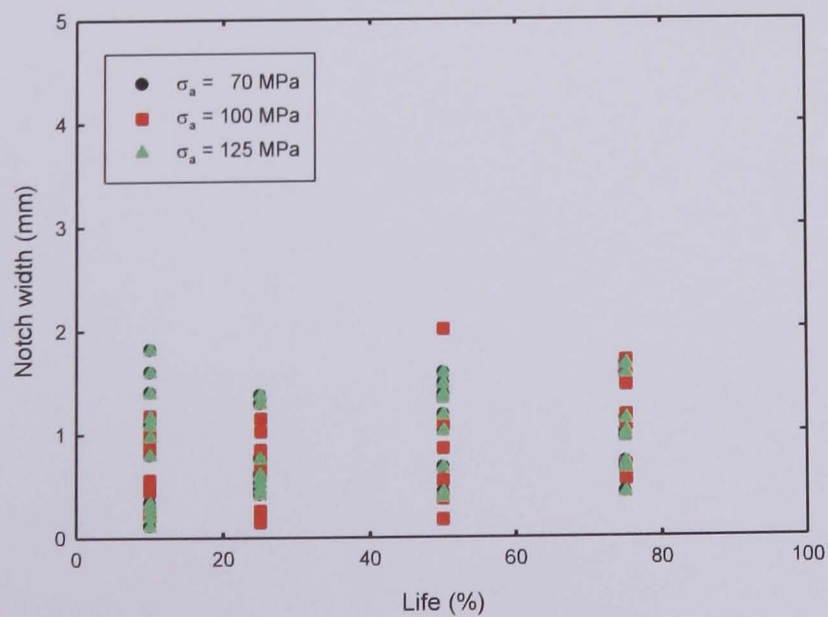
$\sigma_n = 10$ MPa:



$\sigma_n = 60$ MPa:

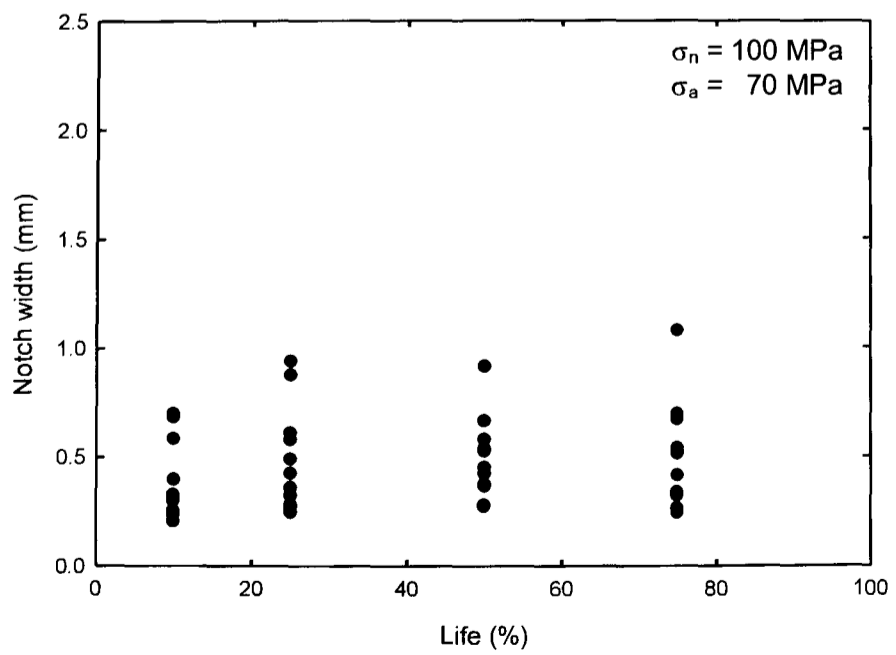
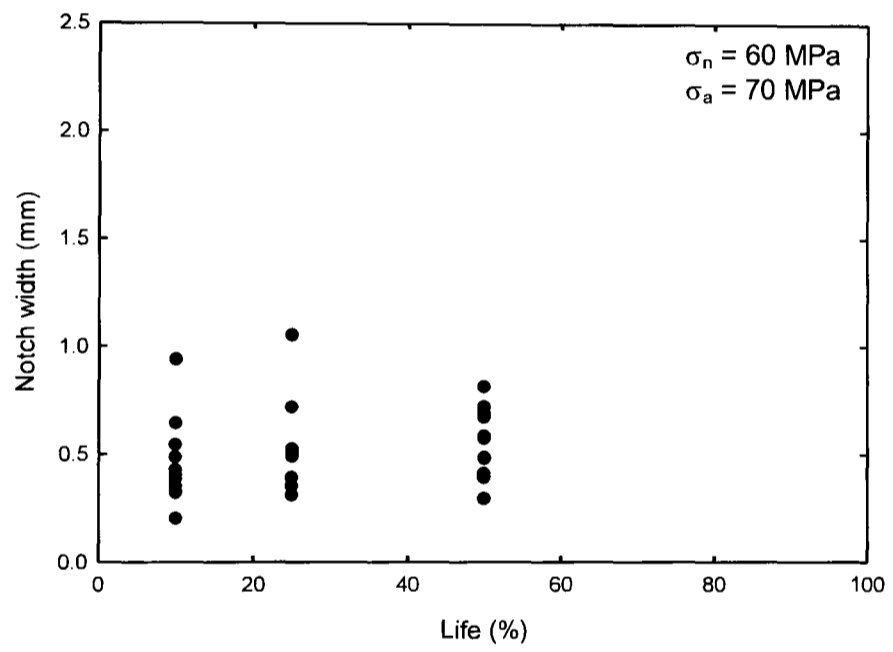
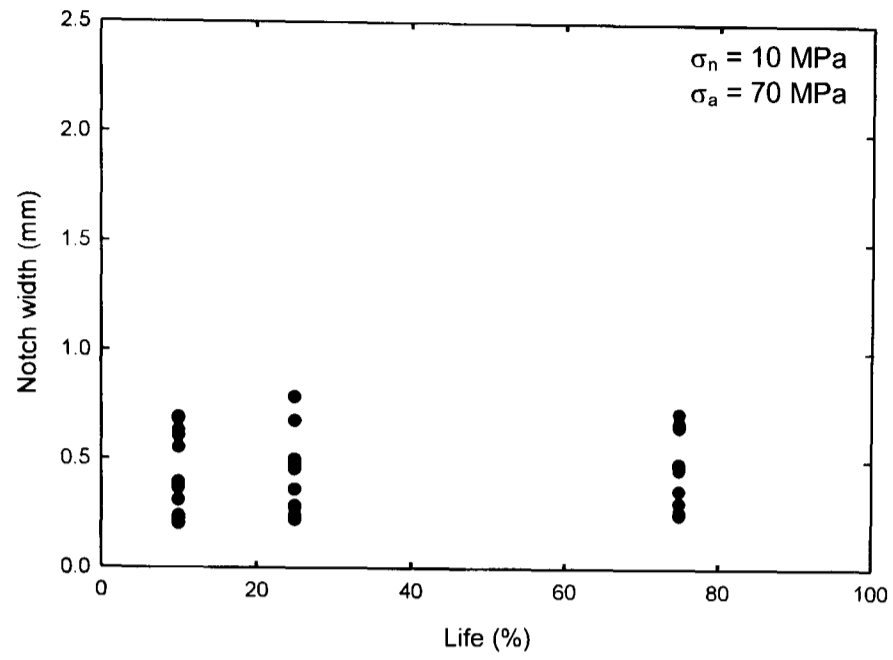


$\sigma_n = 100$ MPa:

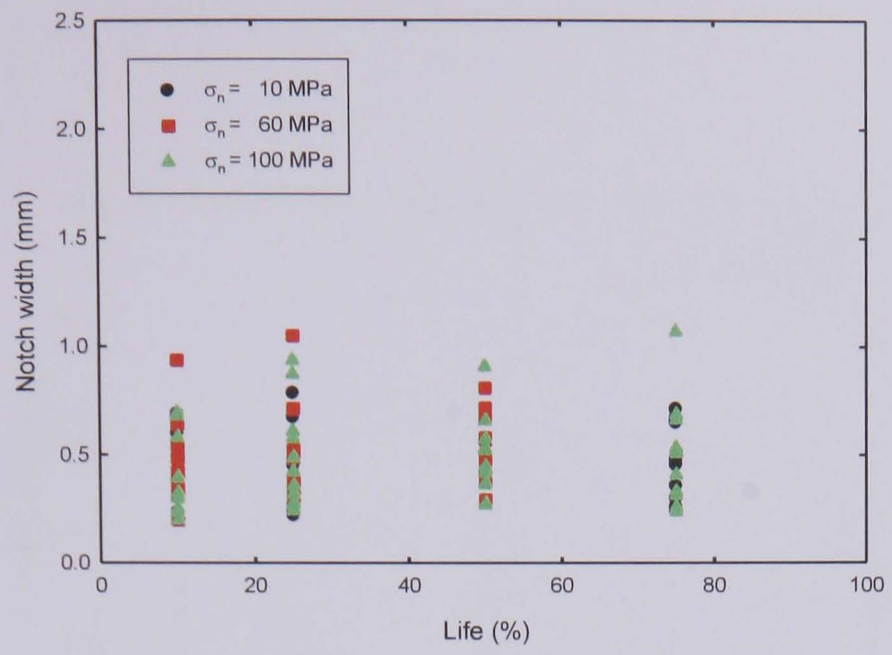


L.5

SCAR WIDTH: $\sigma_a = 70$ MPa peened

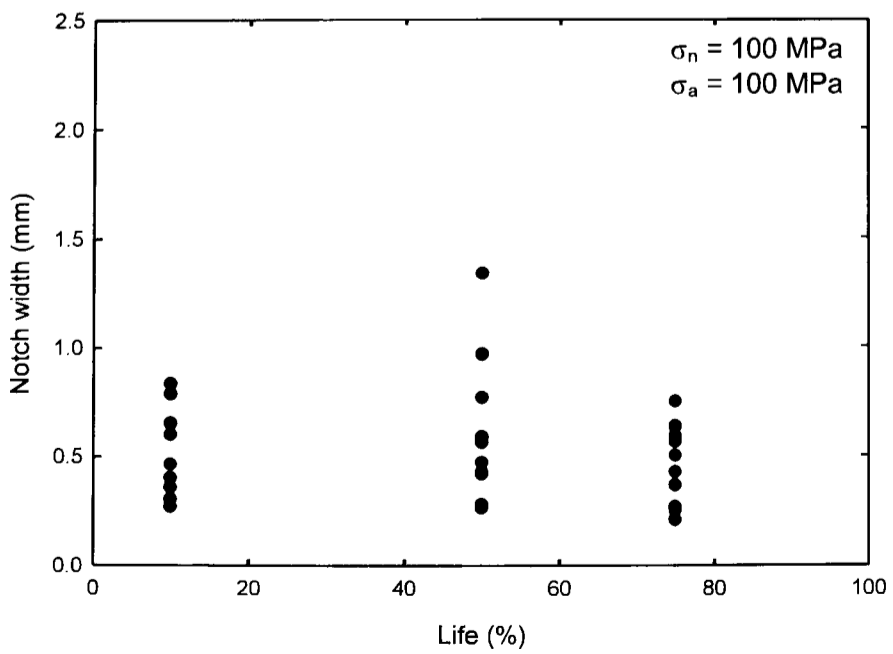
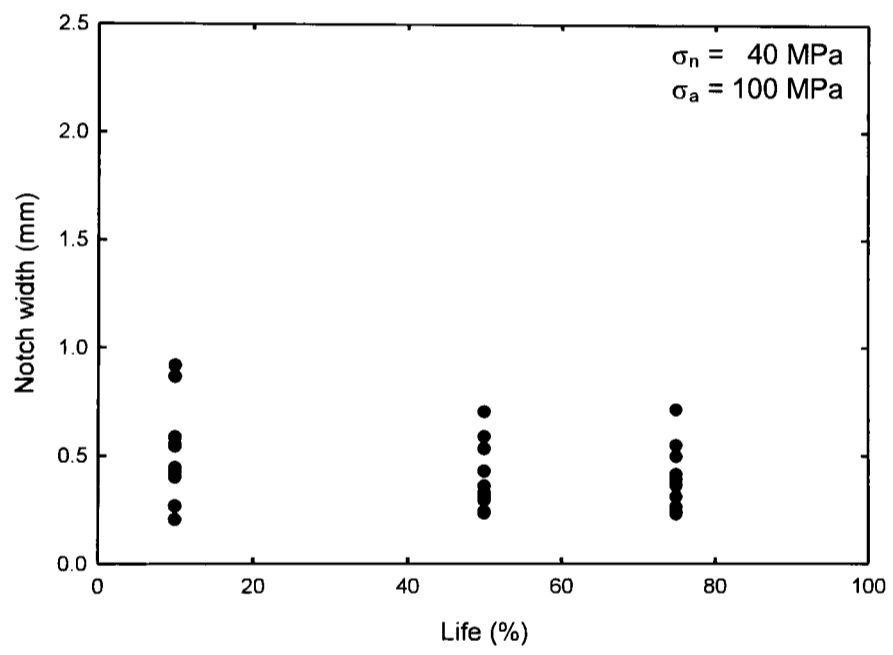
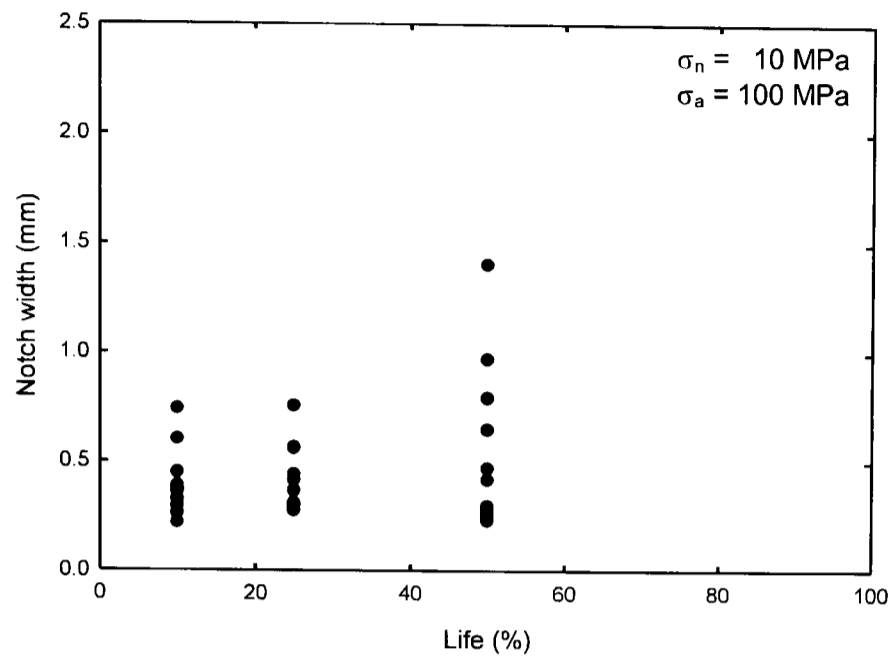


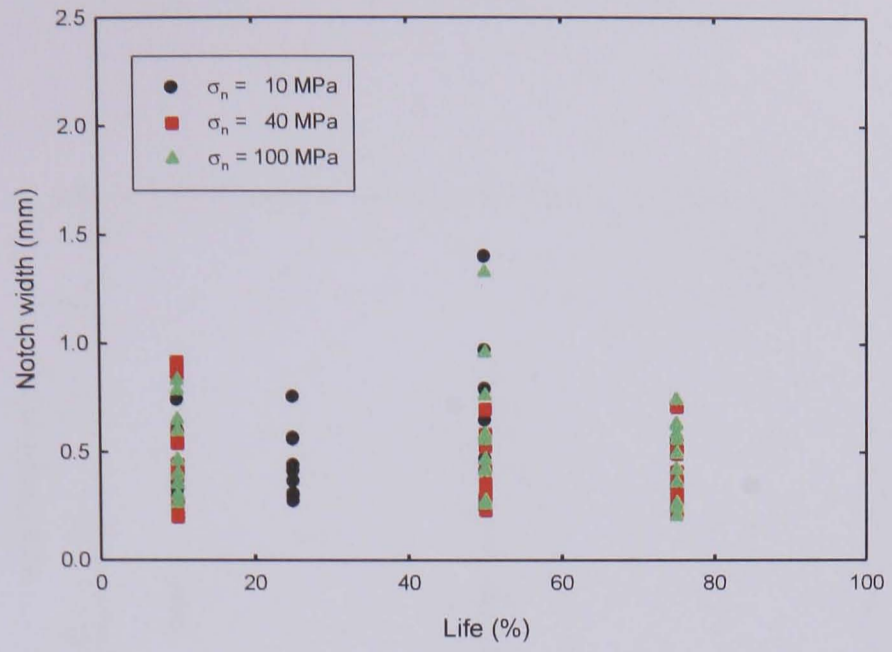
LEADING SCAR WIDTH vs. LIFE



L.6

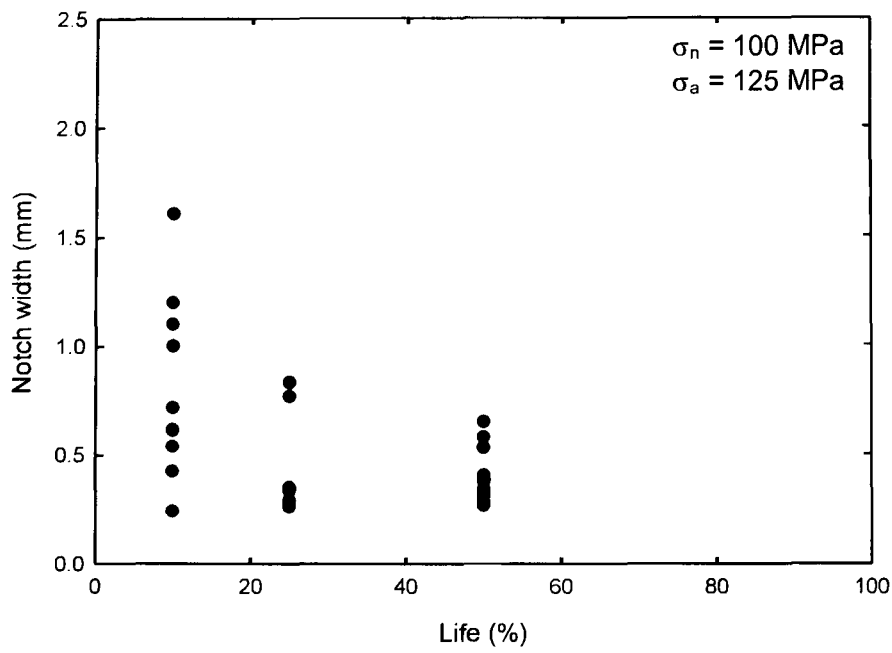
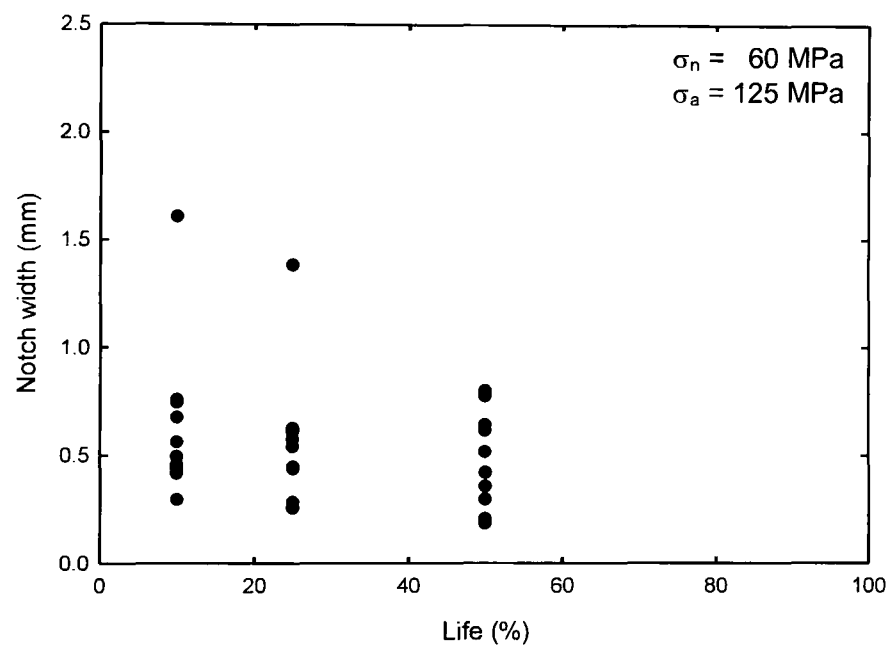
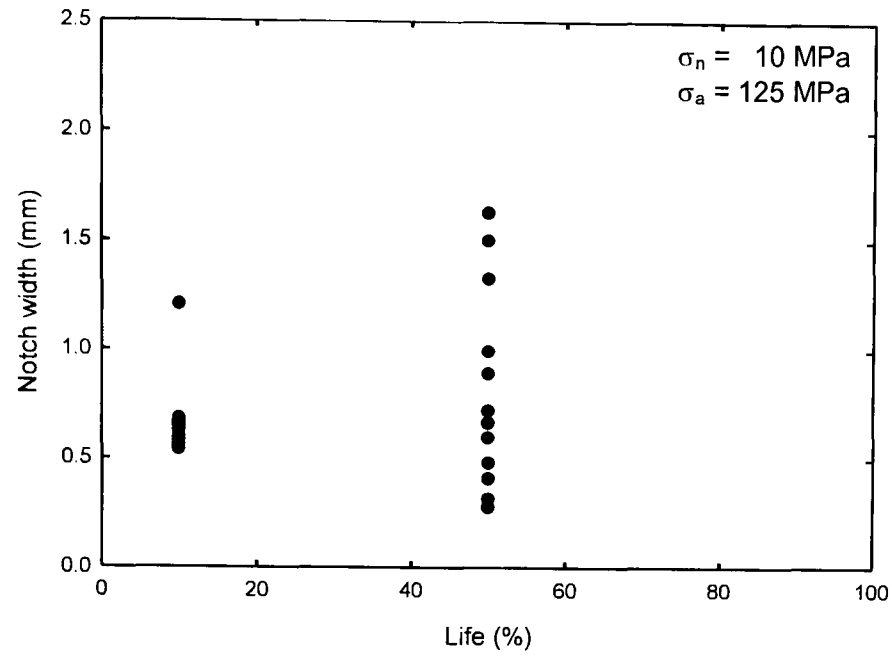
SCAR WIDTH: $\sigma_a = 100$ MPa peened

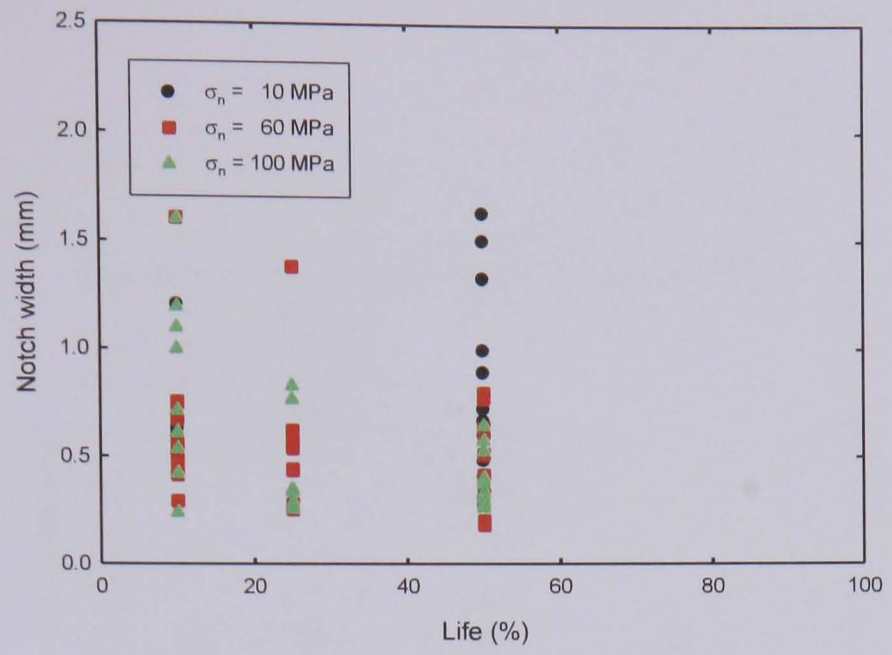




L.7

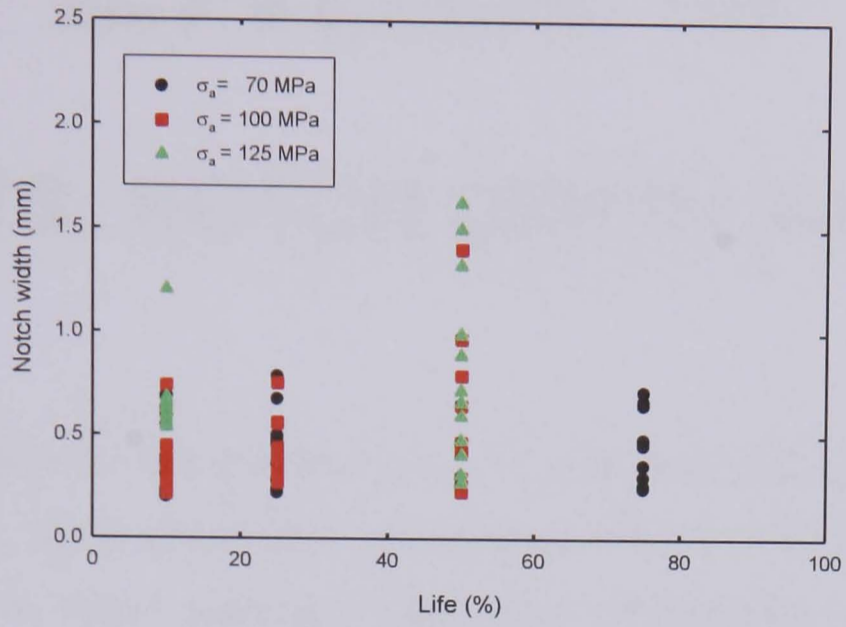
SCAR WIDTH: $\sigma_a = 125$ MPa peened



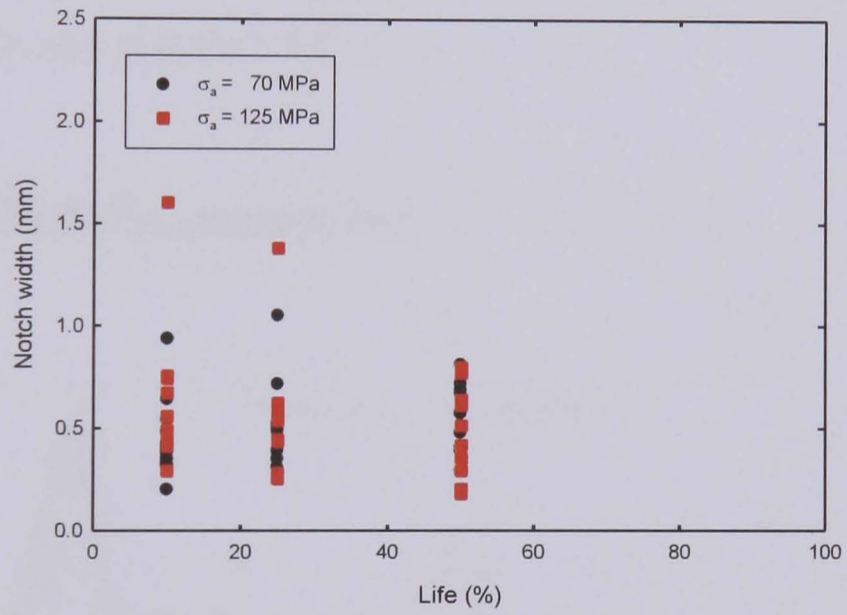


L.8 SCAR WIDTH: Peened

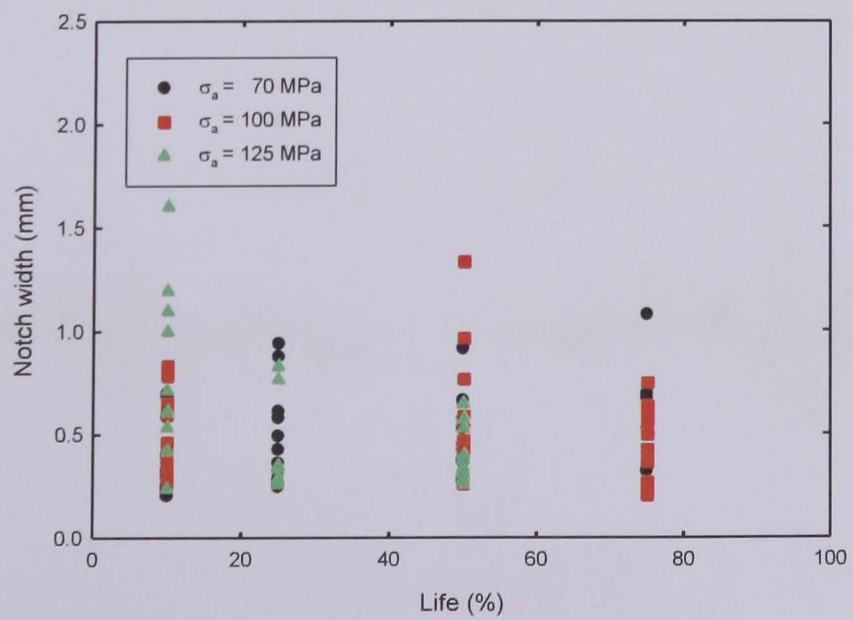
$\sigma_n = 10$ MPa:



$\sigma_n = 60$ MPa:



$\sigma_n = 100$ MPa:

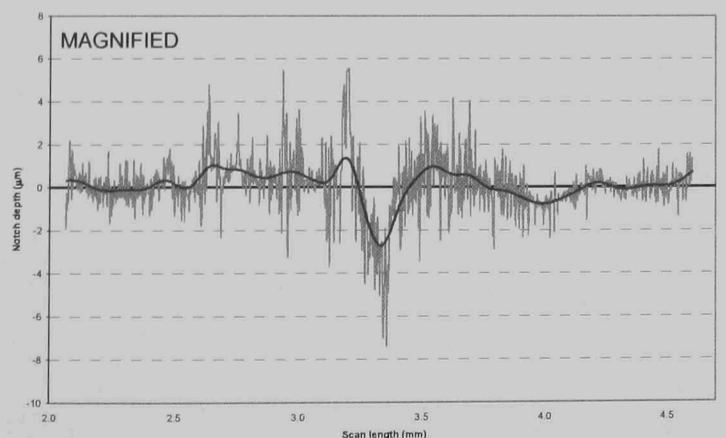
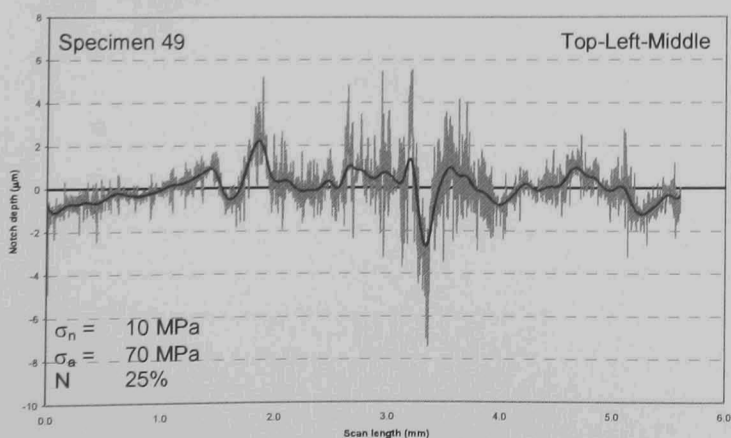
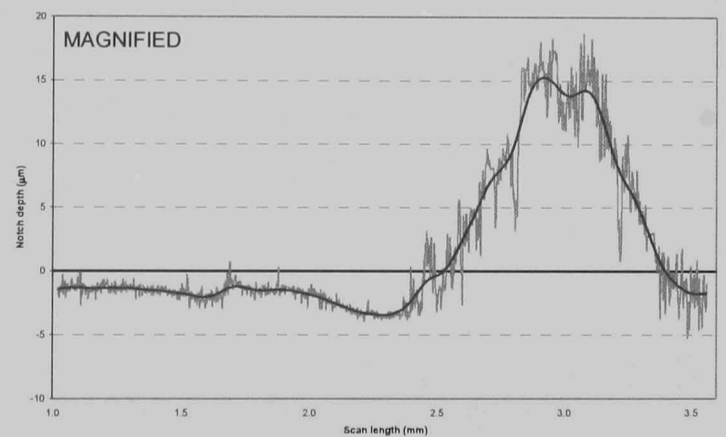
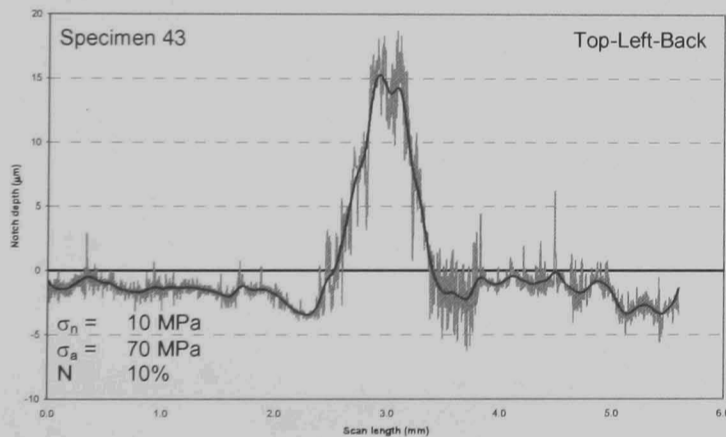


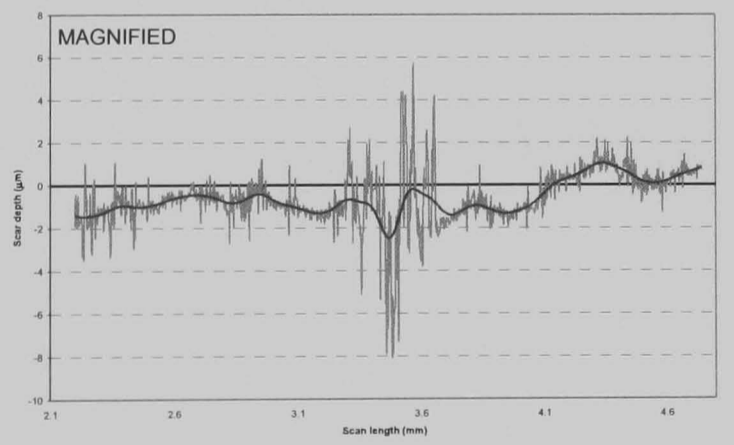
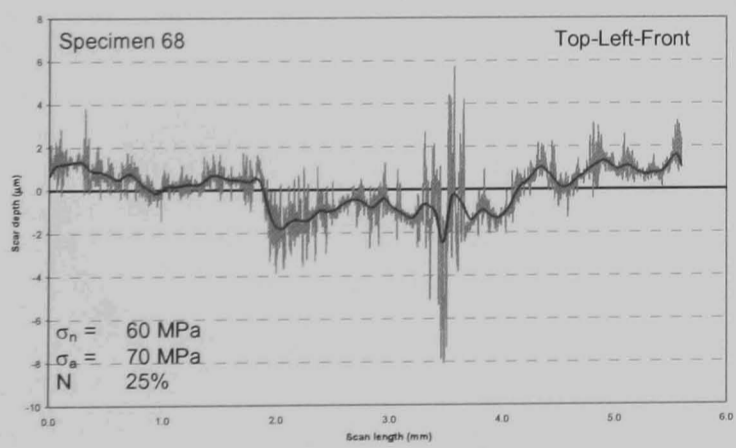
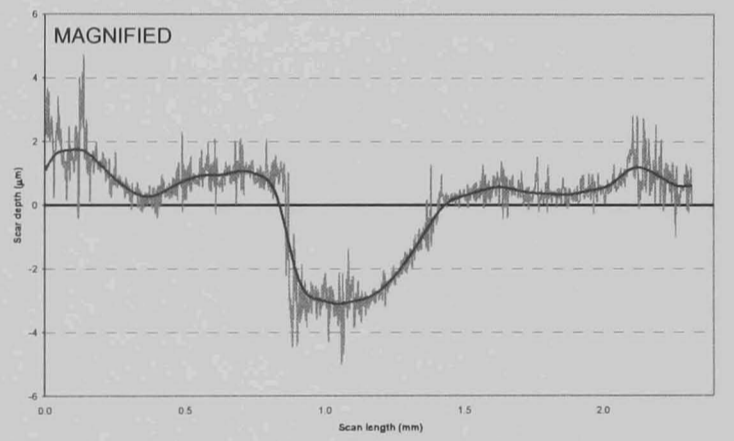
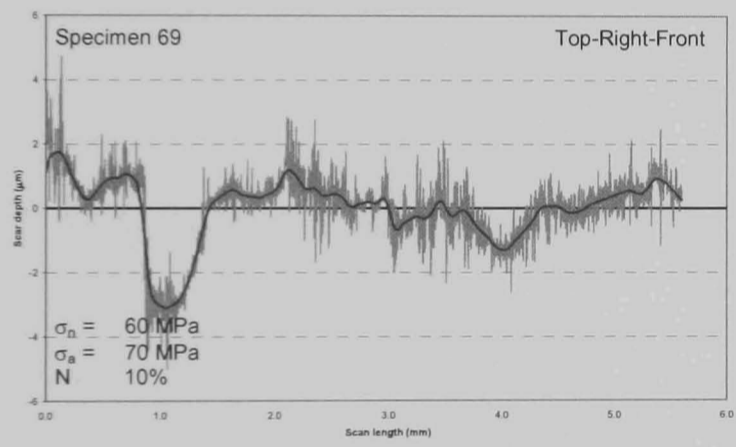
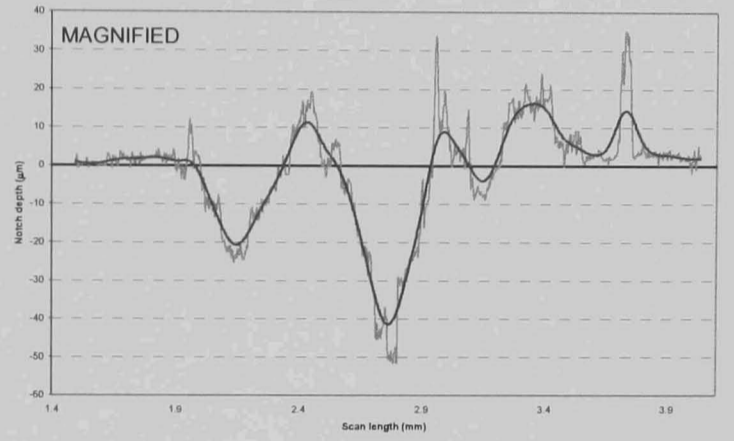
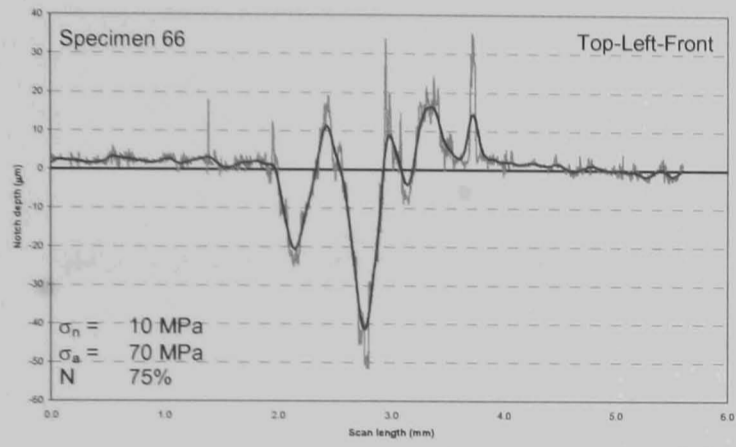
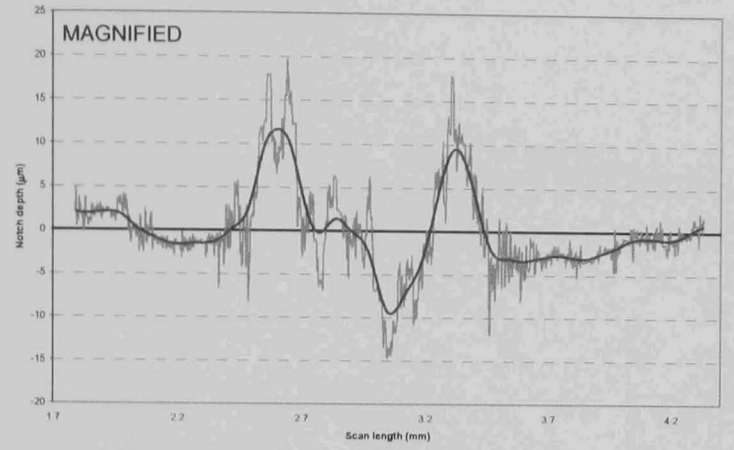
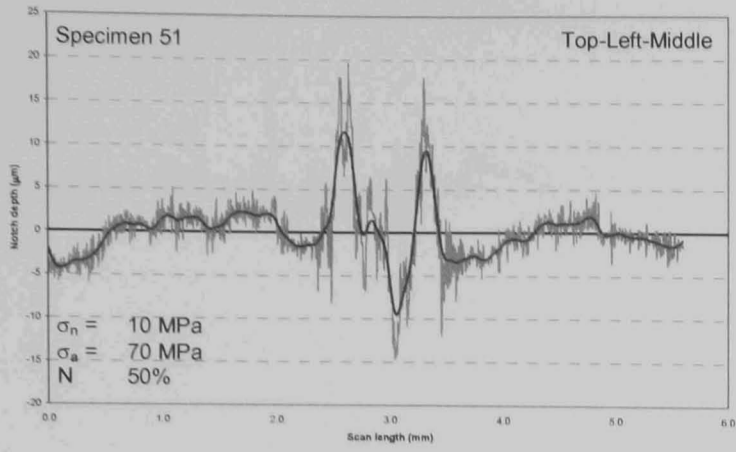
APPENDIX M

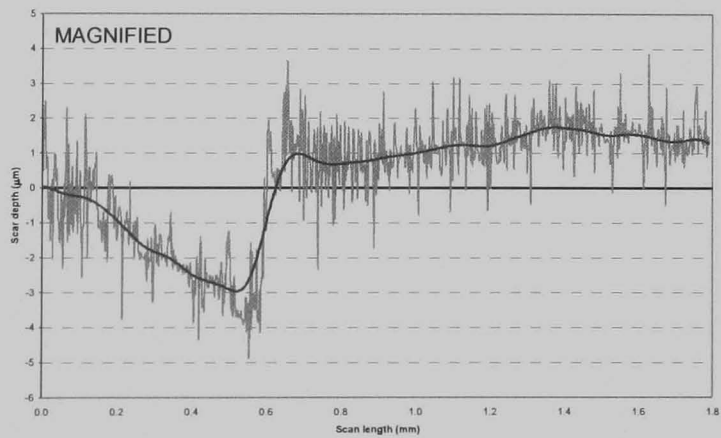
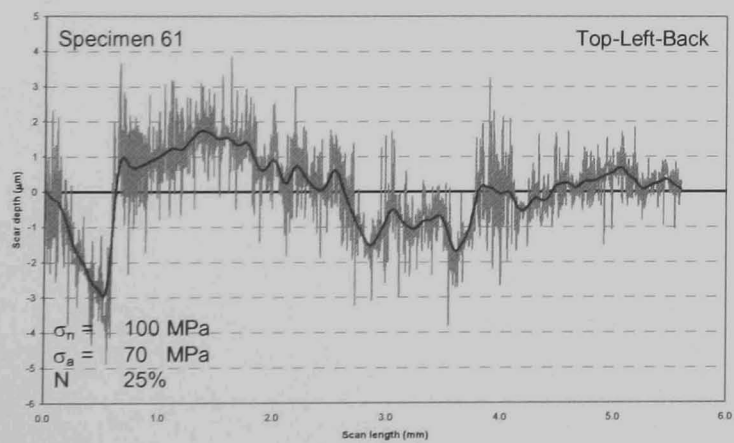
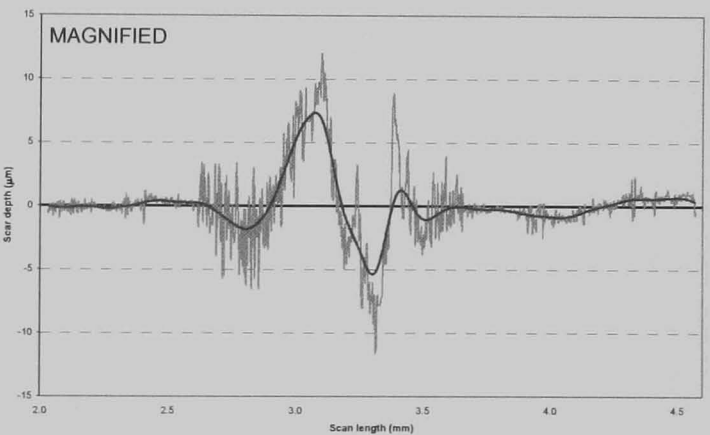
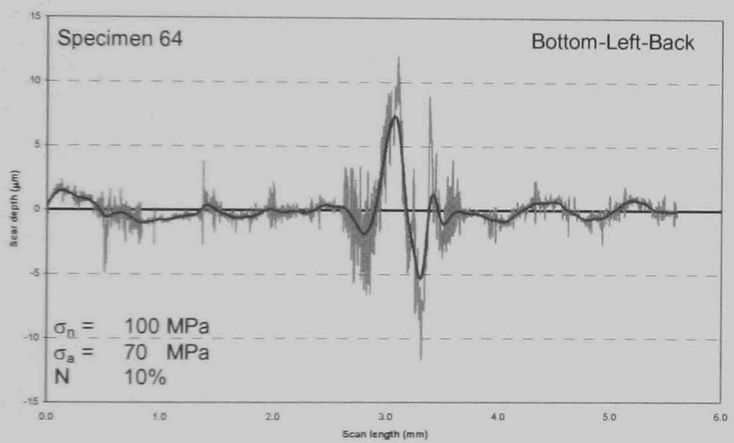
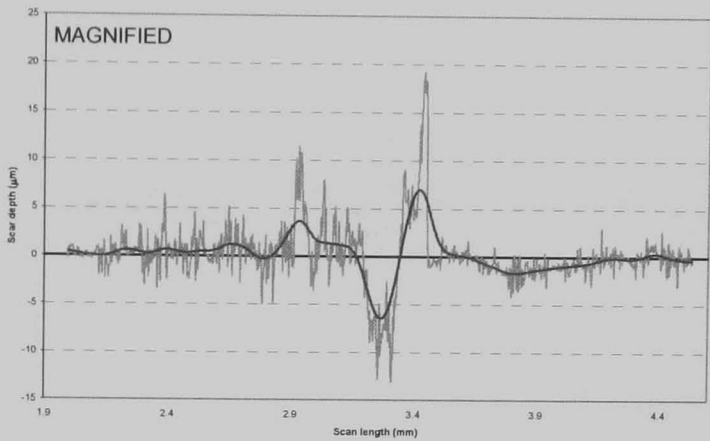
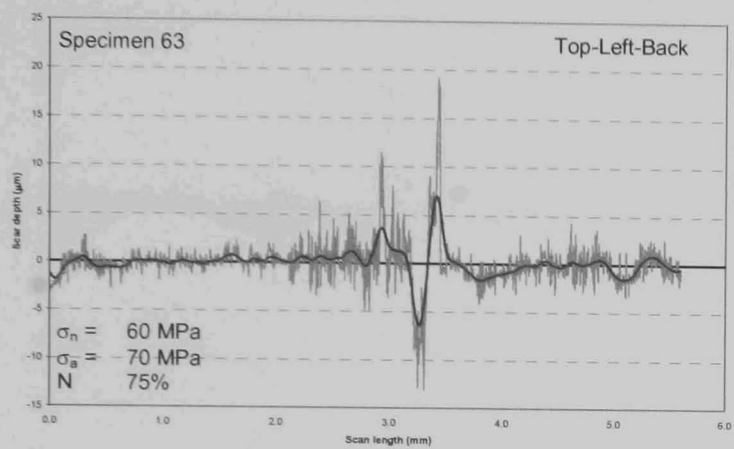
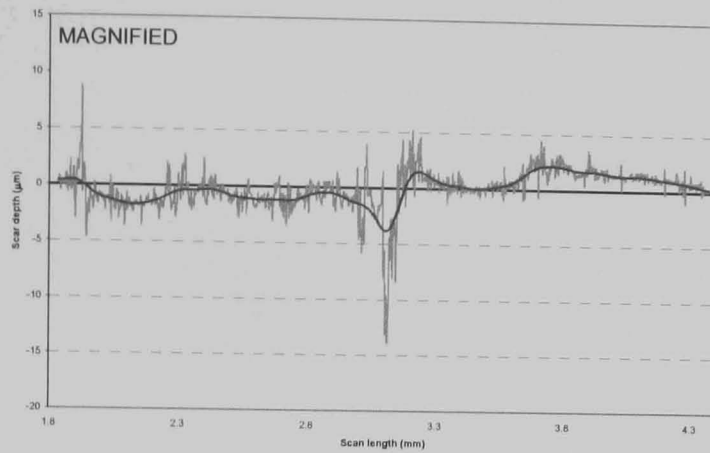
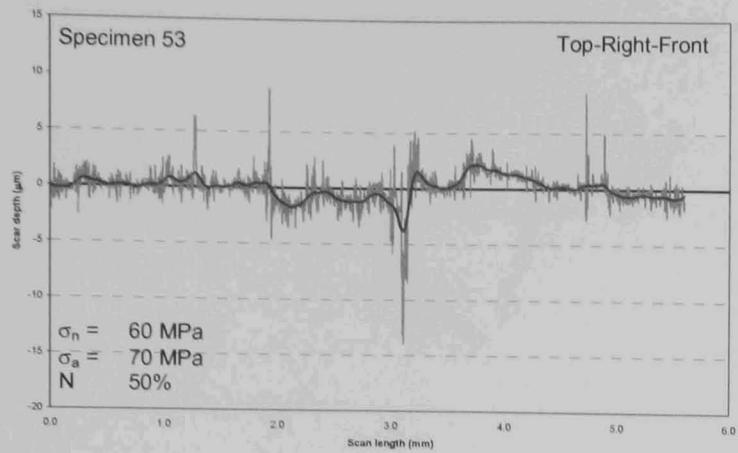
RESULTS: NOTCH DEPTH PROFILES

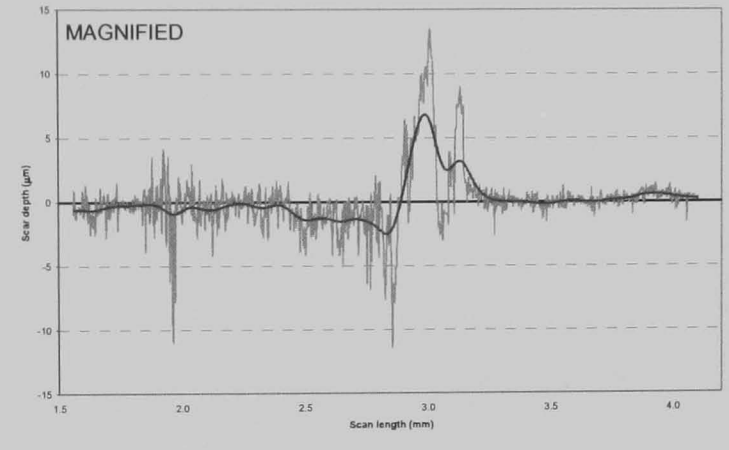
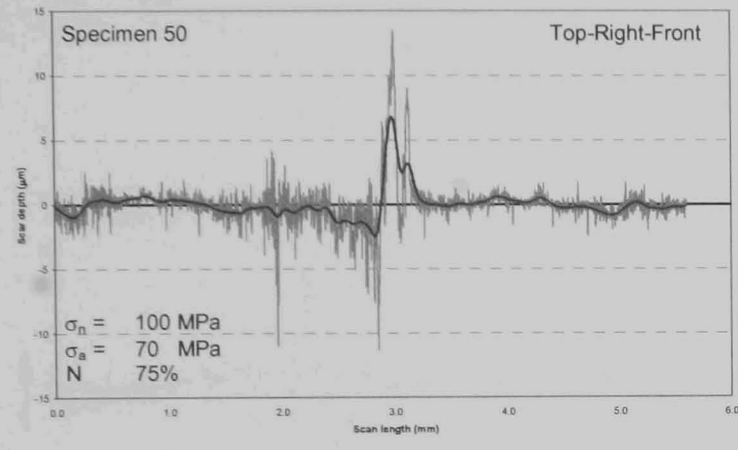
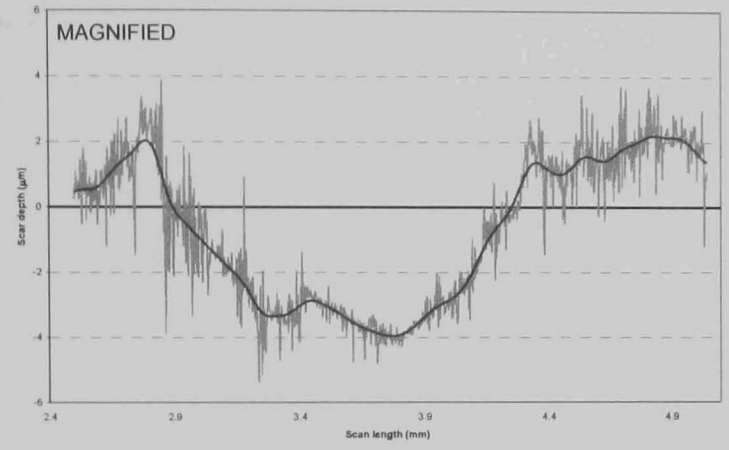
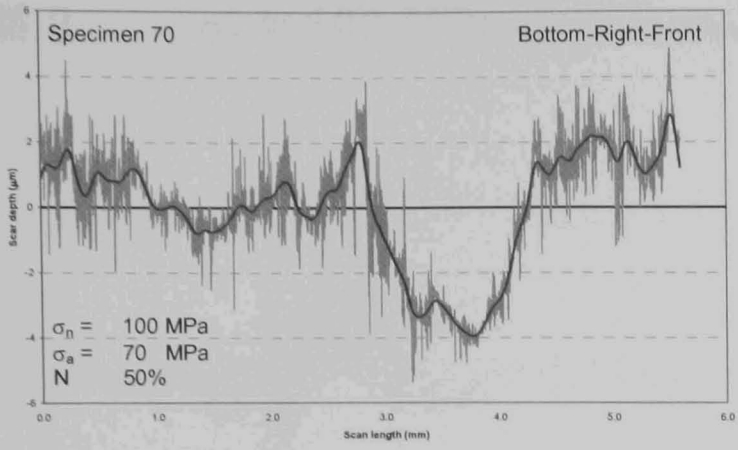
Notch depth profiles for the greatest notch depths found for each combination of normal pressure, axial stress and percentage life for both the unpeened and peened conditions, taken utilising a UBM laser profilometer, with a scan length of 5.6 mm. The original traces are shown, together with a corresponding magnified view of the areas of interest. All traces have been smoothed with a constant, σ , of 20, see Section 3.5.3.

M.1 $\sigma_a = 70$ MPa unpeened

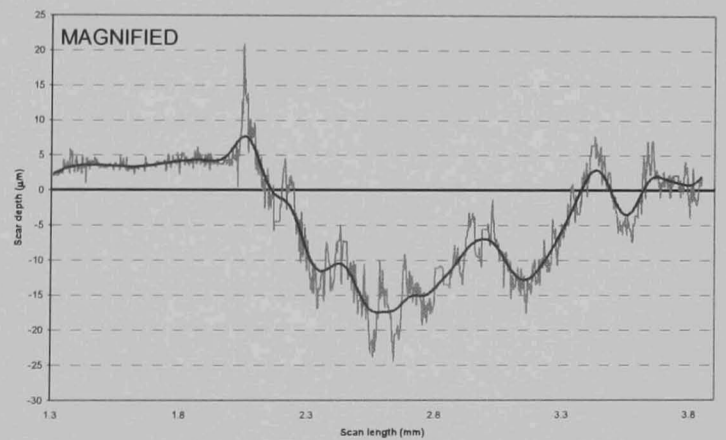
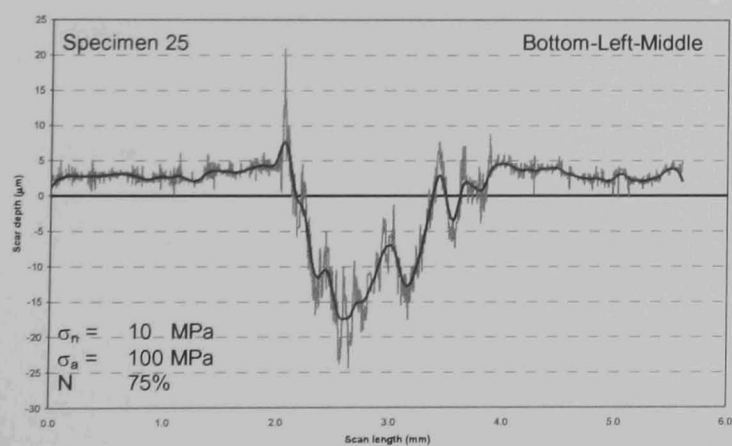
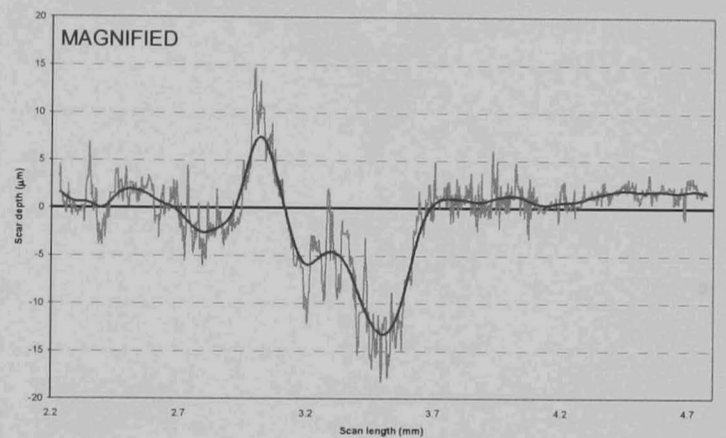
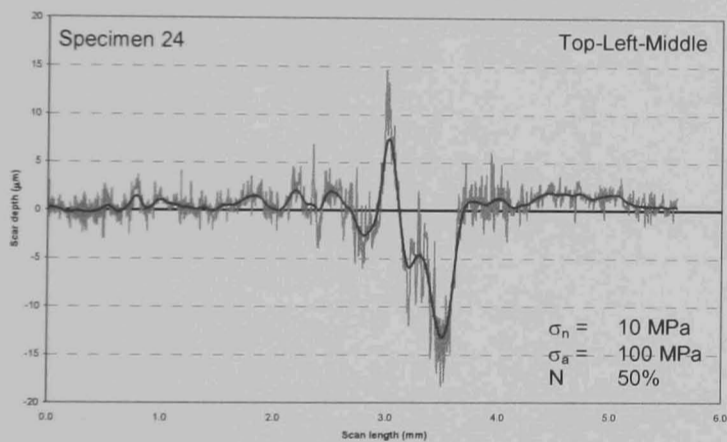
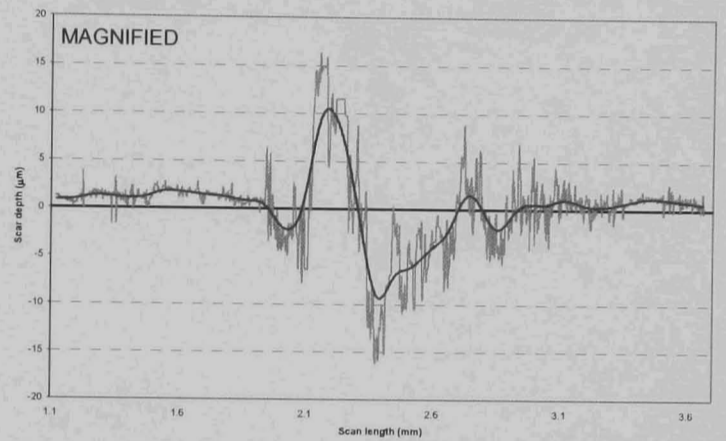
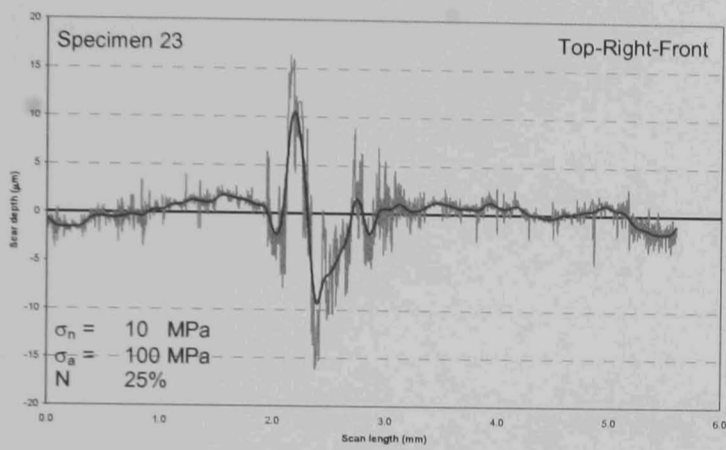
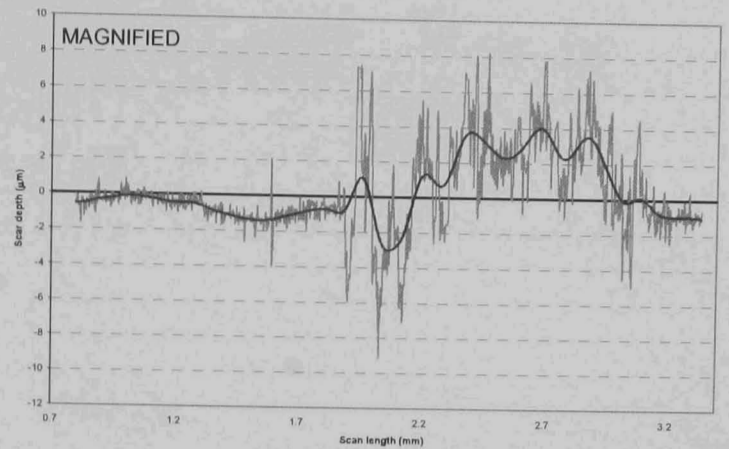
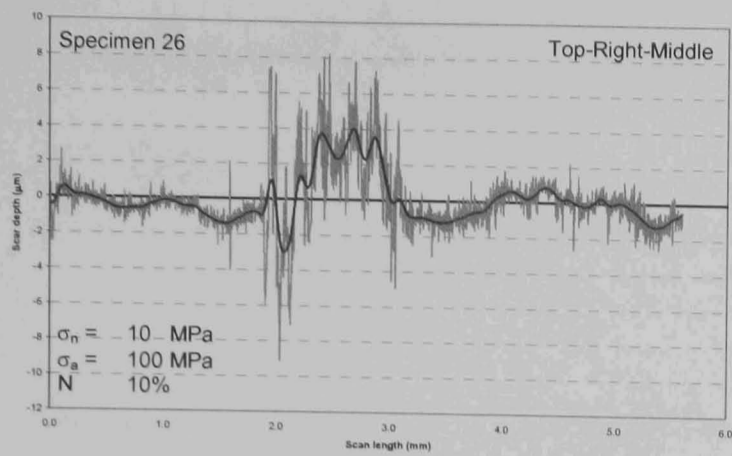


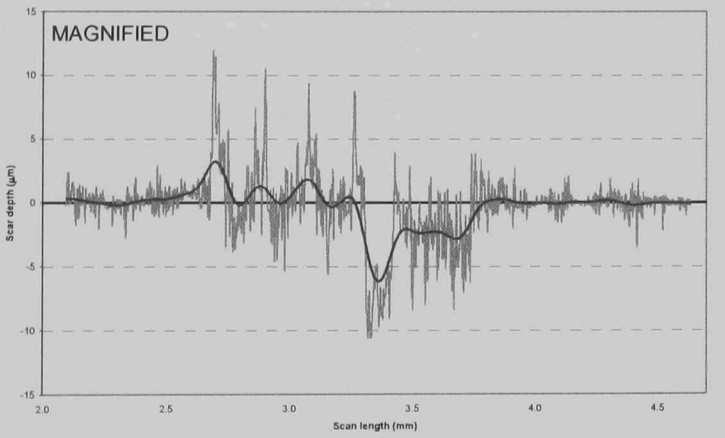
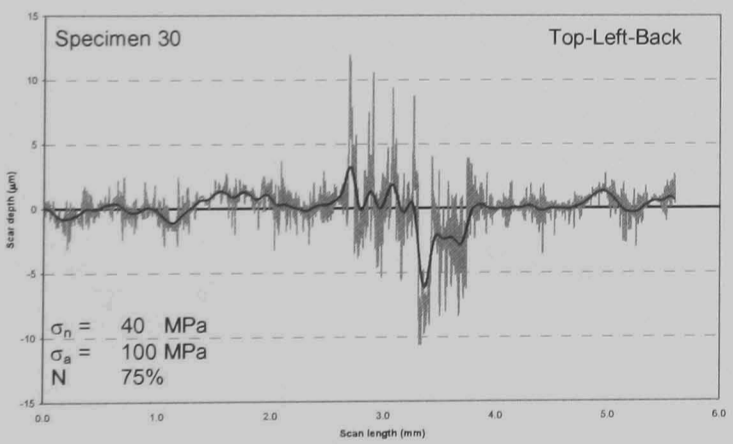
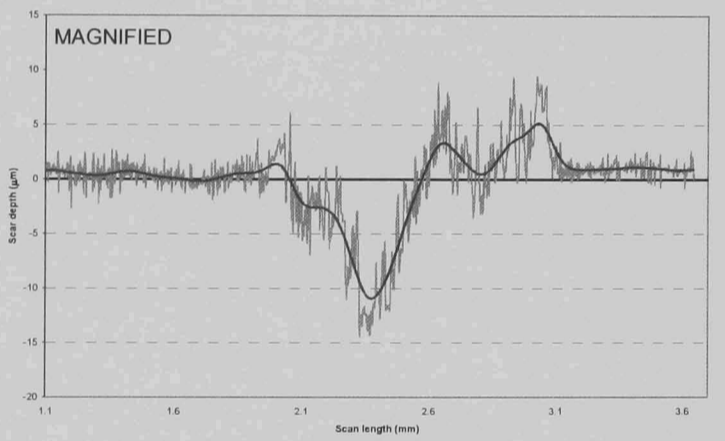
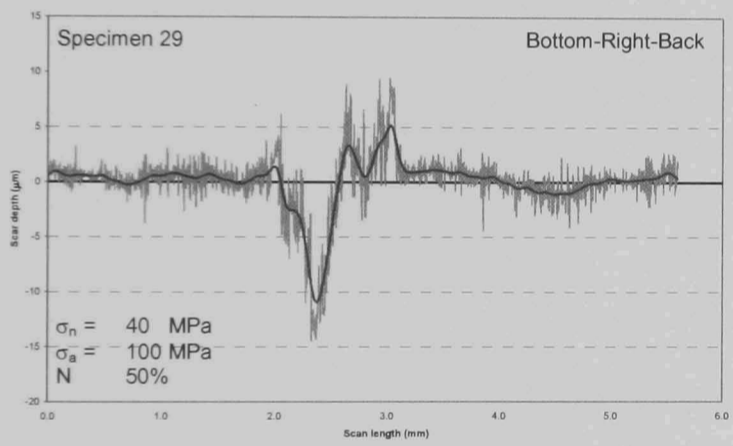
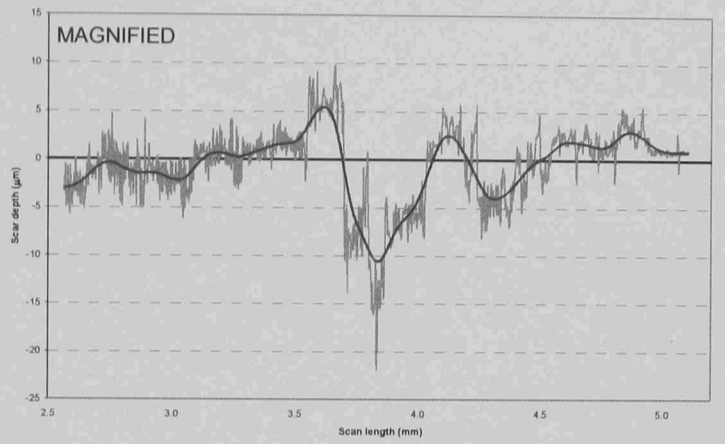
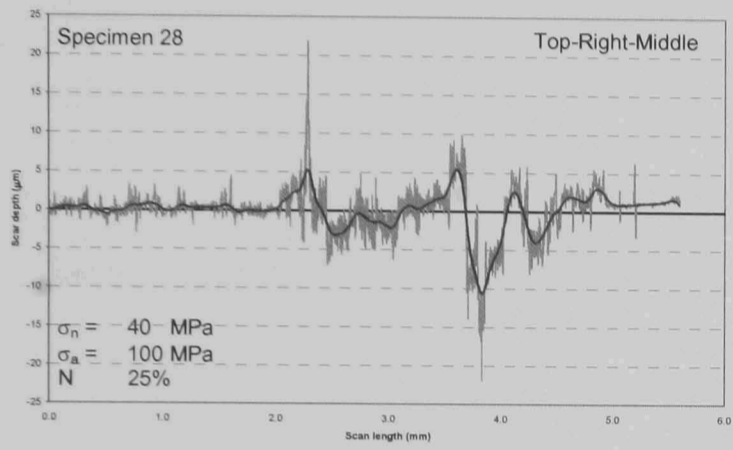
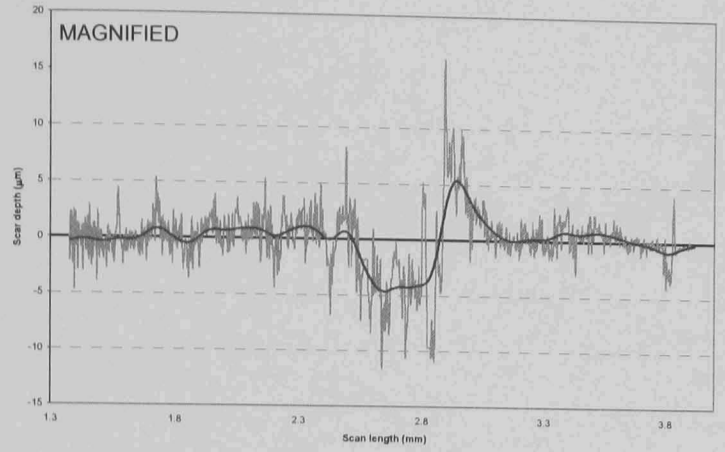
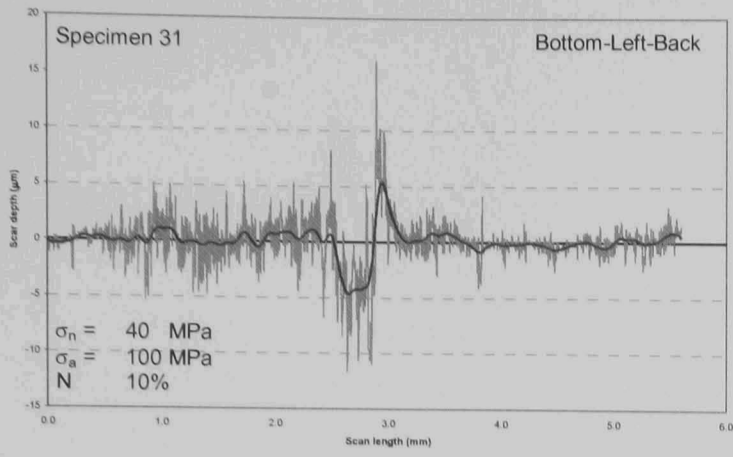


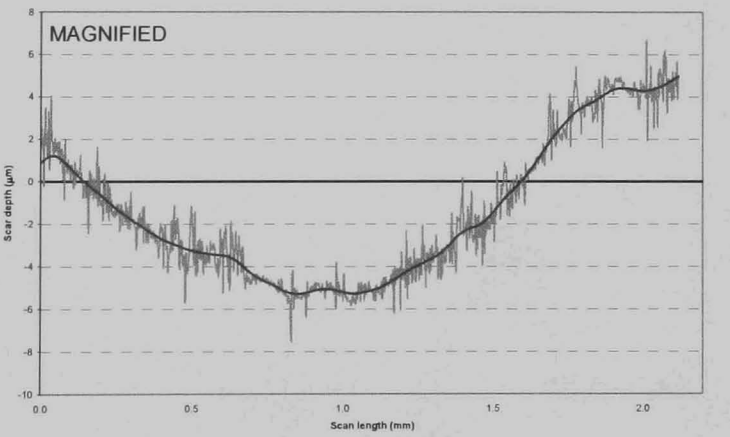
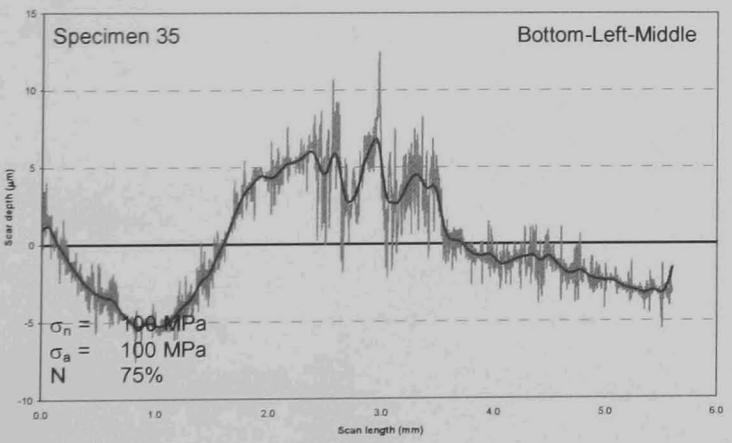
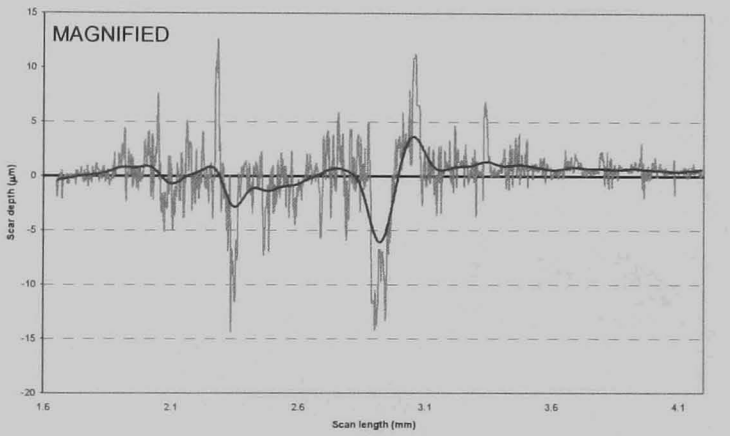
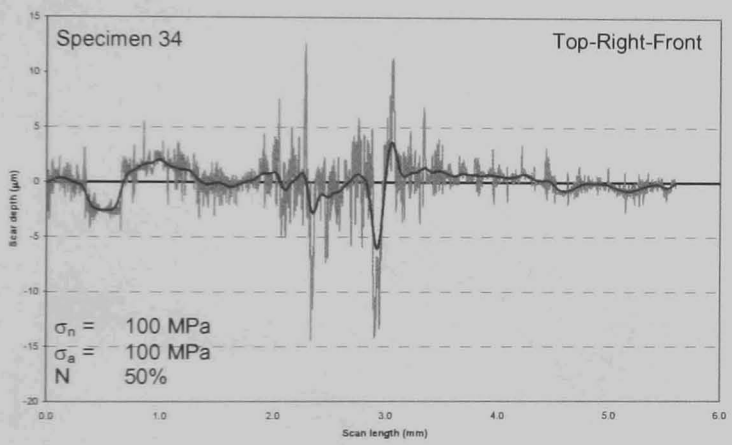
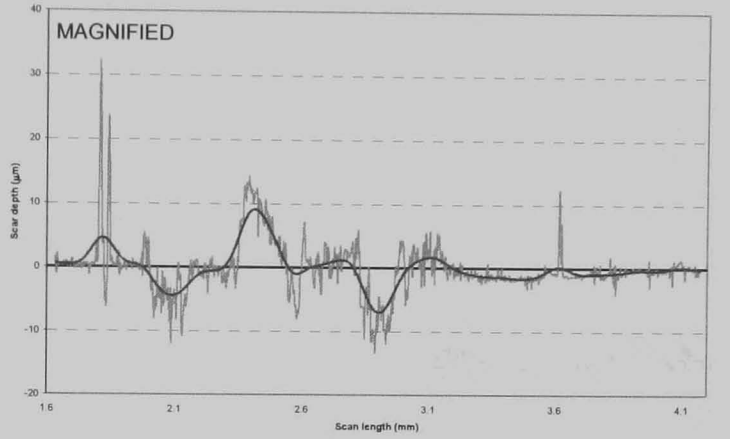
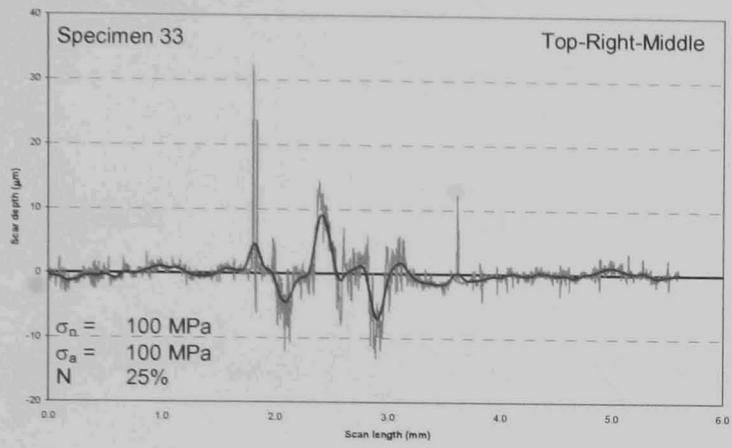
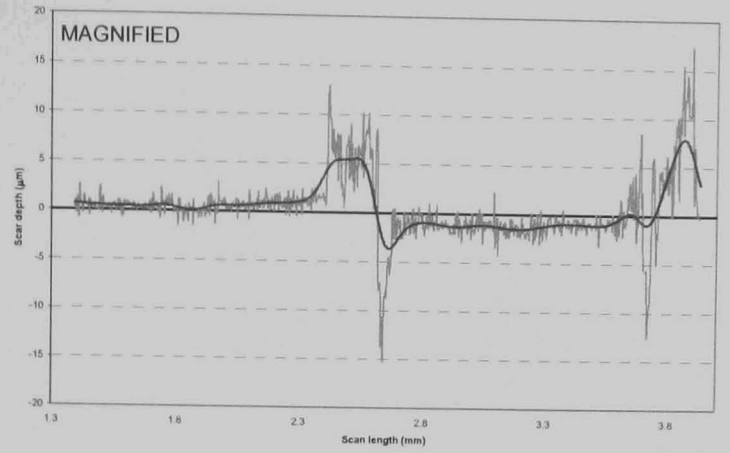
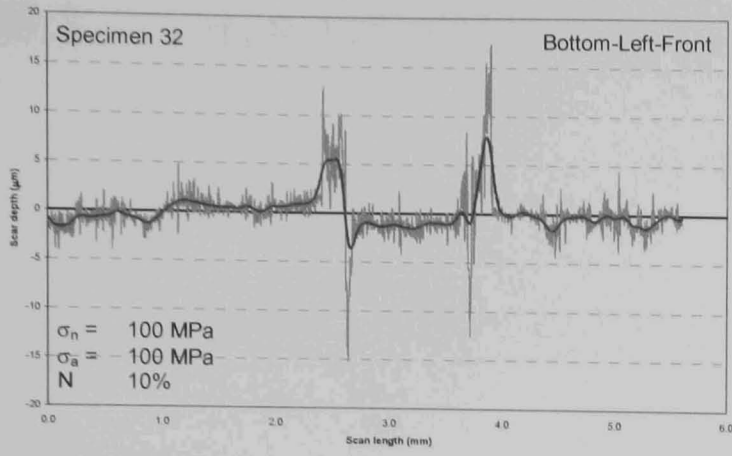




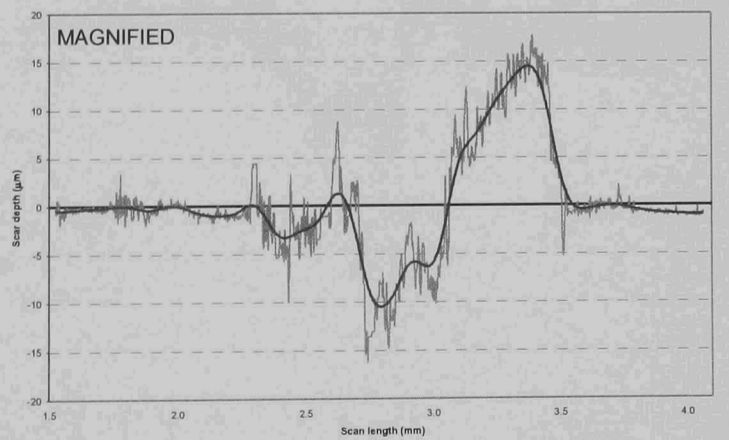
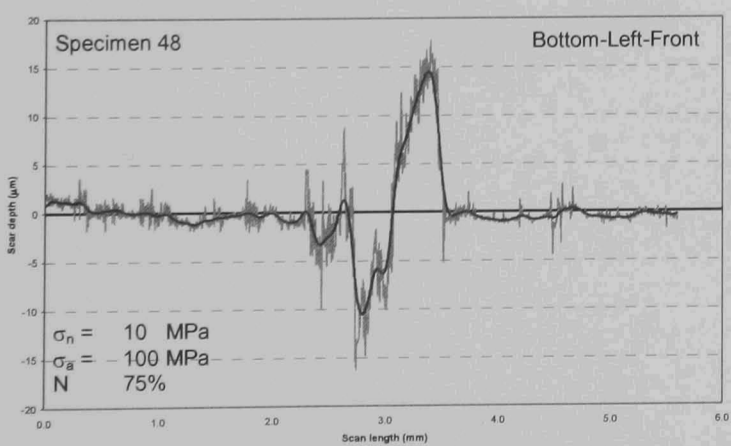
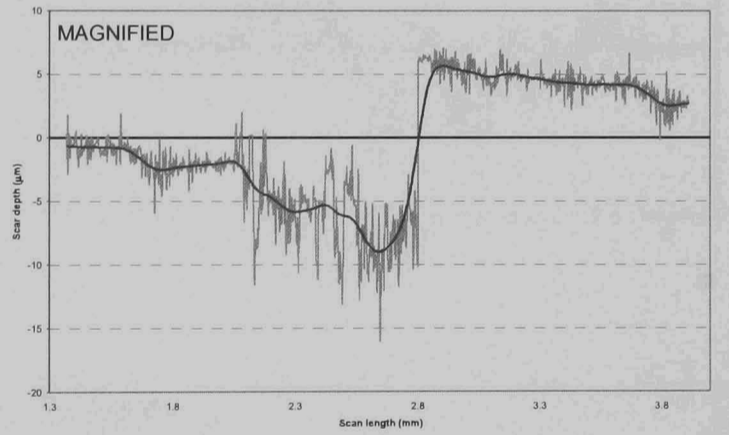
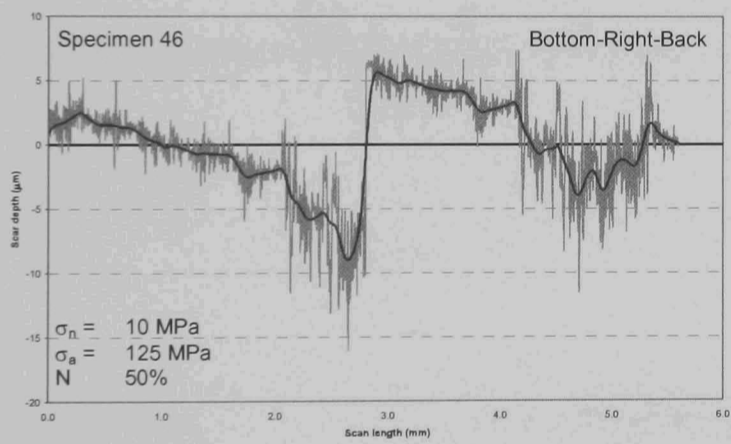
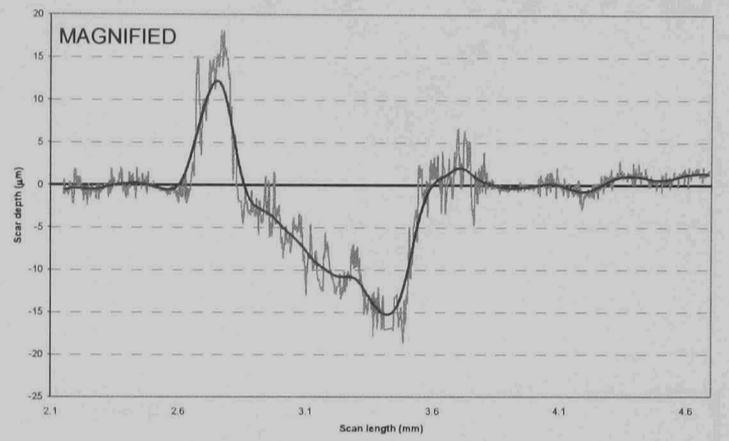
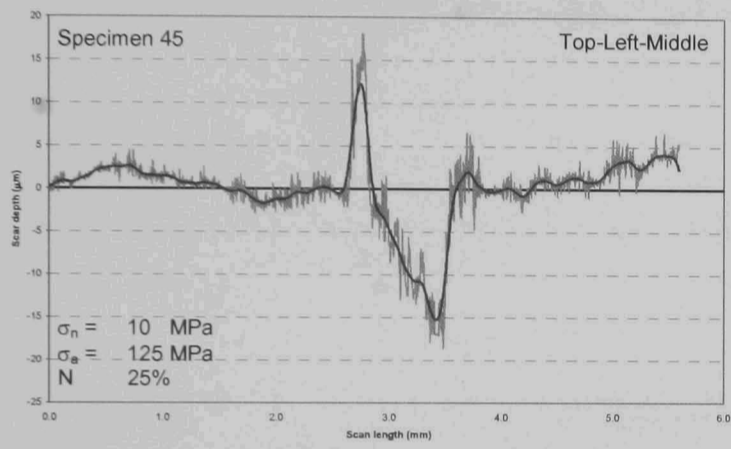
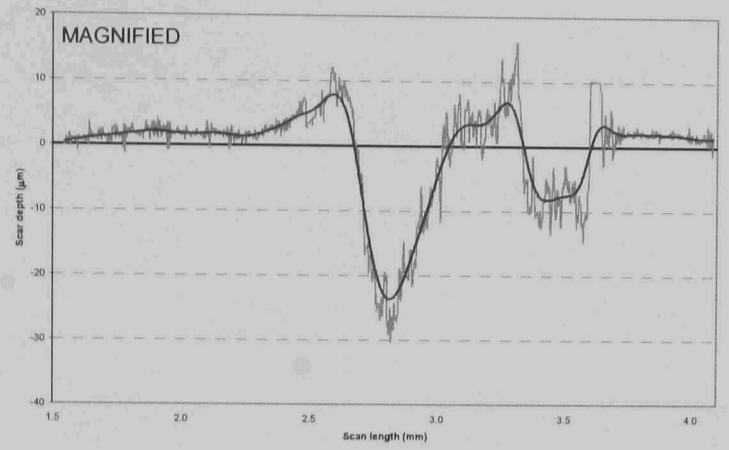
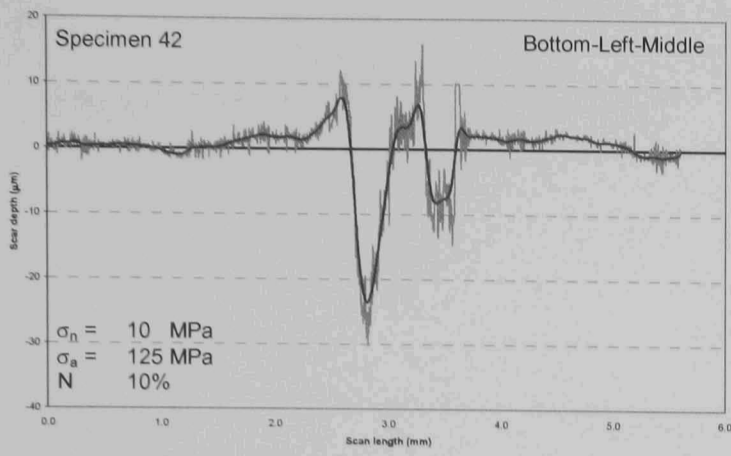
M.2 $\sigma_a = 100$ MPa unpeened

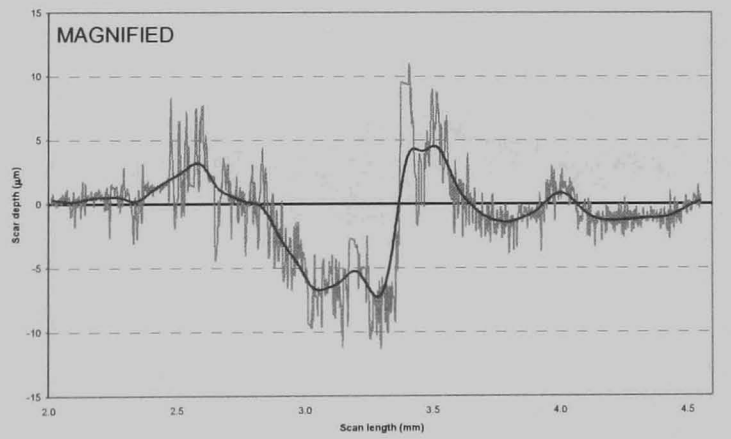
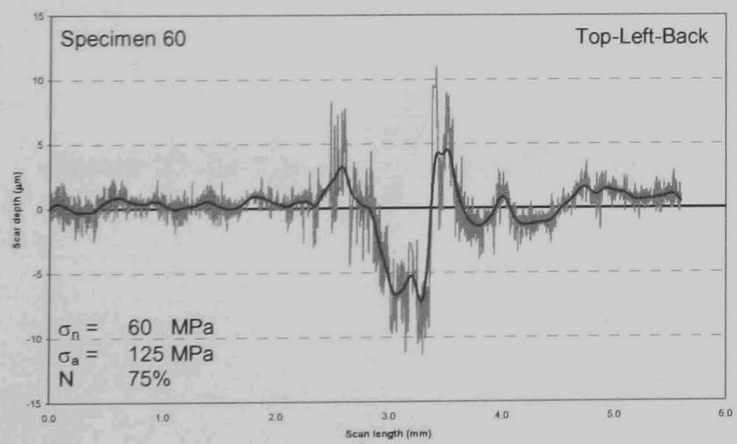
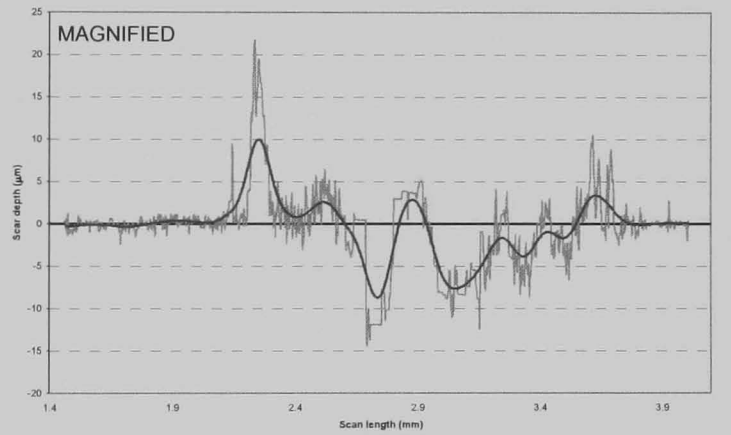
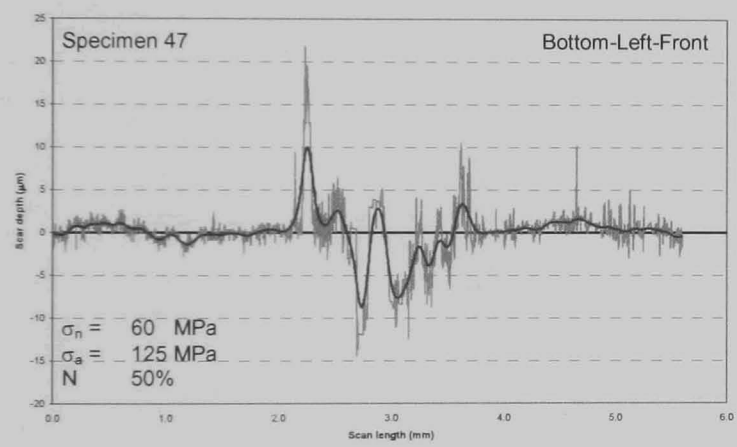
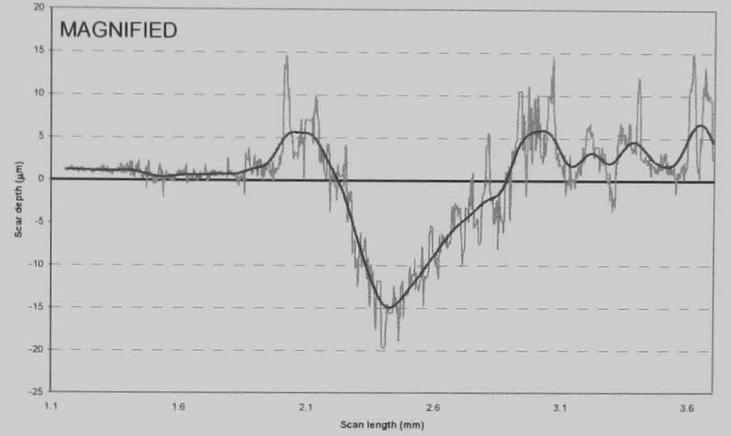
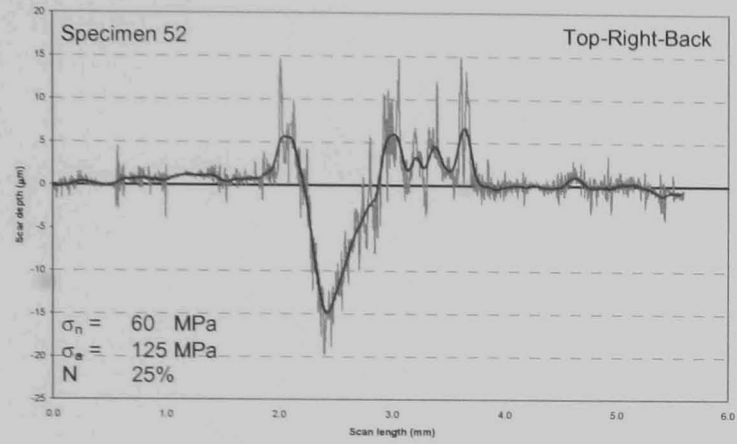
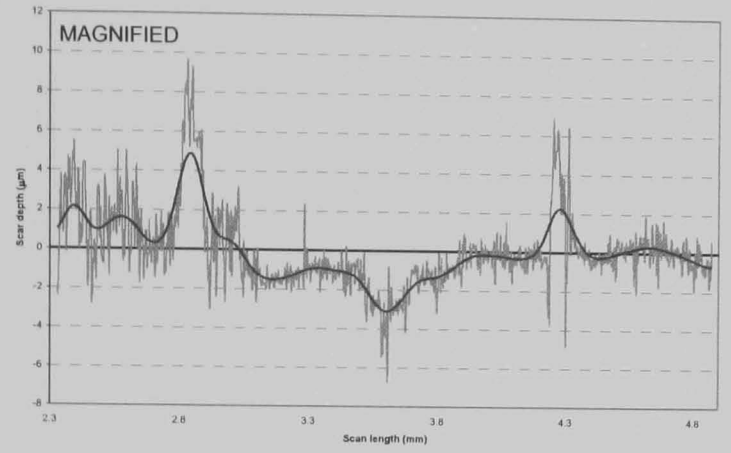
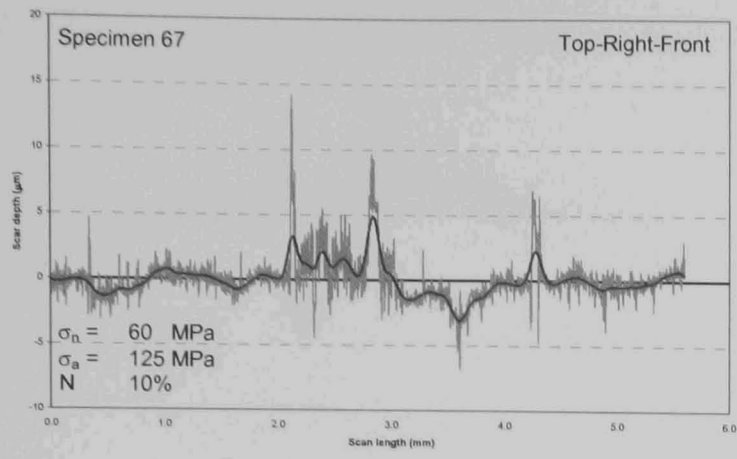


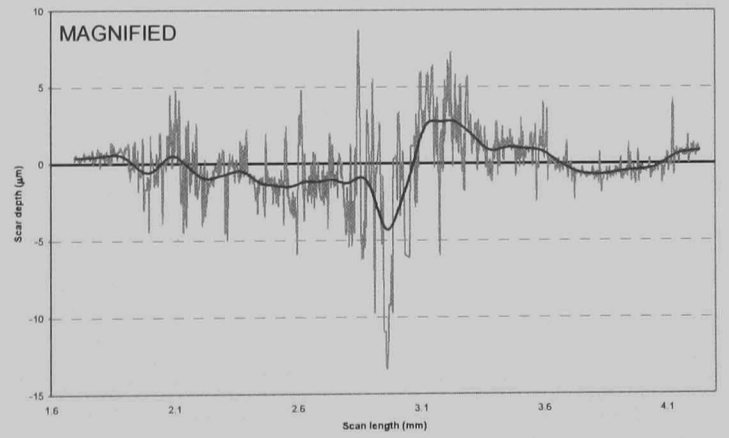
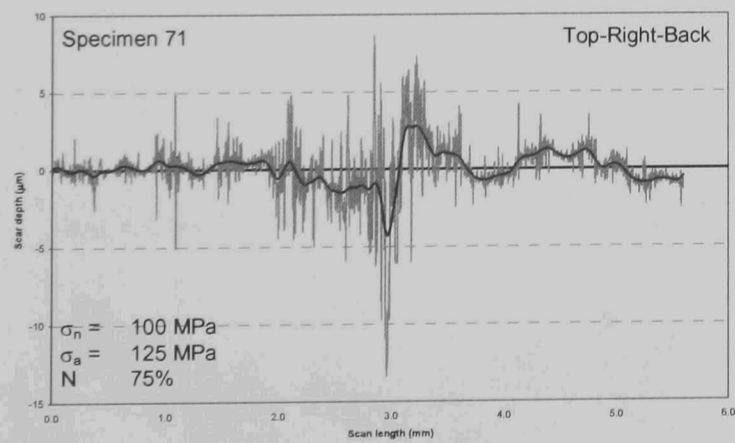
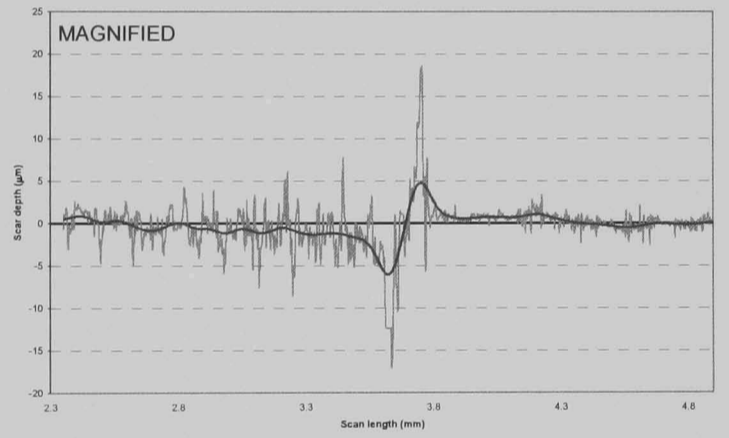
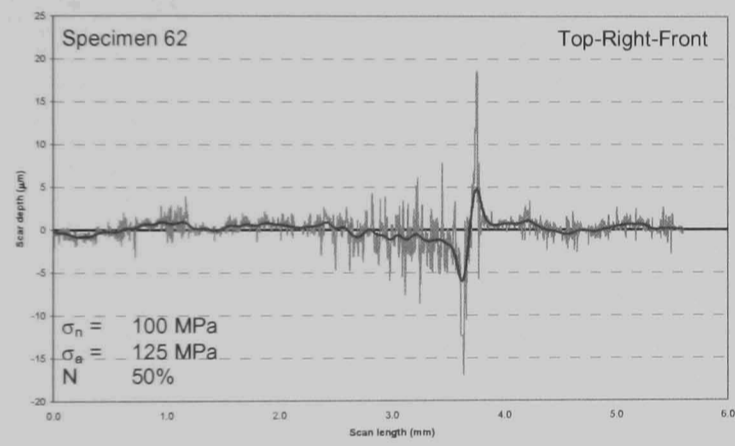
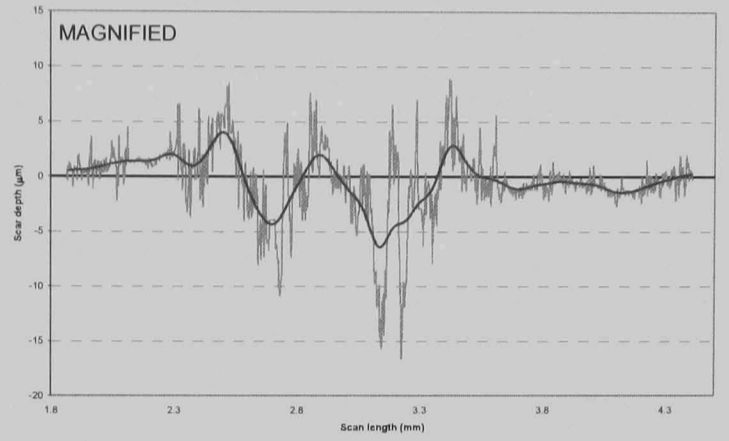
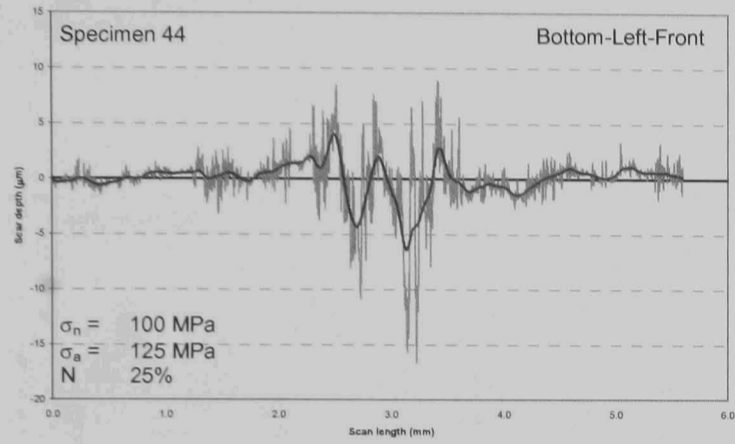
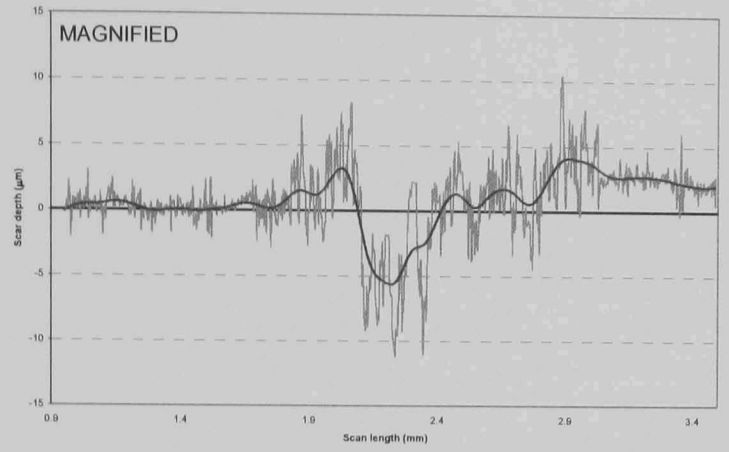
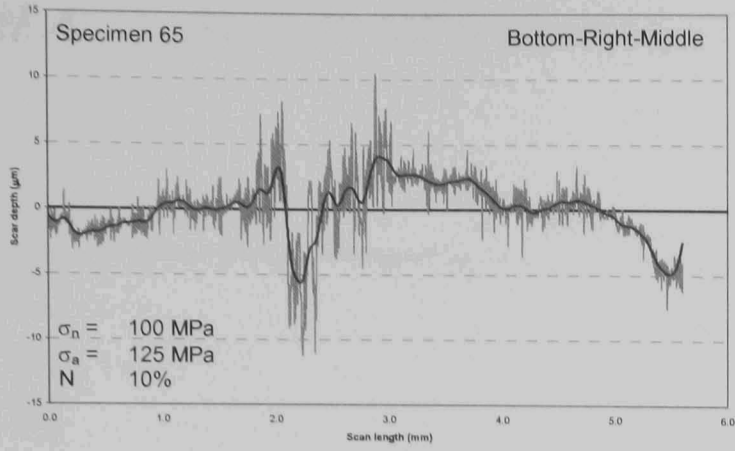




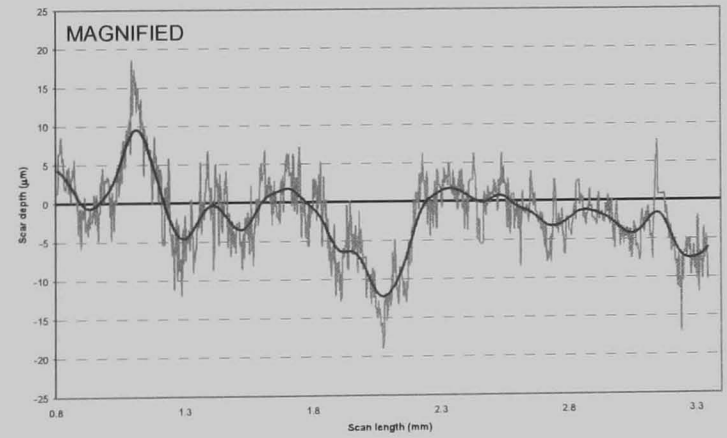
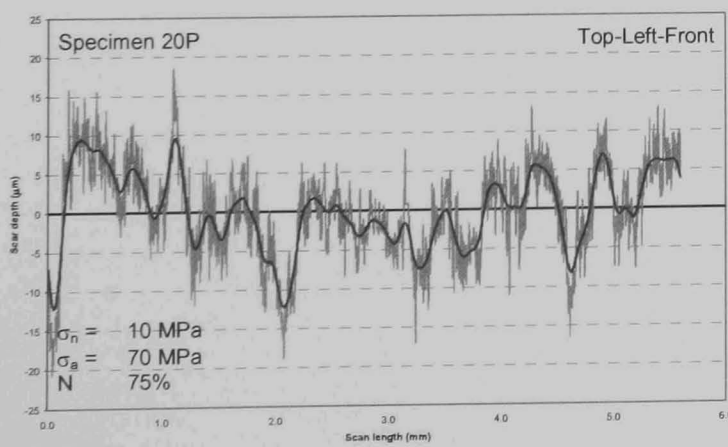
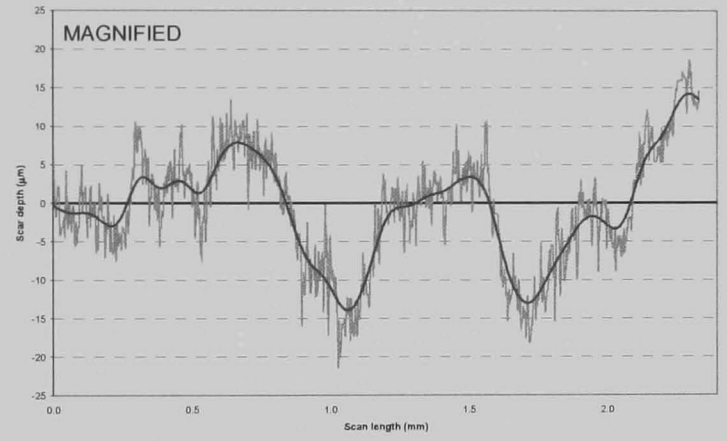
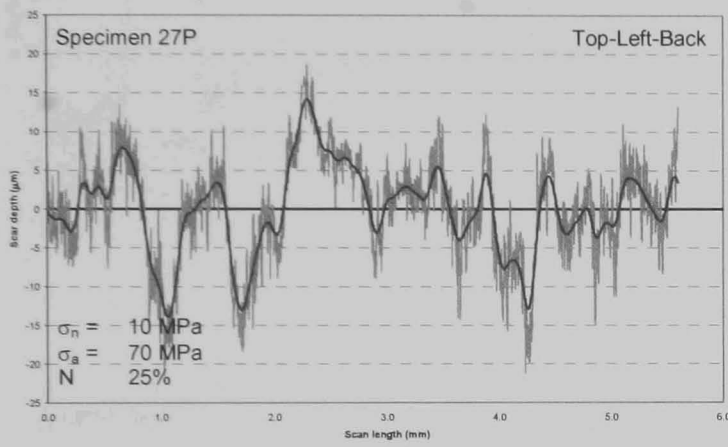
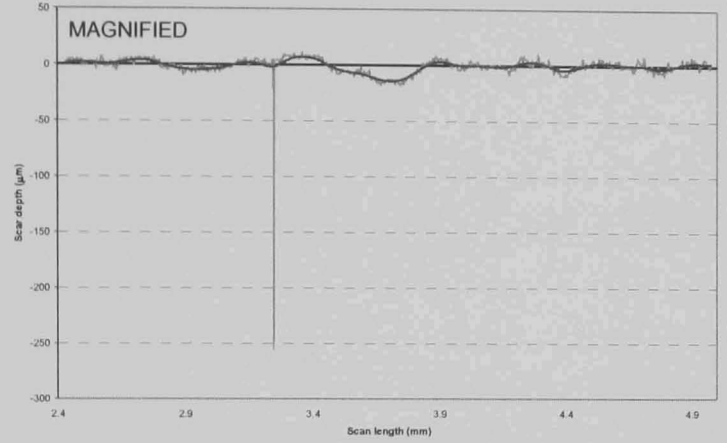
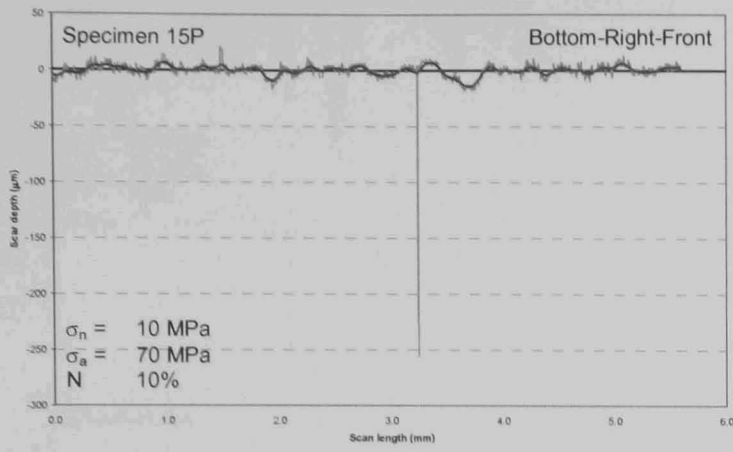
M.3 $\sigma_a = 125$ MPa unpeened

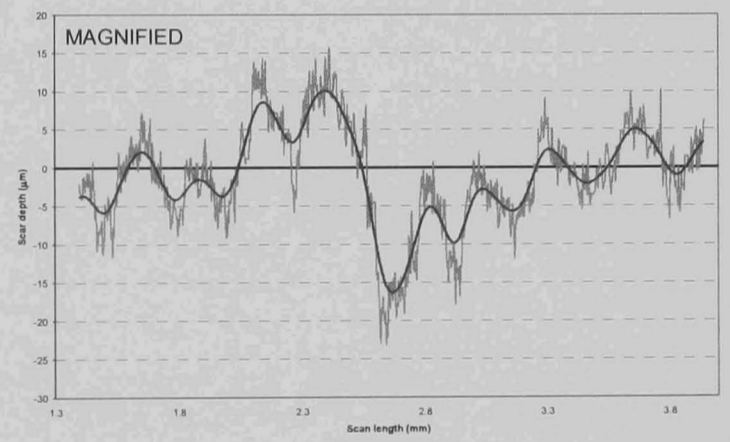
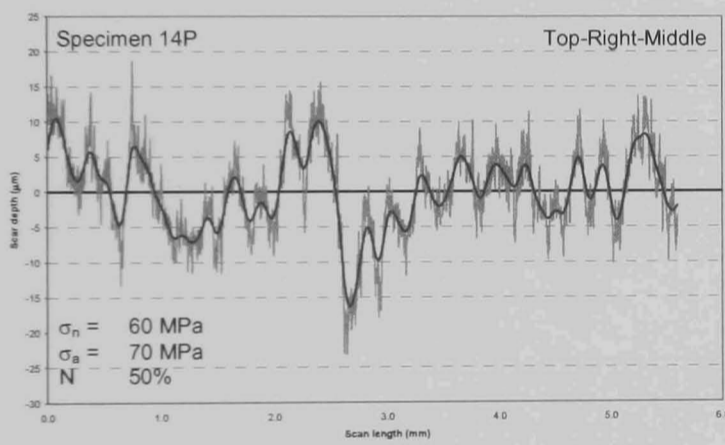
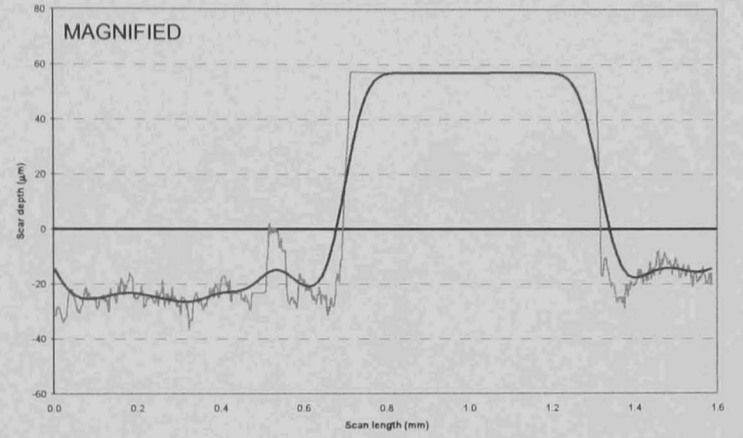
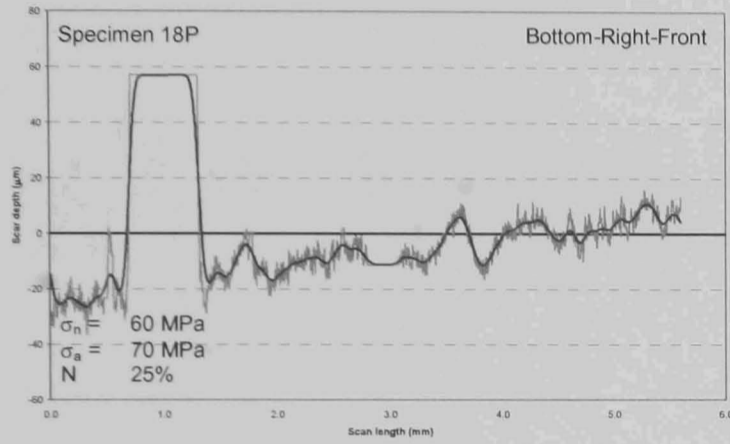
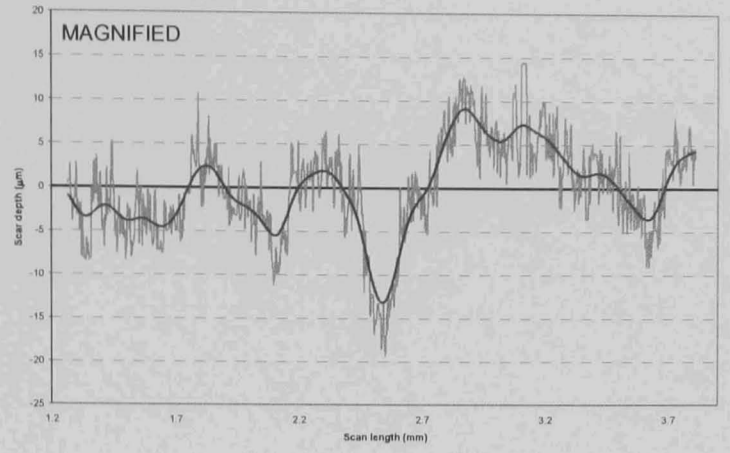
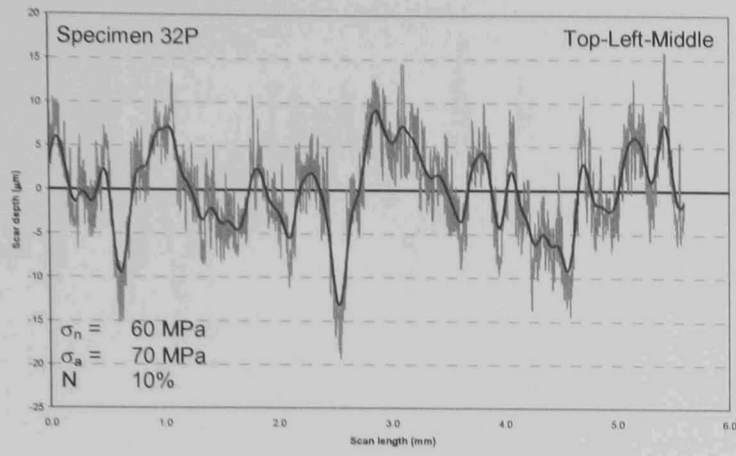


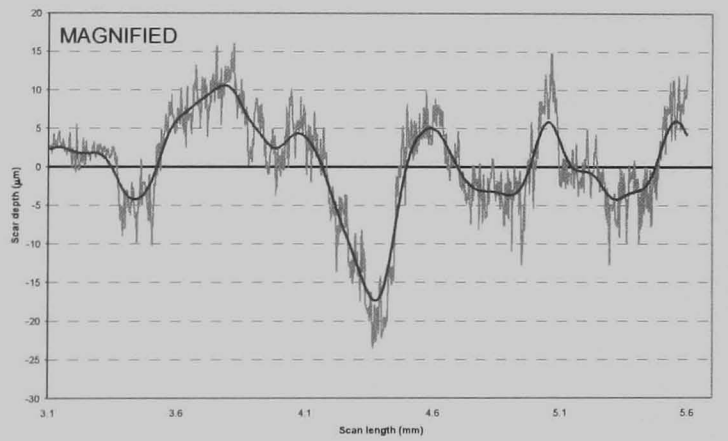
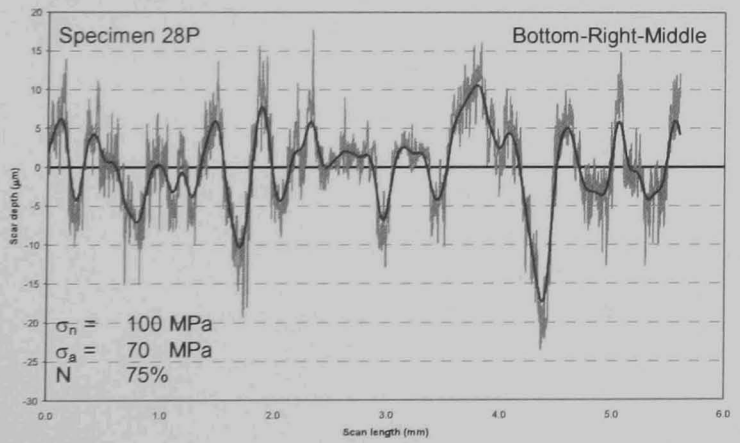
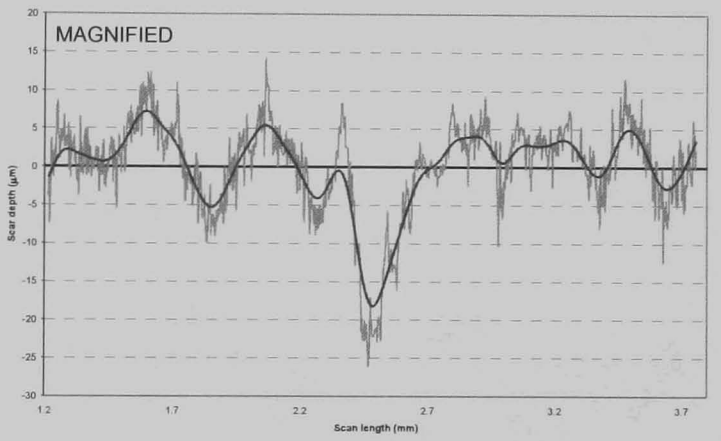
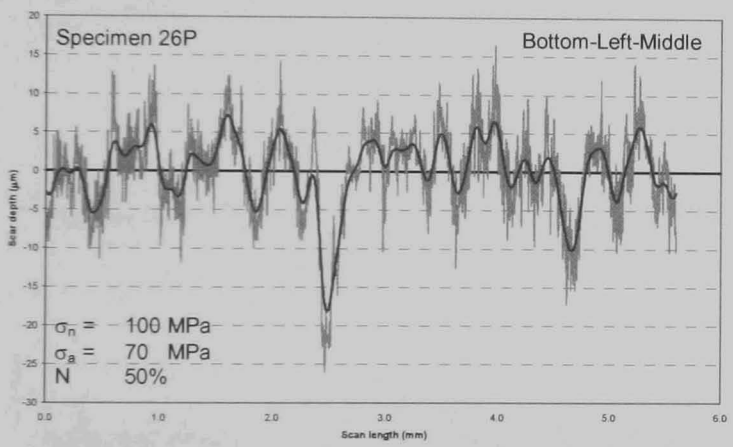
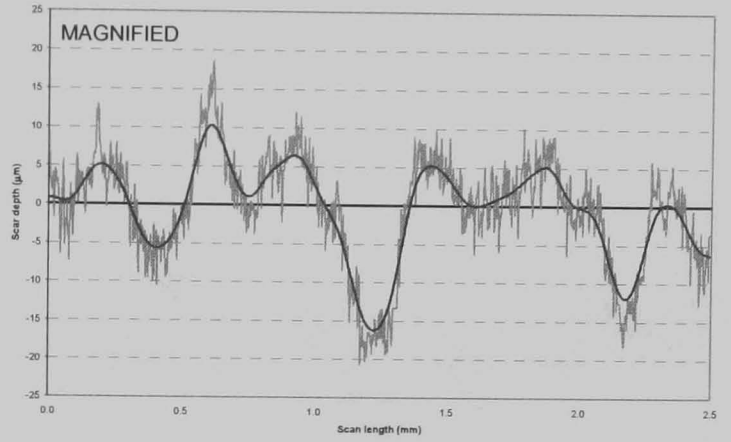
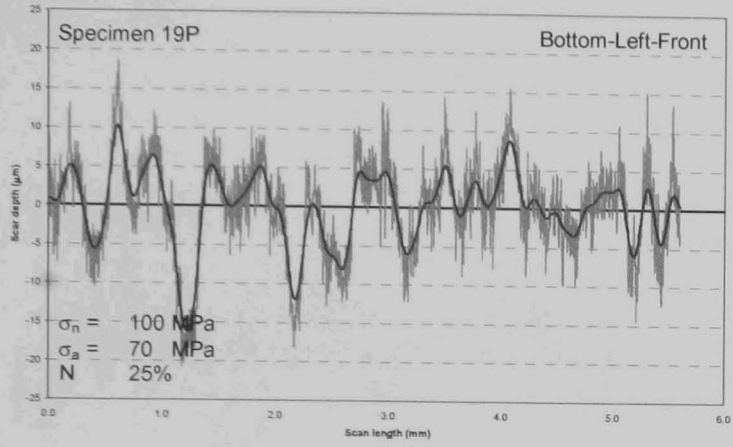
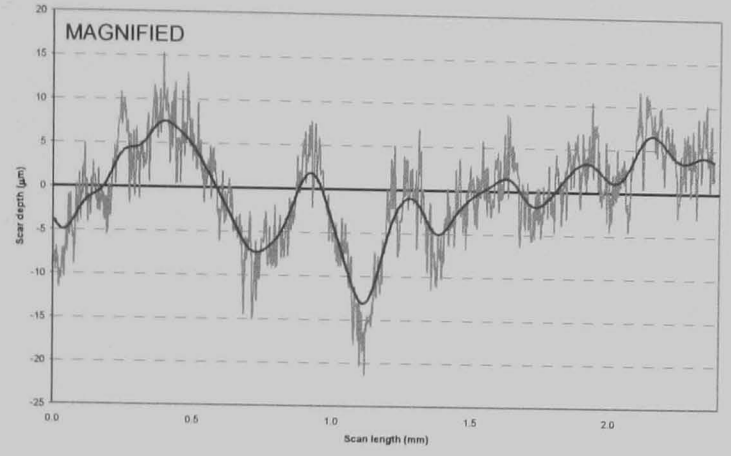
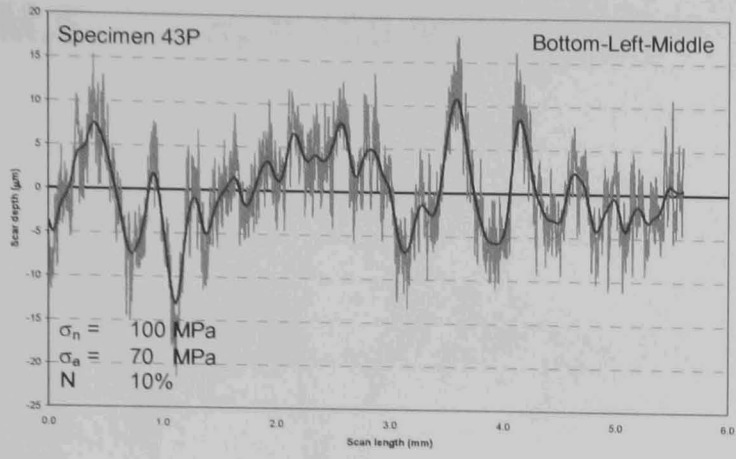




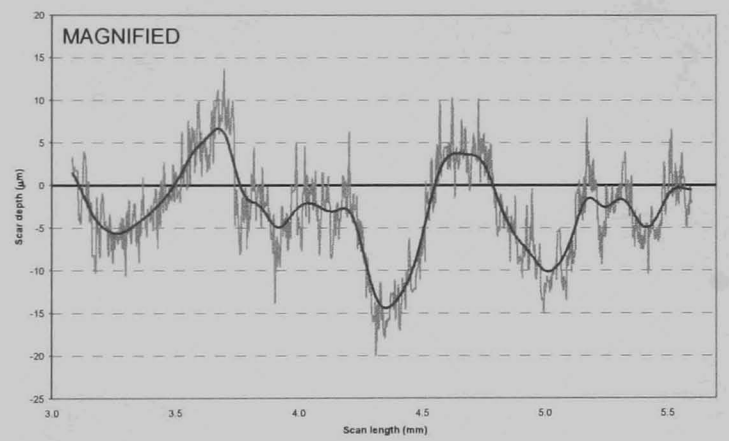
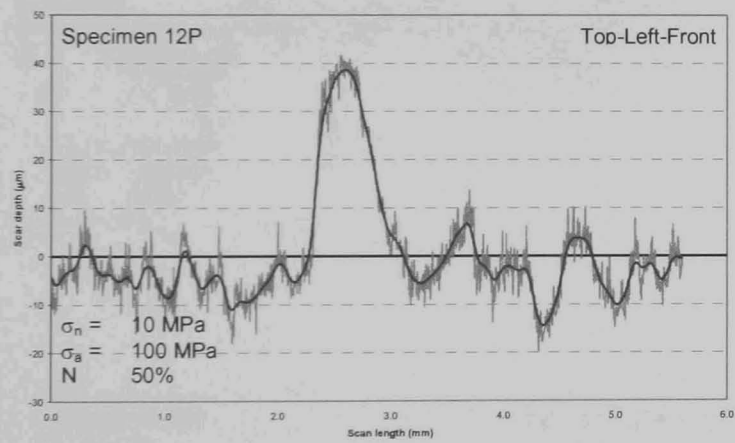
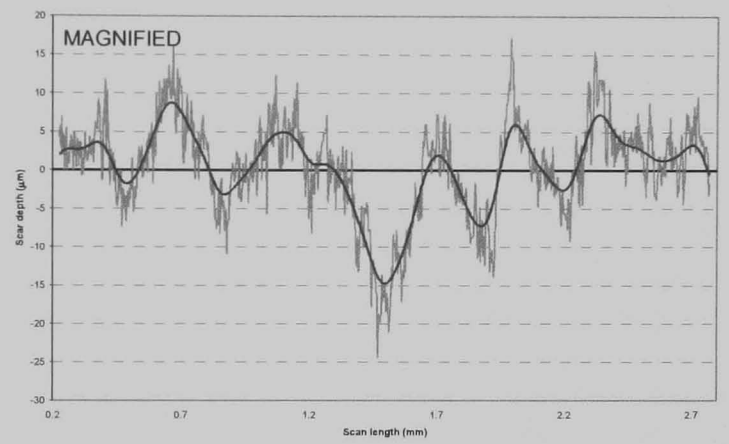
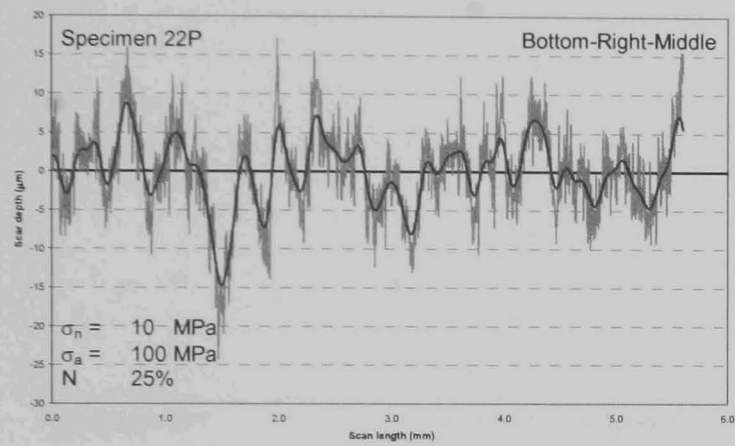
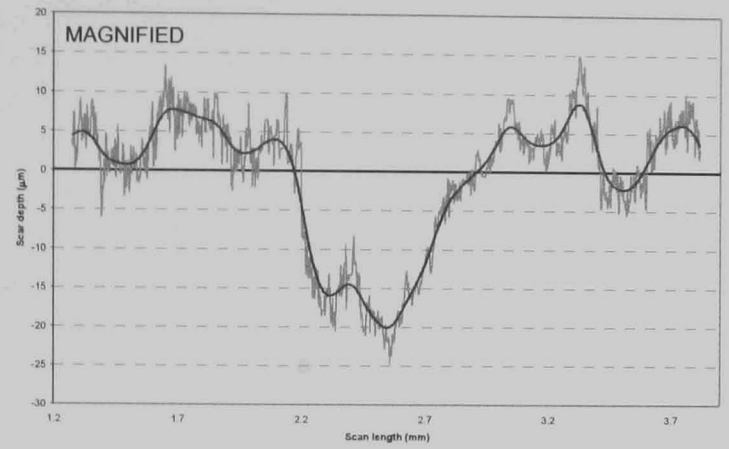
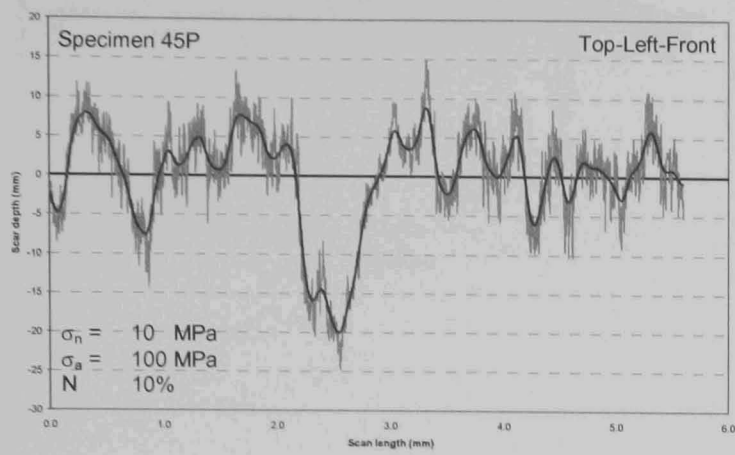
M.4 $\sigma_a = 70$ MPa peened

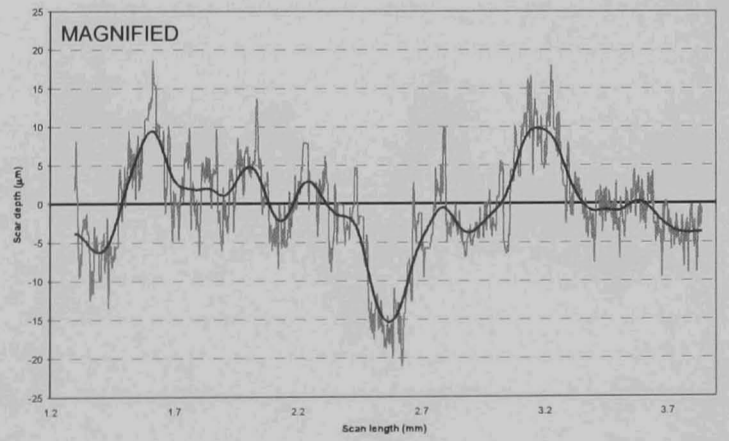
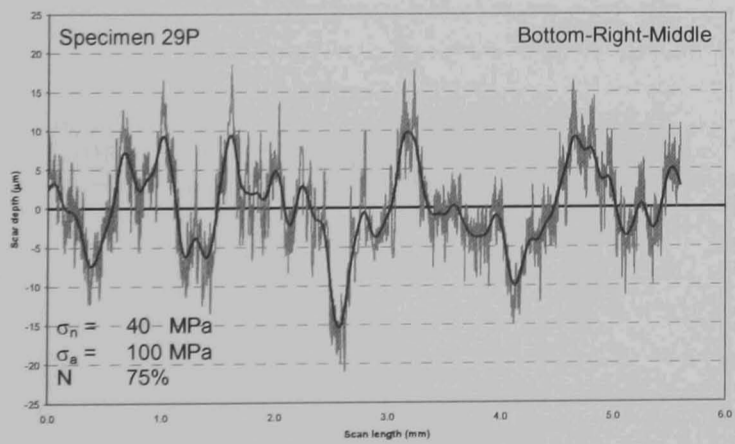
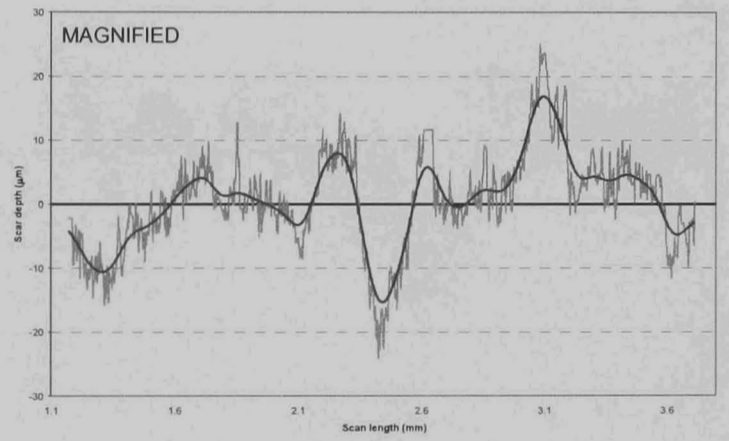
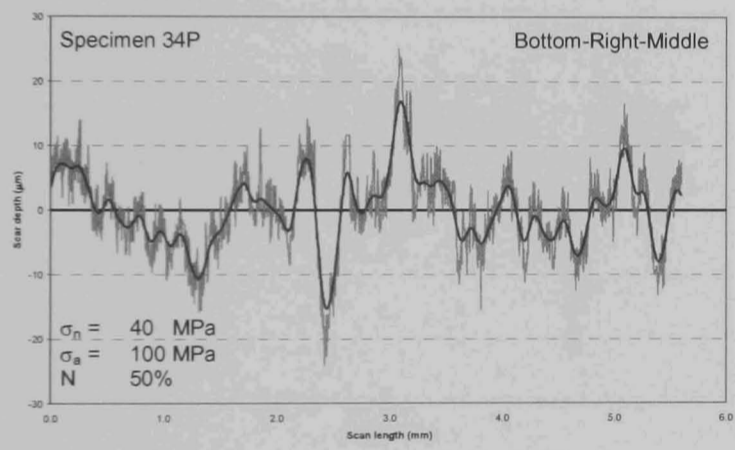
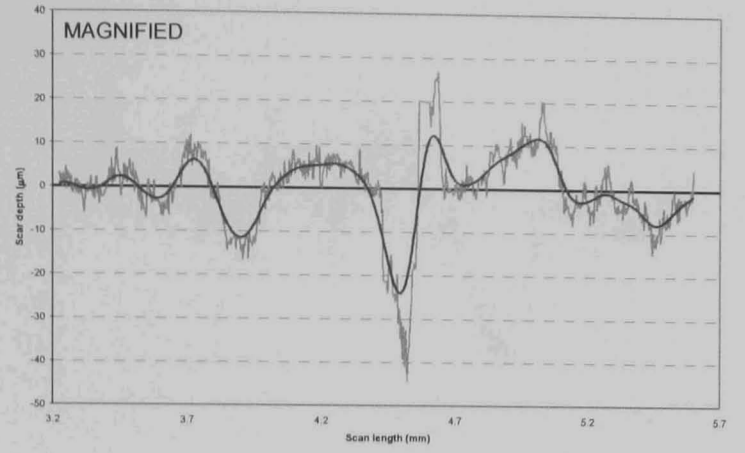
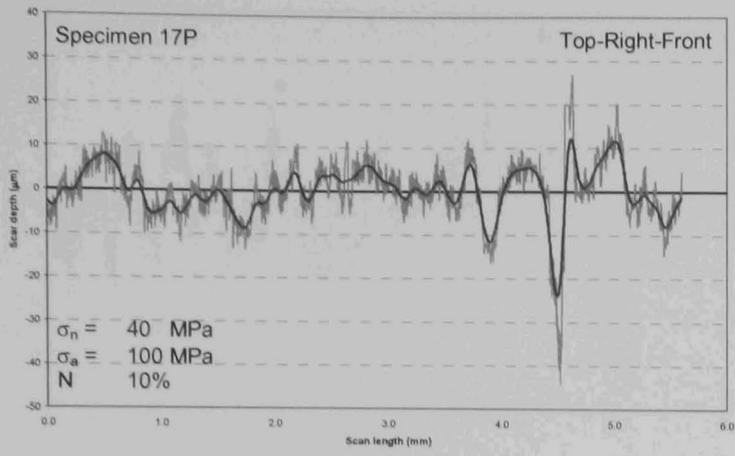


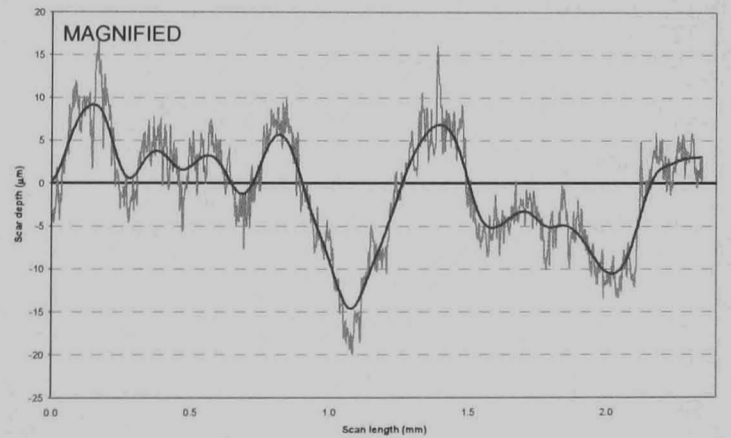
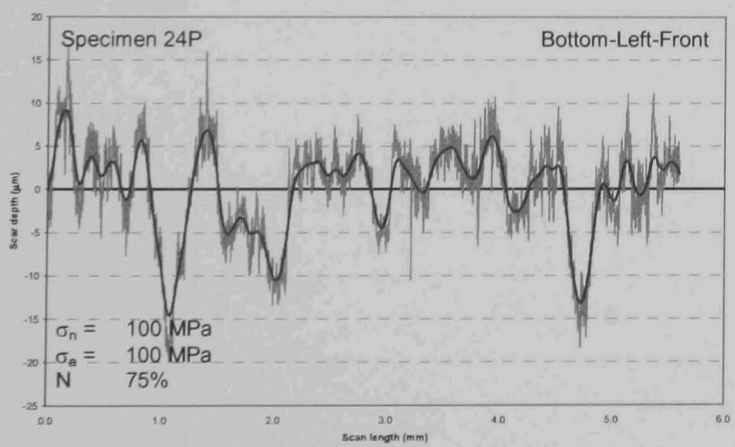
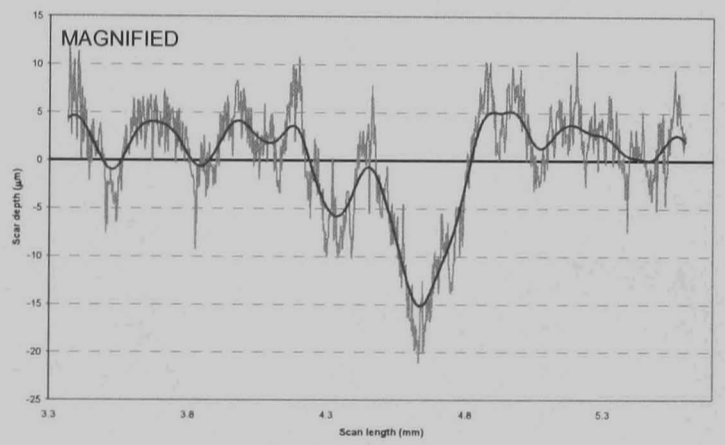
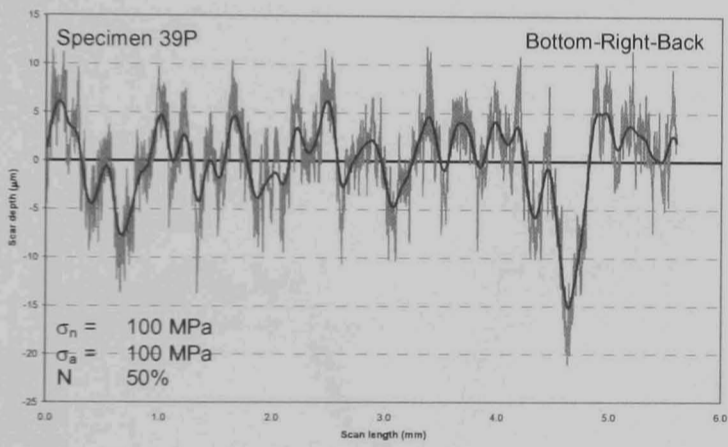
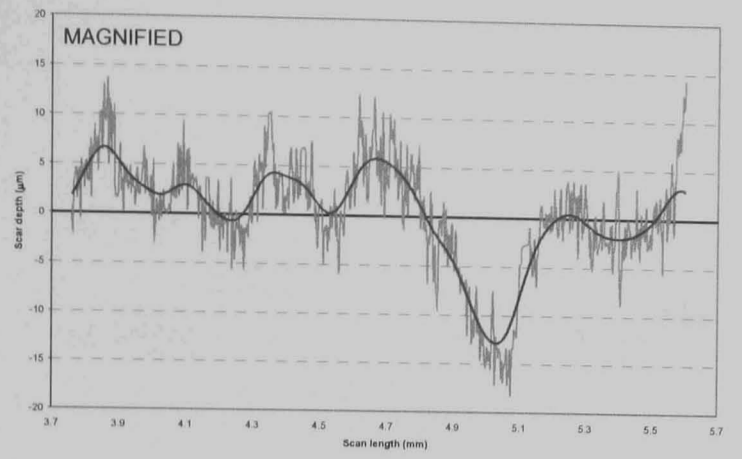
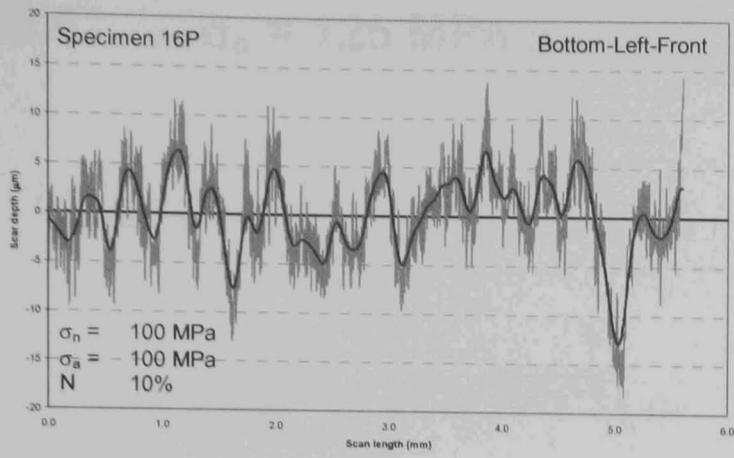




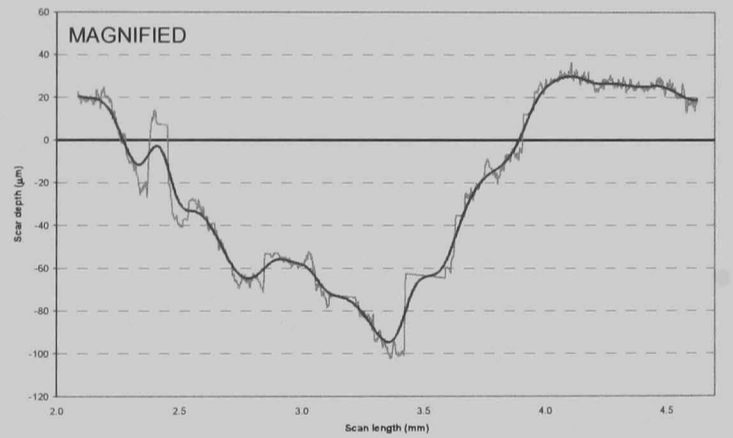
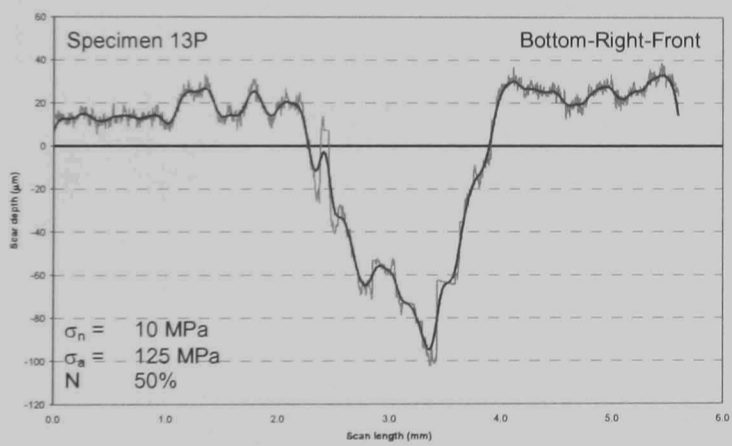
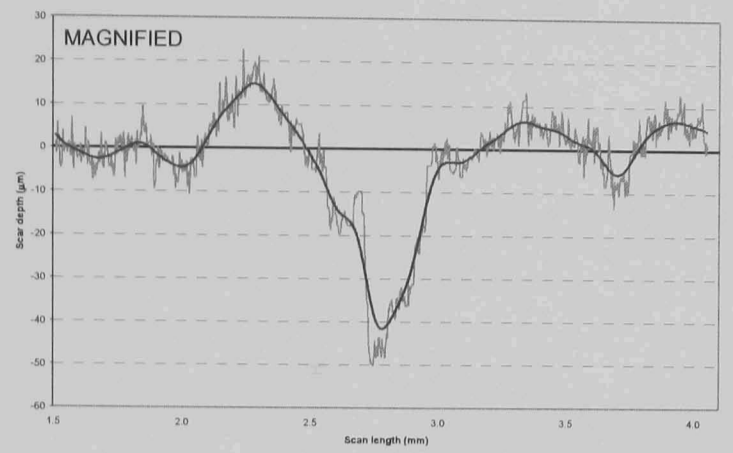
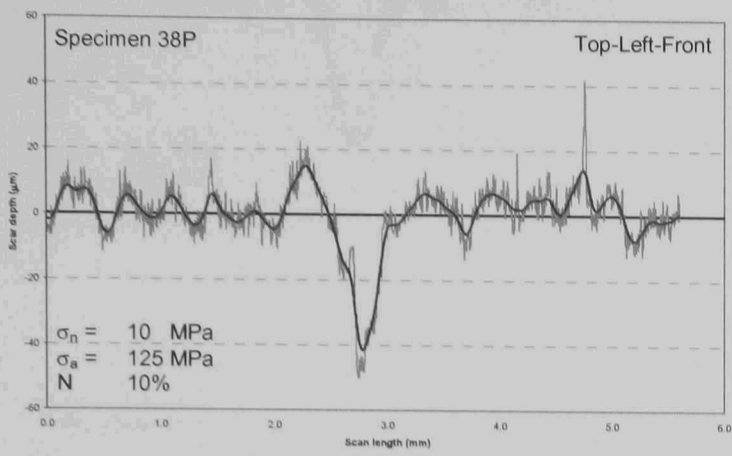
M.5 $\sigma_a = 100$ MPa peened

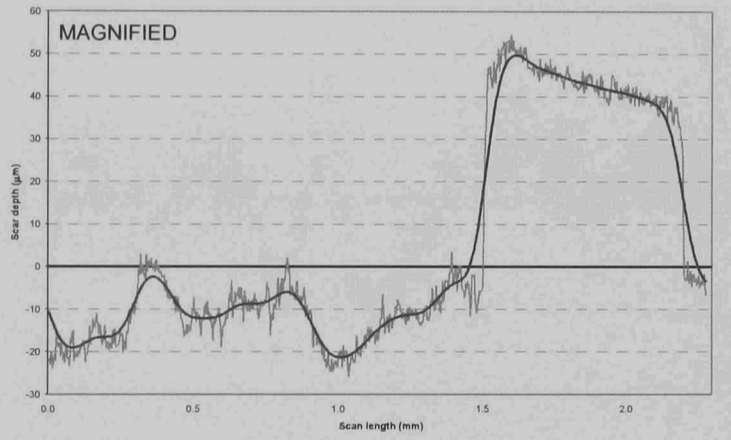
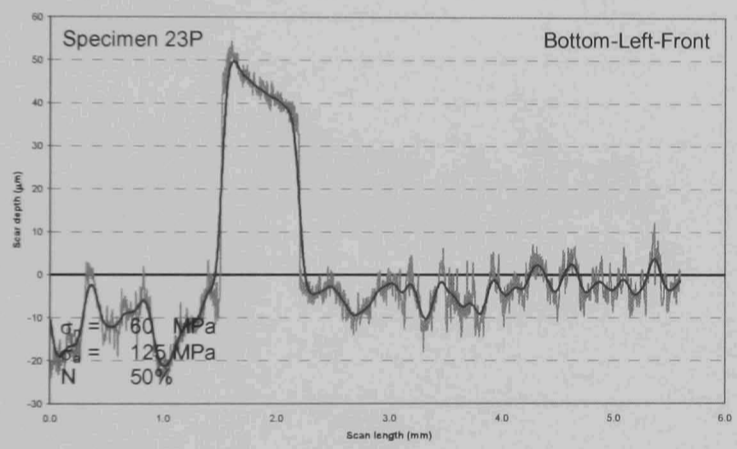
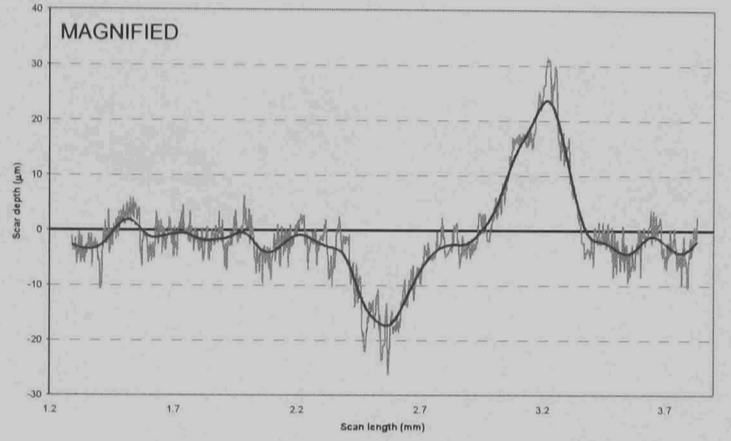
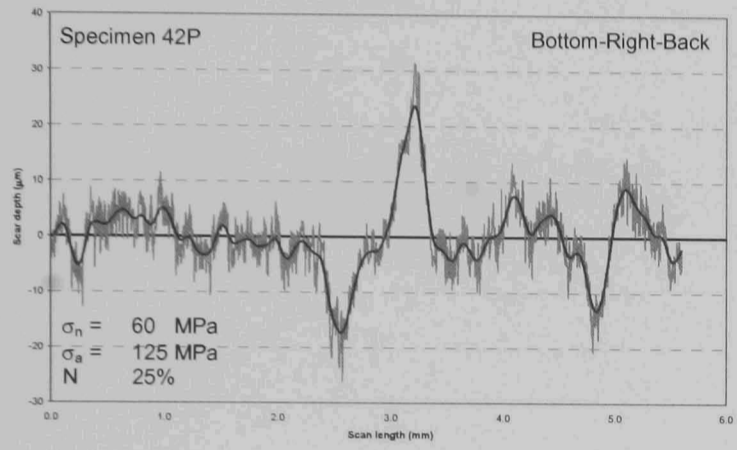
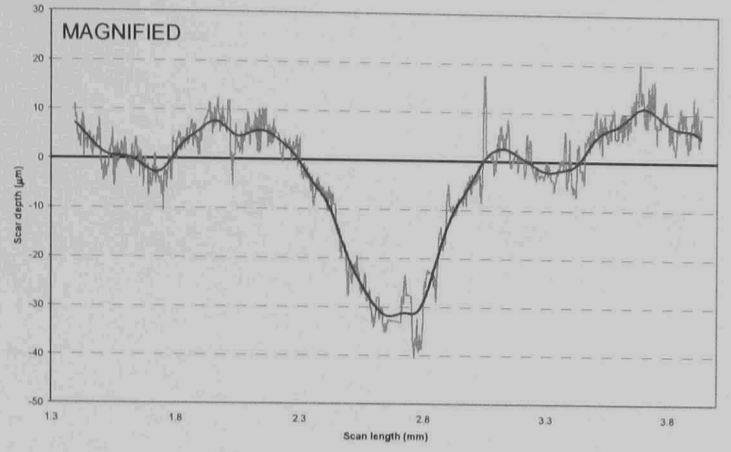
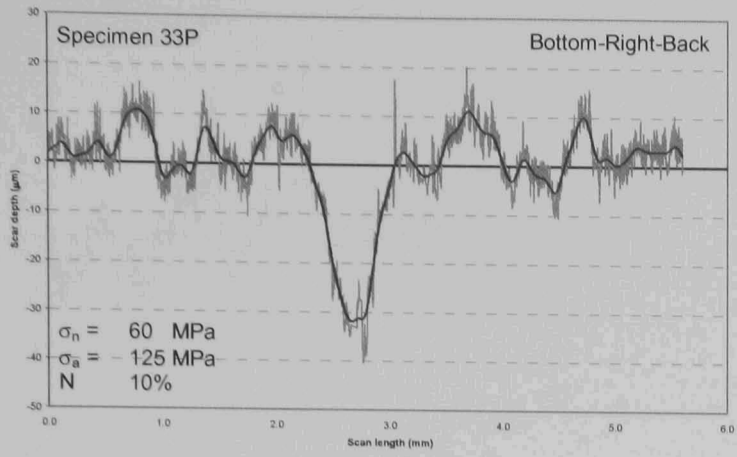


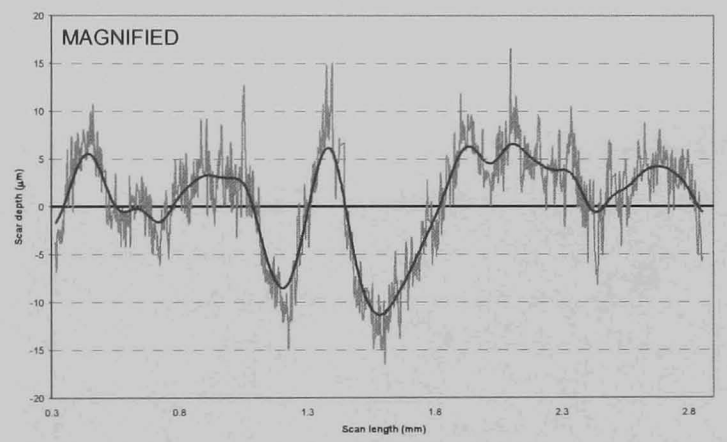
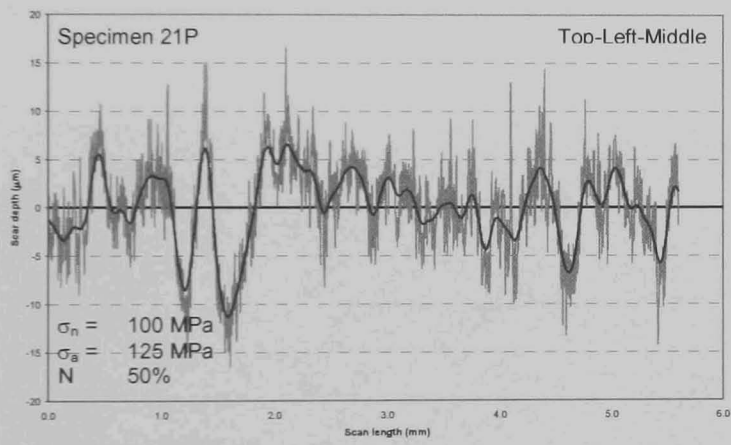
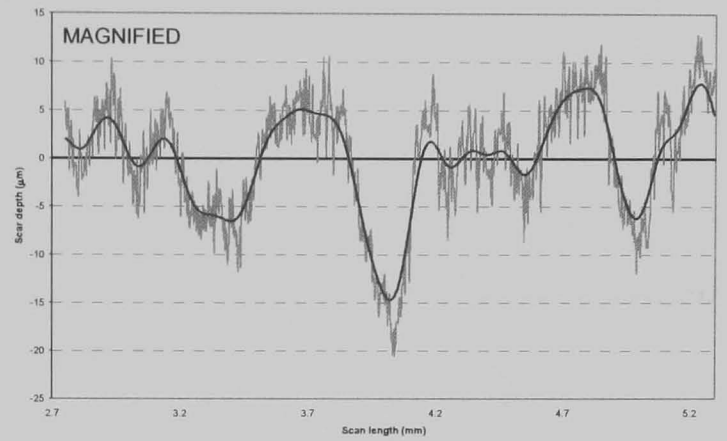
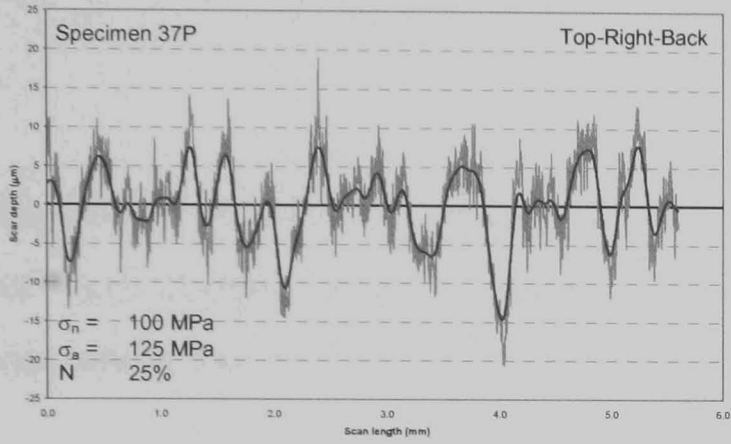
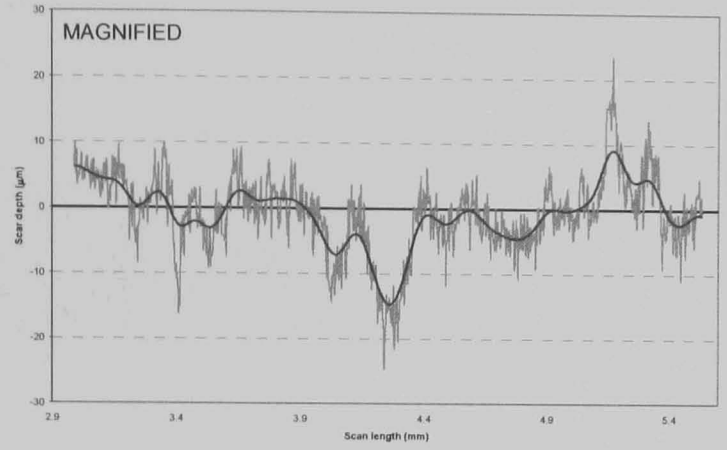
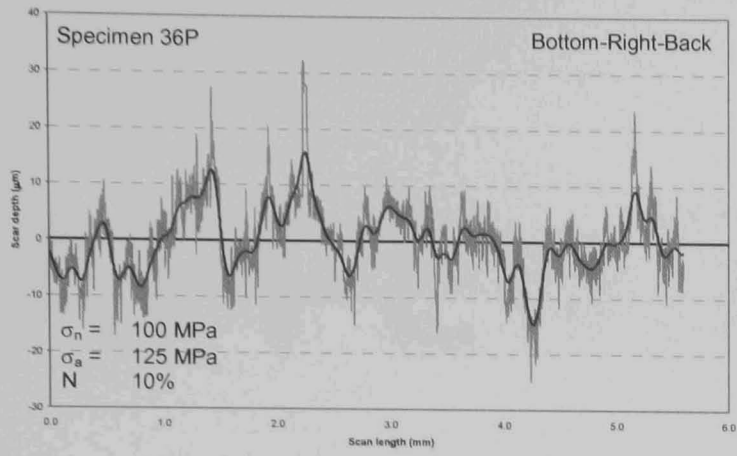




M.6 $\sigma_a = 125$ MPa peened





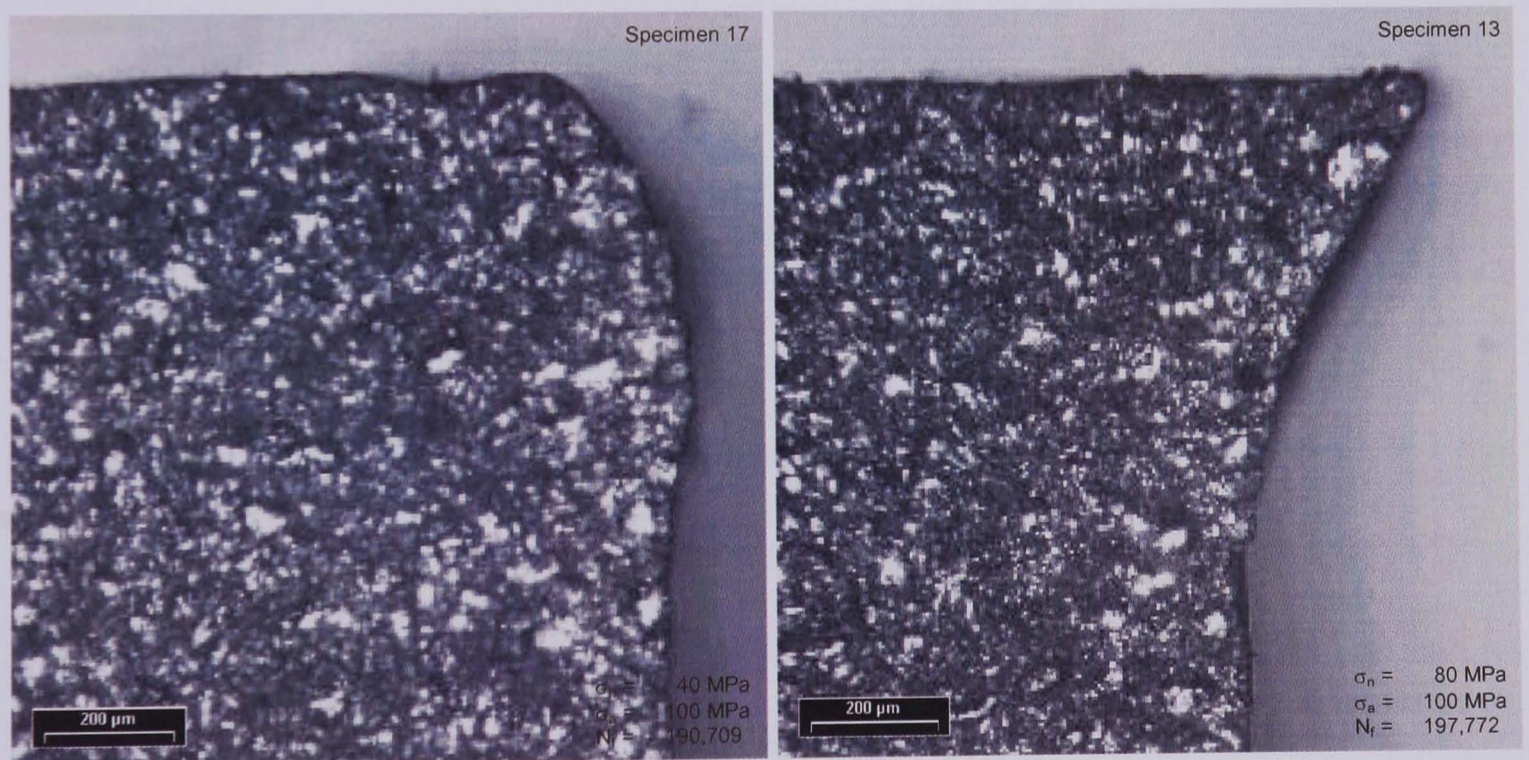


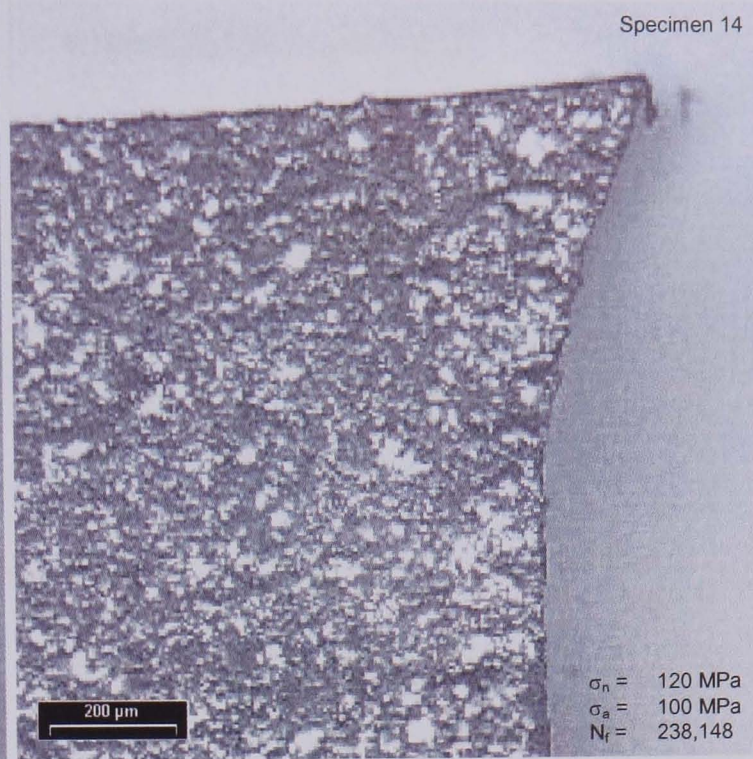
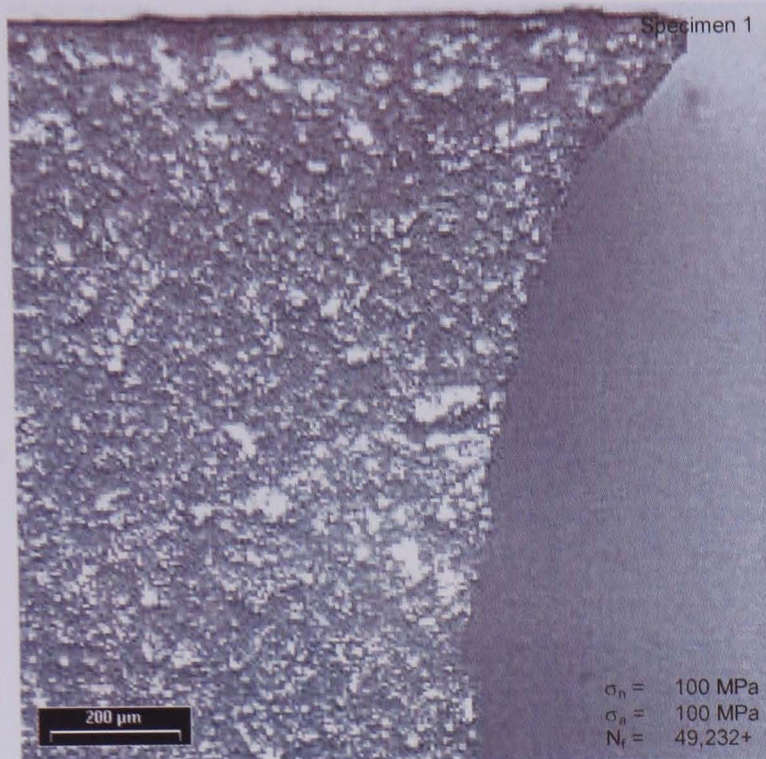
APPENDIX N

RESULTS: CRACK ANGLES

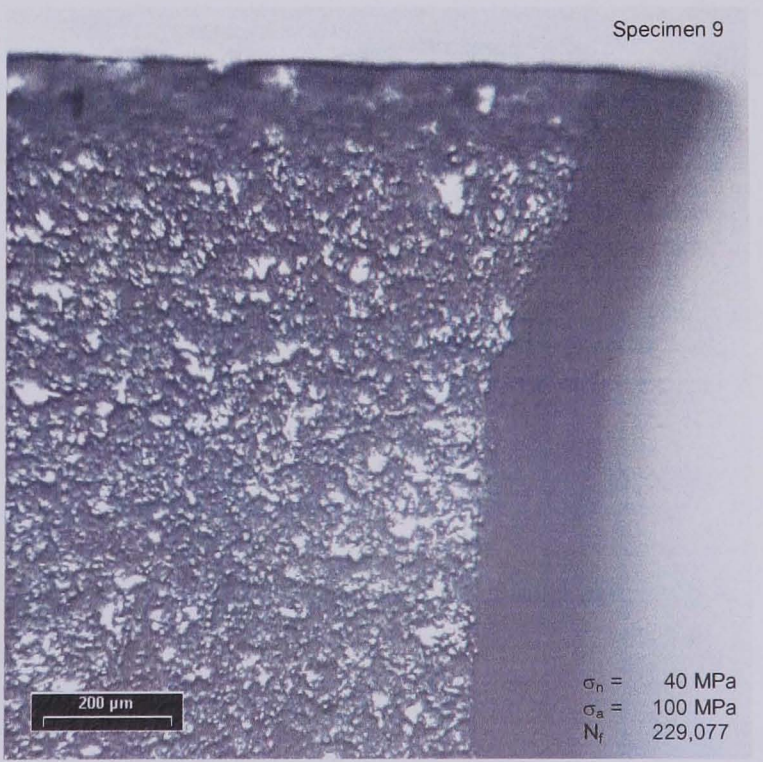
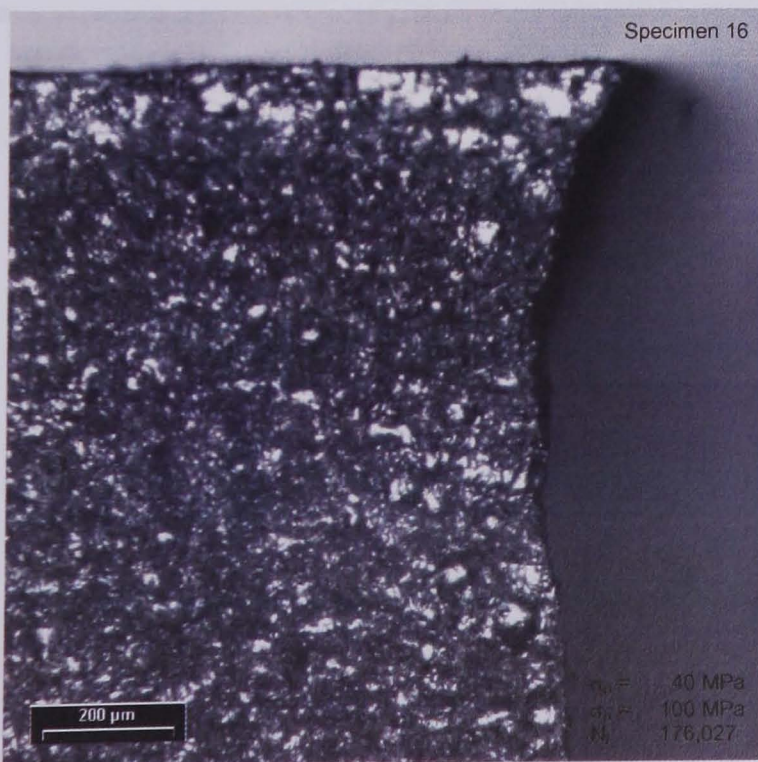
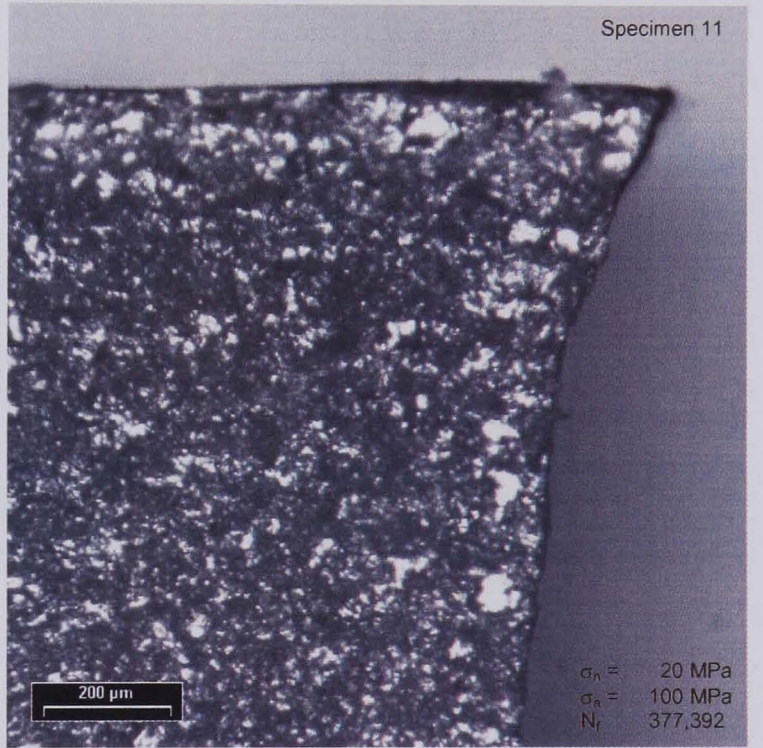
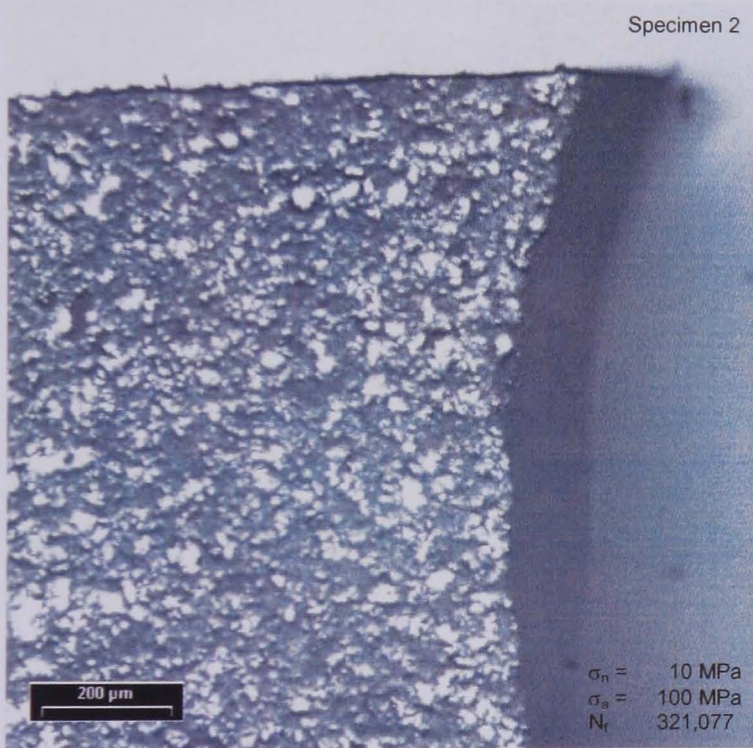
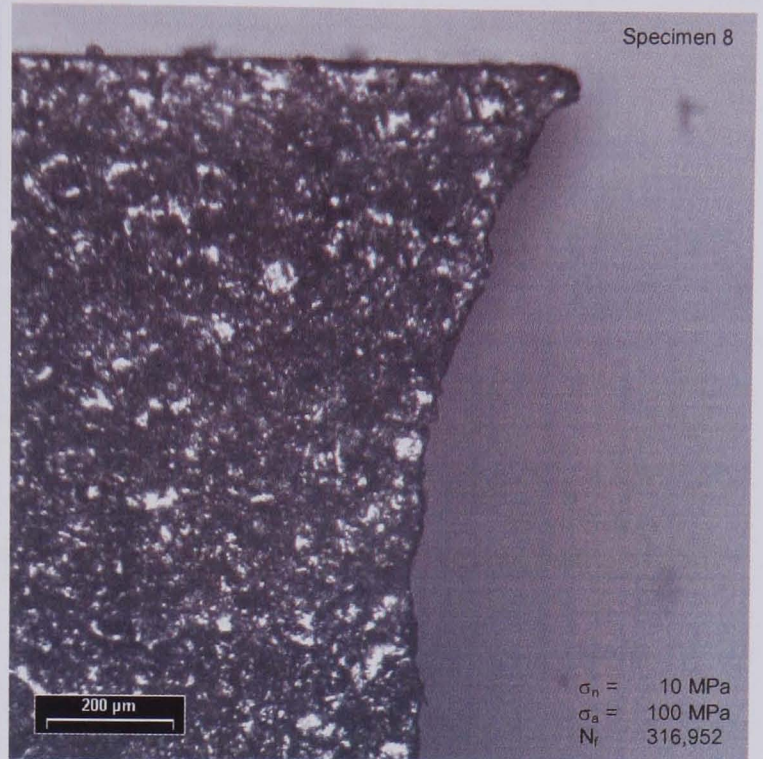
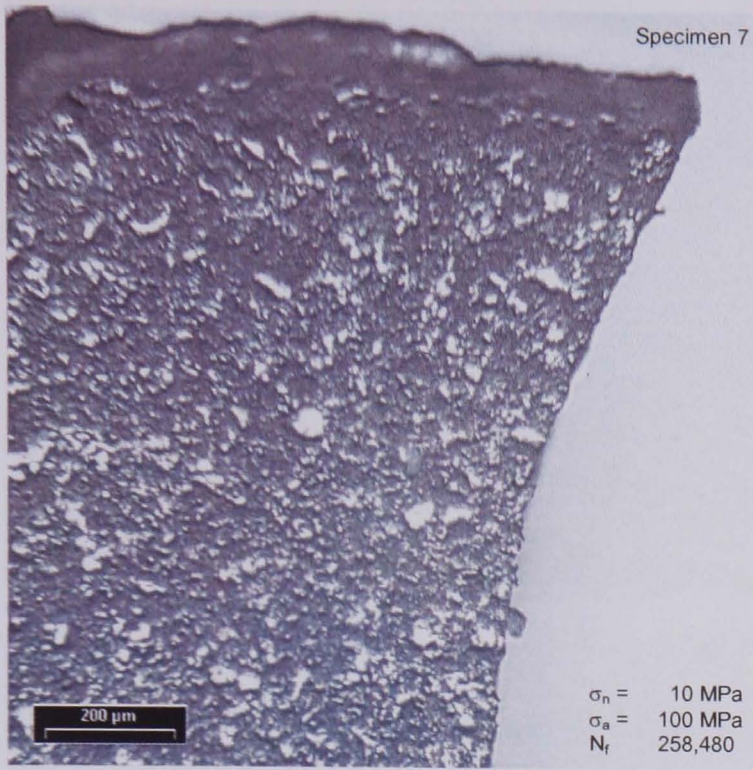
Sectioned, fractured fretting specimens, orientated with a fretting scar at the top of each image. Stage I, angled crack growth, and Stage II propagation nearly normal to the surface is demonstrated, see Section 4.4.2.

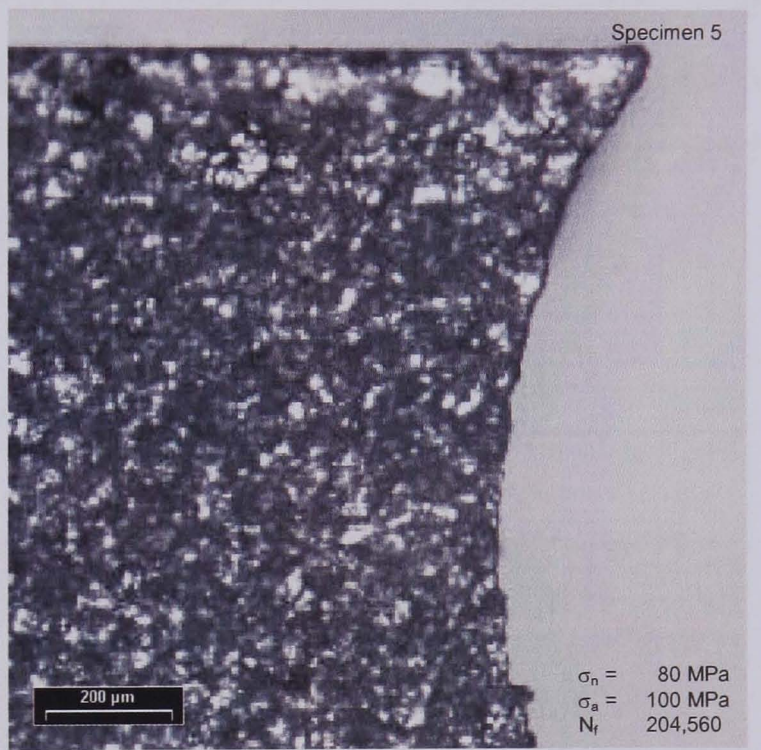
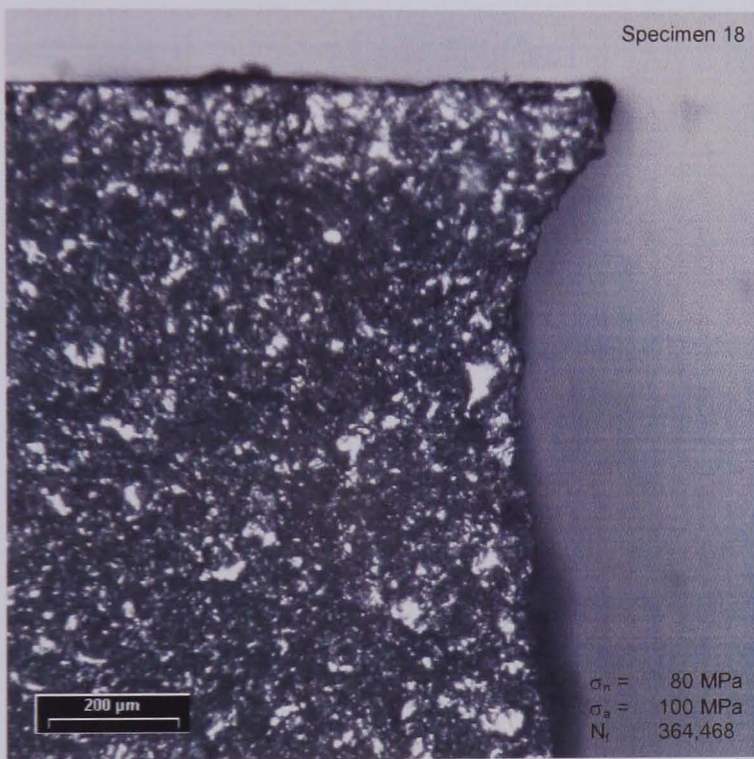
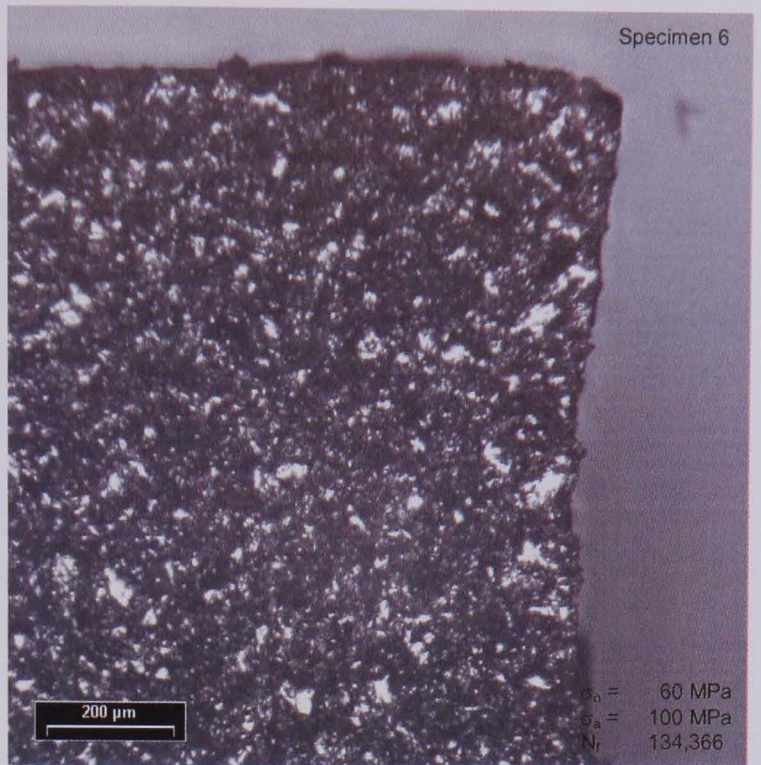
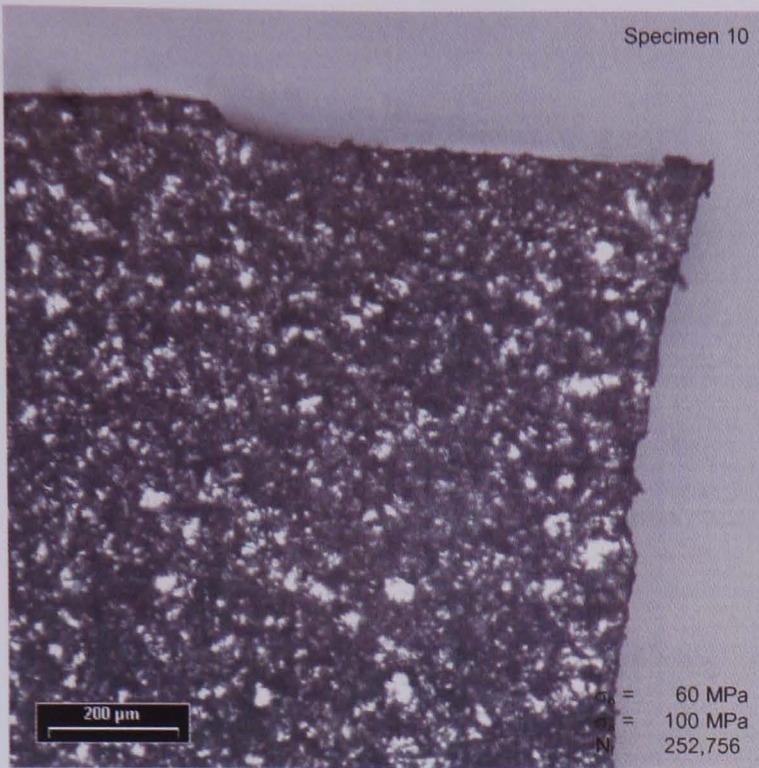
N.2 $\sigma_a = 100$ MPa unpeened – steel bridge





N.2 $\sigma_a = 100$ MPa unpeened – aluminium bridge



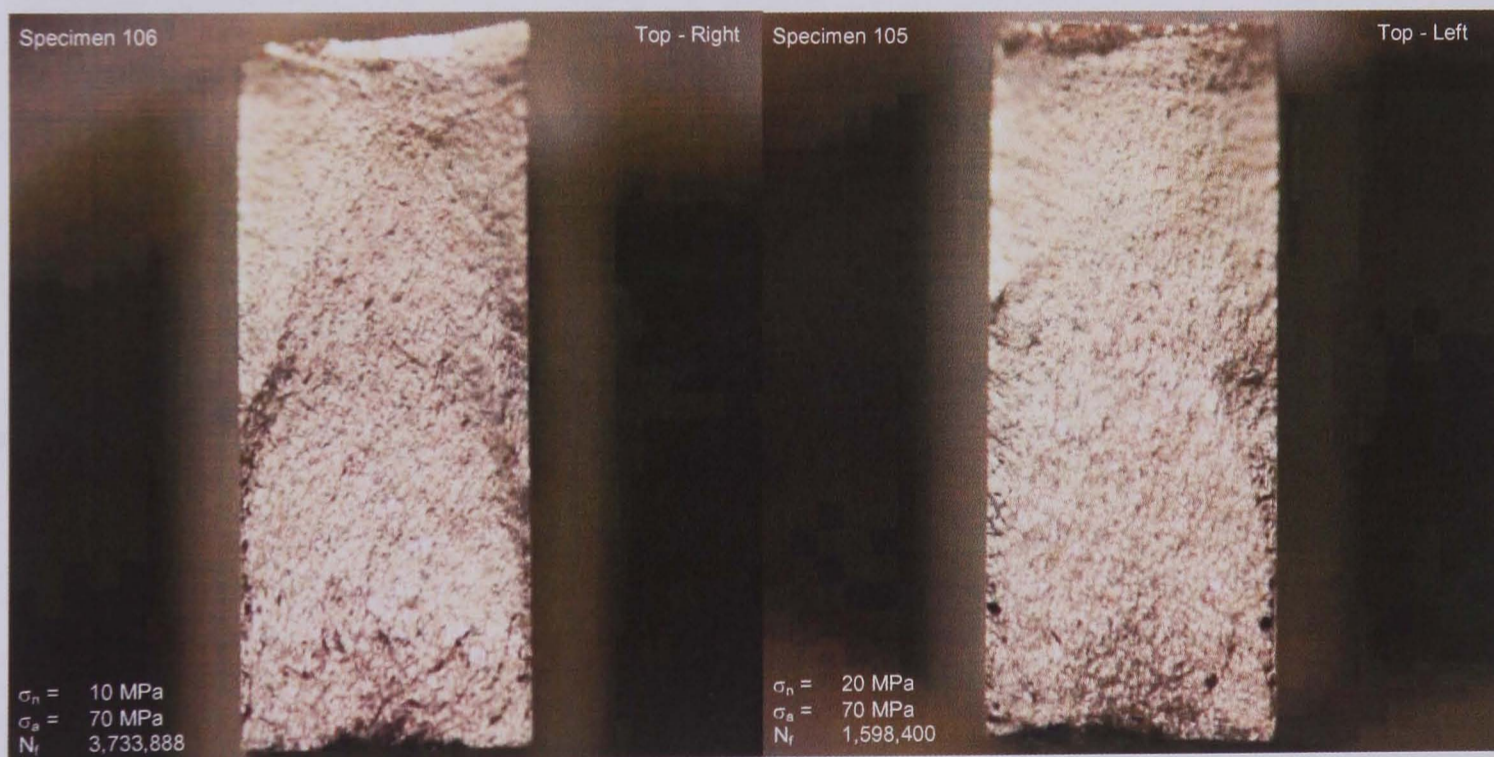


APPENDIX O

RESULTS: FRACTURE SURFACES

This appendix contains digital photographs of the fractured specimens. The label in the top right hand corner denotes the orientation of the fracture surface and the location of the main failure site, be it having initiated from the right hand or left hand scar. These specimens are of a cross section 8 x 20 mm.

O.1 $\sigma_a = 70$ MPa unpeened



Specimen 56



Top - Right

Specimen 59



Top - Right

$\sigma_n = 40 \text{ MPa}$
 $\sigma_a = 70 \text{ MPa}$
 $N_f = 1,224,704$

$\sigma_n = 60 \text{ MPa}$
 $\sigma_a = 70 \text{ MPa}$
 $N_f = 886,320$

Specimen 109



Top - Right

Specimen 54



Top - Right

$\sigma_n = 80 \text{ MPa}$
 $\sigma_a = 70 \text{ MPa}$
 $N_f = 1,033,504$

$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 70 \text{ MPa}$
 $N_f = 3,273,088$

Specimen 104



Top - Left

Specimen 107

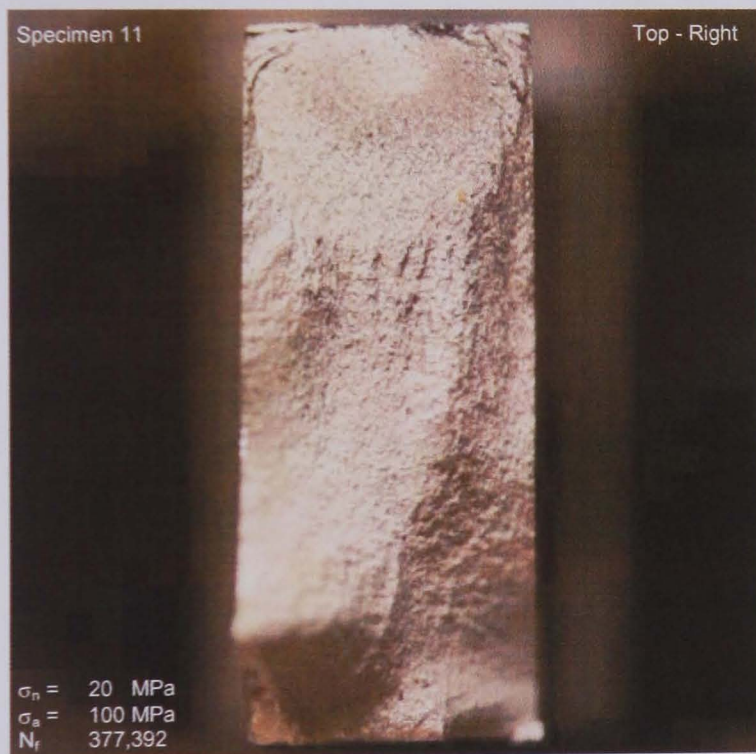
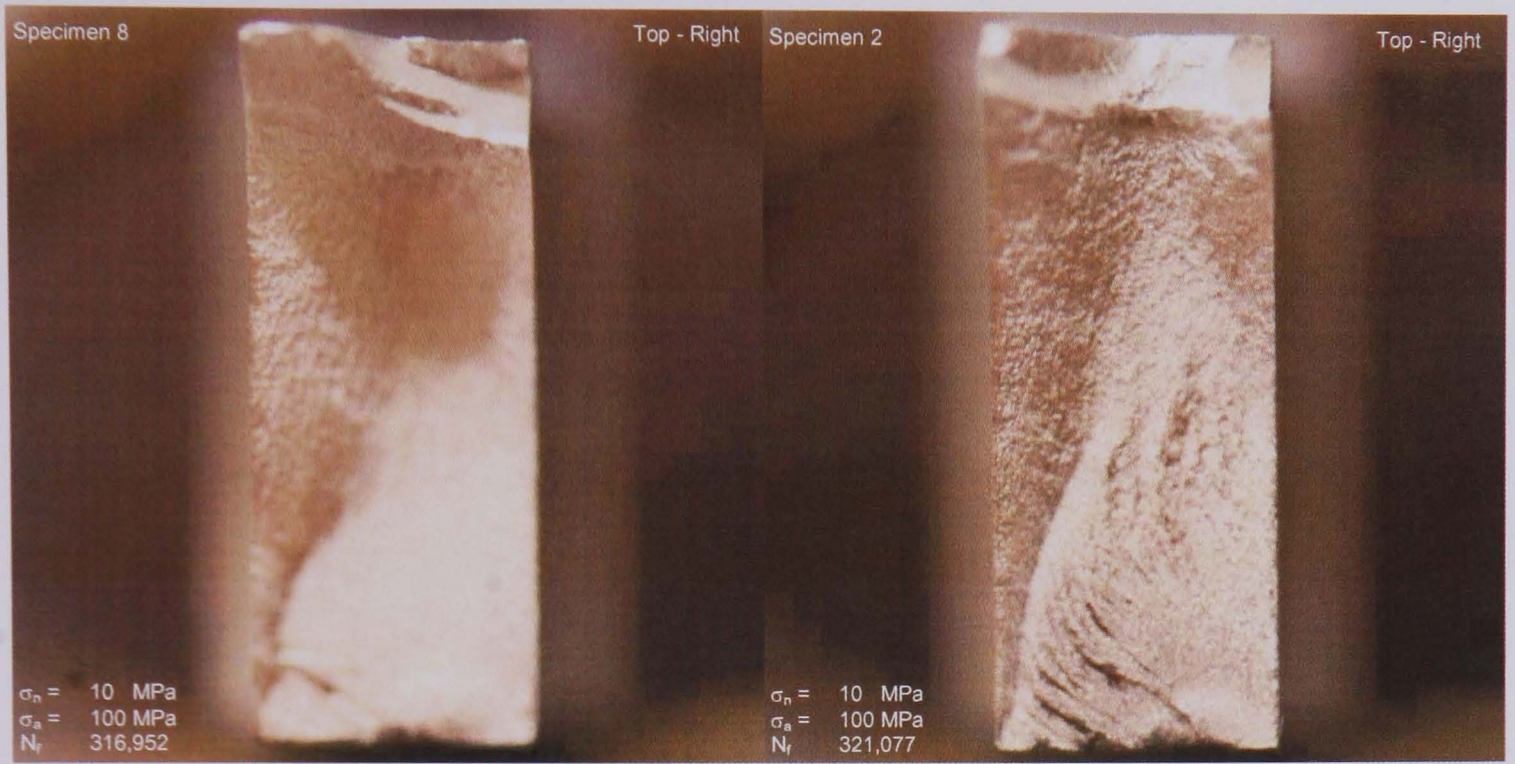


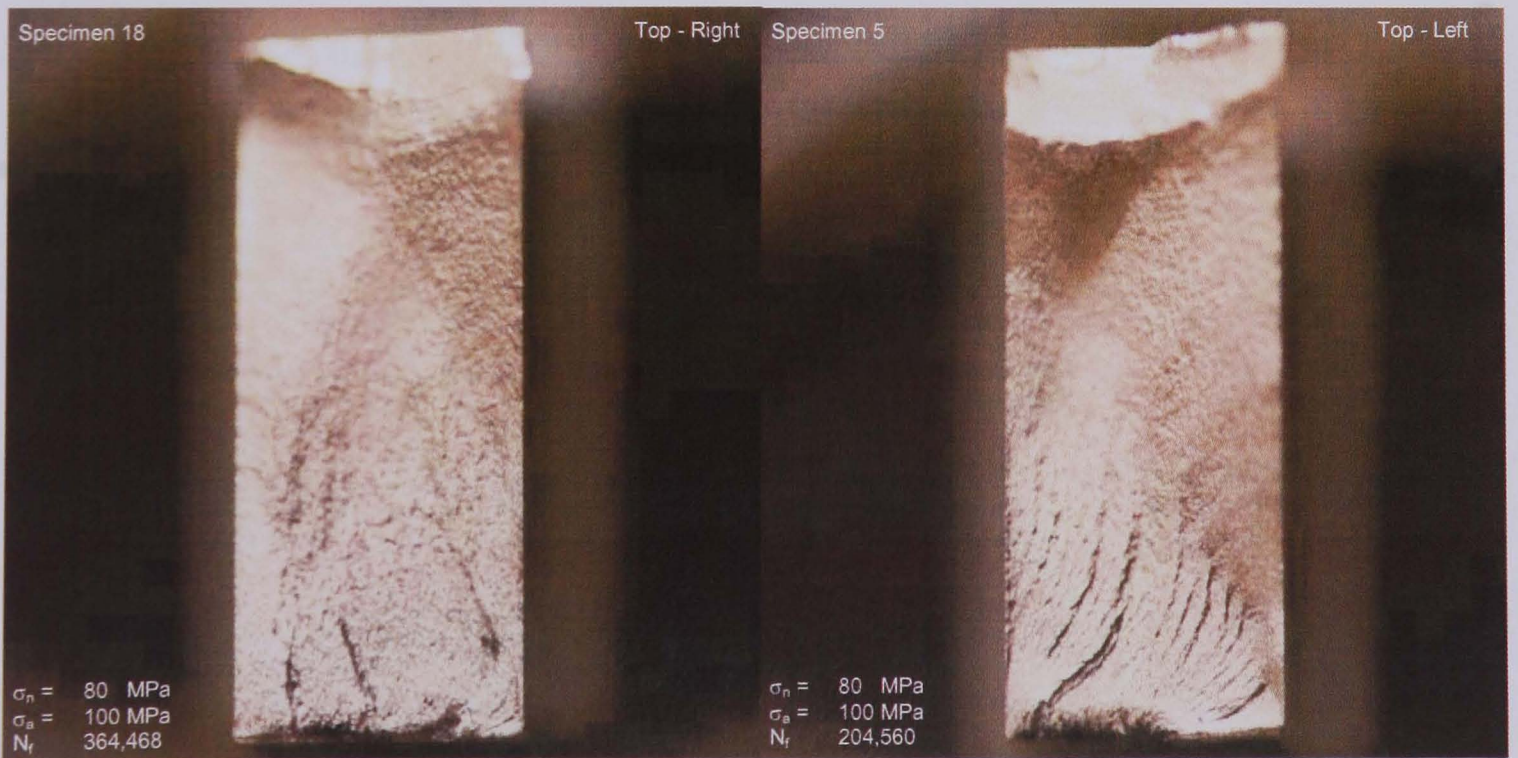
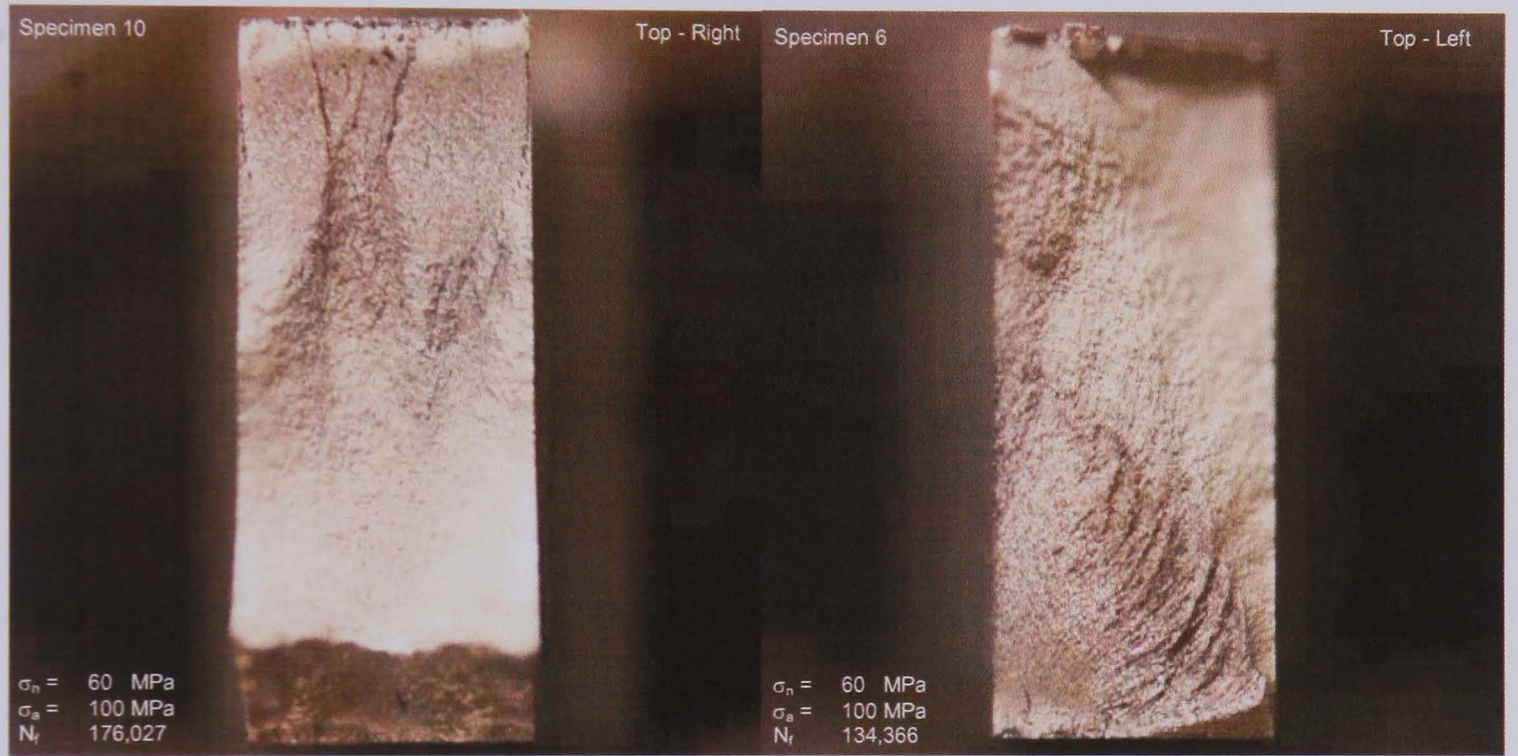
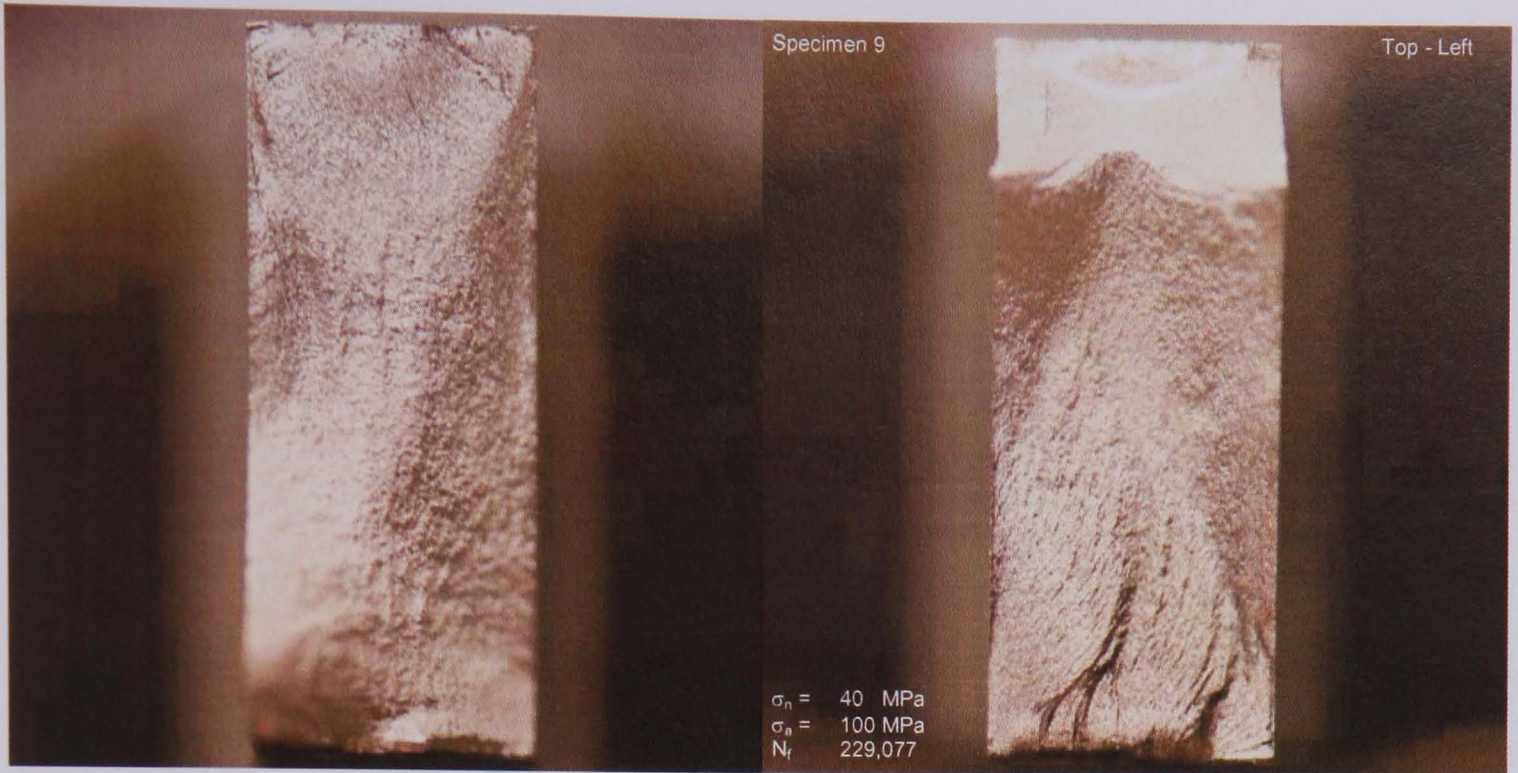
Top - Right

$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 70 \text{ MPa}$
 $N_f = 1,741,888$

$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 70 \text{ MPa}$
 $N_f = 1,253,056$

O.2 $\sigma_a = 100$ MPa unpeened





Specimen 19



$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 100 \text{ MPa}$
 $N_f = 553,971$

Top - Right

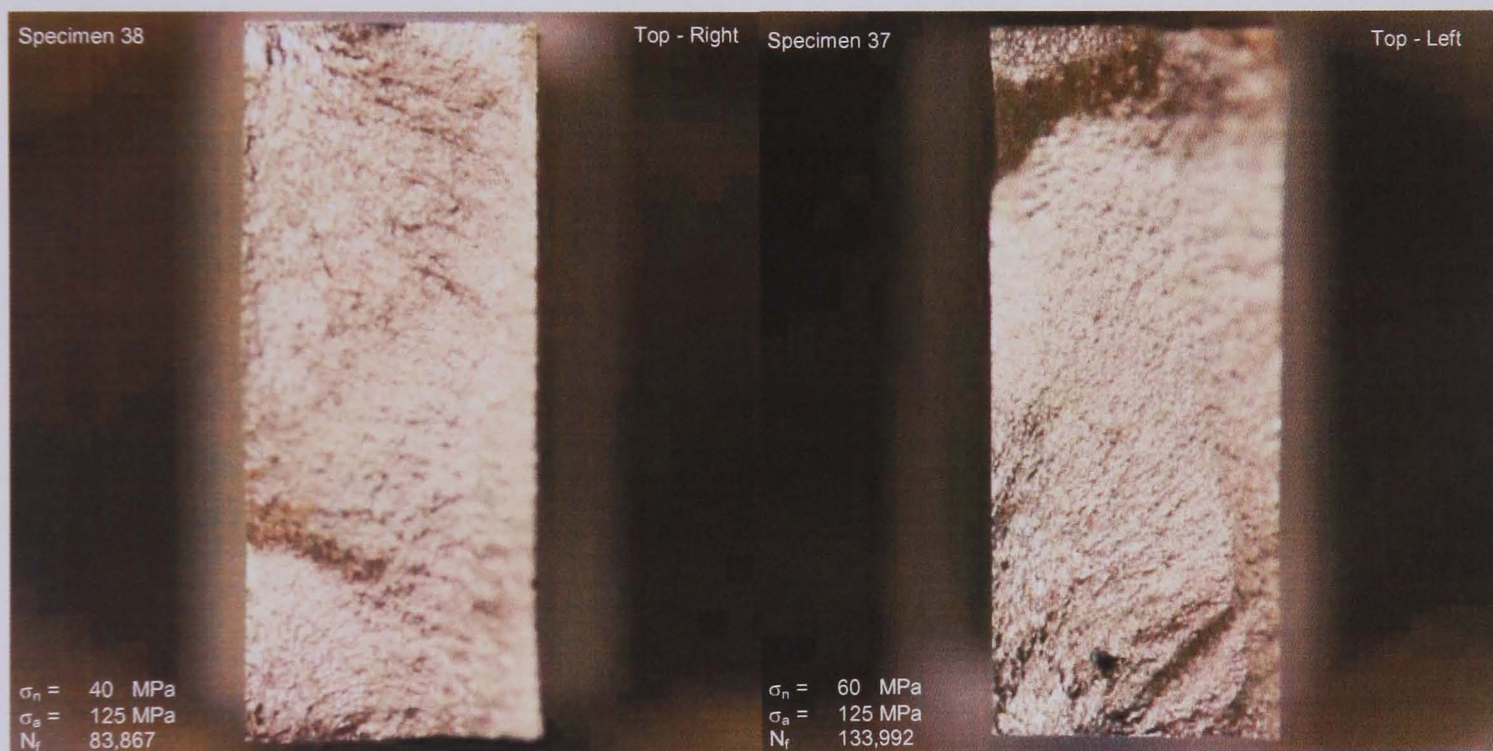
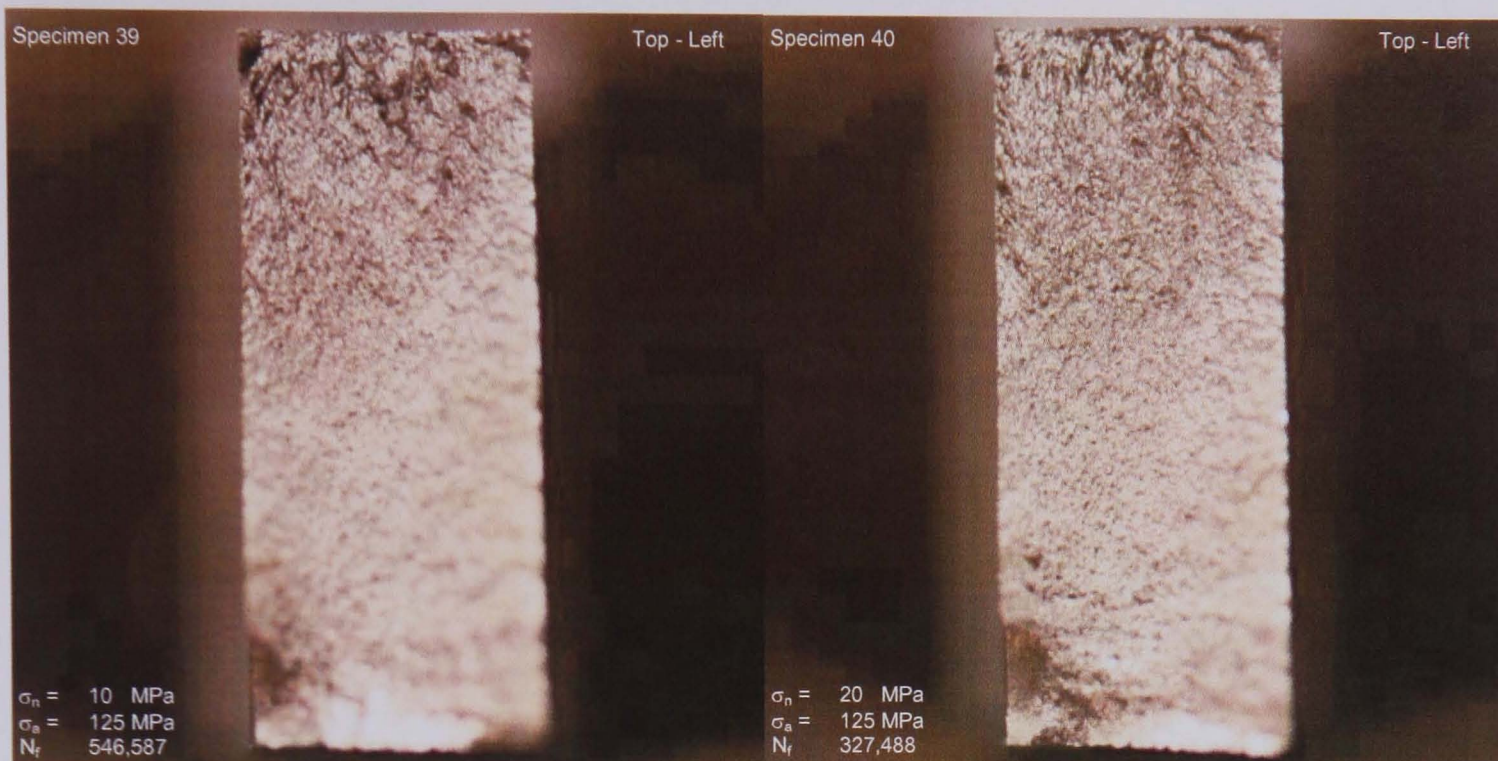
Specimen 20



$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 100 \text{ MPa}$
 $N_f = 404,431$

Top - Right

O.3 $\sigma_a = 125$ MPa unpeened



Specimen 100



Top - Right

Specimen 102



Top - Right

$\sigma_n = 80 \text{ MPa}$
 $\sigma_a = 125 \text{ MPa}$
 $N_f = 176,427$

$\sigma_n = 80 \text{ MPa}$
 $\sigma_a = 125 \text{ MPa}$
 $N_f = 91,600$

Specimen 101



Top - Right

Specimen 108



Top - Left

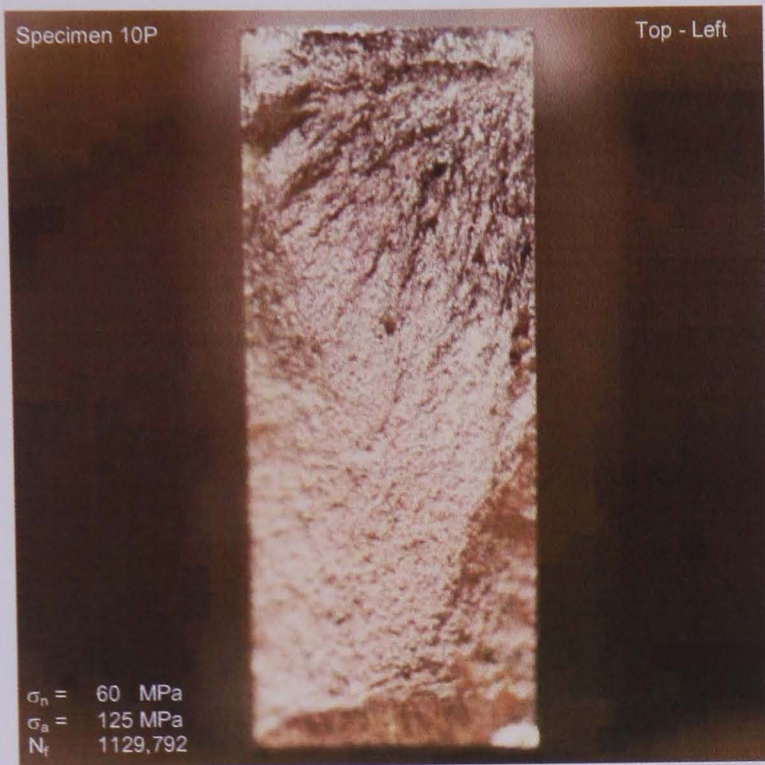
$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 125 \text{ MPa}$
 $N_f = 137,632$

$\sigma_n = 100 \text{ MPa}$
 $\sigma_a = 125 \text{ MPa}$
 $N_f = 145,848$

O.4 $\sigma_a = 100$ MPa peened



O.5 $\sigma_a = 125$ MPa peened

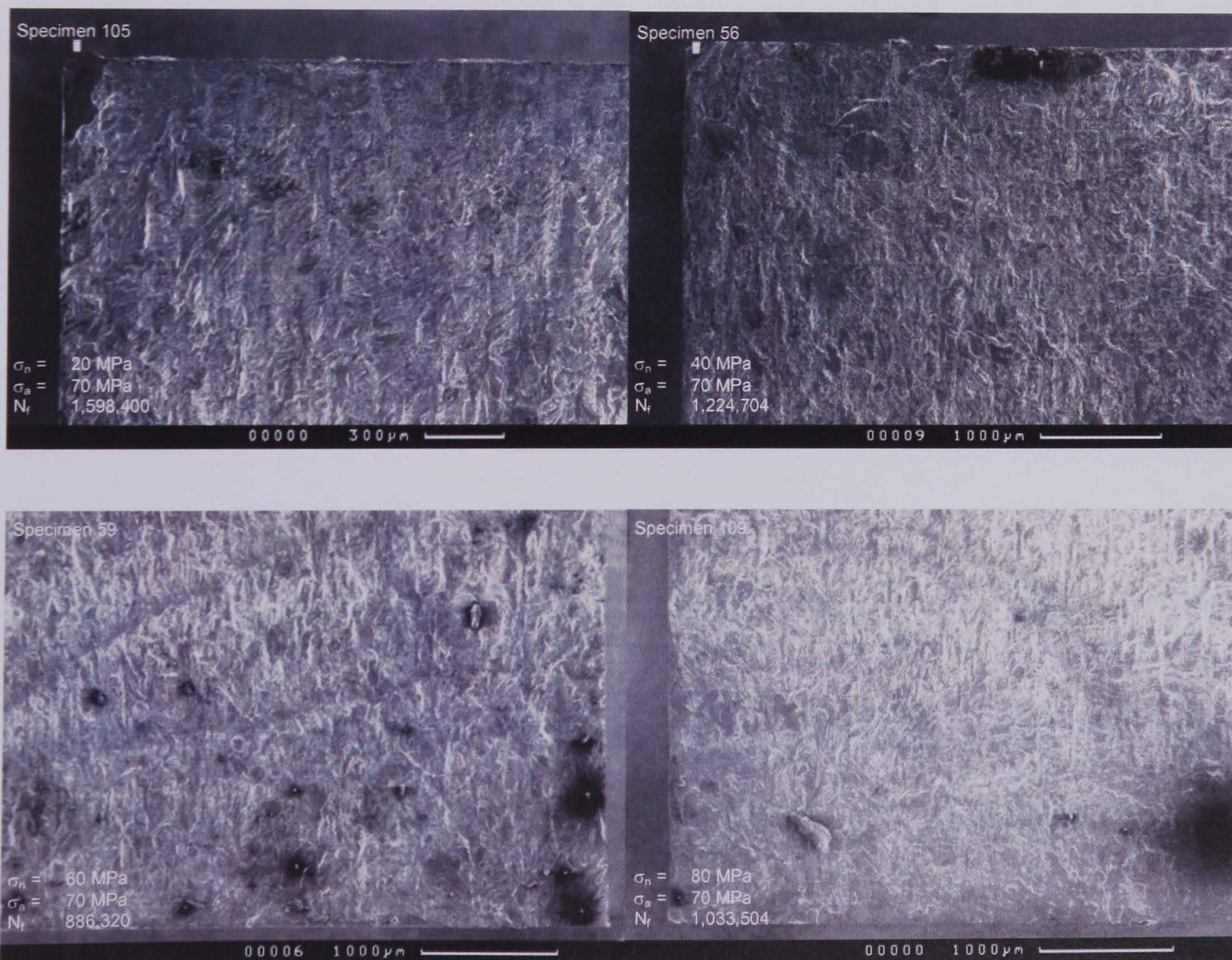


APPENDIX P

RESULTS: SEM IMAGES FRACTURE SURFACES

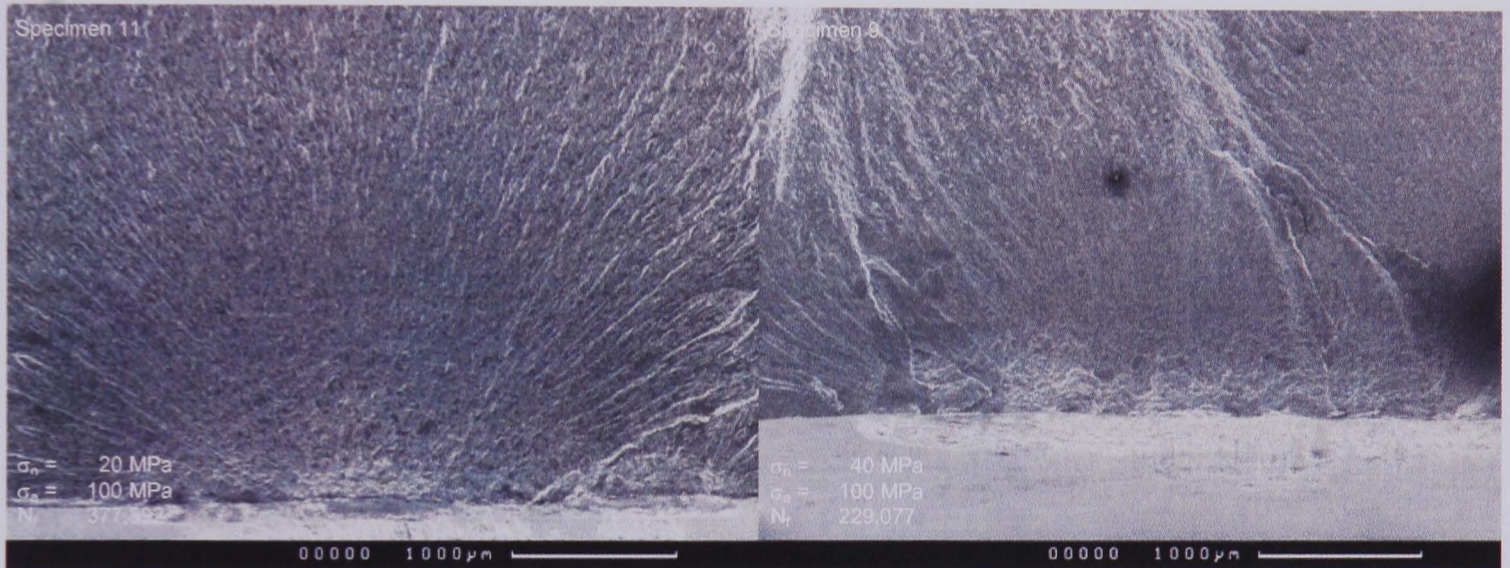
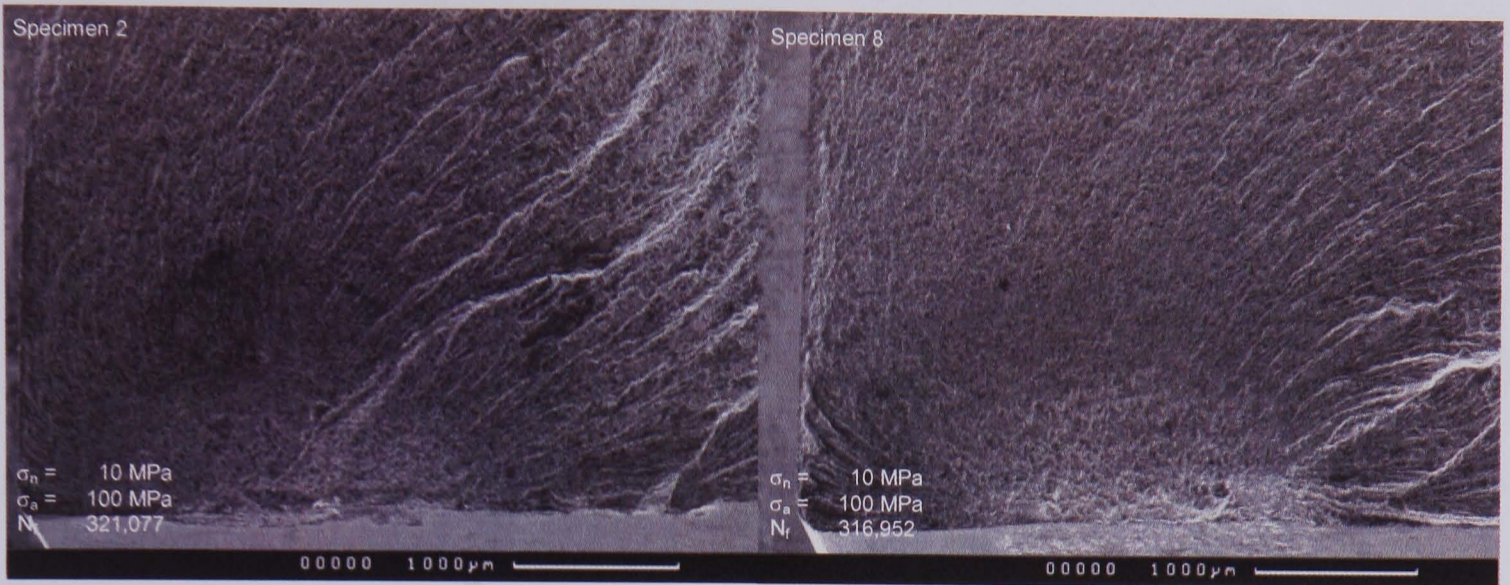
This appendix contains images of the unpeened fractured specimens taken under a scanning electron microscope. Each image shows the main crack initiation sites and displays its own scale marker.

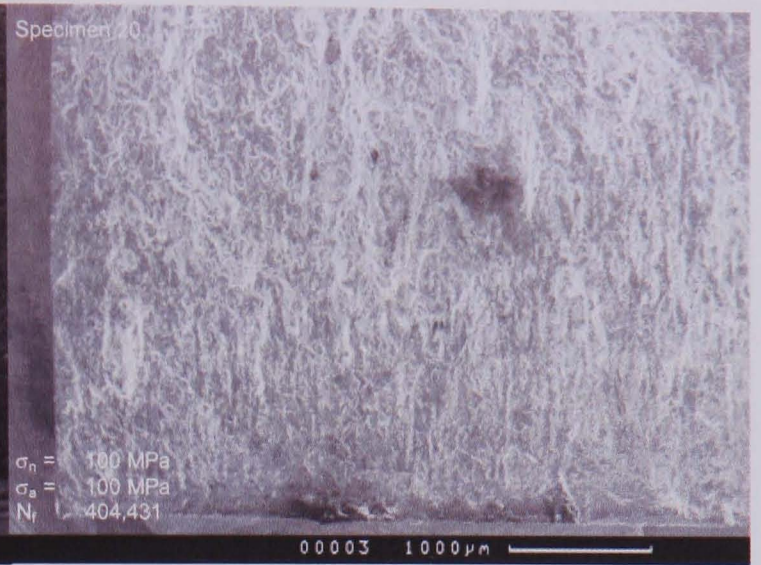
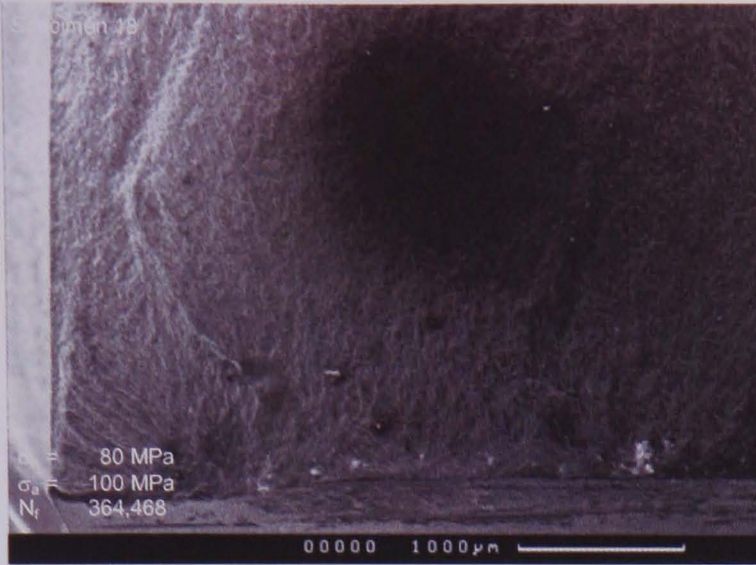
P.1 $\sigma_a = 70$ MPa unpeened



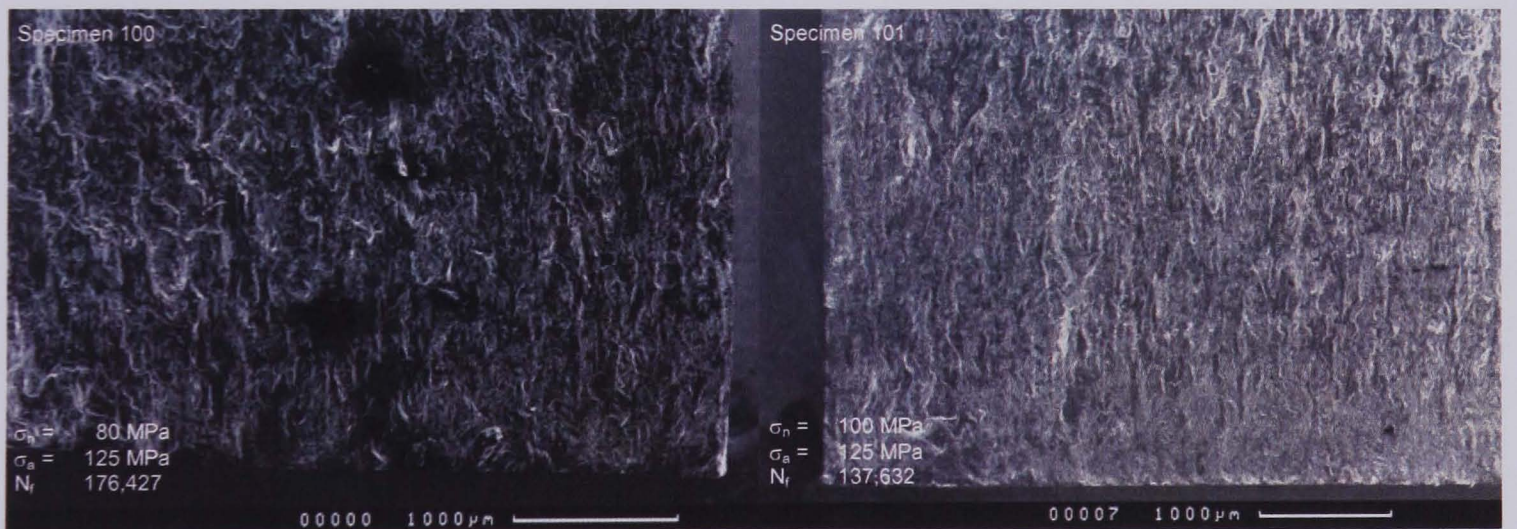
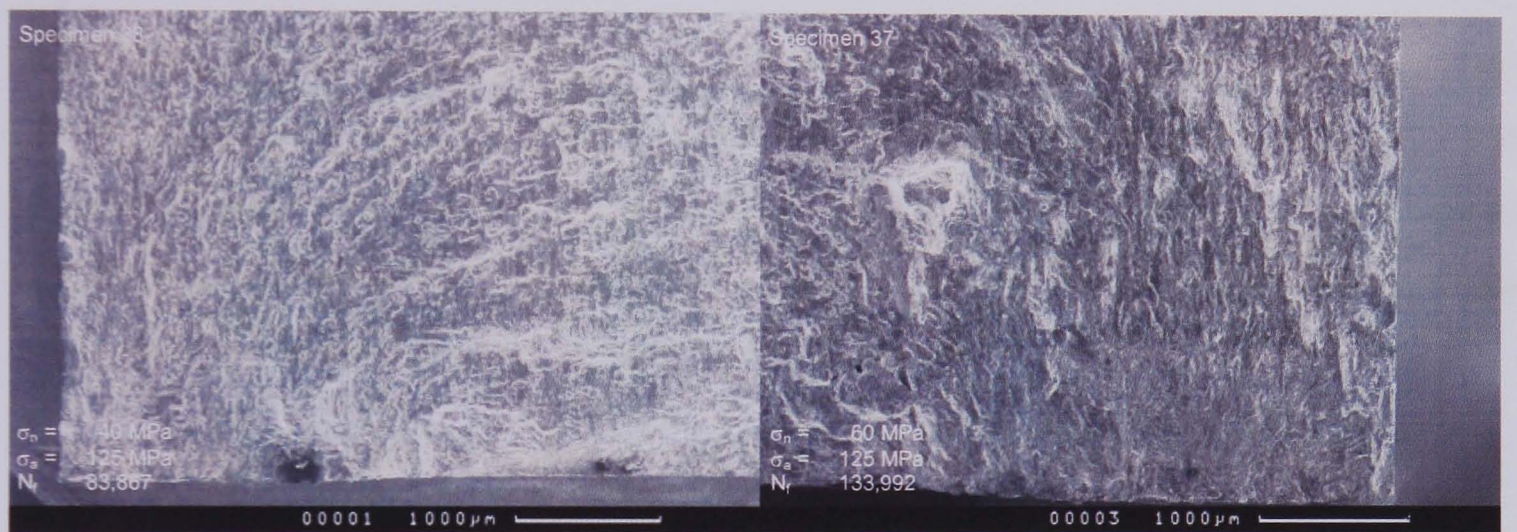
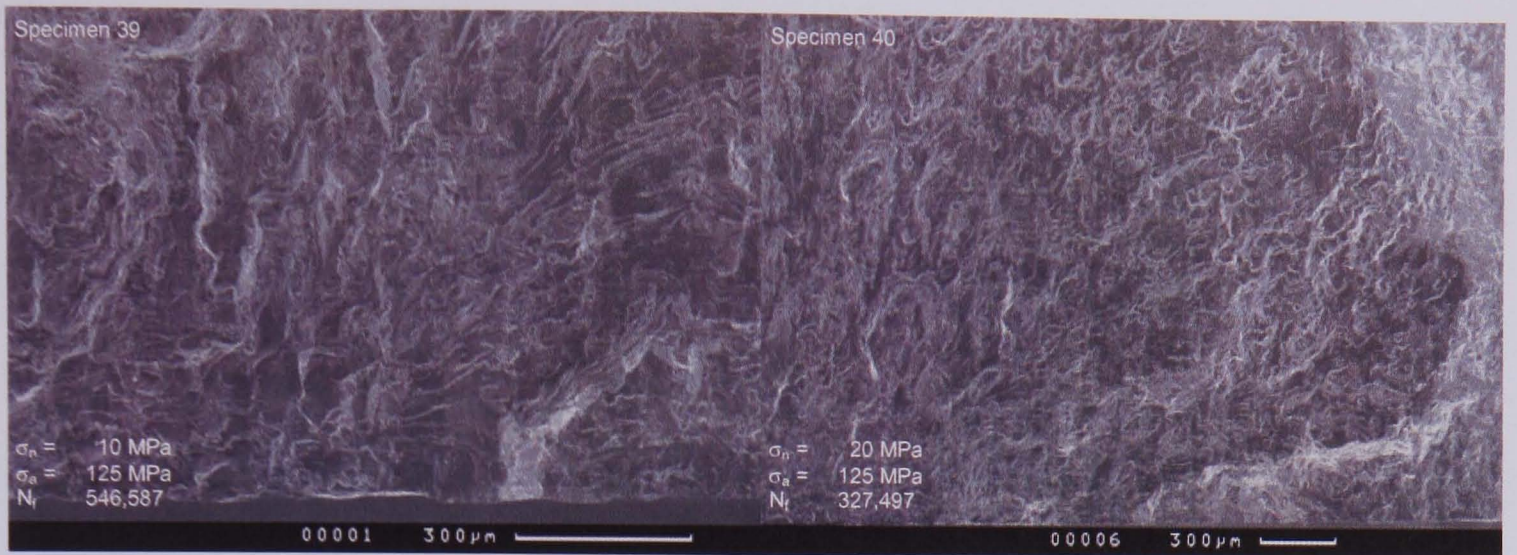


P.2 $\sigma_a = 100$ MPa unpeened





P.3 $\sigma_a = 125$ MPa unpeened

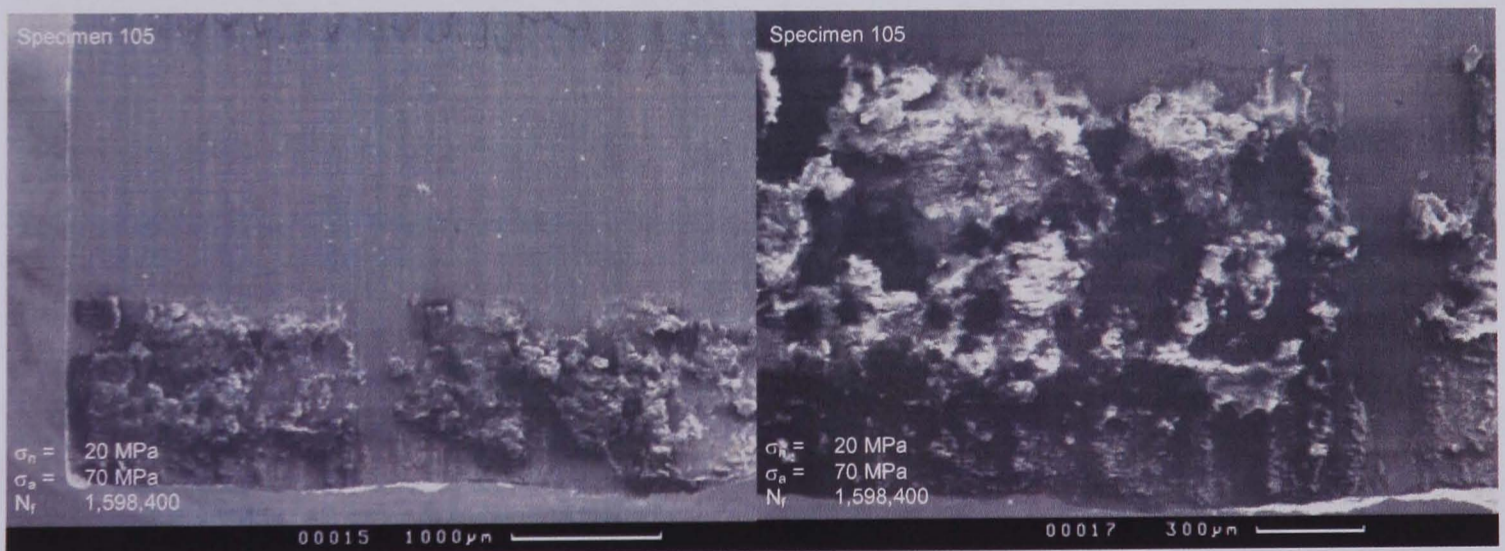


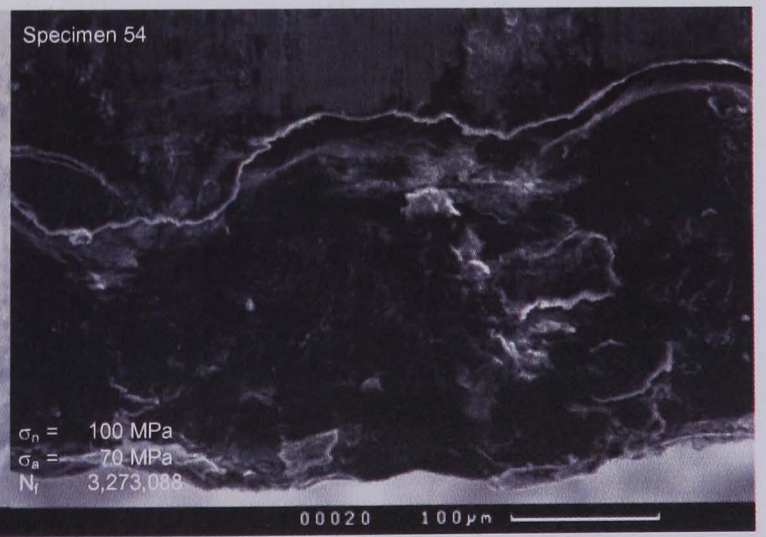
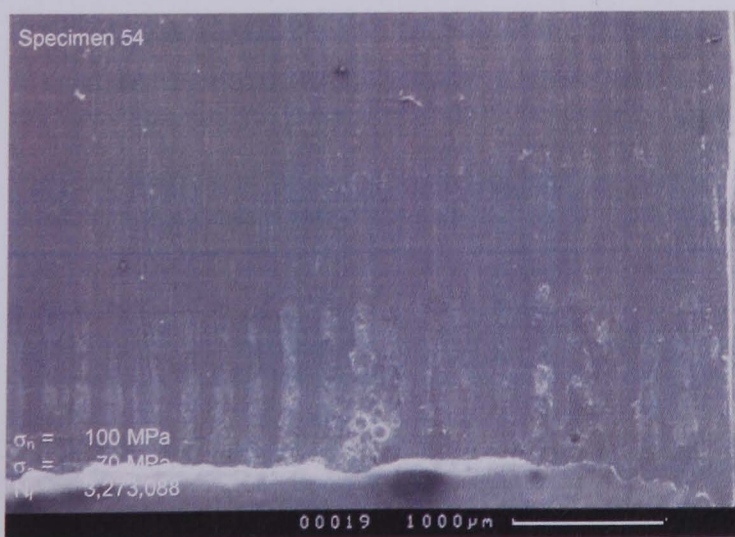
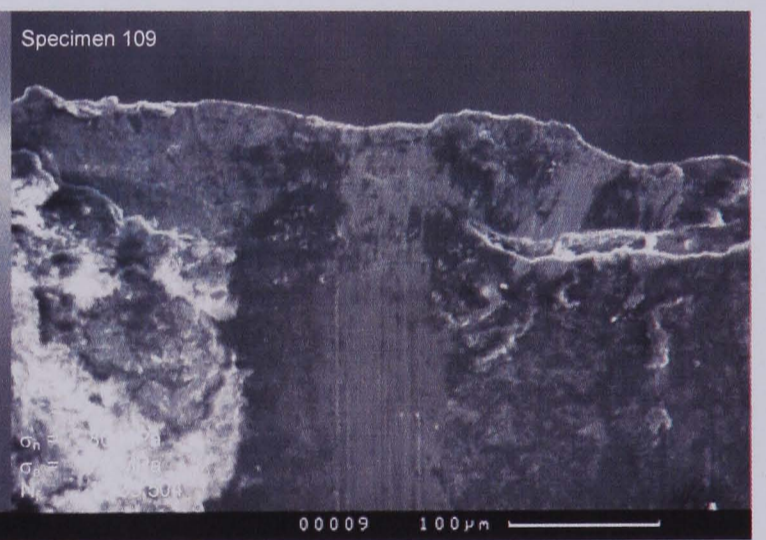
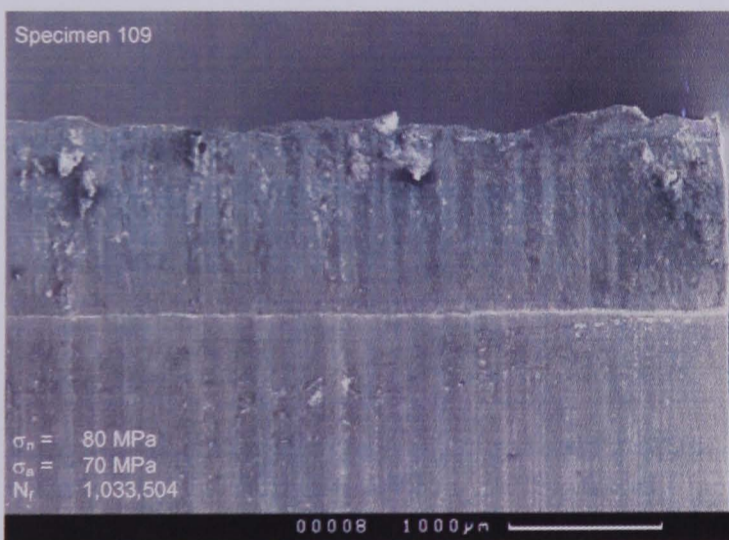
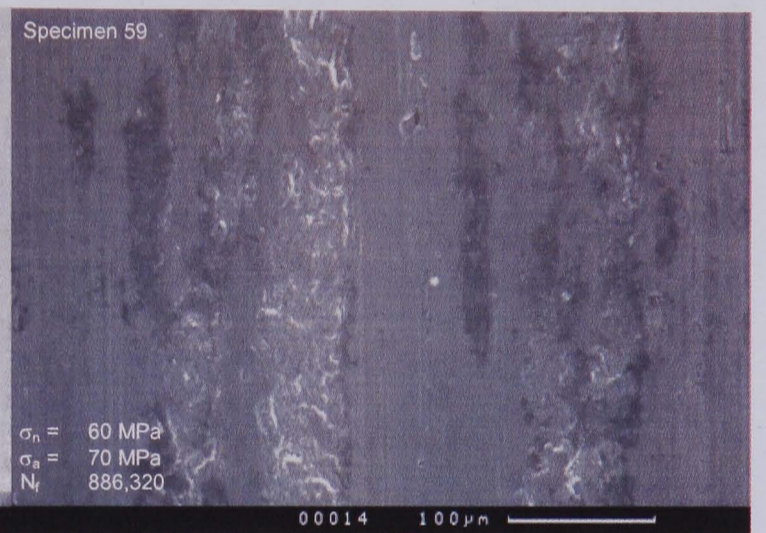
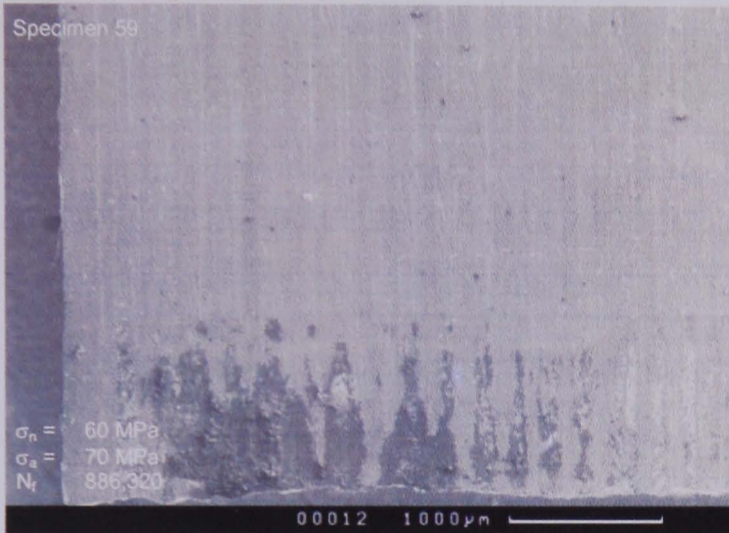
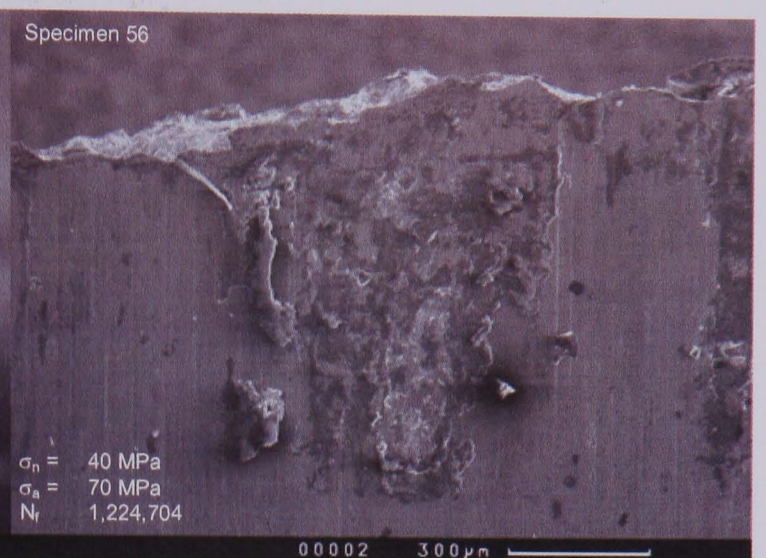
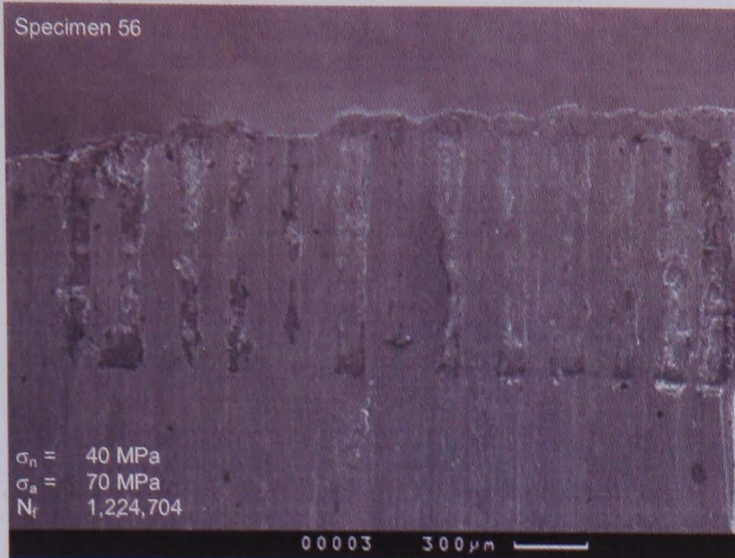
APPENDIX Q

RESULTS: SEM IMAGES SURFACE DEGRADATION

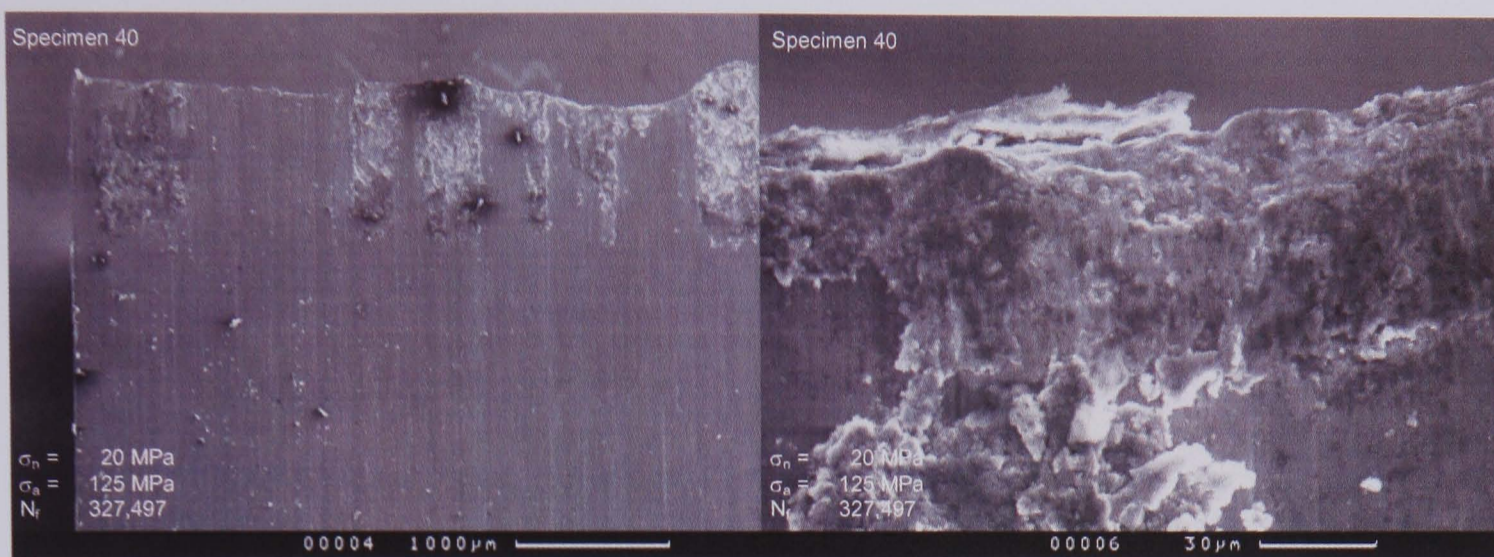
This appendix contains images of the unpeened fractured specimens taken under a scanning electron microscope. Each image depicts a wear scar and shows evidence of surface degradation; the presence of oxide debris, metal adhesion and smearing. Crack initiation occurred at the edge of these wear scars. Each image displays its own scale marker.

Q.1 $\sigma_a = 70$ MPa unpeened





Q.2 $\sigma_a = 125$ MPa unpeened

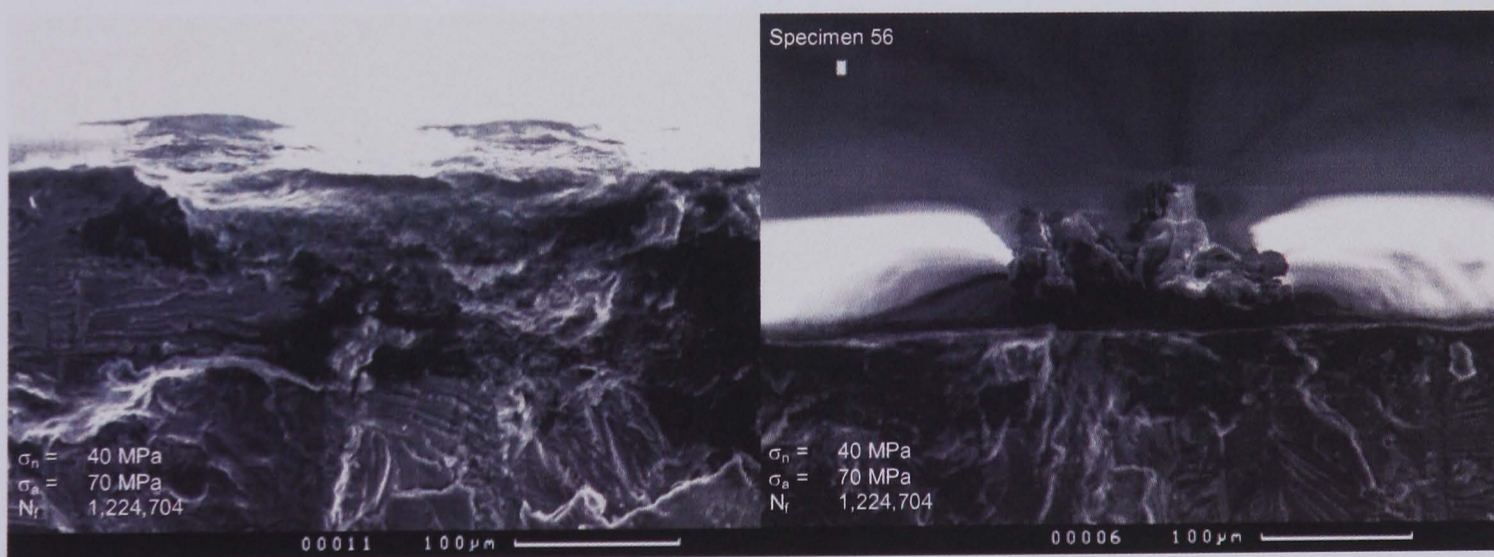


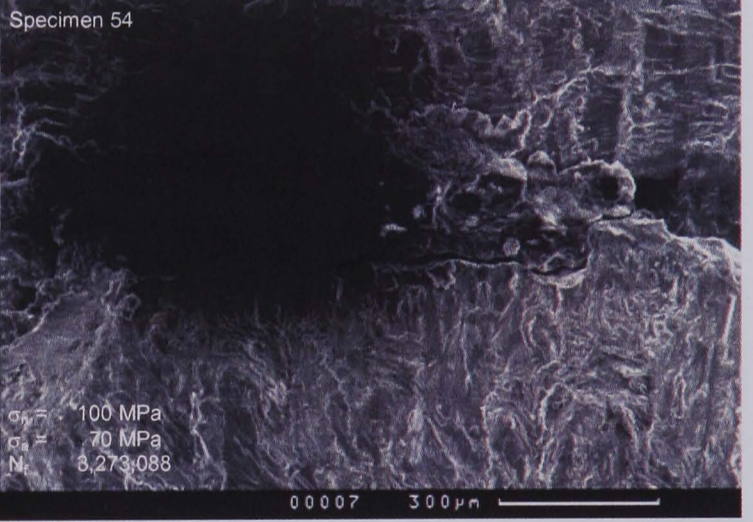
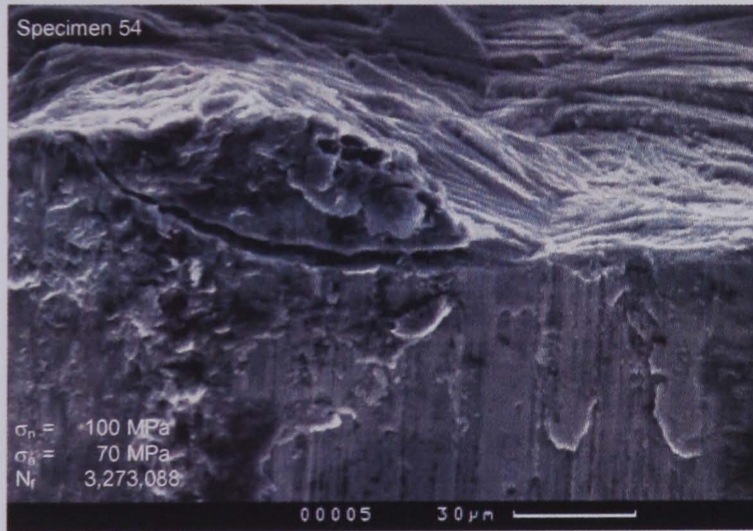
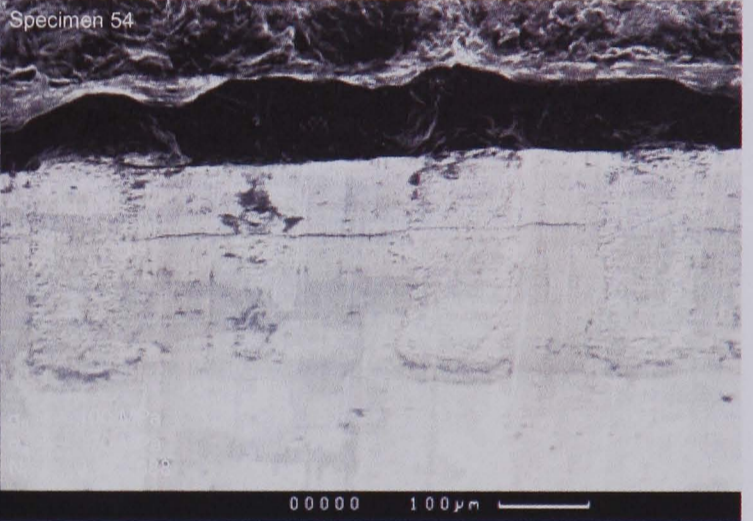
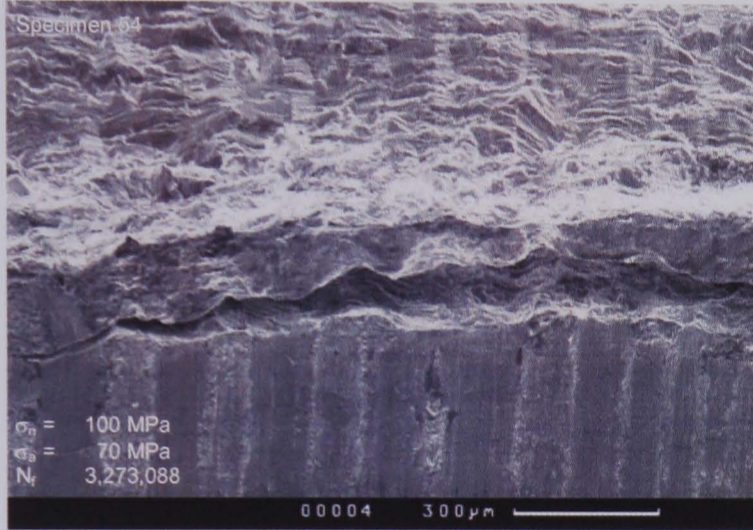
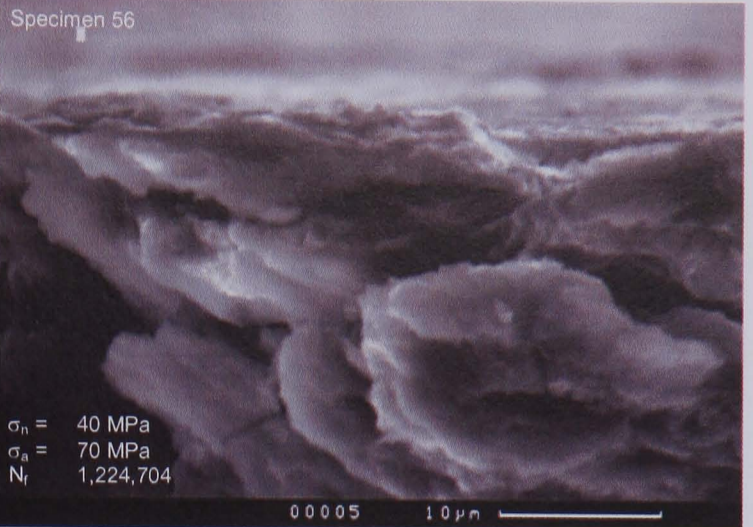
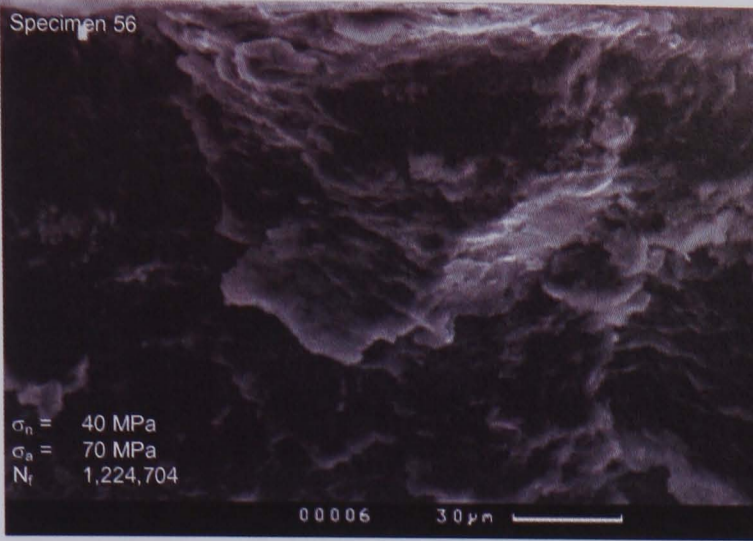
APPENDIX R

RESULTS: SEM IMAGES DEGRADATION

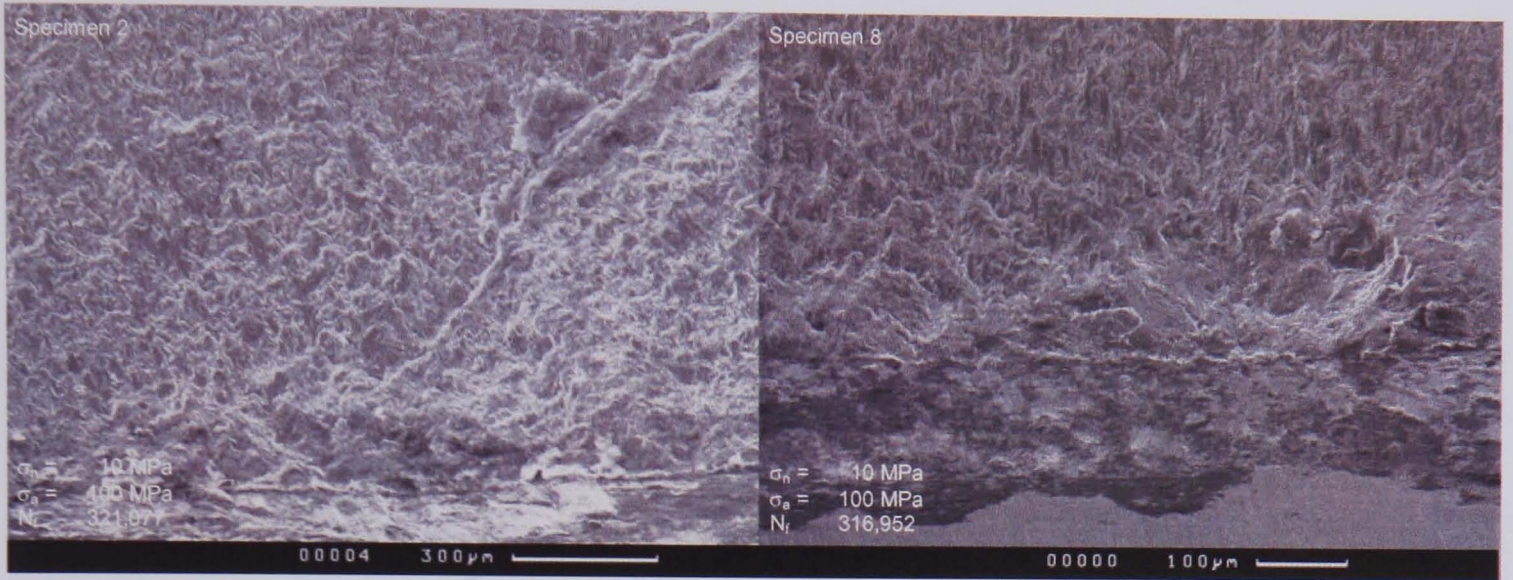
This appendix contains images of the unpeened fractured specimens taken under a scanning electron microscope. Each image depicts sub-surface degradation beneath a wear scar. Regions of rubbing near to the wear scars obliterated the primary features of the crack initiation sites. Each image displays its own scale marker.

R.1 $\sigma_a = 70$ MPa unpeened

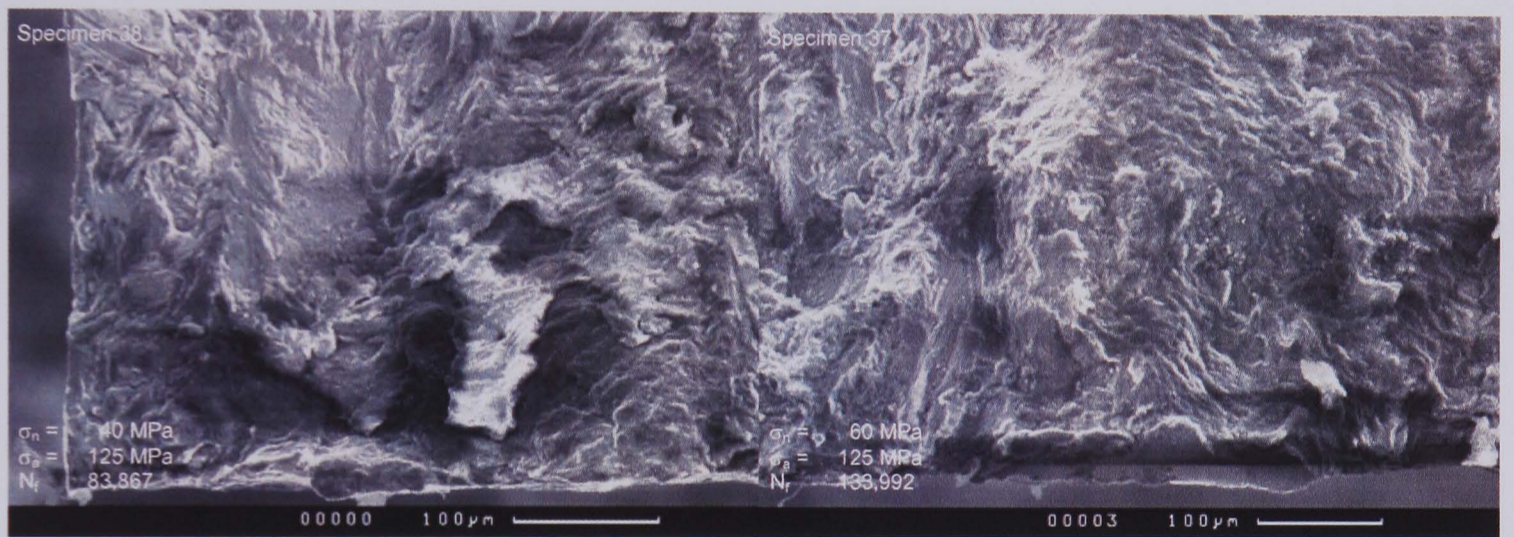




R.2 $\sigma_a = 100$ MPa unpeened



R.3 $\sigma_a = 125$ MPa unpeened

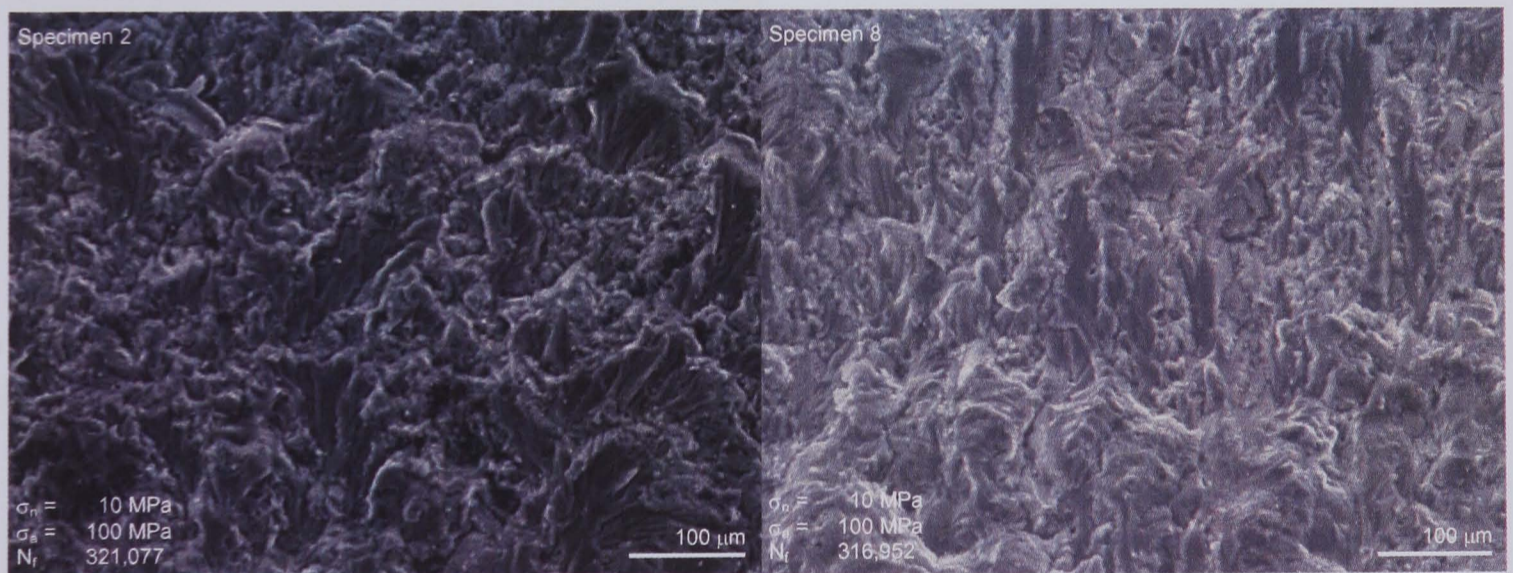


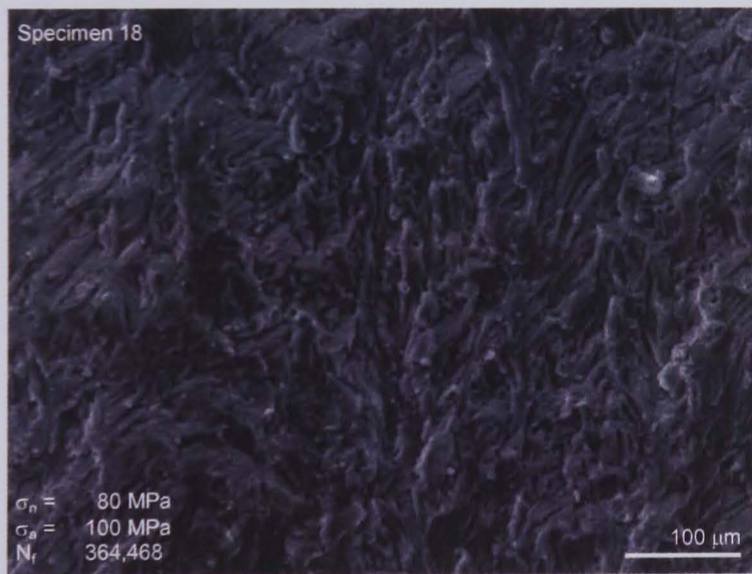
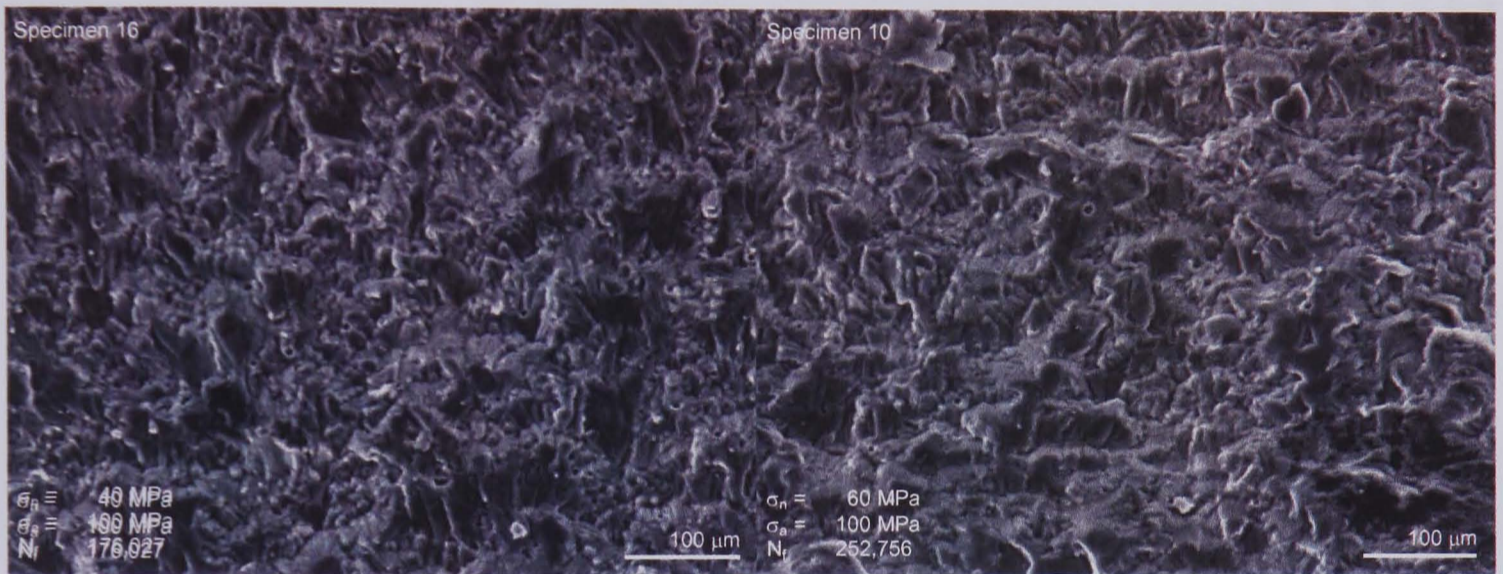
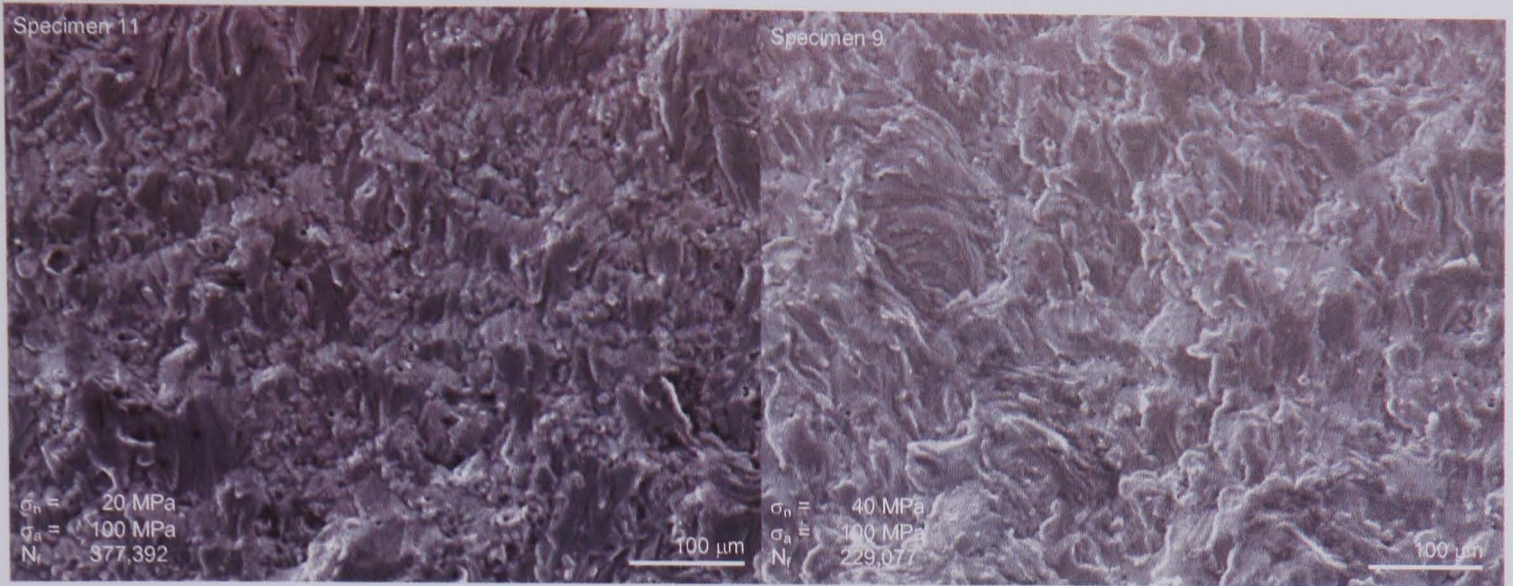
APPENDIX S

RESULTS: SEM IMAGES STAGE I CRACK GROWTH

This appendix contains images of the unpeened fractured specimens taken under a scanning electron microscope. Each image depicts a region of crack growth in Stage I, captured at approximately 100 μm from a fretting scar, see Sections 4.4.2 and 4.5.1. Each image displays its own scale marker.

S.1 $\sigma_a = 100 \text{ MPa}$ unpeened



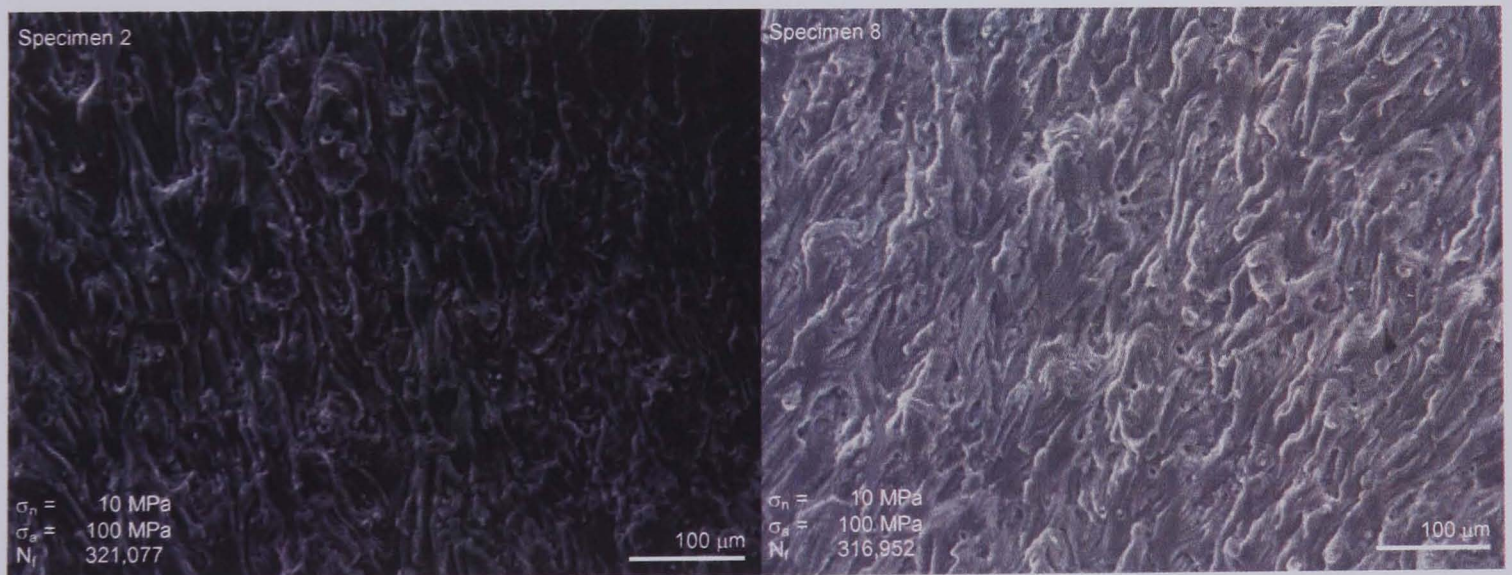


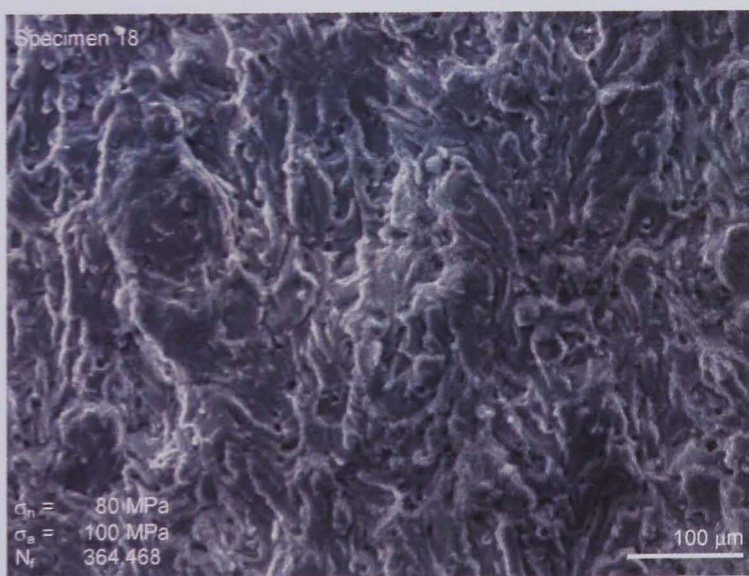
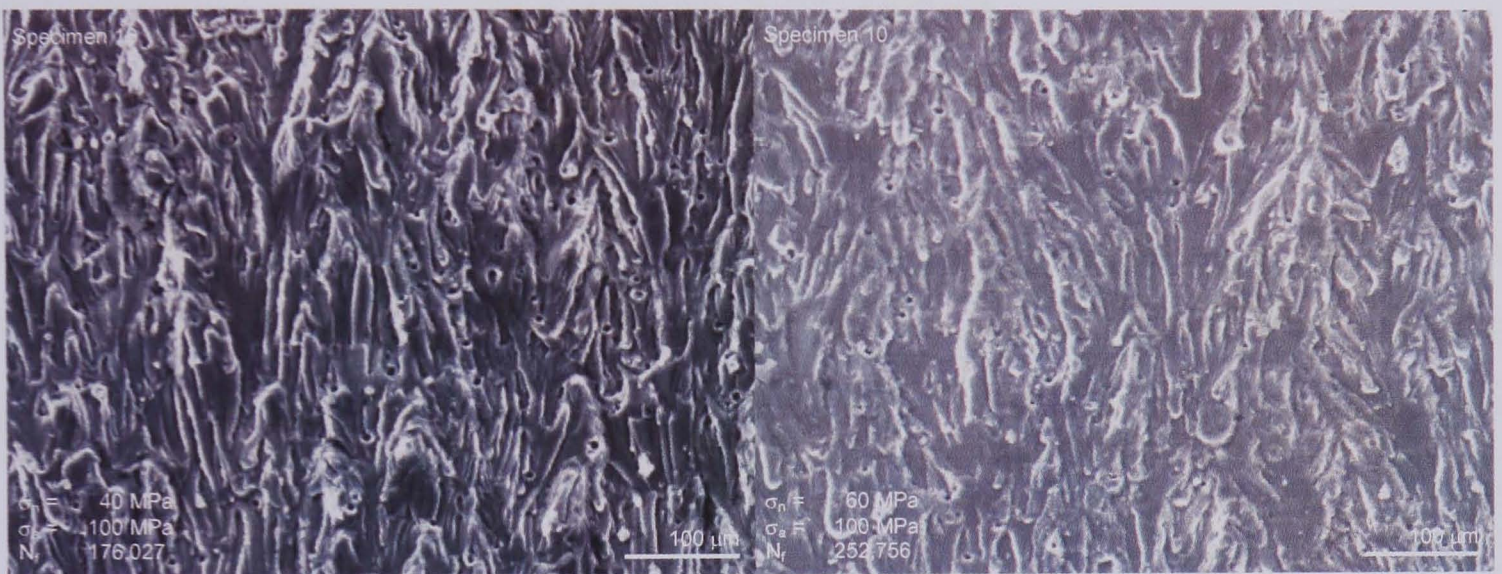
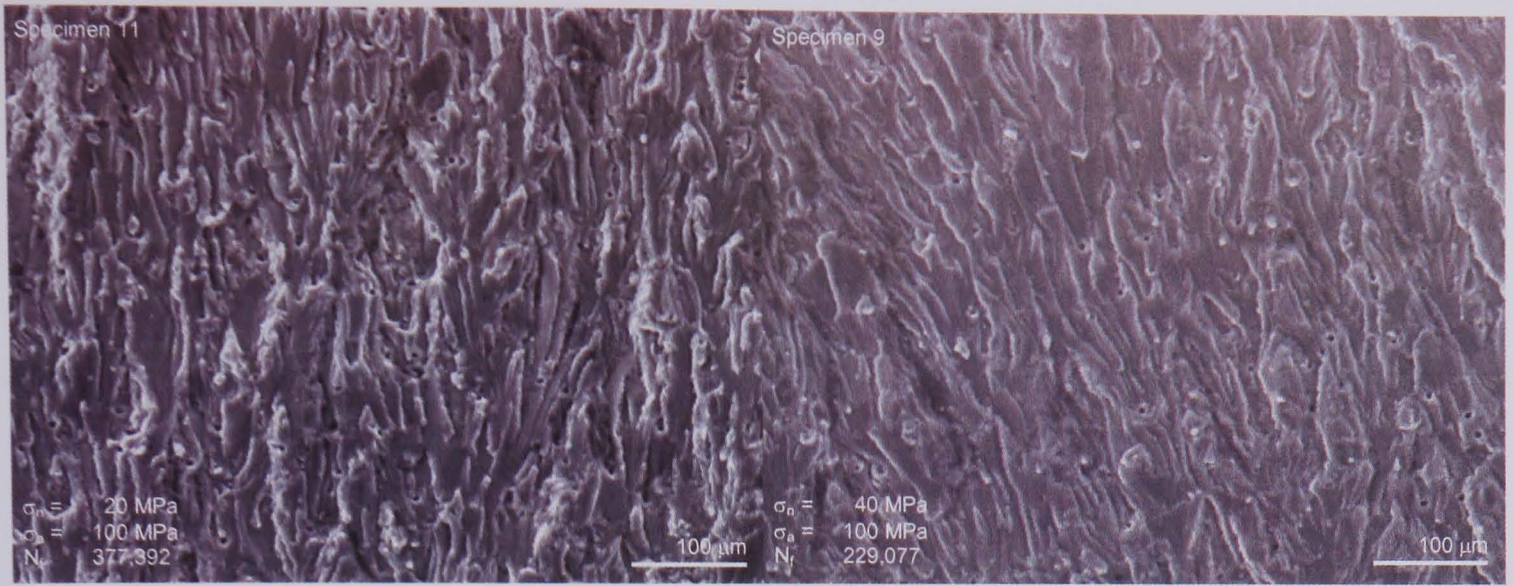
APPENDIX T

RESULTS: SEM IMAGES STAGE II CRACK GROWTH

This appendix contains images of the unpeened fractured specimens taken under a scanning electron microscope. Each image depicts a region of crack growth on a transverse crack face in Stage II, captured at approximately 1 mm from a fretting scar, see Sections 4.4.2 and 4.5.1. Each image displays its own scale marker.

T.1 $\sigma_a = 100$ MPa unpeened



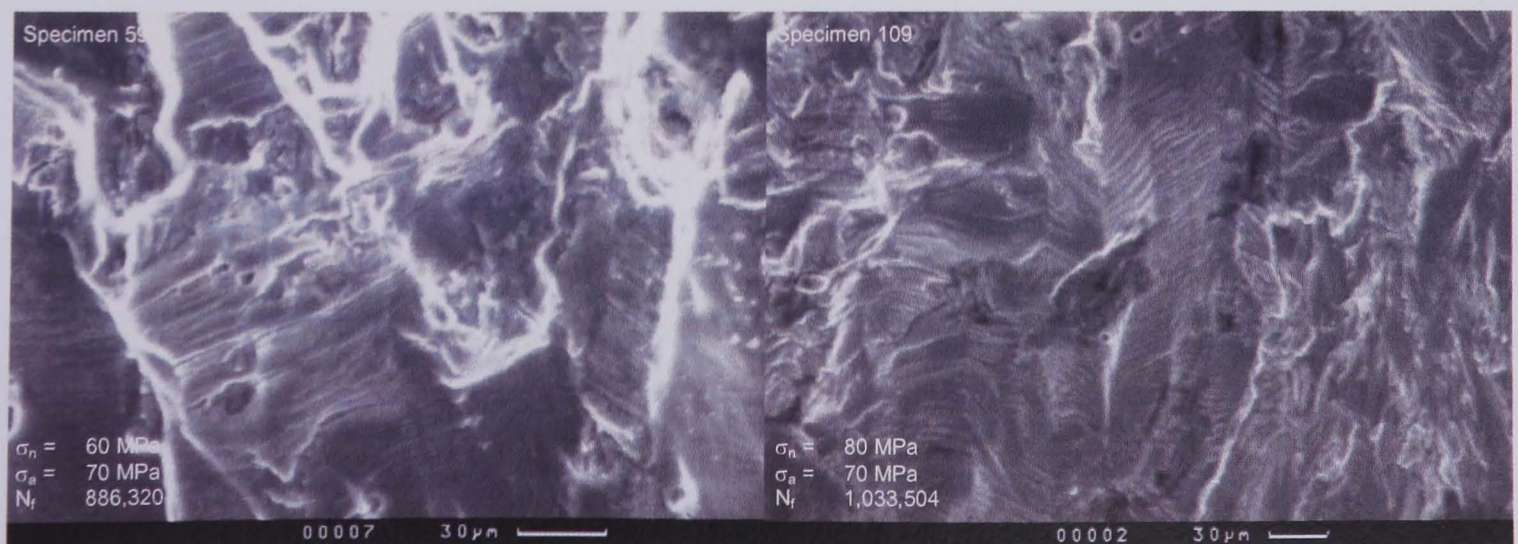
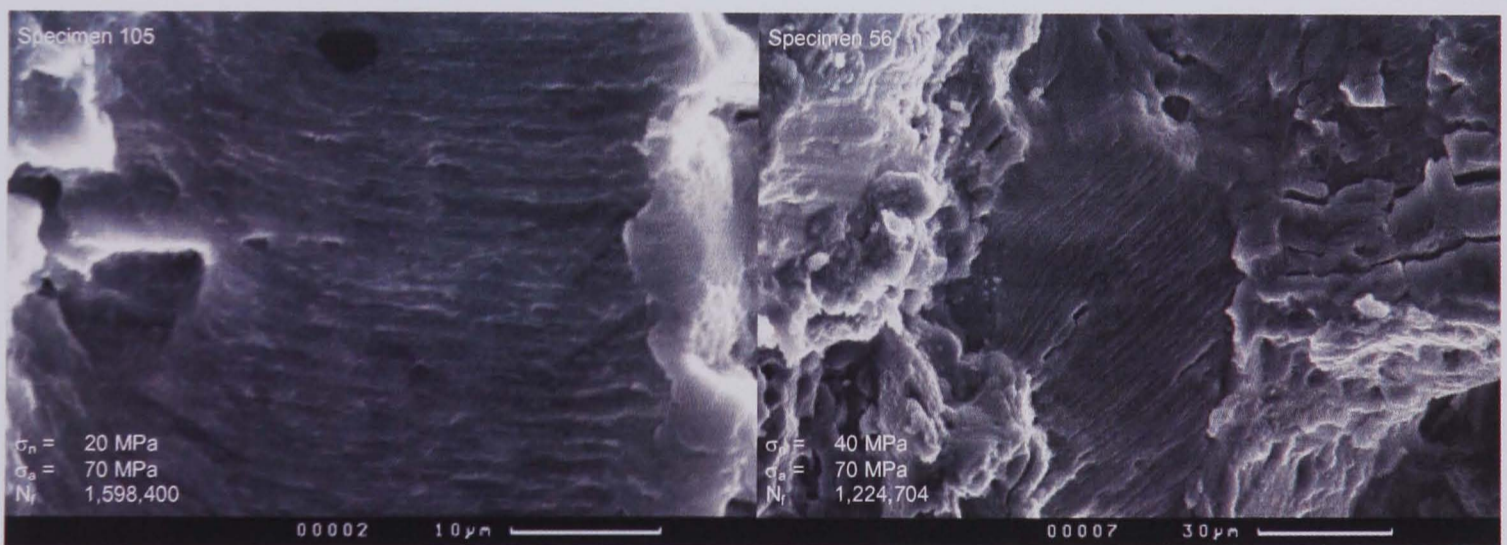


APPENDIX U

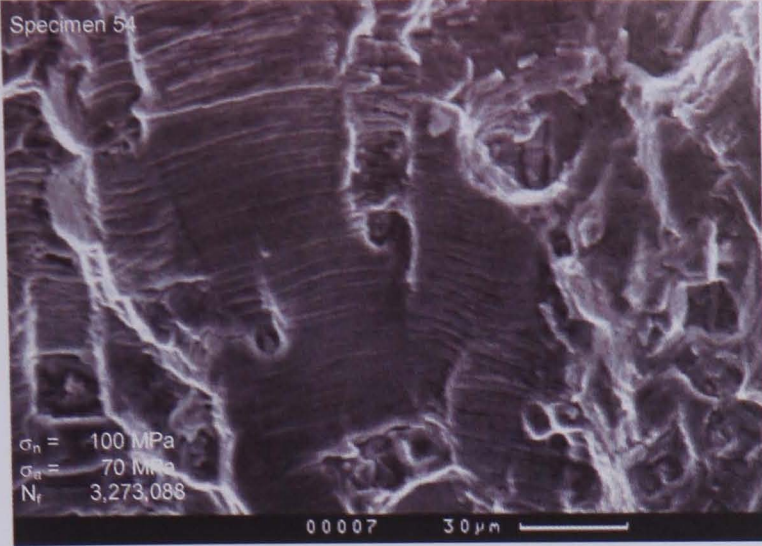
RESULTS: SEM IMAGES STRIATIONS

This appendix contains images of the unpeened fractured specimens taken under a scanning electron microscope. Each image depicts striation markings captured in a region of Stage II crack growth, see Sections 4.4.2 and 4.5.1. Each image displays its own scale marker.

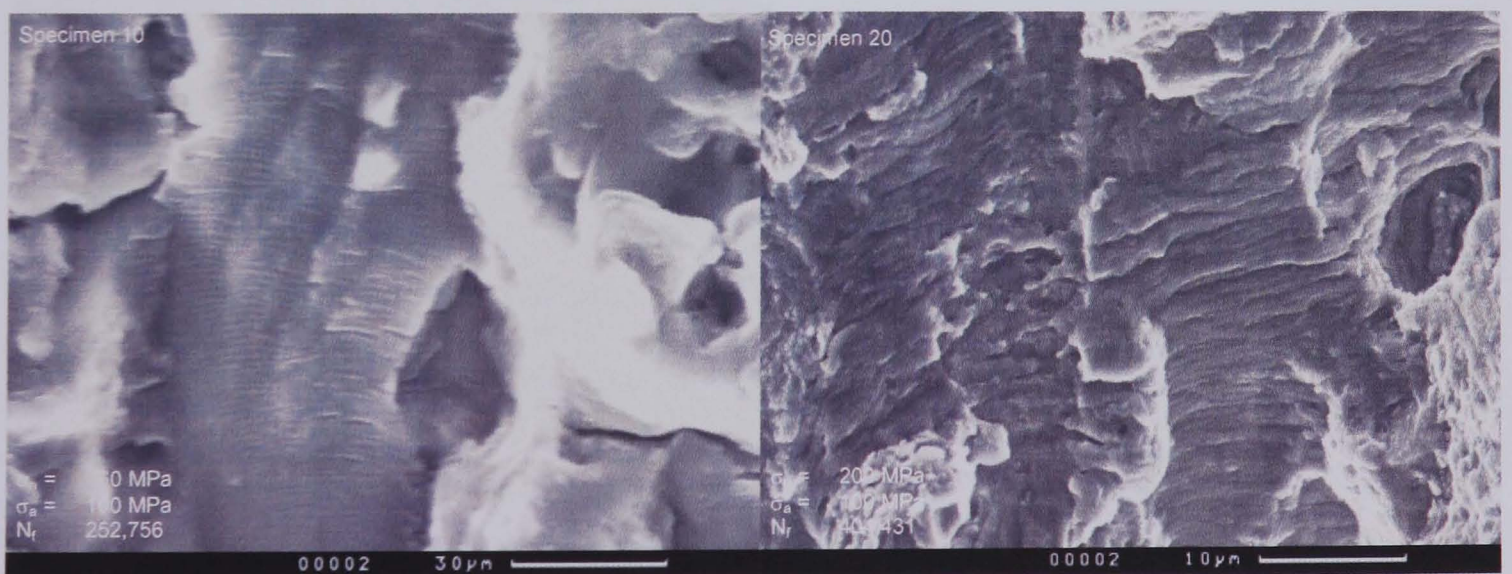
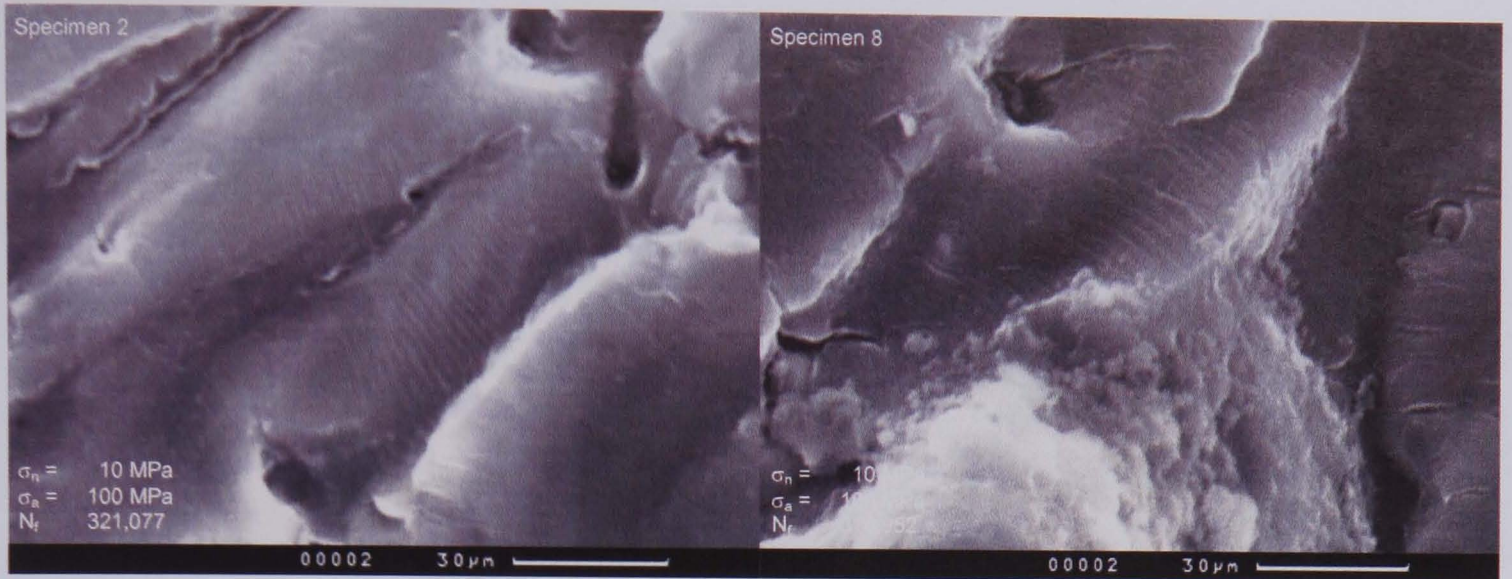
U.1 $\sigma_a = 70$ MPa unpeened



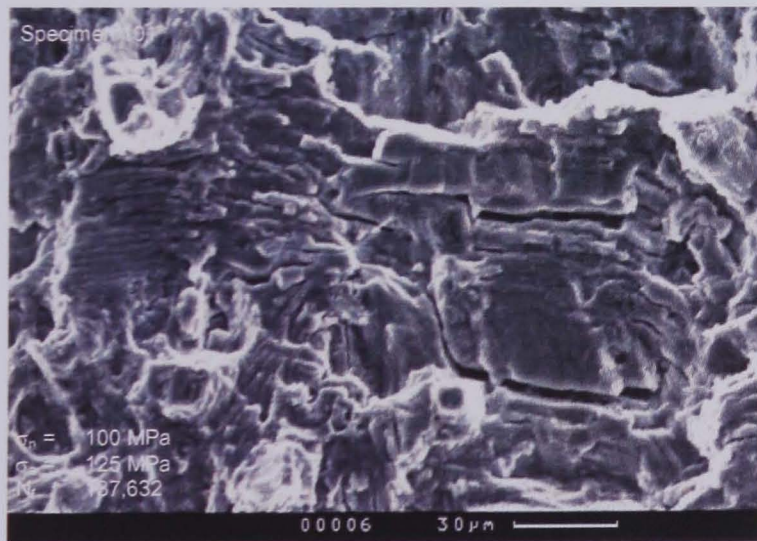
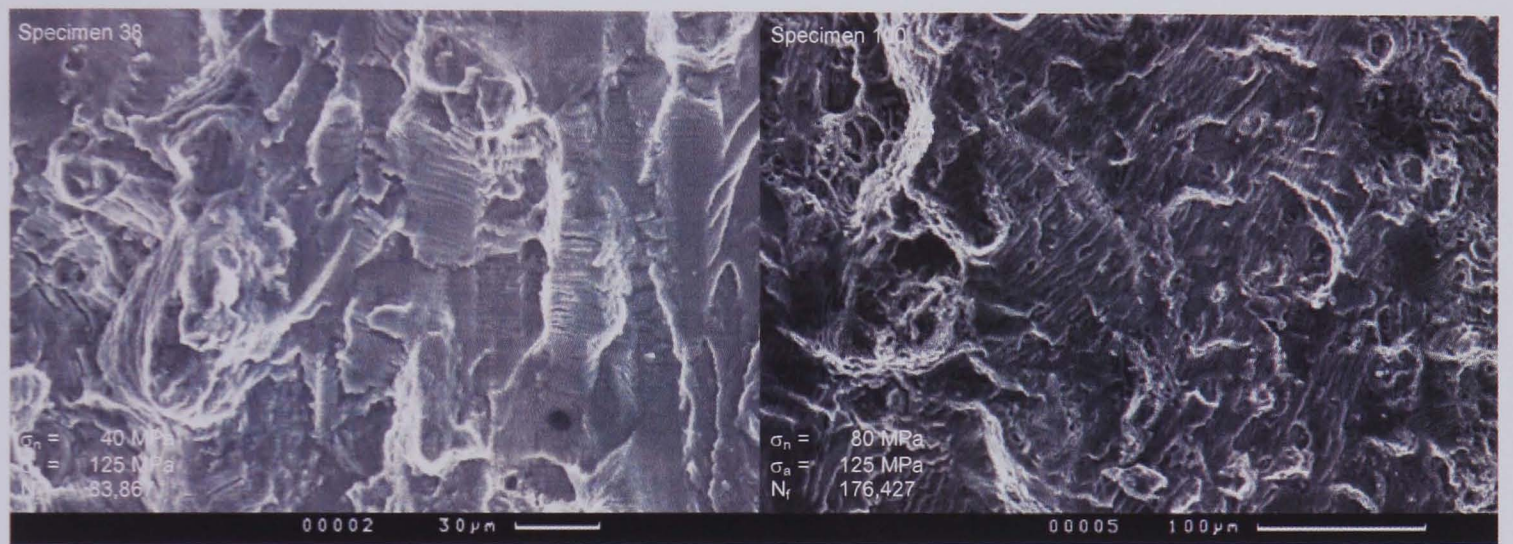
Specimen 54



U.2 $\sigma_a = 100$ MPa unpeened



U.3 $\sigma_a = 125$ MPa unpeened



APPENDIX V

ANALYTICAL MODEL: Y_I AND Y_{II}

a (m)	Y_{axial}	Polynomial (2nd order)	Difference (%)	Polynomial (3rd order)	Difference (%)	Polynomial (4th order)	Difference (%)	Polynomial (5th order)	Difference (%)	Polynomial (6th order)	Difference (%)	Polynomial (7th order)	Difference (%)	Polynomial (8th order)	Difference (%)	Polynomial (9th order)	Difference (%)	Polynomial (10th order)	Difference (%)
0.0001	0.296200	0.349247	0.281	0.319231	0.053	0.302256	0.004	0.299637	0.001	0.298709	0.001	0.298438	0.001	0.299263	0.001	0.299080	0.001	0.299720	0.001
0.0002	0.423142	0.433319	0.010	0.422261	0.000	0.423154	0.000	0.424670	0.000	0.424586	0.000	0.426761	0.001	0.424460	0.000	0.425145	0.000	0.422082	0.000
0.0003	0.535980	0.513972	0.048	0.516605	0.038	0.526432	0.009	0.528867	0.005	0.528815	0.005	0.529597	0.004	0.530249	0.003	0.529679	0.004	0.534022	0.000
0.0004	0.606504	0.591204	0.023	0.602882	0.001	0.615163	0.007	0.616814	0.011	0.616555	0.010	0.615869	0.009	0.617685	0.013	0.617235	0.012	0.617439	0.012
0.0005	0.691132	0.665017	0.068	0.681713	0.009	0.692110	0.000	0.692363	0.000	0.691964	0.000	0.690910	0.000	0.691611	0.000	0.691889	0.000	0.688444	0.001
0.0006	0.761656	0.735410	0.069	0.753717	0.006	0.759734	0.000	0.758692	0.001	0.758333	0.001	0.757843	0.001	0.756920	0.002	0.757486	0.002	0.755980	0.003
0.0007	0.818075	0.802383	0.025	0.819513	0.000	0.820187	0.000	0.818362	0.000	0.818214	0.000	0.818562	0.000	0.816980	0.000	0.817197	0.000	0.819394	0.000
0.0008	0.874494	0.865936	0.007	0.879720	0.003	0.875314	0.000	0.873367	0.000	0.873531	0.000	0.874378	0.000	0.873440	0.000	0.873120	0.000	0.876080	0.000
0.0009	0.930913	0.926069	0.002	0.934959	0.002	0.926655	0.002	0.925201	0.003	0.925680	0.003	0.926386	0.002	0.926761	0.002	0.926233	0.002	0.926524	0.002
0.001	0.973227	0.982782	0.009	0.985849	0.016	0.975443	0.000	0.974908	0.000	0.975624	0.001	0.975614	0.001	0.976991	0.001	0.976740	0.001	0.974120	0.000
0.0011	1.029646	1.036075	0.004	1.033009	0.001	1.022603	0.005	1.023138	0.004	1.023968	0.003	1.023016	0.004	1.024393	0.003	1.024643	0.003	1.022023	0.006
0.0012	1.071960	1.085949	0.020	1.077058	0.003	1.068755	0.001	1.070209	0.000	1.071028	0.000	1.069361	0.001	1.069736	0.000	1.070265	0.000	1.070556	0.000
0.0013	1.114274	1.132402	0.033	1.118618	0.002	1.114212	0.000	1.116159	0.000	1.116890	0.001	1.115081	0.000	1.114143	0.000	1.114463	0.000	1.117422	0.001
0.0014	1.156589	1.175435	0.036	1.158306	0.000	1.158980	0.001	1.160806	0.002	1.161453	0.002	1.160143	0.001	1.158561	0.000	1.158345	0.000	1.160542	0.002
0.0015	1.213008	1.215049	0.000	1.196742	0.026	1.202760	0.011	1.203801	0.008	1.204464	0.007	1.203992	0.008	1.203069	0.010	1.202503	0.011	1.200997	0.014
0.0016	1.241217	1.251243	0.010	1.234547	0.004	1.244944	0.001	1.244691	0.001	1.245541	0.002	1.245633	0.002	1.246334	0.003	1.246056	0.002	1.242611	0.000
0.0017	1.283531	1.284016	0.000	1.272338	0.013	1.284619	0.000	1.282968	0.000	1.284185	0.000	1.283910	0.000	1.285726	0.000	1.286176	0.001	1.286380	0.001
0.0018	1.325846	1.313370	0.016	1.310737	0.023	1.320565	0.003	1.318130	0.006	1.319781	0.004	1.318038	0.006	1.318689	0.005	1.319258	0.004	1.323601	0.001
0.0019	1.339950	1.339304	0.000	1.350363	0.011	1.351256	0.013	1.349740	0.010	1.351586	0.014	1.348449	0.007	1.346148	0.004	1.345463	0.003	1.342399	0.001
0.002	1.382264	1.361818	0.042	1.391834	0.009	1.374859	0.005	1.377477	0.002	1.378706	0.001	1.378015	0.002	1.378840	0.001	1.379024	0.001	1.379663	0.001

Difference 0.704 0.220 0.063 0.056 0.055 0.050 0.049 0.048 0.046

a (m)	Y_{normal}	Polynomial (2nd order)	Difference (%)	Polynomial (3rd order)	Difference (%)	Polynomial (4th order)	Difference (%)	Polynomial (5th order)	Difference (%)	Polynomial (6th order)	Difference (%)	Polynomial (7th order)	Difference (%)	Polynomial (8th order)	Difference (%)	Polynomial (9th order)	Difference (%)	Polynomial (10th order)	Difference (%)
0.0001	-0.242602	-0.312510	0.489	-0.257886	0.023	-0.246142	0.001	-0.245016	0.001	-0.243730	0.000	-0.242830	0.000	-0.242491	0.000	-0.242709	0.000	-0.242556	0.000
0.0002	-0.332872	-0.347981	0.023	-0.327856	0.003	-0.328474	0.002	-0.329126	0.001	-0.330683	0.000	-0.332435	0.000	-0.333381	0.000	-0.332567	0.000	-0.333298	0.000
0.0003	-0.394933	-0.379709	0.023	-0.384500	0.011	-0.391299	0.001	-0.392346	0.001	-0.393587	0.000	-0.394014	0.000	-0.393746	0.000	-0.394423	0.000	-0.393387	0.000
0.0004	-0.434426	-0.407693	0.071	-0.428945	0.003	-0.437441	0.001	-0.438151	0.001	-0.438147	0.001	-0.437169	0.001	-0.436423	0.000	-0.436958	0.001	-0.436909	0.001
0.0005	-0.468277	-0.431934	0.132	-0.462319	0.004	-0.469512	0.000	-0.469620	0.000	-0.468627	0.000	-0.467386	0.000	-0.467098	0.000	-0.466767	0.000	-0.467589	0.000
0.0006	-0.490845	-0.452432	0.148	-0.485748	0.003	-0.489911	0.000	-0.489463	0.000	-0.488182	0.001	-0.487643	0.001	-0.488022	0.001	-0.487350	0.001	-0.487709	0.001
0.0007	-0.496487	-0.469187	0.075	-0.500360	0.002	-0.500827	0.002	-0.500042	0.001	-0.499144	0.001	-0.499591	0.001	-0.500242	0.001	-0.499984	0.001	-0.499460	0.001
0.0008	-0.502129	-0.482199	0.040	-0.507284	0.003	-0.504236	0.000	-0.503398	0.000	-0.503269	0.000	-0.504351	0.000	-0.504737	0.001	-0.505118	0.001	-0.504411	0.001
0.0009	-0.507771	-0.491467	0.027	-0.507645	0.000	-0.501900	0.003	-0.501275	0.004	-0.501931	0.003	-0.502984	0.002	-0.502830	0.002	-0.503458	0.002	-0.503389	0.002
0.001	-0.496487	-0.496992	0.000	-0.502572	0.004	-0.495373	0.000	-0.495143	0.000	-0.496282	0.000	-0.496711	0.000	-0.496145	0.000	-0.496442	0.000	-0.497068	0.000
0.0011	-0.485203	-0.498773	0.018	-0.493193	0.006	-0.485993	0.000	-0.486223	0.000	-0.487362	0.000	-0.486933	0.000	-0.486367	0.000	-0.486069	0.000	-0.486694	0.000
0.0012	-0.473919	-0.496812	0.052	-0.480633	0.005	-0.474888	0.000	-0.475513	0.000	-0.476169	0.001	-0.475116	0.000	-0.474962	0.000	-0.474333	0.000	-0.474264	0.000
0.0013	-0.462635	-0.491107	0.081	-0.466022	0.001	-0.462973	0.000	-0.463811	0.000	-0.463681	0.000	-0.462599	0.000	-0.462985	0.000	-0.462604	0.000	-0.461898	0.000
0.0014	-0.451352	-0.481659	0.092	-0.450485	0.000	-0.450952	0.000	-0.451737	0.000	-0.450839	0.000	-0.450392	0.000	-0.451042	0.000	-0.451300	0.000	-0.450776	0.000
0.0015	-0.440068	-0.468467	0.081	-0.435152	0.002	-0.439315	0.000	-0.439763	0.000	-0.438482	0.000	-0.439021	0.000	-0.439400	0.000	-0.440073	0.000	-0.440432	0.000
0.0016	-0.428784	-0.451533	0.052	-0.421148	0.006	-0.428342	0.000	-0.428233	0.000	-0.427240	0.000	-0.428481	0.000	-0.428192	0.000	-0.428523	0.000	-0.429345	0.000
0.0017	-0.417500	-0.430855	0.018	-0.409603	0.006	-0.418099	0.000	-0.417389	0.000	-0.417385	0.000	-0.418363	0.000	-0.417616	0.000	-0.417081	0.000	-0.417032	0.000
0.0018	-0.406217	-0.406433	0.000	-0.401642	0.002	-0.408441	0.000	-0.407394	0.000	-0.408635	0.001	-0.408209	0.000	-0.407941	0.000	-0.407264	0.000	-0.406228	0.000
0.0019	-0.400575	-0.378269	0.050	-0.398393	0.000	-0.399012	0.000	-0.398360	0.000	-0.399916	0.000	-0.398164	0.001	-0.399110	0.000	-0.399925	0.000	-0.400656	0.000
0.002	-0.389291	-0.346361	0.184	-0.400985	0.014	-0.389241	0.000	-0.390367	0.000	-0.389081	0.000	-0.389980	0.000	-0.389641	0.000	-0.389423	0.000	-0.389270	0.000

Difference 1.655 0.097 0.013 0.012 0.009 0.007 0.007 0.006 0.006

a (m)	$\gamma_{friction}$	Polynomial (2nd order)	Difference (%)	Polynomial (3rd order)	Difference (%)	Polynomial (4th order)	Difference (%)	Polynomial (5th order)	Difference (%)	Polynomial (6th order)	Difference (%)	Polynomial (7th order)	Difference (%)	Polynomial (8th order)	Difference (%)	Polynomial (9th order)	Difference (%)	Polynomial (10th order)	Difference (%)
0.0001	0.710879	0.820886	1.210	0.758920	0.231	0.728295	0.030	0.717797	0.005	0.712637	0.000	0.710710	0.000	0.710539	0.000	0.710665	0.000	0.710905	0.000
0.0002	0.801149	0.807786	0.004	0.784957	0.026	0.786569	0.021	0.792646	0.007	0.798893	0.001	0.802646	0.000	0.803123	0.000	0.802653	0.000	0.801503	0.000
0.0003	0.835001	0.793527	0.172	0.798962	0.130	0.816693	0.034	0.826453	0.007	0.831433	0.001	0.832346	0.001	0.832211	0.001	0.832601	0.001	0.834232	0.000
0.0004	0.829359	0.778107	0.263	0.802215	0.074	0.824370	0.002	0.830989	0.000	0.830973	0.000	0.828879	0.000	0.828503	0.000	0.828812	0.000	0.828888	0.000
0.0005	0.806791	0.761526	0.205	0.795995	0.012	0.814752	0.006	0.815765	0.008	0.811779	0.002	0.809120	0.001	0.808975	0.000	0.808785	0.000	0.807491	0.000
0.0006	0.778582	0.743785	0.121	0.781579	0.001	0.792435	0.019	0.788259	0.009	0.783117	0.002	0.781963	0.001	0.782154	0.001	0.781766	0.001	0.781200	0.001
0.0007	0.756014	0.724884	0.097	0.760248	0.002	0.761464	0.003	0.754146	0.000	0.750544	0.003	0.751502	0.002	0.751829	0.002	0.751681	0.002	0.752506	0.001
0.0008	0.722163	0.704823	0.030	0.733280	0.012	0.725331	0.001	0.717526	0.002	0.717006	0.003	0.719325	0.001	0.719519	0.001	0.719738	0.001	0.720849	0.000
0.0009	0.682669	0.683601	0.000	0.701954	0.037	0.686973	0.002	0.681145	0.000	0.683775	0.000	0.686031	0.001	0.685953	0.001	0.686316	0.001	0.686425	0.001
0.001	0.648818	0.661218	0.015	0.667549	0.035	0.648776	0.000	0.646631	0.000	0.651200	0.001	0.652119	0.001	0.651834	0.001	0.652006	0.001	0.651022	0.000
0.0011	0.620609	0.637675	0.029	0.631344	0.012	0.612571	0.006	0.614716	0.003	0.619285	0.000	0.618366	0.001	0.618082	0.001	0.617910	0.001	0.616926	0.001
0.0012	0.586757	0.612972	0.069	0.594619	0.006	0.579638	0.005	0.585467	0.000	0.588097	0.000	0.585842	0.000	0.585764	0.000	0.585402	0.000	0.585511	0.000
0.0013	0.552906	0.587108	0.117	0.558651	0.003	0.550703	0.000	0.558508	0.003	0.557989	0.003	0.555671	0.001	0.555865	0.001	0.555646	0.001	0.556757	0.001
0.0014	0.530338	0.560084	0.088	0.524721	0.003	0.525938	0.002	0.532255	0.001	0.529653	0.000	0.528695	0.000	0.529023	0.000	0.529171	0.000	0.529996	0.000
0.0015	0.507771	0.531900	0.058	0.494106	0.019	0.504962	0.001	0.509139	0.000	0.503997	0.001	0.505152	0.001	0.505343	0.001	0.505730	0.000	0.505165	0.001
0.0016	0.479561	0.502555	0.053	0.468087	0.013	0.486844	0.005	0.485831	0.004	0.481845	0.001	0.484504	0.002	0.484358	0.002	0.484549	0.002	0.483256	0.001
0.0017	0.468277	0.472050	0.001	0.447941	0.041	0.470096	0.000	0.463477	0.002	0.463461	0.002	0.465555	0.001	0.465179	0.001	0.464871	0.001	0.464948	0.001
0.0018	0.445710	0.440384	0.003	0.434948	0.012	0.452679	0.005	0.442918	0.001	0.447897	0.000	0.446984	0.000	0.446849	0.000	0.446459	0.000	0.448089	0.001
0.0019	0.428784	0.407558	0.045	0.430387	0.000	0.431999	0.001	0.425922	0.001	0.432168	0.001	0.428415	0.000	0.428891	0.000	0.429361	0.000	0.428210	0.000
0.002	0.411858	0.373571	0.147	0.435537	0.056	0.404913	0.005	0.415410	0.001	0.410250	0.000	0.412177	0.000	0.412007	0.000	0.411881	0.000	0.412121	0.000

Difference 2.728 0.725 0.150 0.057 0.022 0.013 0.013 0.013 0.011

a (m)	γ_{axial}	Polynomial (2nd order)	Difference (%)	Polynomial (3rd order)	Difference (%)	Polynomial (4th order)	Difference (%)	Polynomial (5th order)	Difference (%)	Polynomial (6th order)	Difference (%)	Polynomial (7th order)	Difference (%)	Polynomial (8th order)	Difference (%)	Polynomial (9th order)	Difference (%)	Polynomial (10th order)	Difference (%)
0.0001	-0.090270	-0.097429	0.005	-0.088377	0.000	-0.088230	0.000	-0.089748	0.000	-0.088279	0.000	-0.088475	0.000	-0.089841	0.000	-0.089881	0.000	-0.089880	0.000
0.0002	-0.112838	-0.117429	0.002	-0.114094	0.000	-0.114102	0.000	-0.113223	0.000	-0.115001	0.000	-0.114618	0.000	-0.110809	0.000	-0.110658	0.000	-0.110664	0.000
0.0003	-0.135406	-0.136702	0.000	-0.137496	0.000	-0.137581	0.000	-0.136170	0.000	-0.137587	0.000	-0.137494	0.000	-0.138572	0.001	-0.138697	0.001	-0.138689	0.001
0.0004	-0.157973	-0.155248	0.001	-0.158770	0.000	-0.158876	0.000	-0.157919	0.000	-0.157915	0.000	-0.158128	0.000	-0.161134	0.001	-0.161233	0.001	-0.161233	0.001
0.0005	-0.180541	-0.173068	0.006	-0.178102	0.001	-0.178193	0.001	-0.178046	0.001	-0.176912	0.001	-0.177182	0.001	-0.178343	0.000	-0.178282	0.001	-0.178289	0.001
0.0006	-0.191824	-0.190160	0.000	-0.195681	0.001	-0.195733	0.002	-0.196337	0.002	-0.194874	0.001	-0.194991	0.001	-0.193463	0.000	-0.193338	0.000	-0.193341	0.000
0.0007	-0.214392	-0.206526	0.006	-0.211692	0.001	-0.211698	0.001	-0.212756	0.000	-0.211731	0.001	-0.211633	0.001	-0.209014	0.003	-0.208966	0.003	-0.208962	0.003
0.0008	-0.225676	-0.222165	0.001	-0.226322	0.000	-0.226284	0.000	-0.227413	0.000	-0.227265	0.000	-0.227029	0.000	-0.225475	0.000	-0.225545	0.000	-0.225539	0.000
0.0009	-0.242602	-0.237078	0.003	-0.239759	0.001	-0.239686	0.001	-0.240529	0.000	-0.241278	0.000	-0.241048	0.000	-0.241670	0.000	-0.241786	0.000	-0.241786	0.000
0.001	-0.253885	-0.251263	0.001	-0.252188	0.000	-0.252098	0.000	-0.252408	0.000	-0.253708	0.000	-0.253615	0.000	-0.255894	0.000	-0.255949	0.000	-0.255954	0.000
0.0011	-0.265169	-0.264722	0.000	-0.263797	0.000	-0.263707	0.000	-0.263397	0.000	-0.264697	0.000	-0.264791	0.000	-0.267070	0.000	-0.267014	0.000	-0.267020	0.000
0.0012	-0.276453	-0.277454	0.000	-0.274773	0.000	-0.274701	0.000	-0.273858	0.001	-0.274607	0.000	-0.274836	0.000	-0.275458	0.000	-0.275341	0.000	-0.275341	0.000
0.0013	-0.282095	-0.289459	0.005	-0.285302	0.001	-0.285264	0.001	-0.284135	0.000	-0.283987	0.000	-0.284223	0.000	-0.282670	0.000	-0.282599	0.000	-0.282593	0.000
0.0014	-0.293379	-0.300737	0.005	-0.295571	0.000	-0.295577	0.000	-0.294519	0.000	-0.293494	0.000	-0.293591	0.000	-0.290972	0.001	-0.291020	0.001	-0.291015	0.001
0.0015	-0.304662	-0.311288	0.004	-0.305768	0.000	-0.305820	0.000	-0.305216	0.000	-0.303753	0.000	-0.303635	0.000	-0.302107	0.001	-0.302231	0.001	-0.302234	0.001
0.0016	-0.315946	-0.321113	0.003	-0.316078	0.000	-0.316168	0.000	-0.316315	0.000	-0.315180	0.000	-0.314909	0.000	-0.316070	0.000	-0.316131	0.000	-0.316138	0.000
0.0017	-0.327230	-0.330211	0.001	-0.326689	0.000	-0.326796	0.000	-0.327753	0.000	-0.327748	0.000	-0.327535	0.000	-0.330541	0.001	-0.330442	0.001	-0.330441	0.001
0.0018	-0.338514	-0.338581	0.000	-0.337787	0.000	-0.337873	0.000	-0.339284	0.000	-0.340702	0.000	-0.340795	0.001	-0.341873	0.001	-0.341747	0.001	-0.341738	0.001
0.0019	-0.349798	-0.346226	0.001	-0.349560	0.000	-0.349568	0.000	-0.350447	0.000	-0.352225	0.001	-0.352607	0.001	-0.348798	0.000	-0.348949	0.000	-0.348955	0.000
0.002	-0.361081	-0.353143	0.006	-0.362194	0.000	-0.362047	0.000	-0.360529	0.000	-0.359060	0.000	-0.358864	0.000	-0.360229	0.000	-0.360189	0.000	-0.360188	0.000

Difference 0.052 0.007 0.007 0.006 0.007 0.007 0.011 0.011 0.011

a (m)	$Y_{II \text{ normal}}$	Polynomial (2nd order)	Difference (%)	Polynomial (3rd order)	Difference (%)	Polynomial (4th order)	Difference (%)	Polynomial (5th order)	Difference (%)	Polynomial (6th order)	Difference (%)	Polynomial (7th order)	Difference (%)	Polynomial (8th order)	Difference (%)	Polynomial (9th order)	Difference (%)	Polynomial (10th order)	Difference (%)
0.0001	-0.141047	-0.168751	0.077	-0.144228	0.001	-0.138679	0.001	-0.141320	0.000	-0.141108	0.000	-0.140572	0.000	-0.141099	0.000	-0.141051	0.000	-0.140921	0.000
0.0002	-0.203108	-0.213537	0.011	-0.204502	0.000	-0.204794	0.000	-0.203265	0.000	-0.203525	0.000	-0.204585	0.000	-0.203095	0.000	-0.203273	0.000	-0.203894	0.000
0.0003	-0.259527	-0.255064	0.002	-0.257215	0.001	-0.260428	0.000	-0.257972	0.000	-0.258179	0.000	-0.258432	0.000	-0.258848	0.000	-0.258700	0.000	-0.257819	0.000
0.0004	-0.304662	-0.293333	0.013	-0.302874	0.000	-0.306888	0.000	-0.305222	0.000	-0.305221	0.000	-0.304641	0.000	-0.305801	0.000	-0.305684	0.000	-0.305643	0.000
0.0005	-0.344156	-0.328342	0.025	-0.341983	0.000	-0.345382	0.000	-0.345127	0.000	-0.344961	0.000	-0.344224	0.000	-0.344672	0.000	-0.344744	0.000	-0.345444	0.000
0.0006	-0.378007	-0.360094	0.032	-0.375051	0.001	-0.377018	0.000	-0.378068	0.000	-0.377854	0.000	-0.377534	0.000	-0.378945	0.000	-0.377091	0.000	-0.377397	0.000
0.0007	-0.406217	-0.388586	0.031	-0.402582	0.001	-0.402802	0.001	-0.404643	0.000	-0.404493	0.000	-0.404759	0.000	-0.403748	0.001	-0.403804	0.001	-0.403358	0.001
0.0008	-0.423142	-0.413820	0.009	-0.425082	0.000	-0.423642	0.000	-0.425606	0.001	-0.425584	0.001	-0.426227	0.001	-0.425627	0.001	-0.425544	0.001	-0.424944	0.000
0.0009	-0.440068	-0.435795	0.002	-0.443059	0.001	-0.440345	0.000	-0.441811	0.000	-0.441921	0.000	-0.442546	0.001	-0.442786	0.001	-0.442649	0.001	-0.442589	0.001
0.001	-0.456994	-0.454512	0.001	-0.457017	0.000	-0.453616	0.001	-0.454156	0.001	-0.454346	0.001	-0.454601	0.001	-0.455480	0.000	-0.455415	0.000	-0.455947	0.000
0.0011	-0.468277	-0.469970	0.000	-0.467464	0.000	-0.464063	0.002	-0.463523	0.002	-0.463714	0.002	-0.463459	0.002	-0.464338	0.002	-0.464403	0.002	-0.464935	0.001
0.0012	-0.468277	-0.482169	0.019	-0.474906	0.004	-0.472192	0.002	-0.470725	0.001	-0.470835	0.001	-0.470210	0.000	-0.470449	0.000	-0.470586	0.001	-0.470527	0.001
0.0013	-0.473919	-0.491110	0.030	-0.479848	0.004	-0.478408	0.002	-0.476444	0.001	-0.476422	0.001	-0.475780	0.000	-0.475180	0.000	-0.475263	0.000	-0.474662	0.000
0.0014	-0.479561	-0.496792	0.030	-0.482797	0.001	-0.483017	0.001	-0.481176	0.000	-0.481026	0.000	-0.480760	0.000	-0.479750	0.000	-0.479694	0.000	-0.479248	0.000
0.0015	-0.485203	-0.499215	0.020	-0.484258	0.000	-0.486225	0.000	-0.485174	0.000	-0.484960	0.000	-0.485280	0.000	-0.484691	0.000	-0.484544	0.000	-0.484850	0.000
0.0016	-0.490845	-0.498380	0.006	-0.484739	0.004	-0.488137	0.001	-0.488392	0.001	-0.488226	0.001	-0.488963	0.000	-0.489411	0.000	-0.489339	0.000	-0.490038	0.000
0.0017	-0.490845	-0.494286	0.001	-0.484745	0.004	-0.487959	0.000	-0.490424	0.000	-0.490424	0.000	-0.491004	0.000	-0.492164	0.000	-0.492281	0.000	-0.492239	0.000
0.0018	-0.490845	-0.486933	0.002	-0.484782	0.004	-0.487994	0.001	-0.490450	0.000	-0.490658	0.000	-0.490405	0.000	-0.490821	0.000	-0.490968	0.000	-0.490087	0.000
0.0019	-0.485203	-0.476322	0.008	-0.485357	0.000	-0.485649	0.000	-0.487178	0.000	-0.487438	0.000	-0.486398	0.000	-0.484928	0.000	-0.484751	0.000	-0.485372	0.000
0.002	-0.479561	-0.462452	0.029	-0.486976	0.005	-0.481427	0.000	-0.478786	0.000	-0.478571	0.000	-0.479105	0.000	-0.479632	0.000	-0.479680	0.000	-0.479550	0.000

Difference 0.346 0.032 0.013 0.007 0.007 0.006 0.005 0.005 0.005

a (m)	$Y_{II \text{ friction}}$	Polynomial (2nd order)	Difference (%)	Polynomial (3rd order)	Difference (%)	Polynomial (4th order)	Difference (%)	Polynomial (5th order)	Difference (%)	Polynomial (6th order)	Difference (%)	Polynomial (7th order)	Difference (%)	Polynomial (8th order)	Difference (%)	Polynomial (9th order)	Difference (%)	Polynomial (10th order)	Difference (%)
0.0001	0.045135	0.092393	0.223	0.053815	0.008	0.045100	0.000	0.044017	0.000	0.043870	0.000	0.044607	0.000	0.045044	0.000	0.044948	0.000	0.044965	0.000
0.0002	0.112838	0.129267	0.027	0.115054	0.000	0.115513	0.001	0.116140	0.001	0.116318	0.001	0.114883	0.000	0.113664	0.000	0.114021	0.000	0.113940	0.000
0.0003	0.174899	0.162875	0.014	0.166259	0.007	0.171305	0.001	0.172312	0.001	0.172454	0.001	0.172105	0.001	0.172450	0.001	0.172153	0.001	0.172268	0.001
0.0004	0.214392	0.193218	0.045	0.208227	0.004	0.214532	0.000	0.215215	0.000	0.215215	0.000	0.216015	0.000	0.216977	0.001	0.216743	0.001	0.216748	0.001
0.0005	0.248243	0.220295	0.078	0.241754	0.004	0.247092	0.000	0.247197	0.000	0.247083	0.000	0.248099	0.000	0.248471	0.000	0.248615	0.000	0.248525	0.000
0.0006	0.270811	0.244107	0.071	0.267637	0.001	0.270726	0.000	0.270295	0.000	0.270149	0.000	0.270590	0.000	0.270101	0.000	0.270395	0.000	0.270356	0.000
0.0007	0.287737	0.264654	0.053	0.286670	0.000	0.287017	0.000	0.286261	0.000	0.286159	0.000	0.285793	0.000	0.284955	0.001	0.285068	0.001	0.285125	0.001
0.0008	0.293379	0.281935	0.013	0.299652	0.004	0.297390	0.002	0.296584	0.001	0.296570	0.001	0.295683	0.001	0.295186	0.000	0.295020	0.000	0.295098	0.000
0.0009	0.299020	0.295951	0.001	0.307377	0.007	0.303114	0.002	0.302513	0.001	0.302588	0.001	0.301725	0.001	0.301924	0.001	0.301649	0.001	0.301657	0.001
0.001	0.307483	0.306702	0.000	0.310643	0.001	0.305301	0.000	0.305080	0.001	0.305210	0.001	0.304858	0.001	0.305587	0.000	0.305457	0.000	0.305388	0.000
0.0011	0.307483	0.314187	0.004	0.310245	0.001	0.304903	0.001	0.305125	0.001	0.305255	0.000	0.305606	0.000	0.306335	0.000	0.306465	0.000	0.306396	0.000
0.0012	0.304662	0.318406	0.019	0.306980	0.001	0.302717	0.000	0.303319	0.000	0.303394	0.000	0.304256	0.000	0.304455	0.000	0.304730	0.000	0.304738	0.000
0.0013	0.299020	0.319361	0.041	0.301644	0.001	0.299382	0.000	0.300188	0.000	0.300173	0.000	0.301059	0.000	0.300562	0.000	0.300729	0.000	0.300807	0.000
0.0014	0.296200	0.317050	0.043	0.295033	0.000	0.295379	0.000	0.296135	0.000	0.296032	0.000	0.296399	0.000	0.295561	0.000	0.295448	0.000	0.295506	0.000
0.0015	0.290558	0.311473	0.044	0.287944	0.001	0.291033	0.000	0.291464	0.000	0.291318	0.000	0.290877	0.000	0.290388	0.000	0.290093	0.000	0.290054	0.000
0.0016	0.284916	0.302631	0.031	0.281172	0.001	0.286510	0.000	0.286405	0.000	0.286292	0.000	0.285276	0.000	0.285647	0.000	0.285502	0.000	0.285412	0.000
0.0017	0.282095	0.290524	0.007	0.275515	0.004	0.281819	0.000	0.281136	0.000	0.281135	0.000	0.280335	0.000	0.281296	0.000	0.281531	0.000	0.281536	0.000
0.0018	0.276453	0.275151	0.000	0.271767	0.002	0.276812	0.000	0.275805	0.000	0.275946	0.000	0.276295	0.000	0.276640	0.000	0.276937	0.000	0.277051	0.000
0.0019	0.270811	0.256513	0.020	0.270726	0.000	0.271185	0.000	0.270557	0.000	0.270735	0.000	0.272170	0.000	0.270951	0.000	0.270594	0.000	0.270514	0.000
0.002	0.265169	0.234610	0.093	0.273188	0.006	0.264473	0.000	0.265557	0.000	0.265410	0.000	0.264673	0.000	0.265110	0.000	0.265206	0.000	0.265223	0.000

Difference 0.831 0.054 0.007 0.006 0.006 0.005 0.004 0.004 0.004

Note the sign convention of $Y_{II \text{ friction}}$.

APPENDIX W

ANALYTICAL MODEL: K_I AND K_{II}

W.1 $\sigma_a = 70$ MPa unpeened

a (m)	$K_{\geq 0}$ (MPa \sqrt{m})					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0.000	0.000	0.000	0.000	0.000	0.000
0.000052	0.323	0.481	0.523	0.411	0.890	0.411
0.0000572	0.488	0.724	0.770	0.576	1.299	0.537
0.0000624	0.694	0.998	1.044	0.774	1.711	0.694
0.0000676	0.923	1.284	1.326	0.987	2.108	0.863
0.0000728	1.152	1.559	1.594	1.191	2.463	1.021
0.000078	1.370	1.812	1.836	1.375	2.767	1.158
0.0000832	1.576	2.045	2.054	1.541	3.026	1.274
0.0000884	1.775	2.263	2.256	1.695	3.251	1.378
0.0000936	1.971	2.473	2.448	1.844	3.456	1.479
0.0000988	2.168	2.681	2.638	1.995	3.651	1.582
0.000104	2.367	2.888	2.828	2.149	3.840	1.692
0.000156	2.568	3.095	3.018	2.307	4.026	1.808
0.000208	2.768	3.299	3.207	2.466	4.207	1.928
0.00026	2.967	3.499	3.392	2.626	4.381	2.051
0.000312	3.162	3.694	3.572	2.783	4.546	2.175
0.000364	3.353	3.883	3.747	2.938	4.703	2.299
0.000416	3.542	4.068	3.919	3.093	4.853	2.426
0.000468	3.729	4.250	4.089	3.250	5.001	2.557
0.00052	3.918	4.433	4.260	3.411	5.149	2.696
0.000572	4.110	4.618	4.435	3.578	5.301	2.844
0.000624	4.305	4.807	4.616	3.752	5.460	3.002
0.000676	4.505	5.000	4.801	3.933	5.626	3.170
0.000728	4.707	5.197	4.991	4.119	5.796	3.344
0.00078	4.910	5.393	5.181	4.307	5.968	3.521
0.000832	5.112	5.589	5.371	4.494	6.138	3.698
0.000884	5.311	5.781	5.557	4.678	6.305	3.872
0.000936	5.507	5.970	5.740	4.858	6.467	4.042
0.000988	5.701	6.158	5.921	5.038	6.627	4.211
0.00104	5.897	6.346	6.104	5.219	6.790	4.384
0.001092	6.097	6.540	6.293	5.408	6.962	4.565
0.001144	6.304	6.742	6.491	5.606	7.147	4.759
0.001196	6.517	6.952	6.699	5.815	7.345	4.964
0.001248	6.731	7.163	6.908	6.025	7.548	5.174
0.0013	6.934	7.363	7.107	6.224	7.738	5.370
0.001352	7.114	7.537	7.277	6.394	7.893	5.534
0.001404	7.261	7.675	7.407	6.523	7.998	5.651
0.001456	7.390	7.794	7.516	6.630	8.075	5.743
0.001508	7.574	7.971	7.690	6.806	8.232	5.915
0.00156	7.993	8.409	8.152	7.281	8.755	6.432

a (m)	ΔK_{II} (MPa√m)					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0.000	0.000	0.000	0.000	0.000	0.000
0.000052	-0.144	-0.150	-0.153	-0.151	-0.169	-0.154
0.0000572	-0.249	-0.287	-0.305	-0.291	-0.400	-0.310
0.0000624	-0.362	-0.443	-0.482	-0.452	-0.687	-0.492
0.0000676	-0.482	-0.614	-0.678	-0.628	-1.011	-0.694
0.0000728	-0.607	-0.794	-0.884	-0.815	-1.355	-0.908
0.000078	-0.737	-0.979	-1.096	-1.006	-1.707	-1.127
0.0000832	-0.868	-1.165	-1.308	-1.198	-2.058	-1.346
0.0000884	-1.001	-1.350	-1.519	-1.389	-2.400	-1.563
0.0000936	-1.133	-1.532	-1.724	-1.576	-2.730	-1.775
0.0000988	-1.264	-1.709	-1.924	-1.758	-3.046	-1.980
0.000104	-1.394	-1.882	-2.117	-1.936	-3.347	-2.179
0.000156	-1.521	-2.049	-2.303	-2.107	-3.634	-2.370
0.000208	-1.647	-2.211	-2.483	-2.273	-3.907	-2.555
0.00026	-1.769	-2.368	-2.657	-2.434	-4.167	-2.733
0.000312	-1.890	-2.520	-2.824	-2.590	-4.415	-2.904
0.000364	-2.008	-2.668	-2.986	-2.741	-4.652	-3.070
0.000416	-2.123	-2.812	-3.143	-2.888	-4.879	-3.231
0.000468	-2.237	-2.951	-3.295	-3.030	-5.096	-3.386
0.00052	-2.348	-3.086	-3.442	-3.168	-5.303	-3.535
0.000572	-2.457	-3.217	-3.583	-3.301	-5.499	-3.680
0.000624	-2.565	-3.344	-3.719	-3.430	-5.685	-3.818
0.000676	-2.670	-3.467	-3.851	-3.555	-5.860	-3.952
0.000728	-2.775	-3.587	-3.978	-3.676	-6.024	-4.081
0.00078	-2.879	-3.703	-4.100	-3.794	-6.179	-4.205
0.000832	-2.983	-3.818	-4.220	-3.910	-6.325	-4.326
0.000884	-3.087	-3.931	-4.337	-4.024	-6.465	-4.445
0.000936	-3.192	-4.044	-4.454	-4.138	-6.602	-4.562
0.000988	-3.299	-4.157	-4.571	-4.252	-6.737	-4.680
0.00104	-3.407	-4.272	-4.690	-4.368	-6.873	-4.800
0.001092	-3.517	-4.390	-4.811	-4.487	-7.012	-4.922
0.001144	-3.630	-4.510	-4.935	-4.608	-7.155	-5.047
0.001196	-3.745	-4.633	-5.061	-4.731	-7.301	-5.174
0.001248	-3.861	-4.757	-5.188	-4.856	-7.447	-5.302
0.0013	-3.978	-4.880	-5.314	-4.980	-7.589	-5.429
0.001352	-4.094	-5.000	-5.437	-5.101	-7.722	-5.552
0.001404	-4.209	-5.117	-5.554	-5.217	-7.843	-5.669
0.001456	-4.322	-5.229	-5.666	-5.329	-7.955	-5.781
0.001508	-4.432	-5.341	-5.779	-5.442	-8.073	-5.895
0.00156	-4.544	-5.465	-5.909	-5.567	-8.234	-6.026

W.2 $\sigma_a = 100 \text{ MPa}$ unpeened

a (m)	$K_{I \geq 0}$ (MPa√m)					
	($\sigma_n=10 \text{ MPa}$)	($\sigma_n=20 \text{ MPa}$)	($\sigma_n=40 \text{ MPa}$)	($\sigma_n=60 \text{ MPa}$)	($\sigma_n=80 \text{ MPa}$)	($\sigma_n=100 \text{ MPa}$)
0	0.000	0.000	0.000	0.000	0.000	0.000
0.000052	0.474	0.529	0.641	0.581	0.563	0.636
0.0000572	0.721	0.797	0.951	0.839	0.791	0.884
0.0000624	1.027	1.119	1.308	1.146	1.068	1.176
0.0000676	1.364	1.469	1.684	1.475	1.368	1.485
0.0000728	1.700	1.814	2.047	1.793	1.657	1.778
0.000078	2.021	2.139	2.382	2.086	1.920	2.038
0.0000832	2.324	2.443	2.689	2.353	2.158	2.270
0.0000884	2.616	2.734	2.977	2.604	2.380	2.482
0.0000936	2.903	3.018	3.255	2.848	2.597	2.686
0.0000988	3.191	3.302	3.532	3.093	2.815	2.891
0.000104	3.482	3.588	3.809	3.341	3.039	3.101
0.000156	3.775	3.876	4.088	3.592	3.268	3.317
0.000208	4.067	4.163	4.365	3.845	3.499	3.535
0.00026	4.355	4.446	4.638	4.095	3.730	3.752
0.000312	4.638	4.724	4.904	4.341	3.959	3.968
0.000364	4.915	4.995	5.164	4.583	4.185	4.180
0.000416	5.188	5.262	5.418	4.823	4.409	4.393
0.000416	5.459	5.526	5.671	5.063	4.637	4.608
0.00052	5.730	5.792	5.926	5.306	4.869	4.829
0.000572	6.006	6.063	6.186	5.557	5.111	5.060
0.000624	6.287	6.339	6.452	5.816	5.362	5.303
0.000676	6.573	6.620	6.725	6.084	5.623	5.556
0.000728	6.863	6.906	7.003	6.357	5.891	5.816
0.00078	7.154	7.193	7.282	6.632	6.161	6.080
0.000832	7.443	7.479	7.559	6.906	6.431	6.342
0.000884	7.728	7.760	7.832	7.176	6.696	6.600
0.000936	8.009	8.037	8.101	7.441	6.956	6.853
0.000988	8.287	8.311	8.367	7.703	7.214	7.104
0.00104	8.567	8.587	8.635	7.969	7.475	7.359
0.001092	8.854	8.870	8.911	8.243	7.746	7.624
0.001144	9.149	9.163	9.200	8.530	8.032	7.905
0.001196	9.454	9.466	9.499	8.829	8.330	8.201
0.001248	9.759	9.770	9.801	9.131	8.631	8.501
0.0013	10.050	10.060	10.087	9.417	8.917	8.783
0.001352	10.307	10.313	10.335	9.664	9.160	9.022
0.001404	10.517	10.519	10.531	9.856	9.347	9.200
0.001456	10.704	10.699	10.698	10.018	9.503	9.346
0.001508	10.966	10.959	10.952	10.272	9.756	9.593
0.00156	11.561	11.567	11.587	10.925	10.428	10.291

a (m)	ΔK_{II} (MPa \sqrt{m})					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0.000	0.000	0.000	0.000	0.000	0.000
0.000052	-0.206	-0.208	-0.214	-0.213	-0.214	-0.218
0.0000572	-0.357	-0.373	-0.406	-0.402	-0.408	-0.432
0.0000624	-0.518	-0.553	-0.624	-0.617	-0.629	-0.682
0.0000676	-0.691	-0.747	-0.862	-0.851	-0.871	-0.957
0.0000728	-0.871	-0.951	-1.113	-1.098	-1.126	-1.247
0.000078	-1.057	-1.161	-1.371	-1.352	-1.388	-1.545
0.0000832	-1.246	-1.373	-1.631	-1.607	-1.651	-1.844
0.0000884	-1.436	-1.586	-1.889	-1.861	-1.913	-2.140
0.0000936	-1.626	-1.797	-2.143	-2.111	-2.170	-2.429
0.0000988	-1.814	-2.005	-2.391	-2.355	-2.421	-2.710
0.000104	-2.000	-2.209	-2.633	-2.593	-2.666	-2.982
0.000156	-2.183	-2.409	-2.867	-2.824	-2.903	-3.245
0.000208	-2.362	-2.604	-3.095	-3.049	-3.133	-3.499
0.00026	-2.538	-2.795	-3.315	-3.266	-3.355	-3.744
0.000312	-2.711	-2.981	-3.529	-3.478	-3.572	-3.981
0.000364	-2.880	-3.163	-3.737	-3.683	-3.781	-4.210
0.000416	-3.046	-3.341	-3.939	-3.883	-3.985	-4.432
0.000416	-3.208	-3.514	-4.135	-4.076	-4.183	-4.647
0.00052	-3.367	-3.684	-4.325	-4.265	-4.375	-4.854
0.000572	-3.524	-3.849	-4.509	-4.448	-4.561	-5.054
0.000624	-3.678	-4.012	-4.689	-4.625	-4.741	-5.247
0.000676	-3.829	-4.171	-4.863	-4.798	-4.916	-5.433
0.000728	-3.979	-4.327	-5.032	-4.966	-5.086	-5.613
0.00078	-4.128	-4.481	-5.197	-5.130	-5.253	-5.788
0.000832	-4.277	-4.634	-5.359	-5.291	-5.416	-5.958
0.000884	-4.425	-4.787	-5.520	-5.451	-5.577	-6.125
0.000936	-4.576	-4.941	-5.680	-5.611	-5.738	-6.291
0.000988	-4.728	-5.096	-5.842	-5.772	-5.899	-6.457
0.00104	-4.882	-5.253	-6.005	-5.935	-6.064	-6.626
0.001092	-5.040	-5.414	-6.173	-6.102	-6.231	-6.798
0.001144	-5.202	-5.579	-6.344	-6.272	-6.403	-6.975
0.001196	-5.366	-5.746	-6.518	-6.446	-6.578	-7.155
0.001248	-5.532	-5.916	-6.694	-6.621	-6.754	-7.336
0.0013	-5.699	-6.086	-6.869	-6.796	-6.930	-7.515
0.001352	-5.866	-6.254	-7.041	-6.967	-7.102	-7.690
0.001404	-6.029	-6.418	-7.207	-7.133	-7.268	-7.857
0.001456	-6.190	-6.579	-7.367	-7.293	-7.428	-8.017
0.001508	-6.348	-6.738	-7.527	-7.453	-7.589	-8.179
0.00156	-6.507	-6.902	-7.703	-7.628	-7.765	-8.364

W.3 $\sigma_a = 125$ MPa unpeened

a (m)	$K_{I \geq 0}$ (MPa \sqrt{m})					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0.000	0.000	0.000	0.000	0.000	0.000
0.000052	0.670	0.689	0.888	0.920	0.828	0.993
0.0000572	1.025	1.044	1.334	1.364	1.201	1.438
0.0000624	1.449	1.467	1.833	1.859	1.628	1.926
0.0000676	1.906	1.921	2.352	2.370	2.078	2.425
0.0000728	2.358	2.368	2.848	2.855	2.507	2.891
0.000078	2.785	2.789	3.305	3.297	2.897	3.307
0.0000832	3.187	3.183	3.723	3.698	3.250	3.676
0.0000884	3.570	3.557	4.112	4.070	3.578	4.012
0.0000936	3.946	3.924	4.487	4.425	3.893	4.331
0.0000988	4.320	4.288	4.857	4.776	4.207	4.645
0.000104	4.696	4.655	5.226	5.126	4.524	4.959
0.000156	5.072	5.023	5.593	5.476	4.844	5.275
0.000208	5.446	5.389	5.957	5.823	5.163	5.589
0.00026	5.814	5.750	6.312	6.163	5.478	5.897
0.000312	6.174	6.102	6.658	6.494	5.787	6.198
0.000364	6.526	6.446	6.994	6.815	6.089	6.490
0.000416	6.870	6.784	7.321	7.128	6.387	6.777
0.000416	7.210	7.118	7.644	7.439	6.685	7.063
0.00052	7.551	7.453	7.968	7.751	6.986	7.353
0.000572	7.896	7.793	8.296	8.070	7.296	7.652
0.000624	8.246	8.139	8.631	8.397	7.617	7.962
0.000676	8.604	8.493	8.974	8.733	7.947	8.283
0.000728	8.965	8.851	9.323	9.074	8.285	8.612
0.00078	9.328	9.211	9.673	9.418	8.626	8.943
0.000832	9.688	9.568	10.020	9.760	8.964	9.273
0.000884	10.043	9.920	10.362	10.096	9.298	9.597
0.000936	10.392	10.266	10.697	10.425	9.625	9.914
0.000988	10.739	10.610	11.030	10.752	9.949	10.228
0.00104	11.087	10.955	11.365	11.081	10.276	10.546
0.001092	11.443	11.309	11.710	11.421	10.616	10.877
0.001144	11.812	11.676	12.069	11.778	10.972	11.227
0.001196	12.191	12.054	12.443	12.149	11.343	11.594
0.001248	12.572	12.434	12.819	12.524	11.719	11.967
0.0013	12.934	12.795	13.176	12.880	12.075	12.319
0.001352	13.253	13.113	13.485	13.185	12.380	12.617
0.001404	13.514	13.370	13.729	13.422	12.614	12.839
0.001456	13.744	13.595	13.938	13.622	12.811	13.020
0.001508	14.070	13.920	14.253	13.934	13.124	13.326
0.00156	14.816	14.677	15.042	14.745	13.951	14.182

a (m)	ΔK_{II} (MPa \sqrt{m})					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0.000	0.000	0.000	0.000	0.000	0.000
0.000052	-0.260	-0.261	-0.269	-0.272	-0.270	-0.277
0.0000572	-0.461	-0.470	-0.520	-0.536	-0.526	-0.570
0.0000624	-0.681	-0.699	-0.809	-0.843	-0.822	-0.916
0.0000676	-0.916	-0.946	-1.125	-1.181	-1.146	-1.300
0.0000728	-1.164	-1.206	-1.458	-1.538	-1.489	-1.706
0.000078	-1.418	-1.473	-1.801	-1.904	-1.840	-2.122
0.0000832	-1.677	-1.744	-2.145	-2.272	-2.193	-2.539
0.0000884	-1.935	-2.015	-2.486	-2.636	-2.543	-2.950
0.0000936	-2.193	-2.283	-2.821	-2.992	-2.886	-3.350
0.0000988	-2.446	-2.547	-3.148	-3.338	-3.220	-3.738
0.000104	-2.696	-2.806	-3.465	-3.674	-3.544	-4.112
0.000156	-2.941	-3.060	-3.772	-3.998	-3.858	-4.472
0.000208	-3.180	-3.308	-4.070	-4.311	-4.161	-4.818
0.00026	-3.414	-3.550	-4.358	-4.613	-4.455	-5.151
0.000312	-3.642	-3.785	-4.636	-4.906	-4.739	-5.472
0.000364	-3.866	-4.015	-4.907	-5.189	-5.014	-5.782
0.000416	-4.084	-4.240	-5.169	-5.463	-5.281	-6.081
0.000416	-4.297	-4.459	-5.423	-5.728	-5.539	-6.370
0.00052	-4.506	-4.673	-5.669	-5.985	-5.789	-6.648
0.000572	-4.710	-4.882	-5.908	-6.233	-6.031	-6.915
0.000624	-4.910	-5.087	-6.139	-6.472	-6.265	-7.172
0.000676	-5.107	-5.287	-6.362	-6.703	-6.491	-7.418
0.000728	-5.300	-5.484	-6.579	-6.926	-6.711	-7.655
0.00078	-5.492	-5.678	-6.790	-7.143	-6.924	-7.883
0.000832	-5.681	-5.871	-6.997	-7.354	-7.132	-8.104
0.000884	-5.871	-6.062	-7.201	-7.562	-7.338	-8.319
0.000936	-6.062	-6.255	-7.404	-7.768	-7.542	-8.533
0.000988	-6.255	-6.449	-7.608	-7.975	-7.748	-8.747
0.00104	-6.451	-6.647	-7.816	-8.186	-7.956	-8.963
0.001092	-6.652	-6.849	-8.027	-8.400	-8.169	-9.184
0.001144	-6.856	-7.056	-8.244	-8.620	-8.387	-9.411
0.001196	-7.064	-7.266	-8.464	-8.844	-8.608	-9.642
0.001248	-7.275	-7.478	-8.687	-9.070	-8.832	-9.874
0.0013	-7.487	-7.691	-8.908	-9.294	-9.054	-10.103
0.001352	-7.696	-7.902	-9.124	-9.511	-9.271	-10.325
0.001404	-7.902	-8.107	-9.332	-9.720	-9.479	-10.535
0.001456	-8.102	-8.308	-9.533	-9.920	-9.680	-10.735
0.001508	-8.301	-8.507	-9.734	-10.122	-9.881	-10.939
0.00156	-8.505	-8.714	-9.958	-10.352	-10.107	-11.179

APPENDIX X

ANALYTICAL MODEL: da/dN

X.1 $\sigma_a = 70$ MPa unpeened

a (m)	$\frac{da}{dN}$					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0	0	0	0	0	0
0.000052	6.111E-12	1.939E-11	2.505E-11	1.229E-11	1.303E-10	1.242E-11
0.0000572	2.544E-11	7.979E-11	9.743E-11	4.337E-11	4.882E-10	3.810E-11
0.0000624	8.130E-11	2.394E-10	2.832E-10	1.261E-10	1.315E-09	1.064E-10
0.0000676	2.053E-10	5.666E-10	6.567E-10	2.998E-10	2.844E-09	2.511E-10
0.0000728	4.244E-10	1.108E-09	1.266E-09	5.923E-10	5.180E-09	4.966E-10
0.000078	7.563E-10	1.885E-09	2.127E-09	1.017E-09	8.310E-09	8.556E-10
0.0000832	1.215E-09	2.908E-09	3.248E-09	1.582E-09	1.220E-08	1.337E-09
0.0000884	1.819E-09	4.198E-09	4.647E-09	2.304E-09	1.684E-08	1.957E-09
0.0000936	2.597E-09	5.789E-09	6.358E-09	3.208E-09	2.228E-08	2.735E-09
0.0000988	3.580E-09	7.725E-09	8.422E-09	4.323E-09	2.857E-08	3.699E-09
0.000104	4.802E-09	1.004E-08	1.088E-08	5.680E-09	3.575E-08	4.870E-09
0.000156	6.289E-09	1.277E-08	1.375E-08	7.299E-09	4.382E-08	6.266E-09
0.000208	8.058E-09	1.592E-08	1.704E-08	9.193E-09	5.273E-08	7.896E-09
0.00026	1.012E-08	1.947E-08	2.074E-08	1.136E-08	6.238E-08	9.762E-09
0.000312	1.247E-08	2.341E-08	2.483E-08	1.381E-08	7.268E-08	1.187E-08
0.000364	1.511E-08	2.774E-08	2.930E-08	1.654E-08	8.357E-08	1.422E-08
0.000416	1.807E-08	3.246E-08	3.416E-08	1.957E-08	9.504E-08	1.683E-08
0.000468	2.138E-08	3.761E-08	3.945E-08	2.292E-08	1.071E-07	1.973E-08
0.00052	2.508E-08	4.324E-08	4.523E-08	2.666E-08	1.199E-07	2.297E-08
0.000572	2.923E-08	4.943E-08	5.155E-08	3.084E-08	1.334E-07	2.658E-08
0.000624	3.389E-08	5.623E-08	5.850E-08	3.550E-08	1.477E-07	3.062E-08
0.000676	3.910E-08	6.369E-08	6.610E-08	4.070E-08	1.629E-07	3.511E-08
0.000728	4.489E-08	7.183E-08	7.436E-08	4.643E-08	1.788E-07	4.006E-08
0.00078	5.127E-08	8.062E-08	8.325E-08	5.268E-08	1.954E-07	4.545E-08
0.000832	5.820E-08	9.003E-08	9.273E-08	5.943E-08	2.124E-07	5.125E-08
0.000884	6.569E-08	1.000E-07	1.027E-07	6.665E-08	2.298E-07	5.744E-08
0.000936	7.373E-08	1.106E-07	1.133E-07	7.435E-08	2.477E-07	6.405E-08
0.000988	8.240E-08	1.219E-07	1.246E-07	8.263E-08	2.663E-07	7.115E-08
0.00104	9.184E-08	1.340E-07	1.367E-07	9.166E-08	2.862E-07	7.894E-08
0.001092	1.022E-07	1.474E-07	1.501E-07	1.017E-07	3.079E-07	8.764E-08
0.001144	1.138E-07	1.622E-07	1.649E-07	1.129E-07	3.320E-07	9.748E-08
0.001196	1.266E-07	1.784E-07	1.813E-07	1.255E-07	3.587E-07	1.086E-07
0.001248	1.404E-07	1.960E-07	1.990E-07	1.391E-07	3.872E-07	1.207E-07
0.0013	1.546E-07	2.139E-07	2.171E-07	1.532E-07	4.158E-07	1.332E-07
0.001352	1.685E-07	2.310E-07	2.342E-07	1.666E-07	4.418E-07	1.451E-07
0.001404	1.811E-07	2.462E-07	2.492E-07	1.783E-07	4.629E-07	1.553E-07
0.001456	1.932E-07	2.604E-07	2.629E-07	1.892E-07	4.810E-07	1.646E-07
0.001508	2.094E-07	2.799E-07	2.822E-07	2.046E-07	5.084E-07	1.782E-07
0.00156	2.436E-07	3.231E-07	3.272E-07	2.412E-07	5.818E-07	2.124E-07

X.2 $\sigma_a = 100$ MPa unpeened

a (m)	$\frac{da}{dN}$					
	($\sigma_n=10$ MPa)	($\sigma_n=20$ MPa)	($\sigma_n=40$ MPa)	($\sigma_n=60$ MPa)	($\sigma_n=80$ MPa)	($\sigma_n=100$ MPa)
0	0	0	0	0	0	0
0.000052	2.100E-11	2.867E-11	5.031E-11	3.788E-11	3.469E-11	4.949E-11
0.0000572	8.870E-11	1.186E-10	2.006E-10	1.424E-10	1.234E-10	1.710E-10
0.0000624	2.838E-10	3.703E-10	6.010E-10	4.235E-10	3.619E-10	4.882E-10
0.0000676	7.150E-10	9.130E-10	1.430E-09	1.015E-09	8.661E-10	1.144E-09
0.0000728	1.475E-09	1.850E-09	2.814E-09	2.014E-09	1.721E-09	2.237E-09
0.000078	2.623E-09	3.240E-09	4.812E-09	3.469E-09	2.968E-09	3.809E-09
0.0000832	4.205E-09	5.127E-09	7.457E-09	5.411E-09	4.637E-09	5.887E-09
0.0000884	6.286E-09	7.575E-09	1.081E-08	7.893E-09	6.776E-09	8.520E-09
0.0000936	8.955E-09	1.068E-08	1.497E-08	1.100E-08	9.463E-09	1.179E-08
0.0000988	1.232E-08	1.455E-08	2.007E-08	1.485E-08	1.279E-08	1.580E-08
0.000104	1.650E-08	1.929E-08	2.622E-08	1.952E-08	1.686E-08	2.065E-08
0.000156	2.156E-08	2.501E-08	3.350E-08	2.511E-08	2.173E-08	2.640E-08
0.000208	2.757E-08	3.173E-08	4.194E-08	3.165E-08	2.745E-08	3.307E-08
0.00026	3.455E-08	3.947E-08	5.153E-08	3.914E-08	3.403E-08	4.068E-08
0.000312	4.249E-08	4.823E-08	6.224E-08	4.758E-08	4.146E-08	4.921E-08
0.000364	5.142E-08	5.801E-08	7.407E-08	5.698E-08	4.976E-08	5.867E-08
0.000416	6.138E-08	6.886E-08	8.705E-08	6.739E-08	5.900E-08	6.912E-08
0.000468	7.247E-08	8.089E-08	1.013E-07	7.892E-08	6.928E-08	8.067E-08
0.00052	8.486E-08	9.425E-08	1.170E-07	9.174E-08	8.075E-08	9.346E-08
0.000572	9.872E-08	1.091E-07	1.343E-07	1.060E-07	9.359E-08	1.077E-07
0.000624	1.142E-07	1.257E-07	1.535E-07	1.220E-07	1.080E-07	1.235E-07
0.000676	1.316E-07	1.442E-07	1.746E-07	1.397E-07	1.240E-07	1.410E-07
0.000728	1.508E-07	1.646E-07	1.978E-07	1.592E-07	1.417E-07	1.603E-07
0.00078	1.719E-07	1.870E-07	2.229E-07	1.805E-07	1.611E-07	1.812E-07
0.000832	1.949E-07	2.111E-07	2.499E-07	2.036E-07	1.821E-07	2.037E-07
0.000884	2.196E-07	2.371E-07	2.786E-07	2.282E-07	2.046E-07	2.276E-07
0.000936	2.462E-07	2.648E-07	3.092E-07	2.545E-07	2.287E-07	2.530E-07
0.000988	2.748E-07	2.947E-07	3.418E-07	2.828E-07	2.545E-07	2.803E-07
0.00104	3.058E-07	3.271E-07	3.772E-07	3.135E-07	2.827E-07	3.100E-07
0.001092	3.400E-07	3.627E-07	4.161E-07	3.474E-07	3.141E-07	3.430E-07
0.001144	3.780E-07	4.022E-07	4.593E-07	3.854E-07	3.492E-07	3.800E-07
0.001196	4.198E-07	4.459E-07	5.070E-07	4.276E-07	3.885E-07	4.214E-07
0.001248	4.651E-07	4.931E-07	5.586E-07	4.733E-07	4.312E-07	4.664E-07
0.0013	5.118E-07	5.417E-07	6.115E-07	5.204E-07	4.752E-07	5.127E-07
0.001352	5.571E-07	5.886E-07	6.620E-07	5.654E-07	5.172E-07	5.565E-07
0.001404	5.984E-07	6.310E-07	7.069E-07	6.053E-07	5.542E-07	5.945E-07
0.001456	6.380E-07	6.714E-07	7.489E-07	6.426E-07	5.886E-07	6.295E-07
0.001508	6.909E-07	7.257E-07	8.066E-07	6.945E-07	6.372E-07	6.796E-07
0.00156	8.022E-07	8.428E-07	9.365E-07	8.135E-07	7.512E-07	8.010E-07

X.3 $\sigma_a = 125 \text{ MPa}$ unpeened

a (m)	$\frac{da}{dN}$					
	($\sigma_n=10 \text{ MPa}$)	($\sigma_n=20 \text{ MPa}$)	($\sigma_n=40 \text{ MPa}$)	($\sigma_n=60 \text{ MPa}$)	($\sigma_n=80 \text{ MPa}$)	($\sigma_n=100 \text{ MPa}$)
0	0	0	0	0	0	0
0.000052	6.156E-11	6.666E-11	1.412E-10	1.575E-10	1.147E-10	1.989E-10
0.0000572	2.633E-10	2.794E-10	5.777E-10	6.240E-10	4.338E-10	7.428E-10
0.0000624	8.306E-10	8.714E-10	1.722E-09	1.829E-09	1.269E-09	2.110E-09
0.0000676	2.054E-09	2.139E-09	4.051E-09	4.262E-09	2.984E-09	4.828E-09
0.0000728	4.168E-09	4.314E-09	7.888E-09	8.240E-09	5.827E-09	9.218E-09
0.000078	7.309E-09	7.528E-09	1.336E-08	1.388E-08	9.901E-09	1.538E-08
0.0000832	1.158E-08	1.187E-08	2.055E-08	2.124E-08	1.526E-08	2.333E-08
0.0000884	1.712E-08	1.749E-08	2.958E-08	3.044E-08	2.203E-08	3.320E-08
0.0000936	2.413E-08	2.458E-08	4.067E-08	4.171E-08	3.040E-08	4.520E-08
0.0000988	3.287E-08	3.338E-08	5.413E-08	5.533E-08	4.061E-08	5.961E-08
0.000104	4.358E-08	4.414E-08	7.021E-08	7.155E-08	5.290E-08	7.667E-08
0.000156	5.644E-08	5.704E-08	8.907E-08	9.053E-08	6.742E-08	9.653E-08
0.000208	7.155E-08	7.217E-08	1.107E-07	1.123E-07	8.422E-08	1.192E-07
0.00026	8.891E-08	8.953E-08	1.352E-07	1.368E-07	1.033E-07	1.446E-07
0.000312	1.085E-07	1.091E-07	1.623E-07	1.639E-07	1.246E-07	1.725E-07
0.000364	1.303E-07	1.309E-07	1.919E-07	1.935E-07	1.481E-07	2.030E-07
0.000416	1.545E-07	1.550E-07	2.242E-07	2.257E-07	1.738E-07	2.361E-07
0.000416	1.812E-07	1.816E-07	2.593E-07	2.608E-07	2.021E-07	2.720E-07
0.00052	2.107E-07	2.110E-07	2.977E-07	2.991E-07	2.333E-07	3.111E-07
0.000572	2.436E-07	2.438E-07	3.397E-07	3.410E-07	2.678E-07	3.539E-07
0.000624	2.801E-07	2.802E-07	3.859E-07	3.870E-07	3.060E-07	4.007E-07
0.000676	3.206E-07	3.205E-07	4.364E-07	4.374E-07	3.481E-07	4.519E-07
0.000728	3.653E-07	3.650E-07	4.915E-07	4.922E-07	3.942E-07	5.073E-07
0.00078	4.141E-07	4.136E-07	5.509E-07	5.512E-07	4.442E-07	5.667E-07
0.000832	4.668E-07	4.660E-07	6.143E-07	6.141E-07	4.978E-07	6.297E-07
0.000884	5.234E-07	5.222E-07	6.816E-07	6.807E-07	5.549E-07	6.962E-07
0.000936	5.838E-07	5.823E-07	7.527E-07	7.511E-07	6.154E-07	7.661E-07
0.000988	6.487E-07	6.467E-07	8.285E-07	8.260E-07	6.801E-07	8.403E-07
0.00104	7.190E-07	7.166E-07	9.102E-07	9.068E-07	7.502E-07	9.205E-07
0.001092	7.961E-07	7.933E-07	9.998E-07	9.954E-07	8.276E-07	1.009E-06
0.001144	8.815E-07	8.782E-07	1.099E-06	1.094E-06	9.138E-07	1.107E-06
0.001196	9.755E-07	9.720E-07	1.208E-06	1.203E-06	1.010E-06	1.216E-06
0.001248	1.077E-06	1.073E-06	1.326E-06	1.320E-06	1.113E-06	1.334E-06
0.0013	1.181E-06	1.177E-06	1.446E-06	1.440E-06	1.220E-06	1.454E-06
0.001352	1.282E-06	1.278E-06	1.561E-06	1.553E-06	1.321E-06	1.567E-06
0.001404	1.374E-06	1.368E-06	1.662E-06	1.653E-06	1.409E-06	1.665E-06
0.001456	1.461E-06	1.455E-06	1.757E-06	1.745E-06	1.492E-06	1.753E-06
0.001508	1.578E-06	1.570E-06	1.886E-06	1.873E-06	1.607E-06	1.880E-06
0.00156	1.824E-06	1.819E-06	2.178E-06	2.168E-06	1.875E-06	2.185E-06

APPENDIX Y

ANALYTICAL MODEL: ΔN

Y.1 $\sigma_a = 70$ MPa unpeened

a (m)	ΔN ($\sigma_a=10$ MPa)				ΔN ($\sigma_a=20$ MPa)				ΔN ($\sigma_a=40$ MPa)				ΔN ($\sigma_a=60$ MPa)				ΔN ($\sigma_a=80$ MPa)				ΔN ($\sigma_a=100$ MPa)			
	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.000052	17018066	17018066			5363564	5363564			4152178	4152178			8461186	8461186			798138	798138			8375890	8375890		
0.0000572	3296217	20314282	5774899.362	5774899	1048596	6412160	1835262.495	1835262	849117	5001295	1464841.832	1464842	1868304	10329490	3146105.895	3146106	168159	966297	288234.8392	288235	2058786	10434676	3378708.395	3378708
0.0000624	974344	21288626			5774899	6737936			1835262	273254	325776	6737936	613505	10942996			57677	1023974			288235	719667	11154343	3378708
0.0000676	362932	21851558	591833.9645	6366733	129032	8866868	210406.1917	2045669	110657	5385206	180489.1407	1645331	244191	11187187	397976.9593	3544083	25006	1048980	40906.32844	329141	290937	11445280	473958.7177	3852667
0.0000728	165162	21816720			6366733	62097			2045669	54098	5439304	1645331	116586	11303773			12962	1061942			139093	11584373		
0.000078	88080	21904800	146778.5666	6513512	34745	6963810	58382.97378	30652	2104052	30652	5469956	51623.50951	84630	11368403	108402.2543	3652485	7709	1069651	13110.50345	342252	11661280	128893.9174	3981561	
0.0000832	52758	21957558			6513512	21698			2104052	19347	5489303	1698954	40012	11408416			5071	1074723			342252	47425	11708705	3981561
0.0000884	34275	21991833	59051.29492	6572563	14636	7000144	25470.63926	13172	2129522	13172	5502475	22981.62159	26759	11435175	46448.6845	3898934	3582	1078304	6316.413486	348568	31574	11740280	54735.39071	4036296
0.0000936	23551	22015384			6572563	10413			2129522	9450	5511925	1719936	18869	11454044			2659	1080963			348568	22167	11762446	4036296
0.0000988	16838	22032223	29653.31924	6602217	7696	7018253	13695.1919	7036	2143217	7036	5518961	12551.62497	13811	11467855	24494.16563	3723428	2045	1083008	3689.751187	352258	16165	11778611	28642.91954	4064939
0.000104	12408	22044631			6602217	5853			2143217	5388	5524349	1732488	10397	11478252			1617	1084625			352258	12138	11790749	4064939
0.000156	9378	22054009	16786.16312	6619003	4558	7028664	8243.22364	2151461	4223	5528572	7652.691551	1740140	8013	11486265	14435.72219	3737864	1307	1085932	2395.584561	354653	9340	11800089	16820.56806	4081760
0.000208	7249	22061258			6619003	3625			7032289	2151461	5531949	1740140	6306	11492571			1077	1087009			354653	7344	11807433	4081760
0.00026	5723	22066980	10395.70891	6629398	2939	7035228	5390.471869	2156851	2753	5534702	5058.146591	1745199	5059	11497629	9241.292109	3747105	903	1087913	1678.672818	356332	5890	11813323	10757.94108	4092518
0.000312	4606	22071586			6629398	2425			7037653	2156851	5536984	1745199	4131	11501760			770	1088663			356332	4808	11818131	4092518
0.000364	3771	22075357	6937.724593	6636336	2033	7039686	3773.472963	2160625	1921	5538906	3571.841366	1748770	3427	11505187	6332.812176	3753438	666	1089348	1250.471369	357583	3987	11822118	7367.075776	4099885
0.000416	3134	22078491			6636336	1727			7041414	2160625	5540544	1748770	2880	11508067			582	1089930			357583	3350	11825467	4099885
0.000468	2636	22081128	4893.582478	6641230	1484	7042898	2778.195107	2163403	1413	5541957	2648.119974	1751419	2448	11510515	4560.38648	3757998	514	1090445	974.3582607	358557	2845	11828312	5298.3123	4105183
0.00052	2239	22083366			6641230	1286			7044184	2163403	5543185	1751419	2097	11512612			458	1090903			358557	2436	11830747	4105183
0.000572	1915	22085282	3574.877948	6644805	1122	7045307	2111.884275	2165515	1075	5544260	2024.458893	1753443	1809	11514421	3386.477246	3761385	411	1091314	781.814898	359339	2099	11832846	3928.826708	4109112
0.000624	1648	22086929			6644805	984			7046291	2165515	5545205	1753443	1568	11515988			370	1091684			359339	1818	11834664	4109112
0.000676	1425	22088354	2670.792867	6647475	867	7047158	1638.240022	2167153	835	5546040	1578.350744	1755021	1365	11517353	2565.174621	3763950	335	1092019	639.9542272	359979	1582	11836246	2973.484826	4112086
0.000728	1238	22089592			6647475	767			7047926	2167153	5546780	1755021	1194	11518547			304	1092323			359979	1384	11837630	4112086
0.00078	1082	22090674	2036.274591	6649512	682	7048608	1293.878775	2168447	660	5547440	1252.831724	1756274	1049	11519596	1981.015875	3765931	278	1092601	533.473538	360512	1216	11838846	2296.555003	4114382
0.000832	950	22091624			6649512	609			7049217	2168447	5548031	1756274	928	11520524			255	1092856			360512	1076	11839922	4114382
0.000884	839	22092463	1588.382896	6651100	547	7049785	1042.505152	2169489	532	5548563	1014.709685	1757289	825	11521349	1565.032937	3767496	235	1093091	453.2858803	360965	957	11840879	1815.909738	4116198
0.000936	746	22093209			6651100	494			7050258	2169489	5549044	1757289	738	11522086			218	1093309			360965	856	11841735	4116198
0.000988	666	22093875	1265.191154	6652365	447	7050706	854.9168159	2170344	437	5549482	836.3114323	1758125	662	11522749	1261.315026	3768757	202	1093511	390.8612824	361356	769	11842504	1464.620159	4117663
0.00104	597	22094472			6652365	406			7051112	2170344	5549880	1758125	597	11523345			188	1093700			361356	693	11843197	4117663
0.001092	536	22095008	1019.169803	6653384	370	7051482	706.6151278	2171051	363	5550242	693.9117553	1758819	538	11523883	1024.576749	3769782	175	1093875	337.94258	361694	624	11843821	1188.520264	4118851
0.001144	481	22095490			6653384	336			7051818	2171051	5550572	1758819	485	11524368			163	1094037			361694	562	11844383	4118851
0.001196	433	22095922	823.6257769	6654208	305	7052123	583.9196939	2171635	300	5550873	574.596697	1759394	436	11524804	830.7257652	3770612	151	1094188	290.2625164	361985	505	11844888	959.9386314	4119811
0.001248	390	22096312			6654208	278			7052401	2171635	5551146	1759394	393	11525197			139	1094327			361985	454	11845341	4119811
0.0013	353	22096664	674.7200319	6654883	254	7052655	487.6313975	2172122	250	5551396	480.4413996	1759874	356	11525553	681.2581912	3771294	130	1094457	250.7322847	362235	409	11845751	783.3986956	4120594
0.001352	322	22096986			6654883	234			7052888	2172122	5551627	1759874	325	11525878			121	1094578			362235	374	11846124	4120594
0.001404	298	22097284	575.4613877	6655458	218	7053106	423.1707476	2172546	215	5551842	418.1868814	1760292	302	11526180	584.514697	3771878	115	1094693	225.057272	362460	346	11846471	671.3255622	4121266
0.001456	278	22097562			6655458	205			7053311	2172546	5552045	1760292	283	11526463			110	1094803			362460	325	11846796	4121266
0.001508	258	22097820	492.0084152	6655950	192	7053504	367.9250233	2172914	203	5552236	364.568483	1760657	264	11526727	502.3311182	3772381	105	1094908	202.207028	362663	303	11847099	576.0569223	4121842
0.00156	230	22098050			6655950	172			7053676	2172914	5552406	1760657	233	11526960			95	1095004			362663	266	11847366	4121842

Y.2 $\sigma_a = 100$ MPa unpeened

a (m)	ΔN ($\sigma_a=10$ MPa)				ΔN ($\sigma_a=20$ MPa)				ΔN ($\sigma_a=40$ MPa)				ΔN ($\sigma_a=60$ MPa)				ΔN ($\sigma_a=80$ MPa)				ΔN ($\sigma_a=100$ MPa)			
	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.000052	4,952,048	4,952,048		0	3,627,377	3,627,377		0	2,067,135	2,067,135		0	2,745,404	2,745,404		0	2,988,058	2,988,058		0	2,101,494	2,101,494		0
0.0000572	948,017	5,900,064	1,668,059	1,668,059	706,267	4,333,644	1,236,059	1,236,059	414,461	2,481,595	718,965	718,965	2,745,404	3,322,383	985,495	985,495	658,006	3,656,064	1,109,593	1,109,593	471,721	2,573,215	791,258	791,258
0.0000624	279,167	6,179,231		1,668,059	212,736	4,546,380		1,236,059	129,744	2,611,340		718,965	183,780	3,506,163		985,495	214,314	3,870,378		1,109,593	157,774	2,730,989		791,258
0.0000676	104,117	6,283,349	169,785	1,837,844	81,045	4,627,425	132,125	1,368,184	51,207	2,662,547	83,488	802,451	72,300	3,578,463	117,846	1,103,341	84,688	3,955,086	138,015	1,247,608	63,709	2,794,698	103,846	895,104
0.0000728	47,490	6,330,839		1,837,844	37,645	4,665,070		1,368,184	24,503	2,687,049		802,451	34,333	3,612,797		1,103,341	40,197	3,995,263		1,247,608	30,754	2,825,452		895,104
0.000078	25,381	6,356,220	42,311	1,880,155	20,434	4,685,504	34,152	1,402,336	13,638	2,700,687	22,893	825,344	18,968	3,631,764	31,797	1,135,138	22,177	4,017,440	37,166	1,284,774	17,199	2,842,651	28,892	923,996
0.0000832	15,232	6,371,452		1,880,155	12,430	4,697,934		1,402,336	8,477	2,709,164		825,344	11,713	3,643,477		1,135,138	13,674	4,031,115		1,284,774	10,726	2,853,377		923,996
0.0000884	9,913	6,381,365	17,087	1,897,243	8,187	4,706,121	14,157	1,416,493	5,693	2,714,857	9,895	835,239	7,817	3,651,294	13,563	1,148,701	9,112	4,040,227	15,802	1,300,578	7,219	2,860,596	12,553	936,548
0.0000936	6,824	6,388,189		1,897,243	5,698	4,711,819		1,416,493	4,033	2,718,890		835,239	5,504	3,656,798		1,148,701	6,404	4,046,632		1,300,578	5,120	2,865,716		936,548
0.0000988	4,888	6,393,077	8,613	1,905,856	4,123	4,715,943	7,288	1,423,782	2,968	2,721,858	5,273	840,512	4,024	3,660,822	7,134	1,155,835	4,673	4,051,304	8,279	1,308,855	3,769	2,869,485	6,697	943,245
0.000104	3,609	6,396,686		1,905,856	3,073	4,719,016		1,423,782	2,247	2,724,105		840,512	3,026	3,663,848		1,155,835	3,507	4,054,811		1,308,855	2,853	2,872,338		943,245
0.000156	2,733	6,399,419	4,895	1,910,751	2,348	4,721,364	4,217	1,427,999	1,742	2,725,846	3,144	843,656	2,330	3,666,178	4,197	1,160,032	2,695	4,057,506	4,849	1,313,704	2,211	2,874,549	3,990	947,235
0.000208	2,117	6,401,535		1,910,751	1,833	4,723,197		1,427,999	1,379	2,727,225		843,656	1,832	3,668,010		1,160,032	2,114	4,059,620		1,313,704	1,749	2,876,298		947,235
0.00026	1,674	6,403,210	3,044	1,913,794	1,461	4,724,658	2,662	1,430,661	1,113	2,728,338	2,037	845,694	1,469	3,669,480	2,684	1,162,715	1,692	4,061,312	3,087	1,316,791	1,410	2,877,708	2,581	949,816
0.000312	1,350	6,404,560		1,913,794	1,186	4,725,843		1,430,661	914	2,729,252		845,694	1,199	3,670,679		1,162,715	1,378	4,062,689		1,316,791	1,157	2,878,865		949,816
0.000364	1,107	6,405,667	2,039	1,915,833	979	4,726,822	1,806	1,432,468	763	2,730,015	1,414	847,108	995	3,671,674	1,838	1,164,554	1,140	4,063,829	2,105	1,318,897	964	2,879,829	1,785	951,600
0.000416	922	6,406,589		1,915,833	820	4,727,642		1,432,468	646	2,730,660		847,108	836	3,672,510		1,164,554	956	4,064,786		1,318,897	814	2,880,643		951,600
0.000468	777	6,407,366	1,443	1,917,277	694	4,728,337	1,293	1,433,760	552	2,731,213	1,032	848,139	711	3,673,221	1,325	1,165,878	811	4,065,596	1,509	1,320,406	694	2,881,337	1,296	952,896
0.00052	661	6,408,027		1,917,277	594	4,728,930		1,433,760	476	2,731,689		848,139	609	3,673,830		1,165,878	693	4,066,289		1,320,406	597	2,881,934		952,896
0.000572	567	6,408,594	1,058	1,918,335	511	4,729,442	957	1,434,717	414	2,732,103	777	848,917	526	3,674,356	985	1,166,863	597	4,066,886	1,116	1,321,522	517	2,882,451	970	953,866
0.000624	488	6,409,082		1,918,335	443	4,729,884		1,434,717	361	2,732,464		848,917	456	3,674,812		1,166,863	516	4,067,402		1,321,522	450	2,882,901		953,866
0.000676	423	6,409,505	794	1,919,128	385	4,730,270	724	1,435,441	317	2,732,781	598	849,514	398	3,675,210	747	1,167,611	448	4,067,850	842	1,322,364	393	2,883,294	740	954,606
0.000728	368	6,409,873		1,919,128	337	4,730,606		1,435,441	279	2,733,061		849,514	348	3,675,558		1,167,611	391	4,068,242		1,322,364	345	2,883,639		954,606
0.00078	322	6,410,196	807	1,919,736	296	4,730,902	558	1,435,999	247	2,733,308	468	849,982	306	3,675,864	578	1,168,189	343	4,068,585	648	1,323,011	305	2,883,944	576	955,182
0.000832	284	6,410,479		1,919,736	261	4,731,163		1,435,999	220	2,733,528		849,982	271	3,676,135		1,168,189	303	4,068,888		1,323,011	270	2,884,214		955,182
0.000884	251	6,410,730	475	1,920,211	232	4,731,396	440	1,436,439	197	2,733,725	374	850,357	241	3,676,375	457	1,168,646	269	4,069,157	510	1,323,521	241	2,884,455	458	955,640
0.000936	223	6,410,953		1,920,211	207	4,731,603		1,436,439	177	2,733,902		850,357	215	3,676,591		1,168,646	240	4,069,397		1,323,521	216	2,884,672		955,640
0.000988	200	6,411,153	379	1,920,590	186	4,731,789	354	1,436,793	160	2,734,061	305	850,662	194	3,676,784	369	1,169,014	245	4,069,612	410	1,323,931	195	2,884,867	372	956,012
0.00104	179	6,411,332		1,920,590	167	4,731,956		1,436,793	145	2,734,206		850,662	174	3,676,959		1,169,014	194	4,069,806		1,323,931	176	2,885,043		956,012
0.001092	161	6,411,493	306	1,920,897	151	4,732,107	287	1,437,080	131	2,734,337	250	850,912	157	3,677,116	300	1,169,314	174	4,069,980	332	1,324,263	159	2,885,202	304	956,315
0.001144	145	6,411,638		1,920,897	136	4,732,243		1,437,080	119	2,734,456		850,912	142	3,677,258		1,169,314	157	4,070,137		1,324,263	144	2,885,346		956,315
0.001196	130	6,411,768	248	1,921,145	123	4,732,365	234	1,437,314	108	2,734,564	206	851,117	128	3,677,386	244	1,169,558	141	4,070,278	268	1,324,531	130	2,885,476	247	956,563
0.001248	118	6,411,886		1,921,145	111	4,732,476		1,437,314	98	2,734,661		851,117	115	3,677,502		1,169,558	127	4,070,405		1,324,531	117	2,885,593		956,563
0.0013	106	6,411,992	204	1,921,349	101	4,732,576	193	1,437,507	89	2,734,750	171	851,288	105	3,677,606	200	1,169,758	115	4,070,519	220	1,324,750	106	2,885,699	204	956,766
0.001352	97	6,412,090		1,921,349	92	4,732,669		1,437,507	82	2,734,832		851,288	96	3,677,702		1,169,758	105	4,070,624		1,324,750	97	2,885,796		956,766
0.001404	90	6,412,180	174	1,921,523	85	4,732,754	165	1,437,672	76	2,734,908	147	851,435	89	3,677,791	172	1,169,931	97	4,070,721	188	1,324,939	90	2,885,887	175	956,942
0.001456	84	6,412,264		1,921,523	80	4,732,834		1,437,672	71	2,734,979		851,435	83	3,677,874		1,169,931	91	4,070,812		1,324,939	85	2,885,972		956,942
0.001508	78	6,412,342	149	1,921,672	74	4,732,908	142	1,437,814	67	2,735,046	128	851,563	78	3,677,952	148	1,170,079	85	4,070,897	161	1,325,100	79	2,886,051	151	957,093
0.00156	70	6,412,412		1,921,672	66	4,732,974		1,437,814	60	2,735,106		851,563	69	3,678,021		1,170,079	75	4,070,972		1,325,100	70	2,886,121		957,093

Y.3 $\sigma_a = 125$ MPa unpeened

a (m)	ΔN ($\sigma_r=10$ MPa)				ΔN ($\sigma_r=20$ MPa)				ΔN ($\sigma_r=40$ MPa)				ΔN ($\sigma_r=60$ MPa)				ΔN ($\sigma_r=80$ MPa)				ΔN ($\sigma_r=100$ MPa)			
	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)	(Trapezium)	(cumulative)	(Simpson's)	(cumulative)
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.000052	1,689,289	1,689,289		565,781	565,781	1,560,139	1,560,139		736,594	736,594		252,847	252,847	660,202	660,202		906,489	906,489		522,977	522,977		188,716	188,716
0.0000572	320,174	2,009,463	565,781	565,781	300,523	1,860,663	528,063	528,063	144,667	881,261	252,847	252,847	133,065	793,266	230,612	230,612	189,593	1,096,082	324,560	324,560	110,442	633,420	188,716	188,716
0.0000624	95,073	2,104,536		565,781	90,372	1,951,034		528,063	45,222	926,483		528,063	42,391	835,657		230,612	61,068	1,157,149		324,560	36,450	669,869		188,716
0.0000676	36,050	2,140,586	58,777	624,558	34,551	1,985,585	56,328	584,392	18,014	944,497	29,377	282,224	17,074	852,731	27,848	258,459	24,449	1,181,599	39,862	364,423	14,988	684,857	24,453	213,169
0.0000728	16,714	2,157,300		624,558	16,118	2,001,703		584,392	8,711	953,207		282,224	8,319	861,050		258,459	11,802	1,193,401		364,423	7,404	692,262		213,169
0.000078	9,062	2,166,362	15,142	639,700	8,783	2,010,485	14,688	599,080	4,893	958,101	8,229	290,452	4,701	865,751	7,914	266,373	6,612	1,200,013	11,113	375,536	4,229	696,490	7,133	220,302
0.0000832	5,506	2,171,868		639,700	5,360	2,015,845		599,080	3,066	961,167		290,452	2,961	868,712		266,373	4,133	1,204,148		375,536	2,687	699,177		220,302
0.0000884	3,624	2,175,492	6,266	645,965	3,542	2,019,387	6,129	605,209	2,075	963,242	3,614	294,066	2,012	870,724	3,509	269,882	2,789	1,206,935	4,853	380,388	1,840	701,017	3,215	223,517
0.0000936	2,521	2,178,013		645,965	2,472	2,021,860		605,209	1,480	964,722		294,066	1,441	872,166		269,882	1,984	1,208,918		380,388	1,327	702,344		223,517
0.0000988	1,824	2,179,838	3,225	649,190	1,794	2,023,654	3,175	608,384	1,097	965,819	1,954	296,020	1,072	873,237	1,911	271,793	1,464	1,210,383	2,805	382,993	992	703,336	1,773	225,289
0.000104	1,360	2,181,198		649,190	1,341	2,024,995		608,384	836	966,656		296,020	820	874,057		271,793	1,112	1,211,495		382,993	763	704,099		225,289
0.000156	1,040	2,182,238	1,868	651,059	1,028	2,026,023	1,848	610,232	653	967,309	1,182	297,202	642	874,699	1,162	272,955	864	1,212,359	1,562	384,555	600	704,700	1,090	226,379
0.000208	813	2,183,050		651,059	805	2,026,828		610,232	520	967,829		297,202	513	875,211		272,955	686	1,213,045		384,555	482	705,182		226,379
0.00026	648	2,183,698	1,182	652,241	643	2,027,471	1,173	611,406	423	968,252	776	297,978	417	875,629	767	273,722	555	1,213,600	1,016	385,571	394	705,576	725	227,105
0.000312	527	2,184,225		652,241	524	2,027,995		611,406	350	968,602		297,978	346	875,975		273,722	456	1,214,056		385,571	328	705,904		227,105
0.000364	435	2,184,661	804	653,045	433	2,028,428	800	612,206	294	968,895	545	298,523	291	876,266	541	274,263	381	1,214,437	707	386,279	277	706,181	515	227,620
0.000416	365	2,185,026		653,045	364	2,028,792		612,206	250	969,145		298,523	248	876,514		274,263	323	1,214,761		386,279	237	706,418		227,620
0.000468	310	2,185,336	577	653,622	309	2,029,101	576	612,782	215	969,360	403	298,926	214	876,728	401	274,664	277	1,215,037	517	386,796	205	706,623	384	228,004
0.00052	265	2,185,601		653,622	265	2,029,366		612,782	187	969,547		298,926	186	876,913		274,664	239	1,215,276		386,796	178	706,801		228,004
0.000572	229	2,185,830	429	654,050	229	2,029,594	428	613,210	163	969,710	307	299,234	162	877,076	306	274,970	208	1,215,483	390	387,185	156	706,957	295	228,299
0.000624	199	2,186,028		654,050	198	2,029,793		613,210	143	969,854		299,234	143	877,219		274,970	181	1,215,665		387,185	138	707,095		228,299
0.000676	173	2,186,201	326	654,376	173	2,029,966	326	613,536	126	969,980	239	299,473	126	877,345	239	275,208	159	1,215,824	300	387,485	122	707,217	231	228,530
0.000728	152	2,186,353		654,376	152	2,030,118		613,536	112	970,092		299,473	112	877,457		275,208	140	1,215,964		387,485	108	707,326		228,530
0.00078	133	2,186,487	252	654,628	134	2,030,251	252	613,788	100	970,192	189	299,662	100	877,556	189	275,398	124	1,216,088	235	387,720	97	707,422	184	228,714
0.000832	118	2,186,605		654,628	118	2,030,370		613,788	89	970,281		299,662	89	877,646		275,398	110	1,216,198		387,720	87	707,509		228,714
0.000884	105	2,186,710	199	654,827	105	2,030,475	200	613,988	80	970,361	153	299,815	80	877,726	153	275,551	99	1,216,297	188	387,908	78	707,588	150	228,864
0.000936	94	2,186,804		654,827	94	2,030,569		613,988	73	970,434		299,815	73	877,799		275,551	89	1,216,386		387,908	71	707,659		228,864
0.000988	84	2,186,888	161	654,988	85	2,030,654	161	614,149	66	970,500	126	299,941	66	877,865	126	275,677	80	1,216,466	153	388,061	65	707,724	124	228,988
0.00104	76	2,186,964		654,988	76	2,030,730		614,149	60	970,559		299,941	60	877,925		275,677	73	1,216,539		388,061	59	707,783		228,988
0.001092	69	2,187,033	131	655,119	69	2,030,799	131	614,281	54	970,614	104	300,045	55	877,979	105	275,782	66	1,216,605	126	388,187	54	707,837	103	229,091
0.001144	62	2,187,095		655,119	62	2,030,861		614,281	50	970,663		300,045	50	878,029		275,782	60	1,216,665		388,187	49	707,886		229,091
0.001196	56	2,187,151	107	655,226	56	2,030,917	107	614,388	45	970,709	86	300,131	45	878,074	87	275,868	54	1,216,719	103	388,290	45	707,931	86	229,177
0.001248	51	2,187,201		655,226	51	2,030,968		614,388	41	970,750		300,131	41	878,116		275,868	49	1,216,768		388,290	41	707,971		229,177
0.0013	46	2,187,247	88	655,314	46	2,031,014	88	614,476	38	970,787	72	300,203	38	878,153	72	275,941	45	1,216,812	86	388,376	37	708,009	72	229,248
0.001352	42	2,187,290		655,314	42	2,031,057		614,476	35	970,822		300,203	35	878,188		275,941	41	1,216,853		388,376	34	708,043		229,248
0.001404	39	2,187,329	76	655,390	39	2,031,096	76	614,553	32	970,854	63	300,266	32	878,220	63	276,004	38	1,216,891	74	388,450	32	708,075	63	229,311
0.001456	37	2,187,365		655,390	37	2,031,133		614,553	30	970,884		300,266	31	878,251		276,004	36	1,216,927		388,450	30	708,106		229,311
0.001508	34	2,187,400	65	655,455	34	2,031,167	65	614,618	29	970,913	55	300,321	29	878,280	55	276,059	34	1,216,961	64	388,514	29	708,134	55	229,366
0.00156	31	2,187,430		655,455	31	2,031,198		614,618	26	970,939		300,321	26	878,305		276,059	30	1,216,991		388,514	26	708,160		229,366

APPENDIX Z

ANALYTICAL MODEL: K_{RESIDUAL}

a = 1.976 mm
 $K_I = -5.077 \text{ MPa}\sqrt{\text{m}}$

b = 20 mm
a/b = 0.099
 $g_1 = 1.267$
 $g_2 = -0.034$
 $g_3 = -0.667$
 $g_4 = 0.289$

RS effect = 1

θ	c (asin θ)	P			Integrand	Simpson
		(poly)	(linear)	c <> 0.44		
0.000	0.000	-389.654	-145.922	-389.654	-1.140	
0.039	0.078	-291.129	-138.987	-291.129	-0.850	-0.068
0.079	0.155	-213.872	-132.064	-213.872	-0.623	
0.118	0.232	-161.697	-125.162	-161.697	-0.468	-0.038
0.157	0.309	-132.347	-118.291	-132.347	-0.381	
0.196	0.385	-117.749	-111.464	-117.749	-0.336	-0.026
0.236	0.461	-104.444	-104.689	-104.689	-0.297	
0.275	0.536	-74.180	-97.978	-97.978	-0.275	-0.022
0.314	0.611	-4.642	-91.341	-91.341	-0.253	
0.353	0.684	129.701	-84.789	-84.789	-0.232	-0.018
0.393	0.756	356.644	-78.330	-78.330	-0.212	
0.432	0.827	705.229	-71.976	-71.976	-0.192	-0.015
0.471	0.897	1204.690	-65.735	-65.735	-0.173	
0.511	0.966	1883.376	-59.619	-59.619	-0.155	-0.012
0.550	1.032	2767.693	-53.635	-53.635	-0.137	
0.589	1.098	3881.097	-47.794	-47.794	-0.121	-0.009
0.628	1.161	5243.144	-42.104	-42.104	-0.105	
0.668	1.223	6868.656	-36.574	-36.574	-0.089	-0.007
0.707	1.283	8766.990	-31.213	-31.213	-0.075	
0.746	1.341	10941.460	-26.028	-26.028	-0.062	-0.005
0.785	1.397	13388.905	-21.029	-21.029	-0.049	
0.825	1.451	16099.437	-16.222	-16.222	-0.037	-0.003
0.864	1.503	19056.356	-11.615	-11.615	-0.026	
0.903	1.552	22236.245	-7.215	-7.215	-0.016	-0.001
0.942	1.599	25609.252	-3.029	-3.029	-0.007	
0.982	1.643	29139.536	0.937	0.937	0.002	0.000
1.021	1.685	32785.879	4.676	4.676	0.010	
1.060	1.724	36502.446	8.183	8.183	0.017	0.001
1.100	1.761	40239.674	11.453	11.453	0.024	
1.139	1.794	43945.270	14.480	14.480	0.030	0.002
1.178	1.826	47565.289	17.259	17.259	0.036	
1.217	1.854	51045.282	19.787	19.787	0.041	0.003
1.257	1.879	54331.452	22.059	22.059	0.045	
1.296	1.902	57371.835	24.073	24.073	0.049	0.004
1.335	1.921	60117.434	25.824	25.824	0.052	
1.374	1.938	62523.306	27.310	27.310	0.055	0.004
1.414	1.952	64549.563	28.529	28.529	0.057	
1.453	1.962	66162.266	29.480	29.480	0.058	0.005
1.492	1.970	67334.188	30.159	30.159	0.060	
1.532	1.974	68045.429	30.568	30.568	0.060	0.005
1.571	1.976	68283.867	30.704	30.704	0.061	
						-0.200

a (mm)	K_I MPa $\sqrt{\text{m}}$
0.000	0.000
0.065	-5.875
0.068	-5.924
0.070	-5.971
0.072	-6.016
0.075	-6.060
0.079	-6.144
0.084	-6.223
0.089	-6.296
0.093	-6.365
0.098	-6.430
0.103	-6.491
0.112	-6.600
0.121	-6.697
0.131	-6.781
0.140	-6.854
0.149	-6.918
0.159	-6.974
0.168	-7.023
0.177	-7.064
0.187	-7.101
0.196	-7.132
0.205	-7.159
0.215	-7.182
0.224	-7.202
0.233	-7.220
0.243	-7.235
0.252	-7.249
0.271	-7.272
0.289	-7.291
0.308	-7.310
0.327	-7.328
0.345	-7.347
0.364	-7.366
0.377	-7.381
0.390	-7.396
0.403	-7.411
0.416	-7.425
0.442	-7.446
0.468	-7.452
0.494	-7.472
0.520	-7.493
0.546	-7.514
0.572	-7.531
0.598	-7.550
0.624	-7.565
0.650	-7.578
0.676	-7.587
0.702	-7.595
0.728	-7.598
0.754	-7.603
0.780	-7.602
0.832	-7.593
0.884	-7.574
0.936	-7.543
0.988	-7.504
1.040	-7.456
1.092	-7.394
1.144	-7.327
1.196	-7.249
1.248	-7.162
1.300	-7.061
1.352	-6.959
1.404	-6.847
1.456	-6.724
1.508	-6.596
1.560	-6.459
1.612	-6.312
1.664	-6.152
1.716	-5.993
1.768	-5.826
1.820	-5.651
1.872	-5.467
1.924	-5.273
1.976	-5.077