Characterisation of Blast Loading from Ideal and Non-Ideal Explosives

Dain George Farrimond

3



5	The thesis presented is for consideration towards the degree of
6	Doctor of Philosophy in
7	THE DEPARTMENT OF CIVIL AND STRUCTURAL ENGINEERING,
8	UNIVERSITY OF SHEFFIELD
9	Monday 11^{th} December, 2023

$_{10}$ Declaration

I, Dain George Farrimond, certify that all the material contained within this document is my own work, except where it is clearly reference to others.
Date:
Signed:.....

¹⁸ Abstract

Explosive detonation in its simplest form can be characterised by an instantaneous release of energy at an infinitely small point in space as a solid explosive material. This is a result of chemical decomposition of an explosive which reforms as high pressure and temperature gases which expand radially. This supersonic expansion of detonation products compresses the surrounding medium resulting in a shock wave discontinuity which propagates away from an explosive epicentre at high speeds. This has the potential of significant damage to anything the shock wave iteracts with.

26

Shock wave quantification work conducted in 1940's through to the 1980's was done so 27 to understand the effects of large scale explosive detonation which was an immediate 28 threat due to the discovery of the nuclear bomb. Highly skilled experimental and theo-29 retical scientists were assigned the task of capturing the effects of large scale detonations 30 through innovative solutions and development of pressure gauges. The in-depth funda-31 mental understanding of physics, combustion and fluid dynamics the researchers utilised 32 resulted in the well-favoured semi-empirical blast predictions for simplistic free-field spher-33 ical/hemispherical blasts. 34

35

A broad amount of literature has been published on free-air characterisation of spher-36 ical/hemispherical explosives, with the detonation process and subsequent shock wave 37 formation mechanics being well understood. However, there is yet to be a definitive and 38 robust understanding of how deterministic a shock waves spatial and temporal parameters 39 are for simplistic scenarios. This goes as far as some studies suggesting that semi-empirical 40 tools are not as effective as previously assumed. Often the use of numerical simulations 41 provide reasonable insights to blast loading conditions imparted on structures and sce-42 narios with higher complexities. However, when the validation data used is assumed to 43 exhibit erroneousness, the schemes are no longer characteristically high in fidelity. The 44

⁴⁵ lack of quantified variability and confidence in the data which is published, are significant ⁴⁶ issues for engineers when designing infrastructure that is both robust enough to withstand ⁴⁷ extreme loading, and not overly conservative that there are cost and material waste impli-⁴⁸ cations. This issue is investigated thoroughly within this thesis, highlighting the sensitivity ⁴⁹ of blast parameters across the scaled distance ranges, and determining their predictability ⁵⁰ with both numerical simulation and semi-empirical tools.

- The vast majority of free-field characterisation has been conducted using military grade 52 explosive which exhibit ideal detonation behaviours; meaning the detonation reaction is 53 effectively instantaneous. Ideal explosives, by the theoretical definition, can be categorised 54 by a simplistic instantaneous energy release. In far-field regimes, any explosive with ideal-55 like compositions and behaviours should be scalable with mass. This assumption is not 56 valid for homemade explosives (HME), such as ANFO (Ammonium Nitrate + Fuel Oil), 57 whose compositions are usually homogenous, resulting in a finite reaction zone length. 58 These can be long enough to cause failures in detonations and exhibit a variety of dif-59 ferent energy releases depending on the mass of the charge resulting in HME's having 60 different TNT equivlence values depending on their scale. 61
- 62

51

Early works of ANFO characterisation was done so in the desire to replace TNT, to assess its capability of producing similar yields for a fraction of the manufacturing costs. This meant the hemispherical detonations of ANFO which have led to its overall classification, were done using charges of over 100kg and therefore non-ideal reaction zone effects become negligible in comparison to the overall charge size. Yields presented in this region were consistently measured at around 80% of a similar TNT detonation and has therefore been incorrectly assumed a rule for ANFO across all mass ranges within published literature.

There is a distinct lack of characterisation of non-ideal explosives throughout the mass 71 scales, posing a significant implication for designing structures to withstand the threat 72 of HMEs. With the knowledge that energy is released at a much slower rate when deto-73 nating these compositions, the assumption that large scale trials accurately capturing the 74 behaviour of a small charge masses, when scaled down, is not verified. Most HMEs will 75 be hand held devices or, at the very least, backpack size, meaning the threat currently 76 is not predictive with confidence through validated data conducted under well-controlled 77 conditions. Small scale ANFO trials have demonstrated this to be the case within this 78

⁷⁹ thesis, with theoretical mechanisms proposed which offering a prediction method of the⁸⁰ behaviour of non-ideal detonation across all mass scales.

81

Findings in this PhD thesis will offer a conclusion on whether shock waves in free-field scenarios are deterministic for both ideal and no-ideal explosives, with a particular emphasis on the far-field range. The results presented are developments in the accurate quantification of shock wave loading conditions a structure is subjected to through explosive detonation and should be used by engineers to establish robust, probabilistic but accurate designs.

Acknowledgements

It is important to express my deepest thanks to those whom without their consistent 90 support and guidance this thesis would not have been possible. To my PhD Supervisors; 91 Professor Andy Tyas alongside Dr. Samuel Rigby and Professor Samuel Clarke, through-92 out this journey there have been struggles which were unforeseen and unprecedented but 93 despite this the three of you have provided not only insightful knowledge of explosive 94 characterisation invaluable to this research but a support network which has enabled to get the best out of both myself and the situation. I have learnt a great deal from the three 96 of you during my, thus-far, short researching career, and am excited for what the future 97 has in store for where my learning could continue. 98

99

I would also like to pay special thanks to the employees at Blastech, for both the high quality experimental work they conduct and for being incredibly welcoming during my time working alongside them, conducting both University and commercially funded experimental work. I feel privileged to have been able to work within an industry recognised research team concurrently to my studies which has provided me with an invaluable experience other PhD students do not get access to quite as readily.

106

To my friends and family, the people in my life who have provided consistent support throughout the duration of my PhD journey. There has been an overwhelming number of discussions had with all of you regarding both rewarding and challenging aspects of the PhD process. Thank you for being my think tank outside of academia and providing the best advice anyone could ask for when taking the time to listen about the intricacies of my research.

113

¹¹⁴ Finally, and most importantly, I would like to thank Laura. You have been my rock

- throughout this whole process, listening to my endless ramblings, notions and hypotheses
 I have had regarding aspects of my research. Without you this thesis would not have been
 possible.
- 118
- 119 Dain George Farrimond,
- 120 Monday 11th December, 2023

$_{121}$ Contents

122		Abs	tract
123		Ack	nowledgements
124		Con	tents
125		List	of Figures
126		List	of Tables
127		Non	nenclature
128	1	Intr	roduction 1
129		1.1	Background and Motivation
130		1.2	Scope and Objectives of the Thesis
131		1.3	Thesis Outline
132		1.4	Published Articles
133	2	Lite	erature Review and Theoretical Background 7
134		2.1	Introduction
135		2.2	The Detonation of Explosives
136		2.3	Air Shock Formation
137		2.4	Secondary Shock
138		2.5	Scaling Laws
139			2.5.1 Mass and Energy Proportionality
140			2.5.2 Charge Shape

141	2.6	Semi-Empirical Prediction Methods	20
142		2.6.1 Positive Phase Parameters	20
143		2.6.2 Negative Phase Parameters	22
144	2.7	TNT Equivalence	23
145	2.8	Blast Variability - Real or Systematic?	24
146	2.9	Historical Review of 'Best' Practices	26
147		2.9.1 Data Capture between 1950 - 1980	28
148		2.9.2 Data Capture between 1980 - Today	32
149	2.10	Non-Ideal Explosive Characterisation	35
150	2.11	Summary	42
151 3	Sta	ndardising Experimental Methodologies and Analysis	44
152	3.1	Development of Experimental and Analytical Procedures	44
153		3.1.1 Preliminary Test Methodology	44
154	3.2	Pressure Gauge Data	48
155		3.2.1 Analysis of Positive Phase (Ai)	48
156		3.2.2 Modifications for Positive Phase Improvement (Ei)	59
157		3.2.3 Analysis of Negative Phase (Ai)	72
158		3.2.4 Future Considerations for Pressure Gauge Work	78
159		3.2.5 Pressure Gauge Summary	78
160	3.3	High Speed Video (HSV) Recordings	79
161		3.3.1 Far-Field HSV Analysis (Ai)	79
162	3.4	Future Considerations for HSV Work	89
163		3.4.1 Far-Field Methodology Errors (Ei)	89
164		3.4.2 Extracting More Parameters (Ai)	92
165	3.5	Summary	93

166 4 Ideal Explosive Blast Characterisation

167	4.1	Introd	$uction \dots 95$	5
168	4.2	Pressu		3
169		4.2.1	Positive Phase Blast Parameter Variability	3
170		4.2.2	Numerical Simulation	3
171		4.2.3	The Negative Phase	L
172		4.2.4	Pressure Gauge Summary	5
173	4.3	High S	Speed Video Data	3
174		4.3.1	Time of Arrival Variability	7
175		4.3.2	Derivation of Explosive Yield from Arrival Time Data)
176		4.3.3	Capturing Secondary Shock Data	2
177		4.3.4	High Speed Video Summary	3
178	4.4	Future	e Research of Explosive Characterisation	1
179		4.4.1	Near-Field Loading	1
180		4.4.2	TNT Equivalence	5
181	4.5	Summ	ary	3
182 5	No	n-Ideal	Explosive Blast Characterisation 127	7
183	5.1	Introd	uction	7
184	5.2	Exper	imental Setup	3
185		5.2.1	Far-Field Trials	3
186		5.2.2	Rate Stick Trials	L
187	5.3	Pressu	re Gauge Results	2
188		5.3.1	Positive Phase	2
189		5.3.2	Arrival Time Offset	7
190		5.3.3	Disagreement to Published TNT Equivalence	5
191		5.3.4	Was the composition of the explosive actually ANFO? 146	3
192		5.3.5	Negative Phase	5

193		5.3.6	Pressure Gauge Summary	. 162
194	5.4	High S	peed Video Analysis	. 163
195		5.4.1	Fireball Breakout	. 164
196		5.4.2	Variability Analysis	. 166
197		5.4.3	Rate Stick Trials	. 167
198		5.4.4	High Speed Video Summary	. 178
199	5.5	Future	Research into Non-Ideal Detonations	. 179
200 6	Sun	ımary,	Conclusions and Future Work	181
201	6.1	Summa	ary	. 181
202	6.2	Conclu	sions	. 183
203	6.3	Evalua	tion and Future Work	. 184

204 List of Figures

205	1.1	QR code links to published articles	6
206	2.1	Schematic representations of detonation theories: C-J theory (left) display-	
207		ing the planar like pressure wave with distance and no lateral losses, and	
208		the theory proposed by von Neumann $^{[177]}$ (right) which details finite reac-	
209		tion zones and detonation product expansions. Note the numbering system	
210		aligns with detonation process discussed above	10
211	2.2	Schematic representations of detonation velocities and how they vary with	
212		charge diameter for ideal (dashed) and non ideal (solid) explosives adapted	
213		from work presented by Scott ^[142]	11
214	2.3	Schematic representation of the formation of air shock from hemispherical	
215		explosive detonation: Depicted by Initial pressure pulse related to the deto-	
216		nation product breakout (left), transitioning into a front loaded pulse due to	
217		a range of particle velocities (middle) to a point where a near-discontinuous	
218		shock wave forms (right), adapted from Kinney and Graham ^[90]	12
219	2.4	Schematic representation of the the different scaled distance regimes dis-	
220		cussed by $Tyas^{[173]}$	13
221	2.5	Indicative Freidlander shock wave pressure–time history with reference to	
222		both reflected (red) and incident (blue) forms with respect to each other. $% \left({{\left[{{{\rm{cd}}} \right]}_{{\rm{cl}}}}_{{\rm{cl}}}} \right)$.	14
223	2.6	Indicative behaviour of negative phase process: Pre-detonation of charge	
224		with reference air particles (left), and Post-detonation with reference to	
225		shock wave condensed air particles, leaving a vacuum with an under pressure.	15
226	2.7	Indicative Freidlander shock wave pressure–time history with reference to	
227		the secondary shock phenomena and the blast parameters associated	16

228 229	2.8	Secondary shock delay parameter evaluated for all explosives scaled accord- ingly compared with a least-squares fit to data, extracted from Rigby and Cittorman ^[129]	17
230 231 232	2.9	Representative schematic of Hopkinson ^[74] -Cranz ^[33] scaling, adapted from Baker ^[7]	19
233 234 235 236	2.10	The semi-empirical curves for incident and reflected positive phase blast wave parameters for a 1kg TNT explosive detonation with respect to scaled distance, established by Kingery and Bulmash ^[87] : a) Hemispherical charge of TNT detonated of a ground surface, b) Spherical charge of TNT in free	
237		air	21
238 239 240 241	2.11	The semi-empirical curves for incident and reflected negative phase blast wave parameters for a 1kg TNT explosive detonation with respect to scaled distance, established by Granstrom ^[66] : a) Hemispherical charge of TNT detonated of a ground surface, b) Spherical charge of TNT in free air	22
242 243 244 245	2.12	Compiled blast parameters from TNT explosive trials with varying mass as a function of scaled distance, which has been scaled to a 1kg equivalent hemispherical charge, using a shape scaling factor of 1.8 and compared with KB predictions: a) Peak overpressure, b) Scaled peak specific impulse, c)	20
246 247 248 249 250 251 252	2.13	Scaled arrival time, d) Scaled positive phase duration	30
253 254	2.14	Pressure evaluated TNT equivalence ratio for unconfined ANFO with re- spect to the mass of the charge extracted from Petes et al. ^[112] , Figuli	20
255 256 257 258 259	2.15	Compiled blast parameters from ANFO explosive trials with varying mass as a function of scaled distance, which has been scaled to a 1kg equivalent hemispherical charge, using a shape scaling factor of 1.8, a TNTe=0.82 ^[112] , and compared with KB predictions: a) Peak overpressure, b) Scaled arrival	JY
260		time, c) Scaled peak specific impulse, d) Scaled positive phase duration	40

261 262	2.16	The theoretical energy of ANFO as a function of fuel oil content, adapted from Petes et al. ^[112]	41
263 264 265	3.1	General arrangement of the test pad at the University of Sheffield Blast and Impact Laboratory: Site photograph taken approximately from the location of the high speed video camera	45
266 267 268	3.2	Photographs of the moulding stages of a 250g PE10 hemispherical charge in which the 3D printed mould is used to provide consistency in charge shape and density, which can be seen when removed from the casing	46
269 270	3.3	General arrangement of the test pad at the University of Sheffield Blast and Impact Laboratory: Schematic including HSV camera positioning	47
271 272 273	3.4	Example historic test results using a 250g PE4 hemispherical charge re- flected pressure recording at 5 m stand-off compared to KB predictions for a 300g TNT hemisphere	49
274 275 276	3.5	Compilation of the entire raw data set of 250 g PE4 hemispherical ground burst comprising of two recordings at each scaled distance. Positive phase only	50
277 278 279	3.6	Example historic test recording of electrical noise prior to arrival of the shock wave with its distribution presented, where X is associated to the voltage recorded in the system	52
280 281 282 283	3.7	Example historic test results using a 250g PE4 hemispherical charge at 4 m stand-off: a) Raw pressure, and; b) Raw specific impulse with respect to time for a single test, highlighting the assignment of shock wave arrival time, t_a , and positive phase duration, t_d	53
284 285 286 287 288 289	3.8	Example curve-fitting for historic test results using a 250g PE4 hemispher- ical charge at 4 m stand-off: a) all fitted curves to raw data with iterations based on percentage t_d removed immediately after t_a , and; b) Variations in fitted peak pressure and specific impulse as a result of the percentage of t_d removed, and definition of final range (solid markers) for which mean parameters are evaluated	54
290 291	3.9	Example historic test results using a 250g PE4 hemispherical charge at 4 m stand-off with optimal fits overlaid: a) Overpressure, and; b) Specific impulse	56

292 293 294 295	3.10	Compiled blast parameters from hemispherical PE4 trials as a function scaled distance, compared with KB predictions: a) Scaled arrival time, b) Scaled positive phase duration, c) Peak reflected pressure, d) Scaled reflected peak specific impulse	58
296 297 208	3.11	Example historic test results from a 1000lb high explosive height of burst shot recovered from Reisler et al. ^[119] , displaying a comparison between a pressure probe (dotted) and a Kulite pressure gauge within a baffle plate	
299 300		(solid) across two different time bases, similar to the methods adopted in this thesis	60
301 302 303 304 305	3.12	Comparison between experimentally recorded data for a 250 g hemispher- ical PE10 charge detonated 2 m away from a reflected gauge and Apollo numerical modelling (with EOS parameters developed using Cheetah and Explo5): a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs	62
306 307 308 309 310	3.13	Comparison between experimentally recorded data for a 250g hemispheri- cal PE10 charge detonated 2m away from a reflected gauge and numerical model evaluating using APOLLO when accounting for energy losses into the ground a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs	64
311 312 313 314 315	3.14	Comparison between experimentally recorded data for a 250g hemispherical PE10 charge detonated 2 m away from a reflected gauge and numerical model evaluating using APOLLO when accounting for energy losses into the ground and substantial terrain features a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs	65
316 317 318 319 320	3.15	Comparison between experimentally recorded data, time-shifted so the arrival of the positive phases align exactly, for a 250 g hemispherical PE10 charge detonated 5 m away from a reflected gauge with adjustments to the blast arena and without: a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs	66
321 322 323 324	3.16	A comparison of top and bottom detonated 250g hemispherical PE4 charges recordings of reflected pressure and specific impulse against time at 1.25m standoff (corresponding to plots a and c, and b and d respectively) which make reference to KB predictions and numerical simulations.	69

325 326 327 328	3.17	A comparison of two top and bottom detonated 250g hemispherical PE4 charges recordings of reflected pressure and specific impulse against time at 1.25m, 1.5m, 1.75m and 2m standoffs (corresponding to plots a, c, e and g, and b, d, f and h respectively) which make reference to KB predictions	71
329 330 331	3.18	Comparison of negative phase results from a 250g PE4 trial with two re- flective recording points 5m either side of the explosive, where plots a) and b) represent the raw negative pressure-time plots and plot c) and d) are	
332 333		the corresponding impulse-time plots for the blockwork and bunker walls respectively.	74
334 335 336 337	3.19	Compilation of scaled negative phase parameters resulting from visual anal- ysis of 250g PE4 hemispherical charge using a TNTe=1.22: a) Negative Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time Duration.	75
338 339 340 341	3.20	Compilation of scaled secondary shock parameters resulting from visual analysis of 250g PE4 hemispherical charge using a TNTe=1.22: a) Negative Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time Duration.	77
342 343	3.21	HSV stills from a test using 250 g PE4 hemisphere at 4 m stand-off: a) Raw video footage, and; b) Corresponding image subtraction	81
344 345	3.22	Method for detecting location of Shock Front through intensity changes on a virtual 'spoke' overlaid with pixel cluster identification	82
346 347	3.23	Schematic of shock wave radius calculation in 3D space to be used in con- junction with Equations 3.2–3.6	84
348 349 350	3.24	Shock front arrival time from a 250g PE4 hemispherical charge placed at a 5m stand-off, recorded using HSV and scaled using 1.22 TNT equivalence factor to compare to KB predictions	86
351 352	3.25	Method of interpolation of shock front arrival times along a virtual 'spoke' for prescribed scaled distances	87
353 354 355	3.26	Shock front arrival time from a 250g PE4 hemispherical charge placed at a 5m stand-off, recorded using HSV and scaled using 1.22 TNT equivalence factor to compare to KB predictions, detailing the capture of the secondary	
356		shock propagation.	88

357	3.27	Shock front arrival time from a 250g PE4 hemispherical charge placed at a
358		5m stand-off, recorded using HSV and scaled using 1.22 TNT equivalence
359		factor to compare to KB predictions, showing the effect off having testing
360		procedure not perfectly square
361	3.28	Re-analysed data from Figure 3.27 with an adjustment to the calibrated
362		pixel sized to account for the skewing of the FOV during camera rotation 91
363	4.1	Compiled blast parameters from RDX and PETN based explosive trials as
364		a function scaled distance, normalised against the mean of nominally iden-
365		tical trials: a) Peak reflected overpressure (Mean-Normalised P_r), b) Scaled
366		reflected peak specific impulse (Mean-Normalised I_r), c) Scaled arrival time
367		(Mean-Normalised t_a), d) Scaled positive phase duration (Mean-Normalised
368		t_d)
369	4.2	Compiled blast parameters from RDX and PETN based explosive trials as a
370		function scaled distance, compared with KB predictions: a) Peak reflected
371		overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival
372		time, d) Scaled positive phase duration
373	4.3	Compiled blast parameters from RDX and PETN based explosive trials
374		as a function scaled distance, normalised against KB predictions for nom-
375		inally identical trials: a) Peak reflected overpressure (KB-Normalised P_r),
376		b) Scaled reflected peak specific impulse (KB-Normalised I_r), c) Scaled
377		arrival time (KB-Normalised t_a), d) Scaled positive phase duration (KB-
378		Normalised t_d)
379	4.4	RSTD in shock wave arrival time with respect to scaled distance, from
380		historic and current pressure gauge data
381	4.5	A compilation of reflected overpressure-time history plots for the three ex-
382		plosives tested across three different stand-off distances compared to the
383		corresponding validated and APOLLO model predictions
384	4.6	Compilation of scaled negative phase parameters results of 250g PE4, PE8
385		and PE10 hemispherical charges using the representative TNTe: a) Negative
386		Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time
387		Duration

388 389 390 391	4.7	Compilation of scaled secondary shock parameters resulting from visual analysis of 250g hemispherical charges of PE4, PE8 and PE10 using the representative TNTe values: a) Negative Pressure, b) Scaled Negative Spe- cific Impulse and c) Negative Phase Time Duration
392	4.8	Scaled secondary shock delay with respect to scaled distance for all three
393		ideal explosives using representative TNTe values
394	4.9	Dimensionless secondary shock delay parameter evaluated for all ideal ex-
395		plosives scaled accordingly compared with polynomial fit to historical data . 115
396	4.10	RSTD in shock wave arrival time with respect to scaled distance, when
397		comparing pressure gauge and HSV data
398	4.11	Logarithmic RSTD in shock wave arrival time as a function of scaled dis-
399		tance for both pressure gauge and high speed video recordings of 250g hemi-
400		spheres of PE4
401	4.12	Interpolated and unscaled HSV shock wave arrival time from a 250 g PE4 $$
402		hemispherical charge at 5 m stand-off compared with KB predictions for
403		TNT hemispherical charges with different charge mass $\ldots \ldots \ldots \ldots \ldots 121$
404	4.13	Interpolated and unscaled HSV secondary shock delay time from 250 g
405		hemispherical ideal charges compared with pressure gauge recordings of
406		PE4, PE8 and PE10
407	5.1	Schematic of the charge and booster locations used throughout this testing
408		regime
409	5.2	Top detonated arrangement for hemispherical ANFO charges boosted with
410		3g PE10 sphere; the yellow tubes are installed as guides for the detonator
411		to be positioned vertically into the booster
412	5.3	General arrangement of the rate stick trials using a 3mm wall thickness PVC
413		clear tube, a 3D printed end cap which allows for detonator and booster
414		placement and a reference measurement guide to enable distance tracking
415		in the high speed videos $\ldots \ldots 131$

416 417 418 419	5.4	General arrangement of the rate stick trials using a 3mm wall thickness PVC clear tube, a 3D printed end cap which allows for detonator and booster placement and a reference measurement guide to enable distance tracking in the high speed videos	132
420 421 422 423	5.5	Compilation of raw data set of 250g ANFO hemispherical ground bursts, comprising of both top and bottom detonated charges, across the entire range of standoff distances tested in this regime. Positive phase is presented only.	133
424 425 426 427 428	5.6	Compiled scaled blast parameters from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.395, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration	134
429 430 431 432 433	5.7	Compiled mass scaled blast parameters from ANFO explosive trials as a function mass scaled distance, compared with KB predictions, using a TNTe=0.395±0.1 to present variability bounds, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse	136
434 435 436 437	5.8	Compiled raw data from both top and bottom detonated trials at 2m, 4m, 6m and 8m standoff distance compared to KB predictions assuming a TNTe=0.395: Pressure-time history (Top) and Impulse-time history (Bot- tom), showing only positive phase	138
438 439 440	5.9	Scaled time of arrival from experimental work offset from KB predictions based on a TNTe=0.395, against scaled distance for top and bottom detonated tests with reference best fit lines	142
441 442 443 444	5.10	Theoretical schematic of different detonation and shock wave velocities with respect to scaled distance for TNT (Blue) and ANFO charges of various sizes (Red), with reference to the times at which detonation breakout occurs respectively to one another.	144
445 446 447 448	5.11	Compilation of pressure-time and impulse-time histories from 1m standoff distances which related to top (red) and bottom (blue) detonated trials compared to APOLLO simulations of AN: a) Top P-T, b) Top I-T, c) Bottom P-T, and d) Bottom I-T.	. 148

449 450	5.12	Compilation of pressure-time and impulse-time histories from 1m standoff distances which related to top (red) and bottom (blue) detonated trials: a)
451		Top P-T, b) Top I-T, c) Bottom P-T, and d) Bottom I-T
452 453 454 455	5.13	Equivalent TNTe values resulting from applying a nominal 13mm reaction zone to a given ANFO charge and assuming that the region has not fully reacted and instead is fired off as a projectile compared with extract TNTe from experimental pressure and impulse data
456 457	5.14	Extracted TNTe values from 250g hemispherical charge trials of ANFO varying the FO percentage by addition of pure AN
458 459 460	5.15	Compilation of pressure-time and impulse-time histories at 2m (red) and 8m (blue) standoff of 50/50 shells of ANFO/AN compared to 250g ANFO trials (black): a) 2m P-T, b) 8m P-T, c) 2m I-T, and d) 8m I-T 154
461 462 463 464	5.16	Compiled scaled negative phase blast parameters from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.395, with increasing marker sizes to indicate the mass of charge: a) Reflected negative pressure, b) Reflected negative specific impulse, c)
465 466 467 468 469 470	5.17	Scaled negative phase duration
471 472 473 474 475	5.18	Compiled scaled secondary shock blast parameters from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.82, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration
476 477 478 479 480	5.19	Compiled scaled secondary shock blast parameters from all considered ex- plosive trials as a function scaled distance, compared with KB predictions, using each corresponding TNTe value, with increasing marker sizes to indi- cate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration 160

481 5.20	Dimensionless secondary shock delay parameter evaluated for all explosive tested in this thesis, scaled accordingly, and compared with polynomial fit
483	to historic data
484 5.21 485 486	Shock front arrival time from a bottom detonated 250g ANFO hemispherical charge placed at a 5 m stand-off, recorded using HSV and scaled using TNT equivalence factor of 0.3 to compare to KB predictions
487 5.22 488 489 490 491	Ultra high speed video footage of a bottom detonated 250g hemispherical trial displaying the comparison between charge diameter at the time of detonation and at the point in which the detonation wave reached the charge's extents and products began to expand; this is denoted by the charge size extending passed the green lines spaced 80pixels apart in both plots 165
 492 5.23 493 494 	Shock wave velocity with respect to arrival time for a 250g TNT explosives evaluated through KB predictions with reference to the average vlocity extracted from the HSV of hemispherical ANFO detonation
495 5.24 496 497	Logarithmic RSTD in shock wave arrival time of 250g hemispherical ANFO trials as a function of scaled distance for high speed video recordings, compared to empirical model detailed within Farrimond et al. ^[49]
 498 5.25 499 500 	High speed video snapshots with 0.05ms intervals between each plot display- ing the propagation of the detonation wave along a 300mm length 50mm diameter PMMA pipe
501 5.26 502 503 504 505	High speed video snapshots of 104mm internal diameter ANFO filled PMMA tube at $t = 0.026, 0.052, 0.078$ and $0.104ms$ after detonation, highlighting the reaction zone positions assigned (green lines) for the given region con- sidered (green dashed lines) alongside the widths of the pipe (blue dashed lines)
506 5.27 507 508	High speed video snapshots of 104mm internal diameter ANFO filled PMMA tube at $t = 0.026, 0.052, 0.078$ and $0.104ms$ after detonation, zoomed into the area box region considered
509 5.28 510 511 512	HSV tracking results from a 50mm internal diameter rate stick trial, cali- brated both vertically and horizontally, smoothed using a 15 point moving average to present: a) Detonation front velocity and b) Reaction zone length with respect to distance travelled along the pipe

513	5.29	HSV tracking results from all ANFO rate stick trials conducted within this
514		thesis, smoothed using a 15 point moving average to present: a) Detonation
515		front velocity and b) Reaction zone length with respect to distance travelled
516		along the pipe
517	5.30	Equivalent TNTe values resulting from applying a nominal 13mm reaction
518		zone to a given ANFO charge and assuming that the region has not fully
519		reacted and instead is fired off as a projectile compared with extracted TNTe $$
520		values from experimental pressure and impulse data, making reference to
521		the reaction zone range recorded Figure 5.29b

522 List of Tables

523	2.1	Reference list for historic data extracted from within this era for both spher-	
524		ical and hemispherical TNT and Pentolite detonations	31
525	2.2	Historical explosive events across the world noting the explosives which det-	
526		on ated and the overall effects associated adapted from National Academies of $\hfill \hfill \hfill$	
527		Sciences and Medicine ^{$[105]$} . The events noted in bold are accidental whilst	
528		the rest are terror events with D and I corresponding the Deaths and In-	
529		juries respectively.	37
530	2.3	Reference list for historic data extracted for both spherical and hemispher-	
531		ical ANFO detonations.	38
532	3.1	Table of EXPLO5 Equation of State Parameters for Air.	62
533	3.2	Table of EXPLO5 Equation of State Parameters for Explosives	63
534	5.1	EPC-UK material properties of ANFO and AN which have proven useful	
535		for this body of research and article	28

Nomenclature

537	A	Area
538	D_{CJ}	Chapman-Jouguet detonation velocity
539	D_{∞}	Infinite charge diameter
540	E	Detonation energy per unit mass
541	F	Original image
542	i	Specific impulse
543	i_r	Reflected positive phase specific impulse
544	$i_{r,min}$	Reflected negative phase specific impulse
545	i_{so}	Incident positive phase specific impulse
546	$i_{so,min}$	Incident negative phase specific impulse
547	K	Hopkinson-Cranz scaling factor
548	N	Resulting subtracted image
549	P	Pressure
550	P_{CJ}	Chapman-Jourguet pressure
551	P_{max}	Max Overpressure
552	P_o	Ambient air pressure
553	P_r	Reflected pressure
554	$P_{r,neg}$	Negative reflected pressure
555	P_{so}	Incident pressure
556	$P_{so,neg}$	Negative Incident pressure
557	P_{SS}	Secondary shock pressure
558	R	Distance from charge centre (stand-off)
559	R^2	Coefficient of determination
560	ho	Charge density
561	t	Time
562	t_a	Time of arrival

563	t_d	Positive	phase	time	duration	

- t_{d-} Negative phase time duration
- td_{ss} Secondary Shock positive phase time duration
- au_{ss} Secondary shock delay parameter
- $_{\rm 567}$ $~~\delta\tau_{ss}$ Time difference between arrival of primary and secondary shock
- V_{od} Velocity of detonation
- W Charge mass
- Z Scaled distance

572 Chapter 1

573 Introduction

The overall aim of this PhD thesis is to comprehensively characterise the effects various explosive compositions and sizes have when detonated across a full range of distances from a target. This will focus primarily on the far-field range of distances, the time at which the shock wave has propagated to a significant distance away from the explosive centre as to not be affected by late-time chemical reactions within the fireball. The context of this work looks at providing key analytical procedures which are validated for the most simple and ideal explosive compositions and assessing their application to non-ideal compositions.

This chapter will provide an outline of the structure of the thesis as well as detailing the motivation behind the current research.

584

⁵⁰⁵ 1.1 Background and Motivation

The discovery and use of the nuclear bomb in 1945, initiated a critical need across the 586 globe to better understand the effects of explosions with extremely large yields. This 587 was essential to ensure procedures and strategies could be implemented for civilian safety 588 against potential large scale threats. Between 1945-1963, a large number of nuclear tests 589 were undertaken by the United States in the attempt to quantify the disastrous conse-590 quences these events would have on civilian infrastructure. The severe environmental 591 damage caused by these tests induced the first instance of global cooperation to eliminate 592 the testing of nuclear weapons. There was however still a need for quantifying the effects 593

of said events to understand the fundamentals of explosions and how this knowledge could 594 be used to improve design practices of structures to withstand them. Vast investment 595 at this time into testing of high explosives, with yields within similar margins to nuclear 596 detonation, produced some of the more widely regarded quantification data sets^[87]. This 597 was then utilised to develop a semi-empirical prediction tool for free-air blast scenarios $^{[90]}$. 598 Blast resilient design specifications to this day still make use of these tools for prescribing 599 loading conditions a given target will be subjected to for a given mass of Trinitrotoluene 600 (TNT) - the baseline to which all comparisons are made in blast engineering. 601 602

This tool has however had its accuracy questioned over more recent years with researchers 603 debating whether it provides reasonable enough representations of an explosive event 604 across a full-field of distances between charge and target^[13]. Logic would suggest that 605 with more modern and precise experimental procedures, the results should tend towards 606 those predicted, with a reduction in the uncertainty. However, the problem has been that 607 many modern researchers have reported a significant lack of repeatability in experimental 608 measurements when comparing directly to the tool's predicted parameters, and the much 609 older data sets used to produce them^[56]. There is however a clear divide in the blast 610 protection community regarding the fundamental understanding of explosive characterisa-611 tion; those who exhibit large variability in experimental blast measurements and interpret 612 this to be inherent of explosive detonation, and those which undertaking similar testing, 613 recorded consistent and deterministic data. 614

615

Modern day architecture has moved towards more material and energy efficient designs 616 whilst appealing aesthetically through atrium-like open spaces, glazed cladding for addi-617 tional lighting and unique structural forms for visual effect. These three additions, among 618 others, to civilian infrastructure have one key disadvantage: the catastrophic effects, both 619 structurally and to civilians, they can have as a result of being subjected to explosive 620 loading conditions. This in conjunction with the rapid expansion of the geographic extent 621 of urban areas has resulted in a rise in spatially complex civilian environments. Blast 622 resilient design of infrastructure has become essential as a results of an increasing number 623 of explosions occuring in civilian areas. In 2021 alone there were a total of 5,226 recorded 624 terrorist attacks on civilian structures, with the 18 worst events resulting in 1241 deaths 625 alone^[79]. The frequency and variety in modern day explosive events and their interac-626 tion with structures provides enough of a challenge for engineers to combat without the 627

predicted methods used for design being questioned. Whilst ever there is uncertainty in the predictive tools used to design civilian infrastructure, there is also an uncertainty in safety assurances of structures when subjected to explosive loading. There is, therefore, a need to establish whether the prediction tools developed by Kingery and Bulmash^[87] are accurate for a full range of distances between charge and target across various explosive types.

634

This thesis presents research which will contribute to the existing knowledge of quantifying 635 reflected blast loading on targets by characterising the effects across a range of charge-to-636 target distances for a variety of explosives. The research aims to provide evidence which 637 supports the notion of explosive variability through re-examination of both historic and 638 newly recorded data, whilst developing new and robust experimental data processing tech-639 niques. The investigation into different types of explosives will provide improvements to 640 the fundamental understanding of the mechanisms and characteristics of their detonation, 641 and the resulting yields. 642

643

⁶⁴⁴ 1.2 Scope and Objectives of the Thesis

When designing infrastructure to withstand explosive loading conditions, the engineer is 645 faced with the task of assigning a given charge composition, shape, mass and location 646 from a target. These variables often will not be known, and therefore a probabilistic anal-647 ysis is required. The ability to determine an accurate prediction for a prescribed event 648 is essential to introduce confidence in probabilistic studies. Whilst all of these variables 649 can significantly alter the pressures associated with the resulting blast wave, there still is 650 the issue of whether current empirical and numerical predictive methods are reasonable 651 estimations to a real event. 652

653

Whilst there have been significant developments in numerical analysis and their potential to output accurate predictions, it is important to revisit experimental trials to somewhat re-establish the benchmark fundamental explosive parameters from simple scenarios. Only when the discussion over inherent explosive variability is finalised, can reliable and accurate numerical models be developed. This thesis, has several objectives which are directly related to issues outlines above:

- To identify a clear benchmark of free-field explosive characterisation of ideal explosives, and its associated variability with distance, which can be used in yield
 comparison studies of various composition types.
- 2. To develop validated experimental methodologies and tools for analysis to establish
 reliable data to inform the understanding of fundamental explosive physics.
- 3. To establish scalability of explosives which exhibit non-ideal detonation behaviours,
 and evaluate whether TNT equivalence theories are valid.

667 1.3 Thesis Outline

⁶⁶⁸ The remainder of this thesis is organised into the following chapters:

• Chapter 2 - Literature Review and Theoretical Background

This chapter will provide a detailed overview of previously published literature regarding explosive blast loading gained through both experimental and numerical analysis across a number of charge compositions, sizes, shapes and location from a target. The aim of this chapter is to scrutinise existing hypotheses and conclusions authors have made regarding the fundamental principles of blast wave development and loading alongside the quantification of variability a given explosive type exhibits in line with Objective 1.

677

• Chapter 3 - Standardising Experimental Methodologies and Analysis

This chapter establishes both experimental methodologies and methods of analysis through extensive validation against recorded data and numerical modelling with Objectives 2 and 3 in mind. The effects of generally assumed insignificant experimental features are studied and highlight the need for strict control measures during explosive testing and modelling.

684

• Chapter 4 - Ideal Explosive Blast Characterisation

The validated techniques developed in Chapter 3 were used across a range of different ideal high explosive compositions in the far-field ranges to determine whether they are applicable across simplistic free-air scenarios to achieve Objective 4. These

methods are exercised against current standards of readily available prediction toolsto access their accuracy and consistency.

691

692

• Chapter 5 - Non-Ideal Explosive Blast Characterisation

This chapter aims to complete Objective 5 by providing a detailed characterisation of non-ideal explosives not yet fully discussed within the available literature. The content attempts to assess the scalability of non-ideal explosives and compares the resulting yields to that of ideal explosives and the respective prediction tools.

697

• Chapter 6 - Summary, Conclusions and Future Work

This chapter summarises the research presented within this thesis and makes suggestions for future developments towards improving the current understanding of explosive loading conditions within a full-scale range of standoff distances in line with Objective 6.

704 1.4 Published Articles

It is important to note that all experimental work alongside the analysis was undertaken by the author of this thesis with technical assistance from Blastech Ltd. All numerical simulations were undertaken by collaborators at DSTL whom had no further input into the narrative of this research. The work contained within this thesis has been used to publish peer-reviewed journal papers which can be quickly accessed using these QR codes: ⁷¹⁰

Figure 1.1: QR code links to published articles



(a) Farrimond et al.^[49]



(c) Hobbs et al.^[72]



(b) Farrimond et al.^[50]



(d) Barr et al. [10]
711 Chapter 2

⁷¹² Literature Review and Theoretical ⁷¹³ Background

714 2.1 Introduction

This chapter discusses the fundamental understanding of explosive detonation and the subsequent blast wave propagation and interaction with structures. Throughout this discussion, a review of published literature will be undertaken relevant to the subsequent subject areas investigated within the content of this thesis.

⁷²⁰ 2.2 The Detonation of Explosives

During the detonation process of an explosive, enough energy is provided to the physi-721 cal solid mass which propagates through the composition in the form of a reaction wave. 722 This results in an exothermic decomposition over a very short duration of time producing 723 hot dense gases^[1]. The reaction process occurs over a given amount of time (varying 724 dependant on charge composition) and is confined within the explosive mass itself until 725 the wave reaches the extents of the explosive. This means that the gaseous detonation 726 products occupy the same volume as the solid mass previously did and therefore exhibit 727 extremely high temperatures and pressures^[101] of around 10-30GPa and 3000-4000°C re-728 spectively^[32]. The detonation wave is continually reinforced by the energy released from 729 the material detonating immediately ahead of it until the explosives extents are reached. 730

731

⁷³² Developing the knowledge of the detonation process is fundamental to investigating and ⁷³³ characterising the behaviours of detonating explosive compositions. This will be consid-⁷³⁴ ered regardless of reaction chemistry and detonation dynamics, across a range of masses ⁷³⁵ and distances from a target. A clear review of the different detonation processes are pre-⁷³⁶ sented with a discussion around the effect these can have on free air shock loading.

737

Taylor^[167–169] proposed a very simplistic approach to explosive detonation which hypothesised an instantaneous release of energy from a infinity small point in space resulting in a radially expanding shock front. In actual fact, detonation occurs over incredibly small time scales, with the ongoing reactions exhibiting high complexity chemical decomposition and oxidation processes. Zukas and Walters^[182] proposed assumptions for the detonation process which enabled a more robust approach to be adopted to understand an explosives detonation behaviour:

- The implementation of a one dimensional analysis which considers detonation prod ucts only propagating behind the shock front with no lateral loses i.e and infinite
 charge diameter.
- In reality, all charges have a finite boundaries which means loses in energy de velopment will incur due to product expansion prior to full potential detonation
 reactions occur
- A perfectly planar detonation wave propagates through the explosive to avoid shock
 front curvatures.
- When the detonation front reaches the finite boundaries and energy is lost,
 the front slows at its peripheries and propagates at higher speeds towards the
 centre of the charge, therefore exhibiting a curvature.
- The reaction is perfectly stoichiometric and occurs instantaneously, with detonation
 products being in thermodynamic equilibrium.
- Detonation by nature is not in thermodynamic equilibrium, the reaction process
 occurs over some finite amount of time.
- The whole process occurs at constantly velocity which in itself assumed a steady state reaction zone.

762 763 Detonation velocity is directly proportional to the reaction process and therefore is not a constantly velocity in line with the point above.

With these assumptions in mind, the accepted view of a high explosives detonation structure consists of four distinct reaction regions, quoted by Paterson^[111] and displayed in Figure 2.1:

767 768 1. The pre-detonation region which is yet to be subjected to the propagating shock wave and therefore the composition is unaffected.

2. The leading shock front, travelling at supersonic velocities, compresses the explosive 769 and initiates the detonation through exothermic decomposition of molecular bonds. 770 In the simplest form, detonation theories presented by Chapman^[26] and Jouguet^[84] 771 (C-J) assumed the reaction to occur instantaneously with the flow becoming sonic 772 at the C-J point. At this point, the energy released behind the sonic front is able to 773 support the detonation front at constant velocity and pressure^[55]. von Neumann^[177] 774 however argued that detonation was to occur over a finite time and reaction zone 775 length, resulting in a significant difference in pressure and temperature either side 776 of this region. This was further developed to consider the existence of an induction 777 period of time related to reaction initiation time lag once compressed by the leading 778 detonation wave $^{[166]}$. 779

3. The reaction zone, in which an increasing amount of energy is released with a function of distance travelled along a given explosive composition, results in an acceleration of the products away from the shock front and therefore propelling the shock front forward^[11]. The reaction zone is a function of characteristic time taken for the chemical decomposition of the explosive and therefore the rate at which energy is released.

4. Upon reaction completion, the detonation products begin to expand with the loss
of inertial confinement of the solid state with a rarefaction wave travelling in the
opposite direction the detonation wave^[31].



Figure 2.1: Schematic representations of detonation theories: C-J theory (left) displaying the planar like pressure wave with distance and no lateral losses, and the theory proposed by von Neumann^[177] (right) which details finite reaction zones and detonation product expansions. Note the numbering system aligns with detonation process discussed above.

The detonation theories outlined categorise explosives in to two groups: Ideal and non-789 ideal explosives. Ideal explosives, when detonated, exhibit behaviours which are captured 790 by C-J theory with high levels of agreement through the use of thermochemical com-791 puter codes^[48], such as Cheetah^[58] and EXPLO5^[161]. These tools have integrated the 792 C-J theory into their methodology, to predict the behaviour of an explosive based on its 793 composition, heat of formation and density^[179]. In reality, most commercial available 794 explosives, and certainly all home-made explosives (HME), often result in detonation ve-795 locities and pressures which do not follow C-J theory, labelled non-ideal^[159]. This group of 796 explosives are generally heterogeneous fuel-oxidiser mixtures which when detonated result 797 in non-monotonic relationships between detonation and density which is not captured by 798 thermochemical calculations $^{[114]}$. 799

800

The C-J theory makes the assumption that for a planar detonation in an infinite diameter charge, D_{∞} , the reaction zone structure would not alter the maximum velocity of detonation to which is calculated^[75]. The reality is that charges have a finite diameter and therefore are subjected to lateral energy loses through detonation product expansion, thus never exhibiting their maximum potential velocity. Fundamentally, as the diameter of an explosive composition reduces, the amount of energy lost through product expansion increases, resulting in detonation behaviours unclassifiable by standard C-J theory. This reduction in energy continues up to the diameter at which the reaction zone no longer releases enough energy to sustain the detonation process^[142], called the critical diameter of an explosive composition, d_{cr} .



Figure 2.2: Schematic representations of detonation velocities and how they vary with charge diameter for ideal (dashed) and non ideal (solid) explosives adapted from work presented by $Scott^{[142]}$.

The reason C-J theory is unable to capture the behaviour of non-ideal explosives is due 811 to the assumption that reactions occur instantaneously. An increase in non-ideality of 812 an explosive is a direct result of a larger reaction zone and characteristic time for full 813 decomposition of the explosive to occur. For military grade explosives, which exhibit ideal 814 like behaviour, the reaction zone length are small (~1mm) and therefore the d_{cr} can be 815 within a few millimetres. For the non-ideal explosives, the reaction zone is significant 816 larger (~10mm) meaning the d_{cr} is orders of magnitude bigger^[94]. This behaviour is rep-817 resented by Figure 2.2. 818

2.3 Air Shock Formation

Once the detonation process reaches the extents of an explosive composition there is a dis-821 continuity between it and the surrounding medium. This discontinuity results in both the 822 rapid expansion of detonation products into the surrounding medium and a reflective wave 823 propagating back towards the detonation epicentre. The expanding detonation products 824 displace the surrounding medium at speeds dependent on the magnitude of energy con-825 tained within the wave itself. Air is the medium of choice within this thesis it is important 826 to note that it is a compressible fluid. This means that rapid expansions and disturbances 827 to the surrounding air results in higher pressure components of the expansion travelling 828 quicker than the lower pressure components over small periods of time. This transitions 829 the expansion into an effectively instantaneous increase in pressure and density, propa-830 gating away from the explosive in the form of a shock (or blast) wave^[7], represented by 831 Figure 2.3. It is important to note that Figure 2.3 represents the fireball and shock wave 832 breakout of a hemispherical charge. Shapes which exhibit geometrical variations would 833 result in different breakout procedures and thus loading conditions in near-field regimes 834 which self-heals far-field. 835

836



Figure 2.3: Schematic representation of the formation of air shock from hemispherical explosive detonation: Depicted by Initial pressure pulse related to the detonation product breakout (left), transitioning into a front loaded pulse due to a range of particle velocities (middle) to a point where a near-discontinuous shock wave forms (right), adapted from Kinney and Graham^[90].

The detonation of an explosive and the subsequent expansion of the gaseous fireball products displace the surrounding air and compresses it into a high pressure discontinuity with undisturbed air ahead of it. As the expansion propagates, a temporal decay in pressure and velocity back to ambient air pressure is experienced. For spherical/hemispherical explosive charges, the detonation product cloud halts its expansions at distances some 20 charge diameters away from the epicentre, which up til this point would be described as the near-field regime^[173]. The shock wave preceding the detonation products continues to propagate radially until it either interacts with a target (reflected) or decays away (incident), defined as the far-field regime. Figure 2.4 provides a visual representation of this behaviour.

847



Figure 2.4: Schematic representation of the the different scaled distance regimes discussed by $Tyas^{[173]}$

It is important to note that common blast engineering practices consider far-field regimes, 848 in which an air shock is fully formed and has propagated far enough away from the detona-849 tion epicentre to not be affected by the fireball. In close proximity to the detonation, where 850 the air shock has not detached from the fireball, the current knowledge of blast loading 851 is significantly undefined. This is due to the difficulty in measuring such high pressures 852 and impulses without damaging equipment. In conjunction to this, any interaction in this 853 regime is a result of both fireball products and potentially a slower loading profile, as seen 854 in Figure 2.3. 855

856

Naturally, there are a number of variables which dramatically affect the characteristics of these shock waves including: the distance the explosive is away from a target, known as the standoff distance; the shape, size and type of the explosive used; and both the detonation and interaction mechanisms occurring which alter the intrinsic characteristics of the waves. For the contents of this thesis, hemispherical charges are the only shape considered to make direct comparisons with the broad range of historical data available. Having an understanding of how each of these parameters effects the characteristics of a shock wave is important for probabilistic-based analysis of loading conditions on a structure.

865

878

Figure 2.5 presents an idealised shock wave pressure-time history defined as the modified 866 Freidlander waveform which can be approximated by Equation $(2.1)^{[57]}$. Considering a 867 point far enough away from the detonation epicentre to be characterised by a fully formed 868 air shock, the behaviour is characterised by a near-instantaneous rise in overpressure, P_{so} 869 and P_r for incident and reflected results respectively. This has a characteristic arrival time, 870 t_a , and a temporal decay back to ambient conditions, P_o , which occurs over a duration 871 of time, t_d . The waveform parameter, b, controls the decay of the pressure-time curve. 872 Through integrating the pressure-time history with respect to time, a impulse-time history 873 can be plotted. This can be attributed to the change in momentum, or specific impulse 874 i, a given area experiences from the different loading conditions, denoted by the coloured 875 regions in Figure 2.5. This period of a shock waves behaviour is defined as the positive 876 phase which is considered the most destructive part of blast loading $^{[182]}$. 877



Figure 2.5: Indicative Freidlander shock wave pressure-time history with reference to both reflected (red) and incident (blue) forms with respect to each other.

$$P(t) = P_{max}(1 - \frac{t}{t_d})e^{-b\frac{t}{t_d}}$$
(2.1)

The rapid overexpansion of the medium results in a lower density partial vacuum be-879 hind the shock front which forces air back towards the detonation epicentre to maintain 880 equilibrium conditions, defined as the negative phase of a shock wave^[107]. Similarly to 881 the positive phase, the time taken for conditions to return to ambient is defined as the 882 negative phase duration, t_{d-} , with the maximum underpressure defined by $P_{so,min}$ and 883 $P_{r,min}$. Figure 2.6 presents a schematic of the negative phase mechanism which details 884 the aforementioned processes. It is important to note that for hemispherical charges, the 885 negative phase measured at the ground surface is found to be greater due to the rising 886 fireball. This creates a convectional lower pressure regions, thus resulting in a greater 887 underpressure^[133]. Further to this, at some time after the arrival of the positive phase, 888 secondary and tertiary waves arrive at the same recording position. This phenomena is 889 a result of rarefaction waves from detonation product expansion, coalescing at the point 890 of detonation, and reflecting radial outwards. This is similar to a pulsing-like effect with 891 subsequently lower yields associated with each iteration of shock. 892

893



Figure 2.6: Indicative behaviour of negative phase process: Pre-detonation of charge with reference air particles (left), and Post-detonation with reference to shock wave condensed air particles, leaving a vacuum with an under pressure.

⁸⁹⁴ 2.4 Secondary Shock

⁸⁹⁵ Needham et al.^[106] discussed the phenomena of secondary shocks occurring sometime af-⁸⁹⁶ ter the formation and propagation of a primary shock, resulting in an imploding moving ⁸⁹⁷ shock which coalesces at the detonation epicentre and reflects back outwards. The results ⁸⁹⁸ of this process is presented in Figure 2.7, where P_{SS} is the associate shock pressure and ⁸⁹⁹ td_{ss} is the phase duration of the secondary shock. Whilst the feature is documented across a number of articles^[7], historically there seems to have been little effort made to quantify or characterise its effects. This is mainly due to exhibiting low yields and therefore corresponding to low impact on structures or civilians.



Figure 2.7: Indicative Freidlander shock wave pressure-time history with reference to the secondary shock phenomena and the blast parameters associated.

Work presented by Gitterman and Hofstetter^[62] began to compile a considerably large 904 data set of the secondary shock arrival time, and its subsequent delay after the arrival of 905 the positive phase, across a range of explosive compositions, sizes and scaled distances. 906 The reason for this analysis was to help improve the predictions of negative phase pa-907 rameters as currently numerical models struggle to capture them with definitive accuracy. 908 With near-field blast parameters within the fireball holding difficulty to prescribe with 909 standard methods, it is believed that the behaviour of a secondary shock could be used as 910 an indicator for post-detonation products within the fireball. 911

912

With the aforementioned in mind, the secondary shock delay parameter, τ_{ss} , was introduced by Rigby and Gitterman^[129] who attempted to normalise each explosive by scaling the delay parameter by standard detonation velocities and the cube-root of the packing

density, defined by Equation 2.2. The thinking behind this methodology was to correlate 916 the parameter with the characteristic time for complete detonation of a finite hemispheri-917 cal charge, where ρ is charge density, V_{od} is velocity of detonation, W is charge mass and 918 δt_{ss} is the time difference in arrival times between primary and secondary shocks. The 919 data presented in Figure 2.8 was obtained from the authors of the aforementioned articles 920 and improved by including standard TNTe values for each explosive, which seemed to 921 provide increased linearity of the data when compared to the least-squares fit defined by 922 Equation 2.3. 923

$$\tau_{ss} = \delta t_{ss} V_{od} / (\rho W)^{1/3} \tag{2.2}$$

$$\tau_{ss} = 2.45 \log_{10}(Z) + 1.36 \tag{2.3}$$



Figure 2.8: Secondary shock delay parameter evaluated for all explosives scaled accordingly compared with a least-squares fit to data, extracted from Rigby and Gitterman^[129]

The least-square fit, detailed by Equation 2.3, was tested against experimental data and theoretical examples presented by Rigby and Gitterman^[129] and was found to provide remarkably accurate results. The issue with this methodology is that the secondary shock parameter defined by this analysis has units of $m^2/kg^{2/3}$ which holds no physical meaning and therefore a different consideration is required to assign a real mechanism to the behaviour.

930

Despite analysis undertaken of the large data for the delay in arrival time ^[62,129,133], there is still a gap in characterising the other secondary shock blast parameters. There is a need for a theoretical mechanism which captures the behaviour of secondary shocks across a variety of explosives and scaled distances which can be implemented into predictive tools to provide more realistic and valid predictions.

936

937 2.5 Scaling Laws

938 2.5.1 Mass and Energy Proportionality

A fundamental finding proposed separately by Hopkinson^[74] and Cranz^[33], suggested 939 that through cube-root scaling of the distance a charge is away from a target, results 940 in consistencies in the yields from two different explosive charge. This can be achieved 941 provided the same shape of charge and direct equivalent masses can be established. This 942 means that the blast parameters at a given distance away from the centre of the explosive, 943 R, with mass, W, will be comparable to that at a distance, KR from a mass of K^3R . 944 As a blast wave spherically propagates, energy dissipates into the surrounding medium in 945 all three dimensions, hence the cube-root scaling, which led the aforementioned authors 946 to develop Equation 2.4, where E, is the energy released per unit mass of the explosive 947 material. 948

$$\frac{R}{E^{1/3}} = \frac{KR}{(K^3 E)^{1/3}} \tag{2.4}$$

The amount of resulting energy produced upon detonation of an explosive, is inherently dependent on the equivalent mass of the explosive, W. This leads to Equation 2.5, which introduced the notion of scaled distance, Z, measured in units of m/kg^{1/3}.

$$Z = \frac{R}{W^{1/3}} = \frac{KR}{(K^3W)^{1/3}} \tag{2.5}$$

The Hopkinson^[74] and Cranz^[33] cube-root scaling, assumes the pressure associated with a blast is directly proportional to the energy released so does not require scaling. It is only time-related parameters which require scaling by the cube-root of the explosive mass Kinney and Graham^[90].



Figure 2.9: Representative schematic of Hopkinson^[74]-Cranz^[33] scaling, adapted from Baker^[7]

956 2.5.2 Charge Shape

The effect of charge shape has been investigated throughout literature to assess and char-957 acterise the differences in the blast parameters induced. Both Wu et al.^[180] and Sherkar 958 et al.^[146] undertook the numerical simulation of explosive detonation for spherical and 959 cylindrical across a range of scaled distances, charge orientations and detonation positions 960 on the charge. Presented were the distributions in blast parameters which concluded that 961 charge shape has a significant effect. When standoff distance from the detonation point is 962 greater than 35 charge diameters $Z>3m/kg^{1/3}$, the effect of charge shape can be ignored. 963 Similar ranges were presented by Xiao et al.^[181], but all came to the agreement that the 964 information presented was not sufficient enough to identify the precise scaled distance at 965 which charge shape effects could be ignored definitely. Shi et al.^[147] countered this finding 966 when a variety of 1kg TNT explosive trials consisting of four different charge shapes in 967 near-field scenarios were conducted and agreed that the blast parameters recorded are 968 far more sensitive in the near-field when non-spatial symmetry of an explosive creates 969 non-uniform detonation processes. This was displayed by high speed video frames which 970 showed how variability in breakout shape decreased with scaled distance but only becom-971 ing negligible at $Z > 5m/kg^{1/3}$. 972

973

Spherical and hemispherical charges exhibit far more similarities through radial detonation mechanics and subsequent shock wave breakout. Early works presented by Brode^[19] undertook numerical simulations of spherical blast waves which have been used in conjunction with experimental trials using large scale TNT hemispheres^[87] to develop fast-running engineering computer codes, such as ConWep^[76]. These methods were all based on the assumption of spherical charges detonation in free air, or a hemispherical charge detonation on a flat surface.

981

Assuming a perfect reflecting plane, a hemispherical charge of mass, W, in theory a spher-982 ical charge of mass, 2W, would produce the equivalent blast parameters. The issue with 983 this theory is that in reality, hemispherical charges detonated on a ground surface would 984 result some energy be lost through cratering. A shape factor of 2 in this instance would 985 be conservative, however the aforementioned work presented a realistic factor of 1.8. This 986 has been integrated within design code and are validated for spherical and hemispherical 987 charge^[135]. These simplistic scenarios are fundamental to continue the understanding into 988 both detonation and shock wave mechanics. Although uncommon within real-world blast 989 application, without a robust knowledge on the behaviour of blast loading in simplistic 990 scenarios, confidence in the understanding of non-spherical explosive detonation will never 991 be established. 992

993

⁹⁹⁴ 2.6 Semi-Empirical Prediction Methods

995 2.6.1 Positive Phase Parameters

As mentioned previously, Taylor^[167], Brode^[19] and Granstrom^[66] were the pioneers of explosive shock wave prediction. Their developing theories which assumed instantaneous energy release at a infinitesimal small point source captured the behaviour of simple explosive scenarios. These however were not perfectly applicable for use when considering the effects loading as on infrastructure^[126].

1001

There has been significant research since, expanding the fundamental understanding of explosive events alongside characterising resulting blast wave features through experimental

1006

1021

analysis^[85]. Baker^[7], Remennikov^[123] and Esparza^[45] all provide summaries of contem porary and historical experimental quantification of blast parameters.

Discussed in more detail within Section 2.9.2, is this history around the quantification 1007 of blast loading and the effects imposed on structures. The broad range of works in-1008 vestigating high explosive detonations was collated by Kingery and Bulmash^[87], whom 1009 presented high-order polynomial relationships which capture the explosive behaviour of 1010 spherical and hemispherical TNT detonations across scaled distances spanning from the 1011 edge of a explosive charge, out to around $Z \simeq 40 \text{m/kg}^{1/3}$. It is notable that the data 1012 collected was a combination of both direct measurements, in the far-field region, and in-1013 ferred measurements from tracking smoke trials^[37]. This was supported with rudimentary 1014 numerical analysis, in the near-field^[19], therefore holding this region in doubt of its fidelity. 1015 1016

The high-order polynomial relationships only exhibit the behaviour of TNT detonations across a scaled distance range and therefore should not be mistaken for a representation of a physical mechanism directly. With this being said, the relationships are usually summarised and used as a set of well defined curves, as presented in Figures 2.10a-b.



Figure 2.10: The semi-empirical curves for incident and reflected positive phase blast wave parameters for a 1kg TNT explosive detonation with respect to scaled distance, established by Kingery and Bulmash^[87]: a) Hemispherical charge of TNT detonated of a ground surface, b) Spherical charge of TNT in free air.

1022 2.6.2 Negative Phase Parameters

The positive phase of a blast event is reasonably understood in terms of the underly-1023 ing fundamental physics. Vast quantities of experimental and numerical work have been 1024 conducted to characterise and quantify the associated blast parameters and to validate 1025 empirical predictions, as discussed in Section 2.9. Whilst negative phase parameters are 1026 available in literature and blast related design manuals^[176], Bogosian et al.^[13] presented 1027 scepticism of the associated empirical curves due to the original data source being unclear. 1028 Rigby^[126] undertook a thorough review of available historical literature and highlighted 1029 the work by Granstrom^[66] to be the likely source of data used to develop the empirical 1030 curves, seen in Figure 2.11. This is defined as the 'Cubic Negative' curve fit approximation 1031 (detailed in the second case of Equation 2.6). 1032



Figure 2.11: The semi-empirical curves for incident and reflected negative phase blast wave parameters for a 1kg TNT explosive detonation with respect to scaled distance, established by Granstrom^[66]: a) Hemispherical charge of TNT detonated of a ground surface, b) Spherical charge of TNT in free air.

There is however, limited validation of the negative phase on the whole with many researchers historically omitting their effects due to the associated parameters being orders of magnitude lower than the positive phase. The physical mechanisms ongoing during this

23

time of lower pressure in reality can still pose some serious threats to infrastructure andcivilians.

1039

$$P_{r}(t) = \begin{cases} P_{r,max}(1 - \frac{t}{t_{d}})e^{-b\frac{t}{t_{d}}}, & t \le t_{d}.\\ -P_{r,min}(\frac{6.75(t - t_{d})}{t_{d}^{-}})(1 - \frac{(t - t_{d})}{t_{d}^{-}})^{2}, & t_{d} < t \le t_{d} + t_{d-}. \end{cases}$$
(2.6)

1040

1041

¹⁰⁴² 2.7 TNT Equivalence

The mass term, W, referred to throughout this section is actually the equivalent charge 1043 mass in kilograms of trinitrotoluene (TNT), which is widely accepted as the benchmark 1044 in explosive characterisation. Discussed in more detail with Section 2.9.2, the quantity 1045 of TNT free-air testing which has been conducted over a multiple decades. These were 1046 collated by Kingery and Bulmash^[87] and used to develop semi-empirical predictive curves 1047 for 1kg TNT explosives, shown in Figures 2.10 and 2.11. Using these, the results of det-1048 onating explosives of differing compositions have been collated, with their masses scaled 1049 until predictions of 1kg of TNT are able to accurately capture the behaviour of an equiv-1050 alent mass of the given explosive. This scaling factor is defined as the TNT equivalence, 1051 TNT_e . 1052

1053

The problem with TNT equivalence is mainly the lack of significant rigour associated 1054 with the testing methodologies adopted for establishing the parameter. $Cooper^{[30]}$ out-1055 lined in the overview on TNT equivalence that historically there have been various and 1056 widely different testing methodologies to estimate the factor, all of which exhibit their 1057 own uncertainties. This is a direct cause of the published spreads in TNT_e for nominally 1058 identical charge masses and compositions tested, and therefore the same energy release. 1059 It is noted, that in the extreme near-field, where the recorded blast parameters are highly 1060 proportional to the fireball chemistry, different explosive compositions will exhibit a vary-1061 ing TNTe as a result different chemical de-combustion^[81,151]; a finding which was verified 1062 by Shin et al. [149]. 1063

1064

¹⁰⁶⁵ Further justifying the sensitivity of detonation characteristics in the near-field was works

presented by Simoens and Lefebvre^[152]. A variety of experimental trials highlighted how the detonator position, and thus the associated detonation process, caused variations in pressure recordings but impulse effectively stays constant. This is due to impulse being directly related to the overall energy released during detonation. If using impulse as the only measuring parameter for TNT equivalence, the theory proposed by Taylor^[167, 168, 169] on explosives being theorised as infinitesimally small points of energy release would hold credibility.

Far-field scenarios, the region is which the shock wave detaches from the fireball and 1074 therefore no longer influenced by the ongoing thermochemical combustion reactions, there 1075 is presently no physical explanation for TNT equivalence to vary. Dewey^[38] used high 1076 speed video techniques to track a propagating shock wave resulting from a hemispheri-1077 cal propane-oxygen explosion and converting its velocity into the shock waves pressure 1078 through Rankine-Hugoniot relationships^[7]. A constant TNT equivalence value within the 1079 far-field range, Z>3m/kg^{1/3}, was evaluated. Similar findings have been presented when 1080 conducting both well-controlled PE4 explosive trials in far-field regimes and comparing 1081 them to high fidelity numerical simulations, both converge on a $\text{TNT}_{e} \simeq 1.2^{[132,135]}$. How-1082 ever despite a broad range of published literatures attempting characterise this factor for 1083 different explosives, there is no widely accepted methodology of establishing $\text{TNT}_{e}^{[32]}$. 1084 Some authors exhibiting large variation in TNT equivalence across an entire scaled dis-1085 tance rather than variability being confined to the near-field domain [56]. 1086

The TNT equivalency factor of an explosive composition is highly related the variability associated in experimental data captured. It therefore requires further investigation to establish whether all explosives can be defined by an equivalent mass of TNT, or whether variations are inherent of explosions.

1092

1087

¹⁰⁹³ 2.8 Blast Variability - Real or Systematic?

Explosive testing within the available literature provides a wide variety of methodologies for undertaking experimental blast work and the analysis of the resulting data. However, varying conclusions regarding the output yield a given explosive has when detonated a certain distance from a target, alongside the associated variability it exhibits between

¹⁰⁷³

nominally identical tests, have been made. There is therefore a necessity to further im-1098 prove current practices and develop new techniques for experimental testing and data 1099 processing to ensure the fundamental understanding of shock wave propagation is fully 1100 understood. Clearly, if blast experiments are viewed as naturally varying, approximate, 1101 and even first-order in nature, then our ability to rigorously validate numerical modelling 1102 approaches is hampered. This clearly has negative connotations for the use of modelling 1103 tools for design. It is important to fully understand the nature of blast parameter vari-1104 ability, and its dependence on extrinsic features such as experimental set up, control, and 1105 interpretation of data. The contention around this subject matter however poses a clear 1106 need for defined experimental procedure which adopt precision. These require validation 1107 to encouraging a movement towards an acceptable experimental and analytical standard 1108 which provides a consistency in resulting blast parameters from explosive testing. 1109 1110

Whilst any published article will defend and justify its findings, multiple contrasting con-1111 clusions regarding explosive variability from similar testing regimes, cannot all be scientif-1112 ically correct. The philosophy around research in modern times, for blast engineering in 1113 particular, has seemingly moved away from critically analysing why certain data appears 1114 to exhibit particular trends, making links through tangible justification of fundamental 1115 physical mechanisms and principles. Instead, a more literal acceptance of recorded data 1116 is commonly taken. Inductively creating theories justifying the accuracy of the data re-1117 gardless of the underlying physics required for the data to be valid. 1118

The Falsification Principle, proposed by Popper^[113], suggested that scientific theory should make predictions which can be tested, and the theory rejected if these predictions are shown to be incorrect. Adopting critical rationalism is something which enables science to hone in on realistic physical theories which is void of highly-controlled experimental data to falsify them. Take the paradoxical opinions in the blast community regarding consistency in blast parameters; what are the underlying reasons for why different research groups are experiences varying levels of consistency?

1127

1119

It is of great importance to establish the route causes for these conflicting conclusions and to develop best practices based on the findings. This chapter will access the features of a blast waves development as it propagates away from the source of the detonation. Through careful analytics, experimental procedures and improved methods of analysis are ¹¹³² proposed for use across a range of idealised high explosive types.

1133 2.9 Historical Review of 'Best' Practices

The measurement of shock wave data from explosive events has been of interest since the first explosion occurred, most probably around similar times as the invention and subsequent detonation of gun powder. The ability to release significantly large quantities of energy over small periods of time through detonation, created an interest in developing weapons to release shock waves of catastrophic capabilities^[63].

1139

With increasing interest into powerful energetics came extensive testing regimes which looked at detonating large quantities of various types of explosives. This required instrumentation to record characteristics of these events to provide a fundamental understanding of shock wave phenomena. Due to the threat severity of nuclear war at the time, instrumentation engineers and scientists were faced with an incredibly difficult task of recording the effects of equivalent blasts with limited resources and time constraints.

1146

The development of best practice for blast damage and shock data capture is not some-1147 thing which came easy, and has taken many decades to establish reliable instrumentation 1148 in which these events can be recorded with the highest levels of precision. Shelton^[145] 1149 documented that during the first nuclear tests conducted by the US, 'blast damage and 1150 shock data were obtained by two methods: those that were improvised by inquisitive sci-1151 entists; and those that were measured by sophisticated instruments'. The creativity and 1152 innovation from the scientists working on these large scale trials are to be commended 1153 for having a well-rounded understanding of fundamental explosion physics enabling their 1154 efforts in effective instrumentation development. The iterative procedure of testing and 1155 modifying instrumentation over many years resulted in the technology available for us 1156 today. It is however important to establish the historical context of how these instruments 1157 came to be developed. This will help understand why the current methodologies adopted 1158 for testing results in sporadic data sets between nominally identical trials. 1159

1160

Reisler et al.^[118] meticulously reviewed all available literature, both within the public domain and that which is classified. The article detailing the testing and development of systems which were capable of not only withstanding, but recording disastrous effects

from nuclear explosions. The vast majority of devices deployed during these early tests 1164 were passive, inexpensive to produce and required minimal effort to deploy. These how-1165 ever, reported spreads in accuracy of shock wave parameters between 10-20% of the values 1166 numerically predicted. As the development of electronic transducers began, data could be 1167 recorded with respect to a time base, thus establishing a detailed understanding of the 1168 development of explosive shock wave phenomena from the instance of detonation. These 1169 transducer measurements were found to obtain accuracies of between 3-5% which showed 1170 vast improvements in the quality of data recorded despite their need to be coupled with 1171 electronic recording systems such as oscilloscopes. 1172

1173

This brings the thinking back to that discussed by Shelton^[145], in that there was a skill, 1174 and in some scenarios improvisation, required to use these systems to record highly accu-1175 rate data. The capabilities of these scientists to understand and predict what the effects 1176 of a given explosive should be, and testing their predictions against constantly evolving 1177 instrumentation provides definitive confidence in their research. It is safe to conclude that 1178 the instrumentation developed during the nuclear period was successful at capturing shock 1179 parameters with accuracy for long duration blast waves. Despite the era these instruments 1180 were developed, the quoted accuracy of between 3-5% when comparing recorded data to 1181 numerical models are within the similar regions to modern research programmes looking 1182 into high explosive detonations $^{[135]}$. 1183

1184

The use of high explosives for large scale blast phenomena analysis closely followed the 1185 initial ban on atmospheric testing of nuclear explosives in 1958. The reason for this was to 1186 provide effective simulations of a nuclear weapon's blast characteristics without the ma-1187 jor environmental concerns of nuclear detonation. The majority of the instrumentation 1188 adopted for testing at the start of this era was that which were established during the 1189 nuclear testing era. This movement meant that measuring devices no longer required the 1190 need to be radiation-resistant but did require the response and recording rates of gauges 1191 to be considerably faster relating to much shorter shock wave durations associated with 1192 high explosives^[8]. Reisler et al.^[119] again provided a comprehensive overview of the de-1193 velopment of instrumentation during this period. Detailed was how the state of the art 1194 recording systems for electronic gauges progressed from the 20-40 kHz frequency of record-1195 ings range to 500 kHz through the use of digital recording systems which are still used 1196 today. This still achieved the high accuracy recorded data when compared to numerical 1197

1198 models.

1199

Blast related research placed greater demands on data capture systems to provide increased 1200 frequency response whilst upholding precision in the data. However, greater temporal ac-1201 curacy of recordings does not necessarily result in consistency and reliability of recorded 1202 data from repeat trials. The knowledge of what an experimental trial is aiming to accom-1203 plish and an understanding of the physical processes any given instrumentation uses to 1204 capture the data is paramount for achieving reliable and accurate data. When reviewing 1205 the quality of published works between the start of shock wave quantification in the 1940's 1206 all the way through to modern times, there is a clear discrepancy in the results published 1207 which requires investigating. 1208

1209

¹²¹⁰ 2.9.1 Data Capture between 1950 - 1980

Corresponding to the era in which instrumentation was being constantly tested and im-1211 proved, the research undertaken into blast phenomena produced some of the more widely-1212 regarded data sets which helped develop semi-empirical prediction tools for free-air blast 1213 scenarios^[87]. This well-known method utilises poly-logarithmic curves fitted to the com-1214 pilation of both rudimentary numerical analysis results and experimental measurements 1215 ranging from small to large scale events (< 1 kg to >400,000 kg). These semi-empirical 1216 curves are generally accepted standard practice for predicting blast loads from a given 1217 explosive mass at a given distance from the target. As a result, the KB method has been 1218 implemented into the UFC-3-340-02 design manual^[176], the predictive computer code Con-1219 wep^[76,77], and commercial finite element code LS-DYNA^[116]. 1220

1221

Figures 2.12a-d present experimental recordings from TNT charges with masses between 1222 0.45 - 450,000 kg, which were spherical and hemispherical in shape, recovered from 22 1223 individual references dated between 1940 and 1980 (of which were discovered in Reisler 1224 et al.^[119] and documented in Table 2.1, The data points have been scaled to an equivalent 1225 hemispherical shape, if required, using a shape factor of $1.8^{[76,77]}$, and 1kg in mass to 1226 compare accordingly with KB predictions. Despite a low amount of anomalous results, 1227 the four positive phase parameters compare well with the KB curves and are fairly con-1228 sistent across the entire tested scaled distance range. It is worth noting that Kingery and 1229 Bulmash^[87] made use of some of the presented data in order to produce the high order 1230

polynomial predictive curves, so whilst this comparison is self-referential, it does highlight
the general consistency of the measured blast parameters during this era across a full range
of charge masses and distances.

1234



Figure 2.12: Compiled blast parameters from TNT explosive trials with varying mass as a function of scaled distance, which has been scaled to a 1kg equivalent hemispherical charge, using a shape scaling factor of 1.8 and compared with KB predictions: a) Peak overpressure, b) Scaled peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration

Figures 2.13a-d again present experimentally recorded blast parameters when detonating Pentolite - another commonly-used high explosive at the time. A variety of smaller scale masses of between 0.1-3.8kg, of which a collection of spherical and hemispherical charges were used. The raw data was scaled accordingly to be equivalent in shape and size to a surface burst 1kg hemisphere of TNT. The data presented was extracted from 6 individual references, detailed in Tables 2.1 scaled to an equivalent TNT explosive using a TNTe = 1241 1.2. This value is in line with averages for both pressure and specific impulse in far-field 1242 scenarios evaluated by Shin et al.^[149].

1243



Figure 2.13: Compiled blast parameters from Pentolite explosive trials with varying mass as a function of scaled distance, which has been scaled to a 1kg equivalent TNT hemispherical charge using a shape scaling factor of 1.8, and a TNTe = 1.2 (Shin et al.^[149]), comparing to KB predictions: a) Peak overpressure, b) Scaled peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration

The consistency in this data is much the same as that presented in Figures 2.12a-d and holds good agreement with the KB predictions. These two extensive data sets provide reasonable evidence to support the hypothesis that explosive positive phase parameters are predictable for ideal high explosives across a range of charge sizes and scaled distances. It is also important to note that, although not perfect for every single data point, a single TNTe value can be used to establish a generalised equivalent behaviour of ideal explosives. This does however begin to exhibit higher variations at small scaled distances, $Z < 1m/kg^{1/3}$. It is a reasonable conclusion to make that for far-field scenarios, $Z>3m/kg^{1/3}$, where the propagating shock wave has detached and is no longer effected by expanding fireball features, the positive phase blast parameters are consistent and can be defined by a single TNTe value.

Reference	Explosive Type
Granstrom ^[66]	TNT
Ammann and Whitney ^{$[2]$}	TNT
Dobbs et al. ^[40]	TNT
Fisher and Pittman ^[54]	TNT
Shear and Wright ^[144]	TNT
Kingery and Pannill ^[89]	TNT
$Groves^{[69]}$	TNT
Smale and $Sigs^{[155]}$	TNT
Chabia et al. ^[25]	TNT
Shear and $Day^{[143]}$	TNT
$Kingery^{[86]}$	TNT
Reisler et al. ^[121]	TNT
Reisler et al. ^[122]	TNT
Davis et al. ^[35]	TNT
$Swisdak^{[163]}$	TNT
$Esparza^{[44]}$	TNT
Kingery and Coulter ^[88]	TNT
$\operatorname{Rudlin}^{[137]}$	TNT
$\operatorname{Fisher}^{[53]}$	TNT
Weibull ^{$[178]$}	TNT
$Lutzky^{[95]}$	TNT
Reisler et al. ^[120]	TNT
Esparza and Moroney ^[46]	Pentolite
Johnson et al. ^[83]	Pentolite
Kingery and Coulter ^[88]	Pentolite
Sultanoff and $McVey^{[162]}$	Pentolite
$Goodman^{[64]}$	Pentolite
Goodman and Giglio-Tos ^{$[65]$}	Pentolite
Hoffman and Mills ^[73]	Pentolite

Table 2.1: Reference list for historic data extracted from within this era for both spherical and hemispherical TNT and Pentolite detonations.

¹²⁵⁶ 2.9.2 Data Capture between 1980 - Today

The accuracy of the KB method has been questioned over more recent years. Paradoxically, it would seem that with more modern and precise experimental procedures, the results should exhibit a reduction in uncertainty and an improvement on the precision. Many contemporary researchers have however reported a significant lack of repeatability in experimental measurements when comparing directly to KB parameters, and the much older data sets used to produce them.

1263

Bogosian et al.^[13] utilised an extensive experimental database of recorded explosive pa-1264 rameters and compared it with KB predictions of similar explosives. Typical uncertainties 1265 of between 70-150% and 50-130% for peak pressure and specific impulse respectively 1266 from nominally identical far-field $(1 < Z < 40 \text{m/kg}^{1/3})$ tests were presented. Similar levels 1267 of uncertainty have been found in related studies, with the general observation being a 1268 reduction in uncertainty as distance from the charge increases^[16]. Formby and Whar-1269 ton^[56] explored the TNT equivalence of a variety of hemispherical explosive compositions 1270 with the results demonstrating relatively high levels of variability: $\pm 30\%$ and $\pm 15\%$ for 1271 pressure and specific impulse respectively. These recordings were at large scaled distances, 1272 leading to a general impression that there will always be some degree of randomness in 1273 blast pressure measurements [156]. 1274

In Figure 1 of the article presented by Formby and Wharton^[56], a site layout includ-1276 ing pressure gauge position and height, in relation to explosive centre, was presented to 1277 highlight terrain features and large changes in surface height. The authors note that the 1278 presence of these features could influence the recorded data through inducing both wave 1279 reflection and/or shielding yet continue to suggest the yield of an explosive varies with 1280 scaled distance in a free-air scenario. Borenstein^[18] performed a sensitivity study of blast 1281 parameters taken from the 303 individual measurements discussed in Bogosian et al.^[13] 1282 and highlighted that these comprised of different explosive shapes, sizes and composition 1283 and were scaled directly to TNT as a collective. This resulted in quantification of a more 1284 extrinsic representation of blast parameter variability, which the authors seemingly incor-1285 rectly attributed to the inherent randomness of explosives. 1286

1287

1275

¹²⁸⁸ Stoner and Bleakney^[160] reported data recorded from free-air tests, using a variety of

charge shapes, sizes and compositions. When separated into nominally identical test groups and analysed, the results presented much lower levels of variability in pressure, between $\pm 0.6-6.5\%$, again with the observation that variability reduced with an increase in scaled distance. Esparza^[44,45] presented blast parameter results from a variety of high explosive compositions. Despite not quantifying variability in the recordings, visually the data holds agreement with itself for nominally identical tests.

1295

Tang et al.^[164] also undertook a variety of incident and reflected measurements from a 1296 range of PE4 masses, formed into spherical and hemispherical charges, resulting in similar 1297 magnitudes of variability quoted by Stoner and Bleakney^[160]. This experimental data was 1298 compared against both KB predictions and hydrocode numerical simulator, Air3D, which 1299 presented reasonable levels of agreement for medium to large scale charges^[165]. Reflected 1300 data agreed significantly better to KB predictions than incident pressures justified to be a 1301 result of the difficulty in recording purely incident shock waves. Rickman and Murrell^[125] 1302 and Tyas et al.^[175] conducted well controlled small-scale experimental high explosive test-1303 ing using pressure transducers which provided comparable results to KB predictions for 1304 normally reflected conditions at far-field scaled distances. 1305

1306

Ohashi et al.^[108] made use of optical methods to record shock wave propagation of smallscale explosive tests with varying masses. The article presented a method of converting radius-time data into incident pressure of a given shock wave using Rankine-Hugoniot jump conditions. The results of this analysis, when scaled, provided remarkably low variability between tests and also compare well with KB predictions.

1312

The articles mentioned show the other contrasting opinion of the blast industry in that 1313 KB predictions are incredibly accurate, and that variability between nominally identical 1314 tests should be minimal. Rigby et al.^[135] gave an in-depth literature review of articles 1315 which discuss experimental variability of far-field blast parameters and how they compare 1316 with the KB predictions. Systematic experimental and analytical errors are suggested to 1317 be the reason as to why such high levels of variability have been documented, rather than 1318 inherent randomness of explosive events. In an attempt to tackle systematic analytical 1319 variability, the authors used an exponential 'Friedlander' curve fitting method to deter-1320 mine blast parameters from each experimental trial in an unbiased manner. 1321

The results showed very good test-to-test consistency across the measured blast param-1323 eters (arrival time, reflected peak overpressure, and reflected specific impulse) typically 1324 within a range of $\pm 2.5\%$ (arrival time) and $\pm 6-8\%$ (pressure and impulse) of the mean 1325 values for each set of repeat tests. The recorded positive duration was the only parameter 1326 to exhibit higher levels of variability with all but one value achieving a $\pm 9\%$ range of 1327 the mean value. Positive phase duration typically exhibits higher levels of experimental 1328 spread due to the difficulty in determining when overpressure returns to zero when signal 1329 noise is present^[96]. No signal will ever be perfectly noiseless, and therefore the positive 1330 phase duration will always carry an enhanced level of uncertainty. Errors or uncertainties 1331 in this parameter contribute very little to the overall loading, since a curve fit can always 1332 be tailored with a different decay parameter in order to match a prescribed specific im-1333 pulse value. Hence, studying sources of uncertainty in positive phase duration are of lesser 1334 importance and will not be considered further. 1335

Chiquito et al.^[27] and Bogosian et al.^[14] both used similar methods of functional fitting curves to experimental data, and both presented results exhibiting enhanced consistency and reduced subjectivity of analysed blast data. The analytical techniques proposed account for errors during the post processing section of the testing but not account for any systematic errors which may have been introduced into the experiments during test setup.

The aforementioned articles and resulting data presents a clear divide in the blast community in whether it is reasonable or not to accept free air far-field blast parameters as inherently variable. As stated by Borenstein^[18], there are clear reasons as to why extrinsic and intrinsic sources of variability should be considered:

The generalised real-world application of predicting explosive parameters which in clude safety factors and variability margins accounting for the unpredictability of
 explosive size, shape, composition and separation distance from a target (extrinsic).

The specific, scientific approach of assigning precise loading characteristics for a
 particular charge shape, size and composition and looking at how removing those as
 independent variables results in increased consistency (intrinsic).

1353

1336

¹³⁵⁴ This provides an important, but seemingly overlooked steer to the blast research commu-¹³⁵⁵ nity: in order to produce robust and reliable models that account for *extrinsic* variations in ¹³⁵⁶ blast properties, it is imperative to understand and be able to quantify *intrinsic* sources of
¹³⁵⁷ variability. This is where well-controlled scientific testing and processing can make signif¹³⁵⁸ icant contributions to our understanding of, and ability to predict, blast load parameters
¹³⁵⁹ from *known* explosive sources.

1360

¹³⁶¹ 2.10 Non-Ideal Explosive Characterisation

When reviewing the last 50 years of both accidental and intentional terror related large scale explosive events, presented in Table 2.2, there has been an large number of lives lost, people exhibiting significant injury and money spent to remediate the destructive effects. Whilst the information presented in Table 2.2 does not cover every instance of explosive event across the world, it provides a range of masses and types of explosives causing catastrophic effects.

1368

Non-ideal explosives are common across the vast majority of events listed. Home-made 1369 compositions, such as ANFO, are the weapon of choice for most terror related threats 1370 due to the relative ease and low costs associated with acquiring their constituents. The 1371 accidental explosions noted in Table 2.2 were a direct result of stockpiling large quanti-1372 ties of material which does foster the ability to detonate under extreme circumstances of 1373 pressure and temperature. Take the most recent example which discusses the explosion 1374 of approximately 2750 tonnes of AN following a fire in the warehouse where it was being 1375 stored [131]. 1376

In 1963, the Nuclear Test Ban Treaty was enacted, which prohibited the detonation of nu-1378 clear weapons for any form of research. This caused problems for departments of defence 1379 and security across the globe due to an essential requirement to better understand the 1380 effects of devastating explosions on both military and civilian infrastructure. Large scale 1381 trials were conducted using TNT-stacked charges and provided data which is held in high 1382 regard for its accuracy (see Chapter 4), and was used to develop fast-running empirical 1383 models still used today^[87]. This data was the pinnacle of blast data capture for its time 1384 and has provided insights into the fundamental mechanisms and characteristics of explo-1385 sive shock waves. Through vast quantities of research making efforts towards quantifying 1386 and characterising other ideal high explosives (such as Pentolite, PE4, PE8, PE10 etc) 1387

¹³⁷⁷

across an entire range of scaled distances, numerical simulations have been extensivelyvalidated.

1390

The problem with testing regimes using ideal explosives is the cost associated with the 1391 large-scale trials and so an inexpensive and readily-available alternative in ANFO, was 1392 investigated to compare directly with tests conducted using TNT, and nuclear weapons 1393 prior^[112]. Large scale trials were conducted from the 1970s onwards, making use of hemi-1394 spherical charges with masses ranging between 18,000-572,000kg, boosted with various 1395 compositions of explosives at such small percentages of the overall mass they were con-1396 sidered negligible^[61,62,112,138,139]. The findings from these tests began to characterise the 1397 general behaviour of ANFO as an explosive used alternatively and led to an empirical 1398 $TNTe=0.82^{[112]}.$ 1399

1400

As previously mentioned, an ideal detonation is one in which its temporal characteristics 1401 of velocity, time and pressure match those of which can be predicted through theoretical 1402 evaluation. Assuming a planar detonation in an infinite diameter charge, the detonation 1403 process would be independent of reaction zone size, in which case the detonation wave 1404 would propagate at a maximum theoretical value within the charge Horie^[75]. In reality, 1405 charges with a finite diameter are dependent on reaction zone, of which large ones result in 1406 larger losses of energy and thus detonation performance. For every explosive composition 1407 there is a thermodynamic break point at which the diameter is so small detonation cannot 1408 be sustained, denoted by the critical diameter C_d . Ideal explosives are described to exhibit 1409 small reaction zones and thus compare well to theoretical predictions of temporal char-1410 acteristics. Non-ideal explosives, such as ANFO, are known to have much larger reaction 1411 zones - in the order of 100mm^[29]. Scott^[142] suggested that explosive compositions with 1412 large critical diameters as a result of large reaction zones, require much greater masses to 1413 achieve steady detonation which compare to theoretical values. Despite this knowledge, 1414 the findings from the large scale testing of ANFO when collated by Petes et al.^[112] in-1415 fluenced the idea that the non-ideality of ANFO was irrelevant as a seemingly constant 1416 TNTe was assigned to the composition. 1417

1418

Figure 2.14 contains a compilation of data from 7 different testing regimes (see Table 2.3), 6 of which are large scale hemispherical and spherical ANFO trials in free field scenarios and the2 containing smaller mass regimes. It is important to note that whilst the

Effects	57 I, \$13.6million	307 D, 150 I	63 D, 120 I	3 D, 91 I	6 D, 1042 I, \$65 million	1 D, 44 I	168 D, 680 I, \$652 million	212 I	1 D, 44 I	19 D, 498 I	224 D, Over 4000 I	17 D, 40 I	23 D, 1000 I	204 D, 209 I	12 D, 150 I	59 D, 750 I	45 D, 100 I	9 D, 150 I	2 D, 9 I	193 D, 2050 I	52 D, 770 I	18 D, 16 I	77 D, 319 I	3 D, 280 I	15 D, 160 I	137 deaths, 416 injured	181 D	35 D, 340 I	23 D, 107 D, £13 million	Over 200 D, Over 6500 I, \$10-15 billion
Estimated Mass [kg]	~ 100	~ 9000	~ 900	~ 45	$\sim\!600$	1000-2000	${\sim}2500$	$\sim \! 1500$	~ 1500	~ 2300	~ 900	~ 450	${\sim}4000$	~ 1000	~ 50	500 - 1000	5-10	500 - 1000	5-10	5-10	5-10	~ 50	~ 1000	5-10	7500-10,000	5-10	${\sim}800,000$	15-20	Unspecified	\sim 2,750,00
Explosive	ANFO	PETN	ANFO	Semtex	Urea Nitrate	AN/Sugar	AN/NM	AN/Sugar	AN/Sugar	C4	Equivalent TNT	Equivalent TNT	Equivalent TNT	KCIO3/S/AI	KCIO3/S/AI	AN/AI	TATP/AN	KCIO3/S/AI	AN/AI	Dynamite	HP/BP	Equivalent TNT	ANFO/AI	Equivalent TNT	AN	TATP	AN	TATP	TATP	AN
Event	Sterling Hall Bombing (Madison, USA)	Beirut Barracks Bombing (Beirut, Lebanon)	US Embassy Bombings (Beirut, Lebanon)	St. Mary Axe Bombing (London, United Kingdom)	World Trade Center Bombing (New York, USA)	Bishopsgate Bombing (London, United Kingdom)	Oklahoma City Bombing (Oklahoma City, USA)	Manchester Shopping Mall (Manchester, United Kingdom)	South Quay bombing (London, United Kingdom)	Khobar Towers Bombing (Khobar, Saudi Arabia)	US Embassy Bombings (Tanzania, Kenya)	USS Cole Bombing (Aden, Yemen)	Enschede fireworks disaster (Enschede, Netherlands)	Bali Nightclub Bombing (Bali, Indonesia)	Marriott Hotel Jakarta Bombing (Jakarta, Indonesia)	British Consulate Bombing (Istanbul, Turkey)	Casablanca Bombings (Casablanca, Morocco)	Australian Embassy Attack (Jakarta, Indonesia)	US Embassy Attack (Tashkent, Uzbekistan)	Madrid Train Bombings (Madrid, Spain)	7/7 Underground Bombing (London, United Kingdom)	US Embassy Attack (Sana'a, Yemen)	Oslo Bombing (Oslo, Norway)	Boston Marathon Bombings (Boston, USA)	West Fertilizer Company explosion (Texas, USA)	Paris Attacks (Paris, France)	Tianjin explosions (Tianjin, China)	Brussels Attacks (Brussels, Belgium)	Concert Bombing (Manchester, United Kingdom)	Beirut explosion (Beirut, Lebanon)
Year	1970	1983	1983	1992	1993	1993	1995	1996	1996	1996	1998	2000	2000	2002	2003	2003	2003	2004	2004	2004	2005	2008	2011	2013	2013	2015	2015	2016	2017	2020

Table 2.2: Historical explosive events across the world noting the explosives which detonated and the overall effects associated adapted from National Academies of Sciences and Medicine^[105]. The events noted in bold are accidental whilst the rest are terror events with D and I corresponding the Deaths and Injuries respectively.

data extracted from Carton^[22] is presented, the charge shape used was flat and square, 1422 detonated in one corner rather than centrally which introduces complexity. The lower 1423 values of TNTe extracted have been directly related to irregularities in the detonation 1424 mechanics. This occurred due to the variety of geometrical differences this methodology 1425 included when comparing to results from a centrally detonated spherical or hemispherical 1426 charge. Sherkar et al.^[146] explained that charge shape needs to be taken into consideration 1427 when regarding resulting blast parameters, provided standoff distance from the detonation 1428 point is less than 35 charge diameters. Past this standoff the effect of charge shape can 1429 be ignored. The lower two values of TNTe extracted from Carton^[22] were measured at 1430 much closer standoff distances than the quoted 35 charge diameter. They were therefore 1431 omitted from any further analysis to avoid any reasonable doubt relating to charge shape 1432 and detonator position. 1433

Reference	Explosive Type
Sadwin and Swisdak ^[139]	ANFO
$Carton^{[22]}$	ANFO
Gitterman and Hofstetter ^[62]	ANFO
Giglio-Tos and Reisler ^[61]	ANFO
Petes et al. $^{[112]}$	ANFO
Figuli et al. ^[52]	ANFO
$Edwards^{[42]}$	ANFO

Table 2.3: Reference list for historic data extracted for both spherical and hemispherical ANFO detonations.

Clearly shown from the Petes et al.^[112] data alone is that once above a mass of around 1435 120kg, ANFO behaves with a seemingly constant TNTe=0.82. This finding was related to 1436 a stable detonation and having an average detonation velocity of around 4200 m/s ($\sim 80\%$ 1437 of that of TNT). For charges smaller than 120kg, the results suggested that the charge 1438 diameter was not large enough to permit steady state detonation conditions, thus re-1439 sulting in lower equivalence values. This information seems to have been lost in time, 1440 with more modern approaches towards quantifying the effects of smaller-scale ANFO both 1441 experimentally [22,27,52] and numerically [67,68,157] making reference to equivalency features 1442 relating to larger scaled charges. Instead an approach which determines a non-steady det-1443 onation state of ANFO and the resulting blast parameters for smaller charges is necessary. 1444 1445



Figure 2.14: Pressure evaluated TNT equivalence ratio for unconfined ANFO with respect to the mass of the charge extracted from Petes et al.^[112], Figuli et al.^[52] and Carton^[22]

The data from the aforementioned reports of large scale trials has been compiled for the 1446 purpose of validating the assumption that constant TNTe across all scaled distances and 1447 masses of charge was made shown in Figures 2.15a-d. The raw data points have been 1448 scaled to an equivalent hemispherical shape, if required, using a shape factor of $1.8^{[76,77]}$, 1449 and 1kg in mass of TNT using a TNTe=0.82, as defined by Petes et al.^[112], to compare 1450 accordingly with KB predictions. It is clear to see the data presented across all positive 1451 phase parameters agree remarkably well with the aforementioned KB predictions when 1452 scaled appropriately. This finding suggests that whilst non-ideal explosives are considered 1453 to have different time scales associated with their detonation chemistry, that once a certain 1454 scale is reached they behave like an ideal explosive with consistent comparisons to TNT. 1455 This provides validation to^[167] who suggest the theory that all explosive detonations can 1456 be considered as point source energy releases, with localised variations, reaching an equi-1457 librium at a given distance away from the explosive centre. 1458

1459

There is a reasonable increase in the variability of data at smaller scaled distances, similarly to the ideal explosives in Figures 2.12a-d and Figures 2.13a-d. One safe assumption for this would be relating this directly to the variations in booster composition and size creating highly variable chemistry within the regions in which the fireball still has an effect



1465



Figure 2.15: Compiled blast parameters from ANFO explosive trials with varying mass as a function of scaled distance, which has been scaled to a 1kg equivalent hemispherical charge, using a shape scaling factor of 1.8, a $TNTe=0.82^{[112]}$, and compared with KB predictions: a) Peak overpressure, b) Scaled arrival time, c) Scaled peak specific impulse, d) Scaled positive phase duration

Another justification could be related to the inconsistencies in ANFO used for the trials, again referring back to the discussion of introducing systematic errors into a testing regime in Chapter 3. ANFO comes in prill form, with a variety of sizes and fuel oil absorption variations. Without careful consideration of these parameters, explosive yields are speculated to vary. Considering the scale of the historically tested charges, the prill volume is assumed to be generally homogeneous exhibiting consistent characteristics, however when taking small samples, the composition would be heterogeneous.



Figure 2.16: The theoretical energy of ANFO as a function of fuel oil content, adapted from Petes et al.^[112]

Figure 2.16 represents the theoretical energy output and sensitivity of ANFO as a func-1474 tion of the fuel oil content. As detailed by Petes et al.^[112], at 6% FO the composition 1475 is stoichiometric, meaning full potential energy release from both the AN and the FO is 1476 attained during the detonation process. From a thermodynamic standpoint, both oxy-1477 gen rich and deficient compositions result in a reduction in the total detonation energy 1478 available, and therefore the percentage of FO has a major influence on the overall energy 1479 released. Whilst strict regimes of quality control may have been implemented, ensuring an 1480 accurate percentage of FO throughout the entire composition of the charges across each 1481 test would be difficult. With large scale charges, self-compaction and void collapse could 1482 result in displacement of FO within regions of the charge and therefore variations could 1483 be experienced. 1484

¹⁴⁸⁶ Similar can be said for the prill size distribution. Dobrilovic et al.^[41], McKay et al.^[99], Pe-¹⁴⁸⁷ tes et al.^[112], Salyer et al.^[140] all investigated varying the densities of ANFO charges to

quantify how it affected velocity of detonation and other blast parameters. The findings suggested that generally larger prills are harder to detonate than smaller prills, and that a steady state detonation is only consistently achieved at bulk density of between 0.80- $0.85g/cm^3$). This means densities either side of this region would result in variations in detonation affectivity and thus the resulting blast parameters. In the larger scale charges, ensuring a constant bulk density throughout a charge would be incredibly difficult due to hydrostatic compaction of the lower layers of ANFO.

1495

A further difference between ANFO and ideal explosives is the lack of binder, and therefore the overall density, and consequential air voids in a ANFO charge, are thought to be an influence on yields through meso-structural detonation mechanics. With large scale charges, self compaction of the charge would result in a more homogenous material and therefore a more efficient detonation process, comparing closely to ideal explosives. Smaller scale charges could begin to provide evidence to help the fundamental understanding of increased variability in ANFO compared to ideal explosives.

1503

Despite ANFO being used both commercially in mining/quarrying processes, and a com-1504 mon explosive for terror threats, there seems to be little available published data char-1505 acterising the explosive across a range of scaled distances for small charge sizes. Figuli 1506 et al.^[52] undertook free-field ANFO explosive testing using 1kg spherical charges, which 1507 showed yields equating to a TNTe 0.32-0.51, different to figures used within numerical 1508 modelling strategies suggested by Sochet et al.^[157] and Grisaro and Edri^[67]. The lack of 1509 data results in uncertainties on how best to model and predict the blast wave properties 1510 emerging from detonations of small ANFO charges. Specifically, it cannot be definitively 1511 concluded if the TNTe value for ANFO is consistent across scales, or whether the reaction 1512 mechanics are affected by the physical length scale over which the detonation wave transits. 1513 1514

1515 2.11 Summary

¹⁵¹⁶ Whilst explosive characterisation has been investigated heavily over the last few decades, ¹⁵¹⁷ there is still no definitive conclusion on whether or not the associated parameters are de-¹⁵¹⁸ terministic. There requires a fundamental and somewhat crude review of experimental ¹⁵¹⁹ data capture and analysis methods to understand why there are discrepancies between
researchers and to conclude on inherent variability of a given explosive. Standardised
techniques are required to investigate the effects of different compositions with confidence.
Whilst ever there are differences in experimental control, there is an expectation of variable
data. This thesis aims at developing validated methods of characterisation for simplistic
blast scenarios as a result of any given composition detonation. A comparison will be
made between ideal and non-ideal explosives, which exhibit detonation behaviours on significantly different time scales.

1528 Chapter 3

Standardising Experimental Methodologies and Analysis

¹⁵³¹ **3.1** Development of Experimental and Analytical Procedures

This chapter will detail how the experimental methodology used by the University of 1532 Sheffield has been modified and improved through the careful consideration of the control 1533 measures in place for each test and the results gathered from them. The improvements to 1534 the testing regime have been compared to historic data and numerical simulations to both 1535 co-validate the precision of experimental testing and the value of established numerical 1536 models. The aim of this chapter is to confirm the underpinning consistency of shock wave 1537 parameters through developing experimental and analytical techniques of data capture 1538 and processing respectively. 1539

1540

1541 3.1.1 Preliminary Test Methodology

The far-field arena-style tests undertaken at the University of Sheffield (UoS) Blast and Impact Laboratory in Buxton, UK, has been a long established capability resulting in a number of blast quantification research articles^[49,128,129,132–134,175]. Figure 3.1 displays the general arrangement that has been adopted for the far-field blast trials undertaken at Buxton, which makes use of two rigid reflective surfaces in the form of a reinforced concrete bunker 4m in height and a blockwork wall 2.20m in height, 4.46m in width, separated exactly 10.0 m apart. For each of the trials, hemispherical explosive charges, were formed using a 3D-printed mould (see Figure 3.2), and detonated at varying stand-off distances between the two walls.

1551

1565



Figure 3.1: General arrangement of the test pad at the University of Sheffield Blast and Impact Laboratory: Site photograph taken approximately from the location of the high speed video camera

Kulite HKM-375 piezo-resistive pressure gauges were used to record the reflected pressure-1552 time histories in each test at both locations. The gauges were threaded through, and made 1553 flush to the surface of a small steel plate (approximately $110 \times 150 \times 10$ mm) which was 1554 fixed to these walls. The plates were fixed to the two reflective surfaces, achieving a 1555 10mm height from the centre of gauge to the ground surface level to ensure pressures 1556 recorded were normal to the charge. The charges were placed on a small steel plate 1557 $(150 \times 150 \times 25 \text{ mm})$ prior to detonation, in order to avoid repeated damage to the con-1558 crete testing pad. The pressure was recorded using a 16-bit digital oscilloscope and TiePie 1559 software, with a average sampling rate of 195 kHz at 16-bit resolution. The recording was 1560 triggered automatically using TiePie's 'out window' signal trigger on a bespoke break-wire 1561 signal, formed by a wire wrapped around the detonator. The 'out window' trigger initi-1562 ated with a voltage drop outside the normal electrical noise experienced in the break-wire. 1563 This coincides with the detonation of the charge breaking the circuit. 1564



Figure 3.2: Photographs of the moulding stages of a 250g PE10 hemispherical charge in which the 3D printed mould is used to provide consistency in charge shape and density, which can be seen when removed from the casing.

High speed video (HSV) recordings of the propagating shock front were taken in an attempt 1566 to quantify the variability of shock wave arrival time recordings. As seen in Figure 3.3, 1567 the explosive charges were situated between a Photron FASTCAM SA-Z high speed video 1568 camera, fitted with a Tamron SP AF70 70-200 mm zoom (F2.8) lens, and a zebra board ran 1569 perpendicular to the blockwork and bunker walls. The camera was positioned to record 1570 the shock wave as it propagated towards the blockwork wall and had the charge location 1571 out of the camera's field of view to avoid excessive light from the fireball corrupting the 1572 contrast of the images. The camera was placed inside an armoured protective housing to 1573 avoid any fragment damage during testing. 1574

1575

A long-span zebra board served to provide a high contrast background such that distor-1576 tions in light, caused by changes in refractive index of the propagating shock front, would 1577 feature as sharp dark bands in the HSV recordings. This allows the position of the shock 1578 front to be identified in each frame, and therefore enables wider-field arrival time measure-1579 ments from a given trial^[78]. The frame rates of the recordings and exposure time varied 1580 between 10,000–36,000 /s and 9.4–26.2 μs due to varying weather/light conditions. Frame 1581 rates and exposure times were altered before to each test in order to maximise the contrast 1582 of the zebra board stripes, and the sharpness of the propagating shock front. Through 1583 trial and error it was found that a maximum of 20 μs exposure time was allowed to achieve 1584 reliable data which exhibited minimal motion blur. If the lighting conditions meant that 1585 the video was not visible at this shutter speed or faster, then the data would be unreliable 1586

and therefore discarded from analysis. The resolution of the camera, when set to these parameters, was 1024 x 512 which resulted in an average pixel size of around 50mm for the far-field set up adopted. This resulted in a best possible accuracy of $Z=\pm 0.075 m/kg^{1/3}$ per pixel.

1591



Figure 3.3: General arrangement of the test pad at the University of Sheffield Blast and Impact Laboratory: Schematic including HSV camera positioning

The experimental work undertaken aims at achieving the highest precision during trial 1592 setup which includes measurements of distance to a target, charge mass and shape consis-1593 tency. Despite being well regarded, the adopted methods still incorporated both systematic 1594 experimental errors which had room for improvement alongside research dependent bias 1595 into the assignment of blast parameters for a given trial. It was important to establish 1596 methods for eliminating or minimising these errors as best as possible both analytically 1597 and experimentally. The implementation of new experimental capabilities and methods of 1598 analysis are discussed. Within the remainder of this chapter, analytical and experimental 1599 improvements will be denoted by Ai and Ei respectively. 1600

¹⁶⁰² 3.2 Pressure Gauge Data

Detailed within this section is the discussion of experimental and analytical improvements made to testing regimes to ensure high fidelity data capture of free-air reflected blast parameters. The content outlines known systematic features within the adopted methodologies and aims to use fundamental knowledge of shock wave propagation, and its interaction with structures, to omit any errors and establish highly consistent data sets.

¹⁶⁰⁹ 3.2.1 Analysis of Positive Phase (Ai)

The raw pressure-time histories from far-field shots, recorded at the University of Sheffield, have tended to exhibit large uncertainties in the opening few microseconds after the arrival of a shock. This has been associated with sensor ringing and smaller variations in natural electrical noise from the recording apparatus, as seen in Figure 3.4^[135]. Precise determination of key blast wave parameters is therefore challenging and alludes to an emphasis on the importance of functional signal analytics for improved blast parameter characterisation^[14].

The raw trend seen in Figure 3.4 shows reasonable levels of consistency to KB predic-1617 tions, which initially provides justification to the quality of the semi-empirical tool for 1618 far-field shots. There are still some parameters which do not compare quite as accurately. 1619 Background electrical noise precludes accurate and automatic determination of the posi-1620 tive phase duration, t_d . This is the time it takes for the overpressure to return back to 1621 atmospheric conditions. This feature is due to a recorded signal oscillating around the 1622 origin for a non-zero period of time. For the data presented in Figure 3.4, the end of the 1623 positive phase would be prescribed as between 12.6 - 12.7ms and the positive phase time 1624 duration would be prescribed as $t_d = 2.7 - 2.9ms$ depending on where the analyst defines 1625 the parameter. 1626



Figure 3.4: Example historic test results using a 250g PE4 hemispherical charge reflected pressure recording at 5 m stand-off compared to KB predictions for a 300g TNT hemisphere

Prior to any analysis or scaling being applied to the data, it is important to establish 1628 how nominally identical raw recordings compare. Figure 3.5 displays a compilation of 1629 as-recorded positive phase pressure-time history profiles for 250g hemispherical PE4 det-1630 onations at various stand-off distances. Since pressure was recorded at two stand-off 1631 distances for each tests (2m to the bunker wall and 8m to the blockwork wall in test 1, 3m 1632 and 7m respectively in test 2, etc.), the results from different tests but identical stand-off 1633 distances can be compared. Qualitatively, each pair of results are in excellent agreement, 1634 with minimal variations in the blast pressure histories. The raw peak pressures at 2m 1635 stand-off $(Z \sim 3 \text{ m/kg}^{1/3})$ exhibits a higher level of variability when compared to the other 1636 pairings. This is in agreement with the working hypothesis of enhanced variability in the 1637 regions described by Tyas^[173], hypothesised to be due to Rayleigh-Taylor (1882, 1950d) 1638 and Richymyer-Meshkov (1969, 1960) surface instabilities. 1639



Figure 3.5: Compilation of the entire raw data set of 250 g PE4 hemispherical ground burst comprising of two recordings at each scaled distance. Positive phase only

It has previously been shown that the specific impulse of a pressure signal can vary signifi-1641 cantly depending on which value of positive phase duration is taken^[96]. This alongside the 1642 significant drop in the opening few milliseconds of the positive phase, can cause specific 1643 impulse values to be significantly lower than of a perfect reflection recording (as repre-1644 sented by the KB prediction in Figure 3.4). A solution to overcome these errors, discussed 1645 within literature [14,49,135] is to fit a modified Friedlander curve, defined by Equation (2.1), 1646 to the experimentally recorded data. No signal will ever be perfectly noiseless, and there-1647 fore the positive phase duration will always carry an enhanced level of uncertainty. Errors 1648 or uncertainties in this parameter can contribute to the overall loading. However, a curve 1649 fit can always be tailored with a different decay parameter in order to match a prescribed 1650 specific impulse value. Hence, studying sources of uncertainty in positive phase duration 1651 are of lesser importance that other positive phase parameters but it is still a reasonable 1652 indicator of explosive yield. 1653

The aforementioned technique was examined through automatically fitting a modified 1654 Friedlander curve to individual pressure signals. This is done to determine how best to 1655 quantify variability of the pressure signal without introducing user error or losing physical 1656 meaning of the signal. The aim of adopting an automated approach was to provide a 1657 more reliable benchmark of explosive characterisation in far-field regions. The aim of this 1658 was to achieve variabilities associated with the positive phase blast parameters that were 1659 statistically unbiased. The automated method was initially validated using 65 of the 144 1660 historic PE4 pressure-time histories recorded at the University of Sheffield^[128], and was 1661 then used to process the remaining PE4 shots to assess its flexibility. 1662

1664 3.2.1.1 Determination of Best-Fitting Procedures

Considering equation (2.1), the parameters required for the curve fitting approach are ar-1665 rival time t_a , and time duration of the positive phase t_d . Through the use of MatLab's 1666 in-built curve fitting toolbox the max overpressure, P_{max} , and decay parameter, b, can be 1667 established using these known parameters. The process was coded to run through multi-1668 ple variations of curves fitted to a given percentage of the recorded data after the arrival 1669 time was ignored. A curve was fitted to remaining data and extrapolated back to the 1670 defined arrival time. This provided a range of different blast parameters for a single given 1671 trial which could then be statistically investigated whilst trying to omit the effects of the 1672 'sensor' ringing within recorded data. The general algorithm of the curve-fitting routine 1673 is defined as follows: 1674

- 1. Determination of t_a : This parameter typically appears and is recorded as a sharp, unambiguous rise to peak pressure, with a maximum rise time of only a few (< 10) recorded samples ($\approx 50 \ \mu s$) depending on recording frequency of the chosen oscilloscope. This can be seen in Figure 3.7a and is easily discernible in the raw data, i.e. the main peak in the gradient of the pressure signal^[129].
- 1680

2. Assignment of t_d : The electrical noise in each trial was recorded with a 10% pre-1681 trigger to the detonation so an estimation of the effect of the noise could be made 1682 for more accurate t_d determination. As seen in Figure 3.6, the electrical noise is 1683 shown to be normally distributed around the true mean value meaning that when 1684 integrating pressure, with respect to time, the effect of electrical noise cancels out 1685 and has negligible effect on peak specific impulse. Therefore the difference between 1686 the assigned t_a and the time at which the maximum specific impulse occurred would 1687 be assigned as the positive phase duration, t_d , as seen in Figure 3.7b. This finding 1688 of normally distributed noise was consistent across all historical recordings. 1689



Figure 3.6: Example historic test recording of electrical noise prior to arrival of the shock wave with its distribution presented, where X is associated to the voltage recorded in the system

3. Incremental removal of start of positive phase: Inputting the time-based pa-1691 rameters and the raw pressure-time data into equation (2.1) provides a generalised 1692 curve with corresponding values for peak pressure and the decay coefficient, P_{max} 1693 and b respectively. Using Matlab's curve fitting toolbox, these parameters were fit 1694 to successively more curtailed pressure signals (in increments of a single percent, 1695 starting with the full signal) and extrapolating back to the arrival time of the shock, 1696 obtaining a spectrum of different peak pressures, specific impulses and decay coeffi-1697 cients from the results of a single test. 1698

1699

4. Determination of optimal removal ratio: Peak pressure and peak specific impulse values were seen to form a 'fan' around a central representative value (see Figure 3.8a). This was caused by fitting curves to the real physical features in the data and the additional variation induced by sensor ringing and inherent electrical noise. The mean values of the collated results for both peak pressure and specific impulse were calculated and the curve fits which satisfied both mean values within a $\pm 5\%$ region were defined as the 'optimal model fits' to the raw data. The mean of these parameters were then evaluated, giving the automatically-generated peak pressure and peak specific impulse from that test. The decay coefficient was determined from iterations of the integral Equation 2.1, which enables the full pressure signal to be reconstructed.

1711

1712 3.2.1.2 Example of Curve Fitting Procedure

Initially, a simple verification of the automated procedure of blast parameter assignment 1713 was undertaken. Figures 3.7a and 3.7b show the pressure and specific impulse signals 1714 (through cumulative trapezoidal integration with respect to time) from a historic test 1715 with a 250g PE4 at 4m stand-off ($Z = 6.3496 \text{ m/kg}^{1/3}$). Overlaid on both figures are 1716 the automatically assigned time based blast parameters, t_a and t_d , by implementing steps 1717 1 and 2 of the curve fitting algorithm. These automated values are in good agreement 1718 with those determined from visual inspection of the raw data, and provide some initial 1719 confidence in the accuracy of the self-defining parameter routines. 1720



Figure 3.7: Example historic test results using a 250g PE4 hemispherical charge at 4 m stand-off: a) Raw pressure, and; b) Raw specific impulse with respect to time for a single test, highlighting the assignment of shock wave arrival time, t_a , and positive phase duration, t_d

The results from step 3 of the algorithm are shown for the same test in Figures 3.8a1721 and 3.8b. With successive removal of between 0-50% of the positive phase data and back 1722 extrapolating to the defined arrival time parameter, a variety of different fitted Friedlander 1723 curves are seen, represented by the coloured 'fanning' envelope at t = 0ms in Figure 3.8a. 1724 Peak pressures between 50-72 kPa are determined at this stage of the algorithm which is 1725 ± 12 kPa, or $\pm 10\%$, of the KB prediction for the same given scenario. For a non-statistical 1726 based analysis, these variations are an improvement on those seen in articles expressing 1727 the hypothesis of inherent randomness between nominally identical explosive trials. This 1728 provides a potential explanation for sources of error introduced by the analyst. 1729



Figure 3.8: Example curve-fitting for historic test results using a 250g PE4 hemispherical charge at 4 m stand-off: a) all fitted curves to raw data with iterations based on percentage t_d removed immediately after t_a , and; b) Variations in fitted peak pressure and specific impulse as a result of the percentage of t_d removed, and definition of final range (solid markers) for which mean parameters are evaluated

Figure 3.8b visually represents the peak pressures and specific impulse envelopes with respect to the percentage of t_d removed (from the start of the positive phase). The cyclic pattern in the opening 0–35%, and the fanning envelope introduced previously, is a result of fitting to different proportions of peaks and troughs in the electrical signal. The reductions in both parameters after 35% represents the progressive loss of credible data and thus would result in the inaccuracy of representing features of the given blast wave. The dip in peak pressure and specific impulse around 10% is as a result of fitting to the first ¹⁷³⁷ major sensor ringing loss, seen for this test at t = 0.3ms after arrival in Figure 3.8a. A ¹⁷³⁸ region of cyclic parameters was seen consistently at approximately 10–35% positive phase ¹⁷³⁹ removal for all validation tests. Accordingly, this interval was set as the representative ¹⁷⁴⁰ region over which the mean values were evaluated in step 4 of the algorithm, visually ¹⁷⁴¹ displayed by the vertical lines in Figure 3.8b.

1742

Step 4 assigns the most statistically representative parameters within this reduced region. 1743 First, the mean peak pressure and mean peak specific impulse between the entire region of 1744 10–35% positive phase removal is calculated. Then, any percentage positive phase removal 1745 that results in a peak pressure or peak specific impulse deviating from this initial mean 1746 by more than 5% is discounted, and the mean values from each new, reduced dataset are 1747 calculated. This is shown visually in Figure 3.8b, where the vertical lines denote the initial 1748 region where the first mean is taken (10-35%), the hollow markers indicate those that are 1749 excluded from the final mean calculation, and the solid markers indicate those data points 1750 that are included in the final mean calculation that satisfy the requirements stated above 1751 but only the ones falling inside the 10–35% region were considered. 1752 1753



Figure 3.9: Example historic test results using a 250g PE4 hemispherical charge at 4 m stand-off with optimal fits overlaid: a) Overpressure, and; b) Specific impulse

Finally, Figures 3.9a and 3.9b display the raw data from the example historic test (250 g 1754 PE4 hemisphere at 4 m stand-off), and the resulting modified Friedlander curve fits de-1755 termined from the automated process. The high R^2 values noted on each figure show that 1756 the generalised model fits compare well to the raw data. Due to the nature of pressure 1757 signals being easily influenced by ringing and other electrical noise, the R^2 of the model 1758 pressure fit will always be lower than that of a specific impulse fit. This justifies the 1759 findings presented by Bogosian et al.^[16] which discuss the impulse measurements were in-1760 herently more reliable than those for peak pressure. It is worth reiterating that although 1761 Figures 3.9a and 3.9b present optimal fits from a given test, they are evaluated from a 1762 large number of different potential fits. 1763

1764

A secondary aim of this analysis was to confirm whether a consistent value of 0.25 t_d removed after the arrival time was suitable as a general rule in line with conclusions made by Rigby et al.^[135]. Only 10 of the 65 validation pressure-time histories resulted in optimum curves whose parameters were determined from trial fits outside of $0.25 \pm 0.03 t_d$, and this was mainly due to the level of sensor ringing and electrical noise that was present. With low levels of sensor ringing, the optimal amount of data removal was found to range between 0–0.2 t_d , meaning that a Friedlander curve could effectively be fit to the entire data set without any loss of accuracy. For tests with intermediate to excessive sensor ringing, or for poor signal-to-noise ratios, a value of $0.25t_d$ was deemed suitable and can be used as a general rule in the absence of more sophisticated techniques such as the one presented in this article.

1776

1777 3.2.1.3 Compiled Results

The optimal blast parameters determined from the automated process for the 65 PE4 pressure-time histories used to validate the method^[135], the remaining 79 historical PE4 recordings^[133,175] and the additional 10 PE4 trials conducted as part of this research are presented in Figures 3.10a–d as a function of scaled distance. Positive phase duration (Figure 3.10b) was not determined in the historic tests and so are omitted here.

The data presented in Figures 3.10a-d have been expressed using the Hopkinson-Cranz 1784 scaling^[33,74] assuming a constant TNT equivalence of PE4 of $1.20^{[132]}$. For comparison, 1785 KB predictions have also been included in these figures. The recorded blast parameters 1786 demonstrate excellent agreement with the KB predictions, particularly in the region of 1787 $Z > 3 \text{ m/kg}^{1/3}$. The agreement between experiment and prediction reduces when ap-1788 proaching smaller scaled distances, $Z < 3 \text{ m/kg}^{1/3}$, although the results are still typically 1789 within 10-20%. The fundamental cause in this deviation has not been fully determined, 1790 yet the working hypothesis it that it is likely due to irregular features of the fireball/air 1791 interface giving rise to non-consistent shock wave properties between tests in the mid-to-1792 near field. 1793

1794

An additional consideration is a singular value of TNT equivalence may not be appropriate for scaled distance regions in which the fireball and shock wave propagate in unison as the chemical processes ongoing from a TNT detonation may not be directly scalable to those from another given explosive. Upon the shock wave detaching from the fireball, the recorded parameters are scalable as the comparison is made between shock waves travelling through the same medium, unaffected by any external factor. This is the subject of ongoing work considering the mechanisms of explosives.



Figure 3.10: Compiled blast parameters from hemispherical PE4 trials as a function scaled distance, compared with KB predictions: a) Scaled arrival time, b) Scaled positive phase duration, c) Peak reflected pressure, d) Scaled reflected peak specific impulse

When considering test-to-test repeatability, there are two main conclusions to be drawn, 1803 both in agreement with findings published in the literature. Firstly, uncertainty in ex-1804 perimentally record blast parameters generally reduces with an increase in scaled dis-1805 $tance^{[16,115]}$ seen predominantly in Figures 3.10c and 3.10d. Secondly, despite best efforts 1806 to remove unconscious researcher-dependent bias, peak pressure, specific impulse and pos-1807 itive phase duration, in nominally identical scenarios, demonstrate much higher levels of 1808 test-to-test variability than shock front arrival time. This can be seen when comparing 1809 Figures 3.10b–d with 3.10a respectively. It is suggested that test-to-test variations are 1810 non-negligible for $Z < 3 \text{ m/kg}^{1/3}$ and the source of these variations are to be investigated 1811 in future works. 1812

1813

¹⁸¹⁴ 3.2.2 Modifications for Positive Phase Improvement (Ei)

The results from the far-field trials presented in this thesis begin to build a coherent fundamental understanding of the nature of experimentally recorded far-field loading from a given charge composition, shape and mass. The importance of these findings provides a starting point to establish characteristics of more challenging blast loading conditions both in the near-field and those in complex environments. Knowledge of which can be supplemented with high-fidelity, validated numerical modelling.

1821

Considering Figure 3.5, the standard 'sensor ringing' feature can be seen across each of the positive phases recorded at each increment of standoff. The results of which have historically been assigned to being technical incapabilities of the pressure gauges used in the trials. Although the aforementioned analytical techniques have shown to effectively omit the effects of this feature, it was important to establish its root cause and attempt to rectify it for future testing regimes.

1828

Reisler et al.^[119] reviewed extensively the development of pressure gauges throughout the 1829 high explosive era. Examples of recorded pressure-time histories for different gauges across 1830 numerous researchers and trials were provided within. One interesting finding in this arti-1831 cle was that represented by Figure 3.11, which showed similar oscillations in the opening 1832 25% of the positive phase duration recorded as the tests undertaken at the University of 1833 Sheffield. The fact that a similar finding was recorded using a pressure probe directed the 1834 thinking towards a real physical shock feature rather than a individual technical failure of 1835 the gauge causing early time oscillations. 1836



Figure 3.11: Example historic test results from a 1000lb high explosive height of burst shot recovered from Reisler et al.^[119], displaying a comparison between a pressure probe (dotted) and a Kulite pressure gauge within a baffle plate (solid) across two different time bases, similar to the methods adopted in this thesis.

Understanding the mechanisms and magnitudes of blast loading on targets is of key im-1838 portance for the analysis and design of the response of protective structures. Vast amounts 1839 of numerical work has been undertaken throughout literature with experimental work to 1840 validate its accuracy^[179]. However, there has yet to be a synergistic approach to anomaly 1841 or systematic feature finding in experimental trials using validated models. The experi-1842 mental results and analysis discussed within this thesis have been used to validate far-field 1843 numerical models for various high explosives. These can be implemented into much more 1844 complex numerical simulations to produce validated and accurate prediction for near-field 1845 and complex conditions. It was important to use these models to try and reverse engineer 1846

a physical justification to any systematic errors which could contribute to the variabilitiesseen in experimental data.

1849

1850 3.2.2.1 Synergy of Modelling and Experimental Studies

Whittaker et al.^[179] validated APOLLO blastsimulator, developed by EMI, using an in-1851 house explicit afterburn method (leveraging Cheetah and EXPLO5), against experimental 1852 data for PE4 and PE10 explosives and then for PE8 in works presented by Farrimond 1853 et al.^[50]. The agreement attained gives confidence in the standard equation of states 1854 (EOSs) and subsequent parameters developed for these particular explosives, which can 1855 be utilised in numerical modelling for more complex scenarios. Numerical modelling gen-1856 erally is taken at its most simplified form to try to establish key explosive characteristics 1857 from basic scenarios which can then be mapped into more complex settings. These el-1858 ementary numerical models usually do not account for minor environmental variations, 1859 such as terrain levels, reflective surface blemishes and energy loses, therefore omitting any 1860 shock wave mechanisms which could occur because of the aforementioned. 1861

1862

The oscillations identified in the raw pressure-time history traces from Figure 3.12a, and 1863 others within this thesis, have been previously attributed to a consistent feature of 'sensor 1864 ringing^{,[49,135]}, which was an assumed systematic technical limitation of the gauges used. 1865 The numerical models developed in the aforementioned articles with validated EOS's for 1866 a given explosive previously utilise simplistic, and fairly unrealistic baseline conditions. 1867 This is denoted by the idealistic shock wave behaviour simulated against experimentally 1868 recorded reflected pressure and specific impulse for 250g PE10 hemisphere at 2m stand-off 1869 as seen in Figures 3.12a and 3.12b. 1870



Figure 3.12: Comparison between experimentally recorded data for a 250 g hemispherical PE10 charge detonated 2 m away from a reflected gauge and Apollo numerical modelling (with EOS parameters developed using Cheetah and Explo5): a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs

The numerical models utilised quarter-symmetry, with both the ground, vertical symmetry 1872 plane, and a boundary wall at the required stand-off distance defined as perfectly reflecting 1873 surfaces with afterburn features included using an explicit method. The Explosive EOS 1874 parameters used in this study were generated using the thermochemical code Cheetah 1875 v7, which, due to export control reasons, are not available for publication. Therefore, an 1876 alternative thermochemical code, EXPLO5, was also used to determine the EOS for the 1877 explosives. The surrounding medium of the numerical simulation was assumed to be air 1878 defined by the parameters in Table 3.1. 1879

1880

	Parameter	Units	Value
Perfect Gas EOS	R	$Pa/(K.kg/m^3)$	288
Caloric EOS	$E0 \\ c_{v1} \\ c_{v2}$	$J/kg \ J/kg.K \ J/kg.K^2$	-2.375e5 723.3 0.0749

Table 3.1: Table of EXPLO5 Equation of State Parameters for Air.

¹⁸⁸¹ These parameters have only been used for a complementary comparison to the Cheetah ¹⁸⁸² study and have not been fully assessed or validated, but are provided as representative values in Table 3.2. It is important to note the developed parameters were produced purely
based on the explosive composition, correct density and a best guess of plasticiser material
(finding the exact composition may improve the results), all done using the same default
methodology. No calibrating to experimental data or tweaking of technique or parameters
to improve results was performed.

1	8	8	8

			Explosive Type		
	Parameter	Units			
			PE4	PE8	PE10
	Density	$\rm g/cm^3$	1.59	1.57	1.55
JWL	А	kPa	3.62E + 08	3.35E + 08	3.21E + 08
	В	kPa	7.89E + 06	7.24E + -6	9.40E + 06
	R1	N/A	3.99	3.94	4.40
	R2	N/A	1.15	1.13	1.23
	W	N/A	0.27	0.27	0.271
	Detonation Velocity	m/s	7700	7608	7735
Detonation Products	E_0	kJ/kg	-5.36E + 06	-5.32E + 06	-5.18E + 06
	Gas Constant	J/kg.K	282	282	269
	CV1	$J/kg.K^2$	738.8	672.9	738.2
	$\mathrm{CV2}$	$\rm J/kg.K^3$	0.4321	0.4502	0.3847
Combustion Products	E_0	kJ/kg	-3.99E + 06	-3.57E + 06	-4.51E + 06
	Gas Constant	J/kg.K	286	287	283
	CV1	$J/kg.K^2$	488	309	453
	CV2	$\rm J/kg.K^3$	0.295	0.409	0.320
Other	Stoichiometric Ratio (Air/Exp)	N/A	0.716: 0.284	$0.726{:}0.274$	0.709:0.291

Table 3.2: Table of EXPLO5 Equation of State Parameters for Explosives.

Figure 3.12 shows both numerical models to be almost identical in this scenario, but with 1889 both somewhat over-predicting the peak reflected pressure and impulse of the event whilst 1890 not capturing the ringing seen in the opening $\sim 0.5ms$ of the positive phase. Hereafter, 1891 APOLLO blastsimulator using the Cheetah–determined equation of state parameters was 1892 the chosen method of numerical prediction due to the similarity in modelling results. The 1893 arrival time of the primary shock at this scaled distance is predicted sooner than the ex-1894 perimentally recorded which in conjunction with larger pressure predictions too begins the 1895 narrative that the models are experiencing a bigger energy release than what was recorded. 1896 1897

The arrival of the secondary shock in the numerical models is much earlier than that seen in the experimental data, which can lead to artificially high specific impulse predictions as the secondary shock arrives during the positive phase of the event. Other published literature describes the numerical secondary shock as arriving much *later* than the experimentally-recorded value when using numerical codes which do not explicitly account for afterburn^[129], and it has been shown that including a calibrated secondary energy release can bring the secondary shock in line with the experimental recordings^[141].
Whilst this method holds empirically based variable prescription, it is clear that the arrival
of the secondary shock is intimately linked to the post-detonation pressure-volume-energy
relations of the fireball, and is a known limitation of current modelling capabilities. This
feature is believed to be due to the over prediction of the sound speed within the fireball.

The results from the simplest form of the numerical simulation led developments to con-1910 sider energy losses to the ground surface. In the experimental methodology, the explosive 1911 charge was detailed as being placed on top of a steel anvil to reduce progressive damage 1912 to the ground; this alone is enough evidence to suggest some energy is being lost to the 1913 ground surface and therefore the first modification to the simplistic model was to take 1914 these into account. A 10% energy loss was applied to the simulation, in line with TM5-1915 8858^[77], by using 225 g rather than 250 g of PE10, the results of which are shown in 1916 Figure 3.13. This is conceptually similar to the 1.8 spherical equivalence factor adopted 1917 in the KB predictions, and brings the modelling results much more in-line with the exper-1918 imental data. 1919





Figure 3.13: Comparison between experimentally recorded data for a 250g hemispherical PE10 charge detonated 2m away from a reflected gauge and numerical model evaluating using APOLLO when accounting for energy losses into the ground a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs

1935

The 'sensor ringing' seen in the experimental data was still not captured in the model 1921 detailed in Figures 3.13a and 3.13b. In higher fidelity numerical analysis, the pressure 1922 gauges were detailed as being made flush to a steel plate which protruded 25 mm from 1923 the reflecting surface. The significant drop in the pressure seen in Figure 3.14a over the 1924 opening 25% of the positive phase is enough evidence to support the necessity of accurate 1925 models to verify experimental procedures. By capturing some of the more complex early-1926 time behaviour initially attributed to 'sensor ringing', numerical analysis and experimental 1927 procedures can work collaboratively to achieve higher levels of accuracy overall. This is 1928 a key insight for future experimental trials as it means if a truly flush surface can be 1929 achieved without any opportunity for clearing and reflected wave interactions, the statis-1930 tical accuracy of the recorded data quoted in this article may be improved on further and 1931 the 'sensor ringing' maybe omitted. Shin et al.^[148] ran numerical analysis which however 1932 suggests once in the extreme near-field region, $Z < 1.6 \text{ m/kg}^{1/3}$, the effects of clearing is 1933 negligible and should be ignored for design purposes. 1934



Figure 3.14: Comparison between experimentally recorded data for a 250g hemispherical PE10 charge detonated 2 m away from a reflected gauge and numerical model evaluating using APOLLO when accounting for energy losses into the ground and substantial terrain features a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs

1936 **3.2.2.2** Blast Arena Modification

The fact that the numerical modelling has allowed the identification of systematic features within the experimental arrangement is testament to the synergistic nature of modelling and experimentation, especially when high levels of control are attained as they are in this study. A larger steel plate, with a minimum distance of 1.5m from the gauge to the edges of the plate, was affixed to the bunker wall to ensure that the aforementioned localised clearing effects would not interfere with the positive phase of the shock.

A repeat trial was conducted using a 250g PE10 hemisphere detonated 5m away from this surface and compared to the original trials, the data of which is presented in Figures 3.15a and 3.15b. The new results indicate that whilst these 'sensor ringing' oscillations alter the qualitative form of the pressure trace, their influence on the quantitative blast parameters, determined through curve fitting, or integration of the pressure signal to find specific impulse, are negligible when comparing the raw data to the curve fit itself as seen in Figures 3.9a and 3.9b.

1951



Figure 3.15: Comparison between experimentally recorded data, time-shifted so the arrival of the positive phases align exactly, for a 250 g hemispherical PE10 charge detonated 5 m away from a reflected gauge with adjustments to the blast arena and without: a) Reflected overpressure, b) Reflected specific impulse, both with respect to time after detonation occurs

1982

¹⁹⁵² 3.2.2.3 Top vs Bottom Detonation in Ideal Explosives

Another important notion to take from the trial results presented in Figures 3.10 is the 1953 agreement of findings presented by Bogosian et al.^[16]. Both suggest that specific im-1954 pulse values developed from curve fitting techniques are much more reliable than peak 1955 overpressure. However, the physical reasoning for the clear spread in the data seen at 1956 $Z < 3 \text{ m/kg}^{1/3}$ for the two parameters is still yet to be fully determined. The hypoth-1957 esis detailed by Tyas^[173] made definitive justification to the experienced spread through 1958 links to fluid dynamic instabilities which is a physical and logical explanation. What was 1959 not considered in full detail however was how the experimental procedure of top detonat-1960 ing the hemispherical charge could effect the close-in shock wave/fireball blast parameters. 1961 1962

Sherkar et al.^[146] undertook an analysis on the influence of a charge shape and detonation 1963 point on explosive parameters and found that for scaled distances of $Z > 3.15 \text{ m/kg}^{1/3}$ the 1964 independent variable made no difference to shock wave parameters. This finding is in line 1965 with the working hypothesis defined by Tyas^[173]. The predictions at smaller scaled dis-1966 tances are however significantly variable as charge shape and detonation point is altered. 1967 As the majority of the data presented within this thesis, unless specifically specified, was 1968 the result of a top detonated hemisphere it was important to investigate, using both new 1969 experimental data and validated numerical modelling, whether or not detonator position 1970 could be be an influencer of parameter variability in the $Z < 3 \text{ m/kg}^{1/3}$ region. 1971 1972

Using a validated EOS for PE4, both top and bottom detonated scenarios were con-1973 sidered for the standoff range of 1.25-2m assuming a TNTe=1.2, corresponding to Z =1974 $1.87 - 2.99 \text{ m/kg}^{1/3}$. Experimental data used for a direct comparison to both the CFD 1975 simulations and KB predictions presented. According to numerical simulations presented 1976 in Shin et al.^[148], the near-field modelling can ignore the effect of clearing as it is negligi-1977 ble. The gauge plate features discussed in Section 3.2.2 was therefore removed from the 1978 simulation, resulting in minor changes to the overall pressure-time history. It is however 1979 important to note that the aforementioned article makes use of AUTODYN for modelling 1980 capabilities where as the study presented in Figure 3.16 uses APOLLO. 1981

¹⁹⁸³ The nearest standoff of 1.25m, a scaled distance of $Z = 1.87 \text{ m/kg}^{1/3}$, considered was ¹⁹⁸⁴ chosen as it shows to exhibit the most variability in the resulting output blast parameters from historic trials. The results from experimental tests, numerical simulations and KB predictions are presented in Figures 3.16a-d for this region to both consider the effects of detonator position but also test the validity of KB predictions at these scaled distances. What is evident from these plots is the distinct differences between top and bottom detonated results when considering the general form of the experimental pressuretime histories.

The bottom detonated trials, represented by Figures 3.16b and 3.16d, show that both 1992 KB predictions and numerical simulation over-predict the peak reflected pressure, but the 1993 specific impulse values agree reasonably well. This begins to reiterate shock wave develop-1994 ment and formation theory discussed by Kinney and Graham^[90] in Chapter 2. The theory 1995 shows a clear transition of the pressure-time history from a rounded pressure pulse, which 1996 then begins to expand radially at its own speed for each portion of the pulse, therefore 1997 the higher pressure and temperature regions expanding faster, resulting in a progressively 1998 sharper rise to peak pressure, and thus the shock discontinuity. 1999

2000

Figures 3.16b and 3.16d are believed to display a shock in this transition period. The 2001 overall energy released from the detonation is representative of KB and numerical model 2002 predictions for a 250g PE4 charge but the peak pressure is lower and time duration is longer 2003 in the experimental trial. It is clear that neither numerical modelling or KB predictions 2004 are able to accurately capture the transition period of the shock front as both over-predict 2005 the peak pressure considerably. At these scaled distances KB predictions were developed 2006 using numerical simulation which explains why the two compare reasonably well. It is 2007 clear that these methods assume a fully formed shock discontinuity occurs sooner than in 2008 reality and therefore the real physical behaviour of the early development of the shock is 2009 not captured correctly. 2010

2011

Figures 3.16a and 3.16c represent the top detonation of 250g PE4 hemisphere. These result in a much lower peak pressure when compared to KB predictions but peak specific impulse values presents much lower too. This is a direct result of the varying detonation dynamics, resulting in differences in rates of energy release. This induces a more inconsistent behaviour when compared to a standard free-air assumption. Reassuring is the strength of numerical modelling at this scaled distance which although has not captured either the pressure-time or specific impulse-time histories perfectly, the same general trend

¹⁹⁹¹

can be qualitatively seen. Quantitatively, the numerical simulation is different to the ex-2019 perimental data which is speculated to be related to the exact position and orientation 2020 of the detonator. In the numerical simulation, a perfect, infinitesimally small detonation 2021 point is prescribed at the very top of the charge. In reality despite best efforts, the det-2022 onators used in testing are approximately 5mm into the top of a charge, do not expand 2023 radially and may not be perfectly orientated. This therefore will result in different det-2024 onation dynamics. The fact, that qualitatively, the trends show similarities gives rise to 2025 the testing methodology but validates the sensitivity of the results at this scale. 2026 2027



Figure 3.16: A comparison of top and bottom detonated 250g hemispherical PE4 charges recordings of reflected pressure and specific impulse against time at 1.25m standoff (corresponding to plots a and c, and b and d respectively) which make reference to KB predictions and numerical simulations.

For the top detonated trials, there is believed to be a slower expanding detonation cloud and resulting shock wave associated with the top portion of the charge. This expands prior to the detonation wave reaching the bottom of the charge. When the detonation wave reaches the bottom of the charge, and the reflective surface, the resulting detonation products would begin to expand laterally along the reflected surface in the form of jets, and radially back outwards. The jetting-like behaviour has been attributed to the first rise in the pressure-time histories seen in Figure 3.16a, with the secondary radial expansion being attributed to the rise approximately 0.3ms later experienced in both the numerical simulation and experimental data.

2037

The additional near-field experimental results, considering the standoff range of between 2038 1.25-2m, are presented in Figures 3.17a-h. These trials aimed at deducing the distance 2039 the effect of detonator position becomes irrelevant to the overall blast parameter data. 2040 The raw data presented in the aforementioned plots is considered in a qualitative sense 2041 against KB predictions. The results suggest that for standoff distances greater than 1.5m, 2042 $Z > 2.24 \text{ m/kg}^{1/3}$, both top and bottom detonated trials behave consistently in terms of 2043 the overall energy released, and thus the resulting peak specific impulse trends which are 2044 captured well by KB predictions as shown in Figures 3.17f and 3.17h. As the standoff 2045 distance is reduced, the KB predictions generally capture the energy released in bottom 2046 detonated trials, but top detonated results show a lower energy release overall. This is 2047 directly related to the non-spherical expansion of the detonation wave and its products, 2048 resulting in inconsistent energy releases, seen in Figures 3.17b and 3.17d. KB predictions 2049 generally over-predict the peak overpressure at these scaled distances too, which is related 2050 to the lack of comprehension in the physical shock formation in the empirical tool at these 2051 scaled distances. 2052



Figure 3.17: A comparison of two top and bottom detonated 250g hemispherical PE4 charges recordings of reflected pressure and specific impulse against time at 1.25m, 1.5m, 1.75m and 2m standoffs (corresponding to plots a, c, e and g, and b, d, f and h respectively) which make reference to KB predictions.

Interestingly, the blast parameters from the new top detonated data at 1.25m standoff, 2054 shows to be in line with the lower bound of those presented in Figures 3.10c and 3.10d. 2055 The historic data presented in both Figures 2.12a-d and Figures 2.13a-d was conducted by 2056 different research teams, which reinforces the narrative of ensuring the systematic differ-2057 ences between testing regimes are considered when comparing results. The historic data 2058 at $Z > 3 \text{ m/kg}^{1/3}$ shows agreement with the newly conducted trials, which validates the 2059 hypothesis that at this scaled distance blast parameters are less sensitive to the imperfec-2060 tions, but are for near-field scenarios, $Z < 3 \text{ m/kg}^{1/3}$. The team conducting the historic 2061 trials may not have been as strict in their control measures, with variations in the deto-2062 nator placement resulting in greater variability. The fact the repeat shots in this study 2063 show low levels of variability suggests that these are a more appropriate characterisation 2064 of the detonated explosives. Future tests will look at studying the near-field region with 2065 much more rigour to establish the consistency in the blast parameters similarly to that 2066 discussed within this thesis for far-field scenarios. 2067

2068

These trials show that the top detonated experimental methodology utilised for the ma-2069 jority of the data referred to in this thesis, will give rise to spreads of data in near-field 2070 regions, $Z < 3 \text{ m/kg}^{1/3}$. Data recorded in this region will be influenced by detonator 2071 position, orientation, charge geometry and placement imperfections alongside any other 2072 systematic experimental and analytical errors induced during the trials. This finding pro-2073 vides evidence towards the overlooked systematic errors incorporated into blast related 2074 experimental work which result in the justifications of 'inherent' high levels of explosive 2075 yield variability. 2076

2077

2078 3.2.3 Analysis of Negative Phase (Ai)

Rigby et al.^[133] undertook an intensive assessment of the negative phase of the ideal 2079 explosive, PE4, and compared various methods of approximating the associated trends. 2080 The secondary, and subsequent, shock phenomenon are not accounted for in any empir-2081 ical predictions presented within the aforementioned article. This is justified by the low 2082 magnitudes they exhibit compared to the negative phase presented in ideal explosives. 2083 Further noted is the affect clearing has on a pressure trace, a given time after the arrival 2084 of the primary wave. This is associated with the speed of a clearing wave being 340m/s 2085 and then taking the distance from the nearest edge of a reflective surface. Clearing and 2086

reflections from other surfaces are wave phenomena which will be picked up on experimental recordings. Without a fundamental understanding of the systematic errors associated with a testing methodology, data could be misinterpreted, with these features considered to be real physical parameters of a free-air shock interacting with a single surface.

Whilst this thesis neglects both these experimental features, the 'Cubic Negative' curve fit 2092 approximation (detailed in the second case of Equation 2.6), developed by Granstrom^[66], 2093 presents as the most effective method of approximating the negative phase both qualita-2094 tively and quantitatively for the ideal explosive in question. This provides further justifi-2095 cation as to the source of negative phase semi-empirical curves. Shown in Figures 3.18a-d 2096 is the considerable effects experimental features can have on the overall loading from the 2097 same explosive detonation. It is important to note that the data presented in the aforemen-2098 tioned figure was recorded during the same trial using two different recording locations. 2099 Interestingly, the general form of the raw data exhibits rather obvious differences when 2100 t=17.5-22 ms which is approximately 7-12 ms after the arrival of the primary shock. 2101 2102

Using a 340m/s clearing wave speed and the distances to the nearest sides of the walls, 2103 the time at which the clearing waves would arrive at the respective pressure gauges would 2104 be approximately 12ms and 7ms after the arrival of the primary shock. With the bunker 2105 wall being effectively infinitely long but 4m tall, only one clearing wave would interact 2106 with the negative phase data. The blockwork wall on the other hand has three finite 2107 edges, two of which were 2.25m resulting in two clearing waves interacting with negative 2108 phase simultaneously around 17ms after detonation. This is clearly denoted by the lower 2109 pressures in Figure 3.18a associated with the time periods mentioned. 2110



Figure 3.18: Comparison of negative phase results from a 250g PE4 trial with two reflective recording points 5m either side of the explosive, where plots a) and b) represent the raw negative pressuretime plots and plot c) and d) are the corresponding impulse-time plots for the blockwork and bunker walls respectively.

2112 3.2.3.1 Compiled Negative Phase Parameters

The 'Cubic Negative' approximation investigated by Rigby et al.^[133] was implemented on this data set to validate the findings further as presented in Figure 3.18. It is clear to see a reasonable prediction for the negative phase loading is established across all three parameters regardless of secondary shocks and any other experimental features.



Figure 3.19: Compilation of scaled negative phase parameters resulting from visual analysis of 250g PE4 hemispherical charge using a TNTe=1.22: a) Negative Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time Duration.

What is yet to be established is a rigorous validation of quoted negative phase parameters. 2118 The difficulty in characterising these parameters is associated with the lower magnitudes 2119 of the negative phase parameters and therefore it is much easier to misinterpret the ac-2120 tual values within the noise of the recorded data. Reducing the noise for the secondary 2121 shock is not possible as its magnitudes is inherent to the rating of the gauge. To avoid 2122 gauge failure, the rating needs to be high enough to withstand the primary blast wave 2123 prior to secondary waves arriving. That alongside experimental features, related mainly 2124 to clearing, means that developing automated analytical tools, similar to that presented 2125 in Section 3.2.1, hold more difficulty. Taking this into account, the negative phase param-2126 eters are established visually within the contents of this thesis to validate both the 'Cubic 2127 Negative' and semi-empirical approximations across a number of different explosives. 2128 2129

Figures 3.19a-c displays visually interpreted negative phase parameters from 250g hemi-2130 spherical PE4 trials across the far-field testing range. This data was scaled using a 2131 TNTe=1.22, in line with findings from Farrimond et al.^[50], and compared directly to 2132 the empirical curves established by Granstrom^[66]. The agreement with predictions of 2133 peak negative pressure, $P_{r,min}$, suggest that whilst the experimental methodology induced 2134 variations during the negative phase, the general maximum pressure experienced is in 2135 line with approximations. It is important to note, if the reflecting surfaces were smaller, 2136 clearing waves would arrive at the recording positions sooner, resulting in variations to 2137 the established $P_{r,min}$ values. Figures 3.19b and 3.19c present as comparing well to the 2138

approximations due to including the behaviours of secondary shock and clearing features respectively discussed by Rigby et al.^[133]. Section 3.2.3.2 discusses the strength in the 'Cubic Negative' approximations when empirically accounting for secondary shock loading.

2143 3.2.3.2 Secondary Shock Phenomena

The secondary, and successive shocks, of an explosive are noticeable features in a pressure-2144 time history. Despite some preliminary efforts of establishing yield prediction parameters 2145 through experimental work^[62,129,133], there is yet to be a rigorous investigation of all shock 2146 wave parameters. Noted in Rigby and Gitterman^[129] is the inability of numerical mod-2147 elling to capture the negative phase and secondary shock behaviours accurately. The root 2148 cause is currently unknown but is speculated to be related to erroneous detonation me-2149 chanics integrated within simulations, proving it necessary to establish the behaviour of 2150 secondary shocks empirically. The secondary shock, unlike the initial shock, has to travel 2151 through the detonation product fireball and therefore, the properties of the surrounding 2152 medium (such as temperature, sound speed etc.) are believed to strongly influence the 2153 behaviour and timing of the secondary shock. 2154

2155

In Rigby et al.^[133] there is no mention of the inclusion of afterburn within the numerical 2156 simulations and therefore an under prediction of the fireball properties results in addi-2157 tional reactions being omitted and the secondary shock arriving later. The APOLLO 2158 simulations documented in Farrimond et al.^[50], use explicit afterburn which results in an 2159 early arrival of the secondary shock. This was related to inaccuracies in defined caloric 2160 EOS detonation and combustion products over predicting the speed of sound within the 2161 fireball^[179]. Whilst the arrival time of secondary shock is a known flaw in numerical sim-2162 ulation, the loading form of the shock is captured accurately and parameters compared to 2163 experimental work for validation. 2164

2165

With the successive shock waves occurring in the wake of the primary shock, alongside any systematic experimental features within the recordings, producing a standardised and automated analytical tool for all parameters currently holds difficulty. Figures 3.20ad present scaled secondary shock parameters, using a TNTe = 1.22, which have been established and compared to KB predictions for primary shock waves.



Figure 3.20: Compilation of scaled secondary shock parameters resulting from visual analysis of 250g PE4 hemispherical charge using a TNTe=1.22: a) Negative Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time Duration.

KB predictions across the four blast parameters visually shows a lack of agreement when 2171 scaling the PE4 secondary shock data based on the corresponding TNTe=1.22. General 2172 consistency within the data itself is experienced at each increment of scaled distance. This 2173 finding was surprising based on both the difficulty in assigning these parameters within 2174 the negative and the unpredictability of the temporal characteristics of a secondary shock 2175 wave as it propagates through chaotic fireball and detonation products. When comparing 2176 the result directly with those presented in Figures 3.10a-d, similar behaviour are exhibited 2177 with respect to scaled distance suggesting that secondary shock waves present similarities 2178 to a free-air shock wave for far-field scenarios. Future work should consider methods of 2179 predicting secondary shock parameters through the development of similar semi-empircal 2180 prediction curves to that presented by [87]. 2181

2182

The delayed offset of $\sim 5ms$ on average in scaled arrival time of the secondary shock, when 2183 compared to the KB predictions, is displayed in Figure 3.20b. The initial conclusions to 2184 this was that is was directly linked to the time delay between a detonation wave travelling 2185 to the charge extents, a rarefaction wave collapsing towards the centre of detonation, 2186 coalescing and then reflecting back out as the secondary shock. However, this mechanism 2187 in 250g hemispherical charges would be over in around 0.01-0.02ms, when considering a 2188 constant detonation velocity of 7800m/s in PE4. The question then posed was what makes 2189 up the remaining 99% of the offset time in secondary shock arrival time. This phenomena 2190 is discussed in more detail in Section 4.2.3.1 when more data is available across a number 2191 of different explosives. 2192

2193 3.2.4 Future Considerations for Pressure Gauge Work

The main concern with current practices of pressure gauge related blast trials is the lack of systematic feature consideration when designing a testing facility and analysing any resulting data. The shock wave mechanisms of clearing and reflection, discussed in Section 2, can have detrimental effects to a pressure-time history depending on the features the analyst wants to consider. Despite best efforts, the blast arena trials conducted at the University of Sheffield are not absent of systematic features but make best attempts at reducing them, as discussed in Section 3.2.

Future pressure gauge work and blast trials should make more use of numerical models and create synergetic solutions to how data is captured. Through a fundamental understanding of the parameter, variations to experimental methodologies can be made to improve the accuracy and consistency in the desired blast parameter. This will push the community in the direction of a clear and coherent understanding of blast wave mechanics and achieve general consistency across the full range of scaled distances.

2208 3.2.5 Pressure Gauge Summary

This section focusses on the analytical and experimental techniques which can be adopted for pressure gauge type recordings across the far-field range. Within this thesis, the application of the aforementioned methods on PE4 hemispherical detonations, demonstrate high levels of accuracy of output blast parameters from both the positive and negative

²²⁰¹
phase. These have been used to validate the KB predicting tools across the far-field range. These tools will be referenced throughout the duration of this thesis to assess the validity of their application across both ideal and non-ideal explosives in the far-field range.

2217 3.3 High Speed Video (HSV) Recordings

Detailed within this section of the thesis is the discussion of how high speed video recordings can be used to develop a more robust understanding of free-air blast parameters. Ultra high speed recordings are shown to provide both qualitative and quantitative information on the detonation wave physics, alongside the early expansion of the fireball and subsequent shock wave.

2223

2224 3.3.1 Far-Field HSV Analysis (Ai)

As mentioned in Section 3.1.1, high speed video cameras were utilised for recording the 2225 shock wave propagation through the surrounding air medium as the result of an explosive 2226 detonation. Visual representation of an explosive trial offers a full spatial and temporal 2227 understanding of a detonation event, within the confines of camera resolution. If utilised 2228 correctly, HSV provides a much more robust understanding of shock wave development in 2229 far-field scenarios whilst reducing the number of trials required to get a similar represen-2230 tation using pressure gauges alone. The following sections discuss the various procedures 2231 which have been iteratively developed to track shock waves within the literature, and 2232 present newly automated tools to analyse high speed video recordings of far-field explo-2233 sive detonations. 2234

2235 3.3.1.1 Shock Wave Edge Detection Process

Rigby et al.^[130] presented an edge-detection process for explosive video recordings using high speed video cameras. The inbuilt MatLab function, $edge^{[21]}$, was suitable for optical tracking of the fireball/air interface in near-field explosive analysis due to the presence of a clear contrast between the luminous fireball and the ambient air. However, when testing the modified '*edge*' function for far-field scenarios the absence of a fireball in the images and low variations in light intensity across the shock front resulted in the most noticeable edges being those of the zebra board behind the shock front. This caused any analysis
using this method to output alone the outlines of the background image rather than any
shock wave propagation.

2245

Hargather and Settles^[71] presented an image subtraction method which identifies the regions of greatest variation in pixel brightness between two consecutive frames. This method is particularly suited for situations with imagery of low contrast but with a clear schlieren disturbance^[59]. A simplified approach was developed based on this idea is presented in Equation 3.1.

2251

$$N_{i,j,k} = F_{i,j,k+1} - F_{i,j,k} \tag{3.1}$$

2252

2253

where N is the resulting image subtracted video file, F the recorded video file, i and j are 2254 the pixel locations in terms of columns and rows respectively, and k is the frame number. 2255 A comparison exercise was undertaken between the Hargather and Settles^[71] method and 2256 the simplified approach developed during this research in Equation 3.1. The results were 2257 nominally identical for the videos tested but the simplified approach completed much faster 2258 due to the equation being simplistic. Despite the image subtraction method being suited 2259 for low levels of lighting, weather conditions at the University of Sheffield testing site vary 2260 massively throughout the year and therefore had justification for some trial recordings 2261 yielding impractical footage for analytical purposes. 2262

2263

Whilst the method presented in Hargather and Settles^[71] has been shown to work well against a structured, repeatable background, other work using similar methods^[103] has been shown to yield accurate results with a highly variable "noisy" background. The accuracy of this method for images with low contrast backgrounds has yet to be proven, however it is envisaged that more sophisticated techniques (e.g. PIV) would be needed instead of the simple edge detection and image subtraction technique described herein.



Figure 3.21: HSV stills from a test using 250 g PE4 hemisphere at 4 m stand-off: a) Raw video footage, and; b) Corresponding image subtraction

Utilising the simplistic image subtraction method results in frame-by-frame outlines of 2271 the disturbances caused by the propagating shock wave as seen in Figure 3.21b. Whilst 2272 it is clear from the presented images where the spherical expansion of the shock front 2273 is generally, prescribing an actual position of the front held some ambiguity. A bespoke 2274 algorithm was written to accurately locate the propagating shock wave amongst random 2275 light variations between frames from the subtracted images which aimed at identifying 2276 large disturbance regions and assigning a specific singular pixel within said region as the 2277 position of the shock front. The process consists of three stages: Pixel cluster identifica-2278 tion, Intensity changes along radial spokes and Radial distance confirmation, the concept 2279 of which is shown Figure 3.22. 2280



Figure 3.22: Method for detecting location of Shock Front through intensity changes on a virtual 'spoke' overlaid with pixel cluster identification

- 1. **Pixel cluster identification**: After eliminating any random light variation between 2282 subsequent frames through light intensity filtration, a clearly defined propagating 2283 shock wave can be identified by clusters of pixels, as seen in Figure 3.21b. The 2284 clustering size is directly related to the camera's shutter speed, i.e. the lower frame 2285 rates resulted in an increased blurring effect and large clusters. A MatLab script was 2286 written to locate the areas of each frame which had five or more connected pixels 2287 with large levels of light change in the image subtracted video, N. It is anticipated 2288 that with a higher frame rate, the number of connected pixels may reduce along 2289 with a more defined shock front, but 5 pixels was sufficient for all far-field videos 2290 discussed within this thesis. 2291
- 2. Intensity changes along radial spokes: In a similar manner to previous stud-2292 ies^[130], the second stage of the algorithm discretised the camera resolutions domain 2293 into 1° increments along virtual 'spokes' which span from the charge centre to the 2294 extents of the recording boundary. The location of any pixels which have light in-2295 tensity changes along each 'spoke' are stored for each increment of angle and each 2296 frame. Due to the explosive charge being out of shot in each recording, the location 2297 was approximated through scaling-based calculations using the size of a pixel in the 2298 plane of the charge and known geometric relationships between the charge location, 2299 zebra board, camera and the pressure gauge in field of view, following proceedures 2300 outlined by Gerasimov and Trepalov^[60] and Kucera et al.^[93]. Fiducial markers on 2301 the zebra board, spaced 1.23 m horizontally and 1.33 m vertically, were used to cali-2302

2303 2304 brate the corresponding pixel size of ~ 3 mm for video resolution of 1024x560, which was consistent across all far-field videos discussed.

3. Radial Distance Confirmation: The pixel locations saved as a result of stage one 2305 and two were then compared directly to automate the shock front locating algorithm 2306 along each 'spoke' and remove any random light variation between frames. A MatLab 2307 script was written to compare stages one and two with an uncertainty region of ± 2 2308 pixels about the mean pixel location of the stage one results. This presented all 2309 the pixels which satisfied both stages of the analysis. The difficulty then came with 2310 assigning a distance to the regions of pixels which have been assigned in 3D space 2311 from a 2D image. Due to the spherical expansion of the shock wave and a fixed 2312 camera location, considerations had to be made to account for the camera recording 2313 the front of the shock wave in a different position to where the front would be along 2314 the gauge line used as the reference for calibration, as seen in Figure 3.23. To find 2315 the radial distance a given pixel is away from the charge, the locations of the camera, 2316 explosive and shock wave pixel location on the zebra board, denoted by subscript 2317 i, j and k respectively, were set up with coordinates in 3D space, x, y and z. The 2318 distances between each of the three locations were calculated using Equations 3.2, 2319 3.3 and 3.4, where a is the distance between the explosive and the camera, b is the 2320 distance between the explosive and pixel's relative location on the zebra board, and 2321 finally c is the distance between the camera and the pixel's relative location on the 2322 zebra board (again see Figure 3.23 for reference). 2323

$$a = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2 + (z_i - z_j)^2}$$
(3.2)

2324

$$b = \sqrt{(x_j - x_k)^2 + (y_j - y_k)^2 + (z_j - z_k)^2}$$
(3.3)

$$c = \sqrt{(x_i - x_k)^2 + (y_i - y_k)^2 + (z_i - z_k)^2}$$
(3.4)

2326

The distances evaluated from the above outline algorithm are then used to calculate the area of the triangle, A, enclosed between the three points in 3D space using Heron's formula (Equations 3.5 and 3.6). Assuming that the shock wave is expanding spherically, and the line between the camera and the shock wave pixel location is a tangent to the sphere, and therefore the radius, r, of the shock front would be equal to the height of the ²³³³ triangle, *abc*.

2334



Figure 3.23: Schematic of shock wave radius calculation in 3D space to be used in conjunction with Equations 3.2-3.6

After calibrating, the pixel furthest away from the charge centre was identified as the 2335 position of the shock front along a particular 'spoke', at a given time. This was done 2336 to achieve test-to-test consistency regardless of the frame rate and associated blurring. 2337 It is important to note that although strict experimental procedures were in place, focal 2338 lengths were difficult to record as a manual zoom was used. Despite the levels of zoom 2339 being consistent, lens distortion effects subsequently were not accounted for during each 2340 test and thus would cause minor variations between videos recording different stand-off 2341 distances. Previous research has suggested that lens distortion results in minimal levels 2342 of uncertainty in pixel size calibration^[136] but across a large testing pad could begin to 2343 induce some variation between different test setups. The presented within this thesis for 2344 far-field trial minimised the severity of lens distortion by comparing only like-for-like tests 2345 which would therefore remove the uncertainty associated with recordings made at the ex-2346 tents of a camera resolution for one standoff which corresponds to a more central region 2347 for a different standoff tested. 2348

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$
(3.5)

$$s = \frac{a+b+c}{2} \tag{3.6}$$

$$r = \frac{2A}{c} \tag{3.7}$$

2350 2351

2352

3.3.1.2

The results from the edge detection algorithm for a single test (250g PE4 hemisphere at 2353 5m stand-off) are presented in Figure 3.24. KB predictions are also presented on the afore-2354 mentioned figure, again using Hopkinson-Cranz scaling and a TNT equivalence of 1.22 to 2355 compare the raw data directly to an equivalent prediction. The high levels of agreement 2356 highlights the repeatability and accuracy in the results from the presented automated im-2357 age tracking and arrival time interpolation algorithms discussed throughout the section 2358 and therefore validates them for use across all other far-field high speed video recordings 2359 of shock front propagation. When comparing Figures 3.10a and 3.24, the full-field data 2360 extracted from a single video gives a clear justification for the use of HSV over pressure 2361 gauges when studying shock wave arrival time. 2362

Example of Edge Detection Algorithm



Figure 3.24: Shock front arrival time from a 250g PE4 hemispherical charge placed at a 5m standoff, recorded using HSV and scaled using 1.22 TNT equivalence factor to compare to KB predictions

The results from the edge detection analysis of the primary shock, presented in Figure 3.24, 2364 provides confidence in the methodology introduced which could be utilised for all explo-2365 sives tested in the far-field testing regime. Unfortunately for the PE4 trials tested, the 2366 technique was in development and therefore the critical parameters required to achieve 2367 accurate credible data were not yet known. Despite the method being suited for low levels 2368 of lighting, when weather conditions were unfavourable, videos yielded data which exhibit 2369 unclear shock discontinuities and therefore were omitted from detailed analysis. Provided 2370 the lighting conditions during testing are ideal, the analysis presents clearly defined edges 2371 of the shock with less noise from over-exposing the video. In certain instances when the 2372 conditions were preferable, the analysis was able to extract secondary shock wave data 2373 which was visible to the naked eye providing another benefit for this analytical method; 2374 this will be discussed in Chapter 4.3.3. 2375

2377 3.3.1.3 Shock Wave Arrival Time Interpolation

Blast parameters such as peak incident and reflected pressure can be linked to shock velocity (Mach number) through the well-known Rankine-Hugoniot jump conditions^[90]. There is motivation, therefore, to understand how blast wave arrival time (and thus Mach number) varies with changing distance from the centre of the explosive, as this will provide insights into the variability of pressure and impulse parameters and the implications therefore on designs.

2384

A method, presented visually in Figure 3.25, was proposed to interpolate arrival time data at increments of 0.1 m/kg^{1/3} scaled distance along each virtual '*spoke*' for a given far-field shock wave tracking HSV recording. In doing this, a direct comparison could be made between pressure gauge recordings of arrival time, with discrete scaled distances, and high speed video recordings with discrete increments of time between each frame but a variety of processed scaled distances using the methods detailed in Section 3.3.1.1.



Figure 3.25: Method of interpolation of shock front arrival times along a virtual 'spoke' for prescribed scaled distances

Through collecting the interpolated arrival times with respect to scaled distance along each radial spoke, different types of analysis become available for comparing the results from HSV trials directly to those corresponding the pressure gauge trials. The synergy ²³⁹⁵ between two testing methodology provides validation of the each data acquisition and
²³⁹⁶ analytical method adopted alongside providing both precise measurements from discrete
²³⁹⁷ individual gauges and more generalised full-field representation using camera footage.
²³⁹⁸

2399 3.3.1.4 Extrapolating Blast Wave Features

An important thing to note, is that the techniques discussed in Section 3.3.1 can be used 2400 to evaluate a more robust understanding of other features of free-air blast waves, provided 2401 that the experimental conditions are favourable. The tools aforementioned could be im-2402 plemented to track not just the primary wave propagation but all subsequent waves and 2403 reflections. The ability of tracking secondary shocks is purely down to the sharpness of the 2404 visible propagation on the video recording, improved providing the lighting is adequate. 2405 This data extraction can be used to develop the understanding of the secondary shock 2406 phenomena discussed in Section 3.2.3.2 when acquired through pressure gauge recordings. 2407 2408



Figure 3.26: Shock front arrival time from a 250g PE4 hemispherical charge placed at a 5m standoff, recorded using HSV and scaled using 1.22 TNT equivalence factor to compare to KB predictions, detailing the capture of the secondary shock propagation.

²⁴⁰⁹ Figure 3.26 is an example of extracting subsequent shock data from a 250g hemispherical

2410

2411

which disagree with the data. The cluster of data points at the extents of the camera 2412 view, $Z > 7 \text{m/kg}^{1/3}$ in this test, is a result of the primary wave reflecting back towards the 2413 charge centre detailed by a reduction in distance travelled with time. The reflected wave 2414 propagation was not of interest for the contents of this thesis and so improvements to the 2415 tracking algorithm was not made to account for this change in direction of the wave. The 2416 other anomalous results which appear around the secondary shock data points are analyt-2417 ical errors associated with the light intensity of pixels during the image subtraction being 2418 more variable for weaker shocks. As mentioned above, with preferable lighting conditions, 2419 the HSV extracted data for both primary and subsequent shocks will exhibit less scatter. 2420 2421

2422 3.4 Future Considerations for HSV Work

2423 3.4.1 Far-Field Methodology Errors (Ei)

Despite the clear capability of the presented HSV data capture techniques and analysis, 2424 there are still concerns with the accuracy due to systematic errors which have yet to 2425 be fully considered and mitigated from the current experimental practice. Figure 3.272426 displays the results of implementing the shock wave arrival time tracking algorithm, dis-2427 cussed in Section 3.3.1.1, for a nominally identical trial to that presented in Figure 3.242428 - a 250g PE4 hemispherical detonation at 5m standoff from a reflected surface. It is im-2429 portant to note during this trial, an arbitrary intentional but non-obvious skew of the 2430 camera's field of view was made during the experimental setup away from the charge to 2431 assess the sensitivity of the analytical techniques to systematic errors in camera placement. 2432 2433



Figure 3.27: Shock front arrival time from a 250g PE4 hemispherical charge placed at a 5m standoff, recorded using HSV and scaled using 1.22 TNT equivalence factor to compare to KB predictions, showing the effect off having testing procedure not perfectly square.

The systematic rotation in any direction would skew the number of pixels contained be-2434 tween the reference markers used to calibrate each frame of the video. This causes it to 2435 appear a smaller distance than what it would be if all equipment was perpendicular as 2436 per the analytical techniques assumptions. If a lower number of pixels is measured for the 2437 same known distance, each individual pixel size would increase in value. As the lengths 2438 calculated at each stage of the analytical process are directly proportional to these pixel 2439 sizes, a reduction in size would result in everything appearing to travel faster than a real 2440 shock wave. This is visible from the behaviour presented between the experimental data 2441 and KB predictions within Figure 3.27. With this knowledge, a reduction is required to 2442 the calibrated pixel size to account for the skew in the experimental setup. 2443

In doing so, a skewed angle between the camera and the zebra board of approximately 2° was evaluated. This value of angular rotation was used to investigate the sensitivity of evaluated shock wave positions when only minor tweaks to assumed camera positions are made. The magnitude of this rotation is minor but across the distances covered during this experiential setup accounts for almost 750mm additional distance theoretically assigned

hence the shock wave tending to arrive sooner than KB predictions in the experimentaldata.

2452



Figure 3.28: Re-analysed data from Figure 3.27 with an adjustment to the calibrated pixel sized to account for the skewing of the FOV during camera rotation.

The HSV data when adjusted for this skew presented a more reasonable comparison to 2453 KB predictions with an offset in the data. This generally suggests the shock wave has 2454 travelled further than predictions in the same amount of time, as seen in Figure 3.28. 2455 This has been deduced to be an effect of the prescribed initial boundary conditions set 2456 for the theoretical charge location, not visible within the video but is known through 2457 real-world measurement. The distance to which the camera's FOV extends is calculated 2458 using the visible pressure gauge position and the pixel size established during calibration. 2459 This distance was then subtracted from the known standoff to assign the location of the 2460 theoretical charge with respect to the pressure gauge in the respective video. Knowing 2461 the pixel size is larger during the skewed test means that the location of the explosive off 2462 screen has been re-defined as being closer to the gauge wall that what it is in reality. This 2463 is why generally a faster arriving shock wave is established. 2464

2465

²⁴⁶⁶ It is essential to ensure the correct positioning of all initial reference markers and bound-

ary conditions prior to conducting any future far-field HSV recordings. Despite the large quantity of data which can be extracted from HSV recordings, if the positions are not in-line with assumption made in the analytical procedures then the results will be inaccurate. The time committed to setting up cameras with high levels of precision is significant but the gain in data quantity in comparison to that collected during pressure gauge trials outweighs this.

```
2473
```

This is just one of many errors which could result in strange behaviours of the analyt-2474 ically established arrival time data which should be consistent with KB predictions in 2475 far-field regimes. Ensuring the assumptions made in the analytical procedures align with 2476 the actual experimental setup clearly holds importance for data accuracy. This finding is 2477 linked with that discussed in Section 2.9 where the clear disregard for systematic errors 2478 in methodologies and analysis have resulted in published articles suggesting far-field blast 2479 parameters exhibit inherent variability. In actual fact, if these errors are accounted for, 2480 nominally identical data is consistent and is highly comparable to KB predictions. 2481 2482

2483 3.4.2 Extracting More Parameters (Ai)

The strength in using high speed video techniques for experimental trial data extraction is the vast quantity obtained from a single trial. Despite work being undertaken relating arrival time data to pressure within the available published literature using Rankine-Hugoniot principles, there is still a gap in extracting the specific impulse of a shock wave using optical methods.

2489

Murphy and Adrian^[104] looked at developing a particle image velocimetry (PIV) system 2490 which measures velocity fields as a result of detonating explosives. The method was effec-2491 tive in far-field scaled distance ranges when comparing to assumed triangular blast wave 2492 profiles, but struggled in near-field instability and turbulence regions. Hargather and Set-2493 tles^[70] made efforts at using optical techniques to measure and attempt to scale explosive 2494 parameters in the gram-range. Whilst the authors made efforts at characterising arrival 2495 time and pressure through Rankine-Hugoniot conditions and time duration through the-2496 oretical assumptions proposed by Kinney and Graham^[90], no link was made to specific 2497 impulse of the shock wave. 2498

The current background orientated schlieren methodology used for far-field HSV data cap-2500 ture at the University of Sheffield could be developed to incorporate PIV analysis. To do 2501 so, it is essential for the far-field recordings to be calibrated to account for lens distortion 2502 and any further experimental errors associated with camera orientation which can be done 2503 so effectively using MATLAB's in-built camera calibration software. Once calibrated, an 2504 interesting development of this method would be to assess the velocity field measured 2505 using PIVlab, another in-built MATLAB GUI, in the attempt assign the time at which 2506 the positive phase ends for a propagating shock wave. Adopting a triangular blast wave 2507 profile approximation, the pressure at a given position, evaluated through arrival time, 2508 and the time at which positive phase ends, an estimation of specific impulse of the shock 2509 wave can be achieved at that given point. 2510

2512 **3.5** Summary

2511

The main body of established blast literature covers yield results of idealised high explosives when detonated in various scenarios. As mentioned throughout Chapter 3, the variety in conclusive findings does pose difficulty for truly understanding the fundamentals of blast wave phenomena alongside the associated inherent variability of recorded data.

The real-world implications of this lack of clarity is the uncertainty of both the effects 2518 an explosive threat yields alongside the confidence in protective measures to withstand 2519 the given threat. Engineers face a constant battle of providing improved efficiency and 2520 aesthetics in design, both of which may result in a reduction in the intrinsic robustness 2521 of a structure, thereby increasing the need for considered and holistic blast protection 2522 measures. Whilst ever there is a major disagreement between the consistency of yields 2523 resulting from a given explosive, there will always be a lack of confidence in protective 2524 structures implemented and therefore massive safety factors applied to ensure the upper 2525 bound of quoted variability is accounted for. 2526

2527

The need for a precise intrinsic quantification and characterisation of prescribed blast scenarios will enable better probabilistic assessments of threats which can be taken into consideration with more confidence at design stages of any protection regime. The idea that extrinsic sources of variability are included in experimental work used for numerical model validation is concerning when considering that some article quote spreads in pressure and impulse $\pm 50\%$. This uncertainty should be prescribed at a later stage when considering the likely threats rather than including extrinsic error through poorly executed research.

2536

This chapter has focussed on developing validated methods of experimental and analytical 2537 capabilities which result in consistent data from nominally identical trials. A detailed 2538 review of historical blast data has been presented which opens up the discussion, in line 2539 with Objective 1 of this thesis, of whether recorded blast parameters are in fact deter-2540 ministic across a range of scaled distances. The historic data provides confidence in the 2541 consistency in explosive yields across two well documented compositions used during the 2542 high explosive era, but more recent research has highlighted variability regions as high as 2543 $\pm 130\%$. 2544

2545

This chapter has scrutinised experimental methodologies adopted during free-air blast 2546 loading trials and the subsequent data analysis with the aim of providing validated tech-2547 niques and procedures. This can provide data which facilitates development in blast wave 2548 theory as opposed to causing further confusion within the industry as to whether explo-2549 sions are inherently variable or not. The presented techniques in this chapter have shown 2550 that for far-field scenarios, $Z > 3 \text{m/kg}^{1/3}$, blast parameter variability can be minimised 2551 and is therefore considered deterministic regardless of early-stage detonation mechanics. 2552 The techniques have however highlighted the need for strict experimental procedures, espe-2553 cially when considering near-field loading conditions as these are highly sensitive to spatial 2554 variation of the energy release upon detonation. The remainder of this thesis will focus 2555 primarily on far-field studies to characterise the effects of a variety of different explosive 2556 compositions across a range of scaled distances. 2557

²⁵⁵⁸ Chapter 4

²⁵⁵⁹ Ideal Explosive Blast²⁵⁶⁰ Characterisation

2561 4.1 Introduction

Considering the established hypothesis in Chapter 3, in that explosive yields are in fact deterministic when experimental methodologies adopt strict experimental control and automated analytical tools, a variety of different ideal high explosives have been examined to simultaneously further validate the tools presented in the aforementioned chapter. The aims of these analyses are to improve data consistency across a range of different ideal explosives and to quantify the levels of variability each blast parameter exhibits across a range of scaled distances.

2569

Through conducting well-controlled trials across a number of ideal explosives and scaled distances a comprehensive understanding of definitive variability regions, in line with the hypothesis proposed by Tyas^[173], can be established. When comparing the extracted data set independently and to semi-empirical predictions, developments to the fundamental understanding of explosive air shock and confidence in KB predictions and TNT equivalence can be established for different ranges of scaled distance.

2577 4.2 Pressure Gauge Data

In similar fashion to Chapter 3, this section will consider the data captured using pressure gauges during experimental trials. This will be used in the attempt to both validate the on-going hypothesis of far-field blast parameters being deterministic and to assess the capability of the methods developed for analysis across a number of ideal explosives.

2583 4.2.1 Positive Phase Blast Parameter Variability

This section will evaluate the explosive output of three ideal high explosives; PE4 (nominally 88% RDX with 12% Plasticiser/Taggant), PE8 (nominally 86.5% RDX with 13.5% Plasticiser/Taggant) and PE10 (nominally 86% PETN with 14% Plasticiser/Taggant), using tools established in Chapter 3. The choice of explosives used for the assessment techniques was based on their usage within a military setting, ease of acquisition through UK energetics vendors and predominantly due to the vast amount of historical testing undertaken at the University of Sheffield.

2591

PE4 and PE8 are effectively the same explosive, with similar RDX and binder percentages, 2592 despite the variation in their binder compositions. The former explosive, PE4, was de-2593 signed to match the American standard miltary grade explosive of C4 which is confirmed 2594 in the findings presented by Bogosian et al.^[15], Rae and McAfee^[115]. PE8 was a later 2595 developed RDX based explosive which was designed to supersede PE4, therefore providing 2596 no change for the end users of the explosive. PE10 again was designed to provide a similar 2597 explosive yield to PE4 but was PETN based rather than RDX offering a different explosive 2598 composition. The reasoning behind the development of this explosive was two fold: firstly 2599 to work better in colder environments; and secondly due to RDX being recognised as a 2600 problematic and bioavailable explosive which has tendencies to infiltrate watercourses^[171]. 2601 2602

With all the above mentioned, the results of any trials adopting the same methodology and data analysis for these three explosives is hypothesised to yield the same blast parameters. This was assumed true for far-field free-air scenarios, where any afterburn related to secondary chemical reactions ongoing in the fireball minimally affects the overall positive phase pressure-time history. The results of the far-field tests will be assessed and 4.2.1.1

2612

2613

compared against both semi-empirical predictions and high-fidelity numerical modelling. This comparison had the overall aim of demonstrating that far-field blast parameters, $Z > 3m/kg^{1/3}$, can essentially be considered deterministic, whilst providing an example of the synergistic nature between the two.

Intrinsic Data Set Variability

To assess the intrinsic variability in a given data set, each positive phase blast parameter 2614 has been normalised against the mean value of that particular parameter for nominally 2615 identical recordings. By adopting this analysis approach, the consistency in the data set 2616 can be deduced and can help determine as to whether the working hypothesis of deter-2617 ministic blast parameters holds credibility across a range of scaled distances and explosive 2618 types. The analysis considered the three explosives mentioned above to determine the 2619 inherent variability in the explosive yield of three ideal high explosives when adopting val-2620 idated methods of conducting experimental trials and data analysis discussed in Chapter 3. 2621 2622

Figures 4.1a-d represent the findings from the initial intrinsic data set variability assessment of each positive phase blast parameter after adopting experimental procedures and analysis as detailed in Chapter 3. Notably what can be seen is a high level of repeatability in the processed positive phase blast parameters across all three explosives and scaled distances considered.

2628

Reflected peak pressure, peak specific impulse and positive phase duration exhibit similar levels of spread across the entire range of scale distances tested; typically around $\pm 6-8\%$, with a slight reduction in consistency as scaled distance reduces seen in Figures 4.1a, 4.1b and 4.1d.



Figure 4.1: Compiled blast parameters from RDX and PETN based explosive trials as a function scaled distance, normalised against the mean of nominally identical trials: a) Peak reflected overpressure (Mean-Normalised P_r), b) Scaled reflected peak specific impulse (Mean-Normalised I_r), c) Scaled arrival time (Mean-Normalised t_a), d) Scaled positive phase duration (Mean-Normalised t_d)

The arrival time of the shock wave, in Figure 4.1c, exhibits a considerably smaller spread, within $\pm 2\%$ when $Z > 3 m/kg^{1/3}$, which is to be expected for a parameter of generally much lower magnitudes. Again, a noticeable increase in variability as scaled distances reduces in line with findings presented in Rigby^[127].

2638

The consistency of the experimental results presents a clear indication that for small-scale, far-field, geometrically simple scenarios, the blast positive phase parameters are essentially deterministic with quantifiable but limited levels of variability. Despite only a few data points at each scaled distance, there is a clear reduction in arrival time variability as scaled distance increases which holds true for all three explosive types. Although not as evident across the other blast parameters, a reduction is present, which agrees with the idea proposed by Stoner and Bleakney^[160] and Bogosian et al.^[16] that variability levels differ with scaled distance.

2647

The results of this analysis provides enough evidence to suggest that as the near-field is 2648 approached, $Z < 3m/kg^{1/3}$, a much greater spread in the arrival time data, and thus 2649 other blast parameters, is observed which agreed with findings presented by Simoens and 2650 Lefebvre^[153]. This not only provides evidence to the hypothesis of scaled distance regions 2651 over which fireball surface instabilities are prominent, as discussed by Tyas et al.^[174]. Rae 2652 and McAfee^[115] and Rigby et al.^[130], but when compared with other published works 2653 on blast variability starts to build a more robust understanding of the development of 2654 explosive shock fronts. 2655

2656

2657 4.2.1.2 Comparison Against Semi-Empirical Predictions

To assess the robustness of the KB prediction method and the accuracy of the data presented within this thesis, a Mean Absolute Error (MAE) analysis was undertaken between the results from each explosive and those predicted for varying quantities of TNT. This analysis was done to establish the best possible TNT equivalence value to represent each explosive. It is expected that due to the three explosives in question being designed to result in similar explosive yields on detonation, that the TNT equivalence values for farfield free air scenarios should be similar across all explosives tested.

The results presented in Figure 4.2d shows that generally speaking the positive phase duration tends to hold higher levels of variability due to the difficulty in assigning a specific value to the parameter. This is due to noise in the signal making the true point at which conditions return briefly back to atmospheric difficult to determine. It is further deduced that experimentally recorded results are around 90% of KB predictions which would cause any MAE analysis for a TNT equivalence value to be skewed. Thus, positive phase duration has been omitted from the considered MAE analysis.



Figure 4.2: Compiled blast parameters from RDX and PETN based explosive trials as a function scaled distance, compared with KB predictions: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration

The analysis was performed for definitive far-field scenarios, $Z > 3 \text{m/kg}^{1/3}$, in light of 2674 the fact that for smaller scaled distances the variability levels rise. This believed to be 2675 a result of not only systematic experimental errors but also ongoing chemical reactions 2676 in the fireball resulting in fluid dynamic instabilities which differ from composition to 2677 composition. Therefore the decision was made that evaluating a TNT equivalence value 2678 for only the free-air shock propagation in the far-field was the philosophy of this analysis. 2679 This was undertaken through comparing the scaled mass equivalent shock produced from 2680 the explosives in question to KB predictions for 1kg of TNT. 2681 2682

It was found through averaging of the MAE values for pressure, specific impulse and arrival time at all far-field scaled distances, the three explosives all resulted in very similar TNT equivalency factors: PE4 and PE10 resulting in an equivalence of 1.22; and PE8 resulting in an equivalence of 1.24. This was a further reassurance and validation in both the experimental and data analysis techniques adopted for these trials as the three explosives were designed to have the same explosive yield. The TNT equivalence factors were applied to each of the corresponding compositions and subsequent recorded blast parameters presented in Figures 4.2a-d. The scaled results show a striking agreement between each blast parameter (expressed as a 1kg hemispherical TNT charge), and KB predictions.



Figure 4.3: Compiled blast parameters from RDX and PETN based explosive trials as a function scaled distance, normalised against KB predictions for nominally identical trials: a) Peak reflected overpressure (KB-Normalised P_r), b) Scaled reflected peak specific impulse (KB-Normalised I_r), c) Scaled arrival time (KB-Normalised t_a), d) Scaled positive phase duration (KB-Normalised t_d)

²⁶⁹³ Despite Figure 4.2d again showing experimentally recorded values generally lower than ²⁶⁹⁴ KB predictions, this finding follows the same trends presented in Figures, 2.12d, 2.13d ²⁶⁹⁵ and 3.10b. This, along with the agreement of each blast parameter with KB predictions in all of the remaining subplots in the aforementioned figures, validates the hypothesis that for far-field scenarios, ideal high explosive blast parameters are deterministic despite the variety in researcher, methodology, composition, analysis techniques and finally the year the trials were undertaken.

2700

2705

In order to establish specific levels of variability that the scaled experimental recordings had in comparison to KB predictions, a similar approach to that discussed in Section 4.2.1.1 was adopted in which the experimental recordings were normalised but by the KB prediction of the parameter at each scaled distance for which data was available.

Figures 4.3a-d present the results of the KB normalisation, which shows that for far-field 2706 loading in simple geometrical scenarios, existing semi-empirical predictions are in fact 2707 remarkably accurate and compare well to experimental data. This suggests that semi-2708 empirical methods can be used with confidence as a first-order approach for quantifying 2709 the blast load conditions from a small-scale high explosive in simplified far-field situations. 2710 The slight increase in the variability as the scaled distance reduces to the extent of those 2711 presented in these trials. This gives rise to the ongoing hypothesis that as recordings 2712 approach the near-field there is less certainty in the data captured. 2713

2714

Interestingly to note from Figures 4.3a and 4.3b is the opposing correlation of recorded peak pressure and specific impulse to KB predictions. Taking into account the fact that the data presented was the result of a purely top detonated testing regime, the findings presented in Figure 3.16, found in Section 3.2.2.3, show comparable results to facilitate this discussion.

2720

The peak pressure recorded in a top detonated blast is much lower than that of a bottom 2721 detonated simulation as result of inconsistent detonation product break out. The faster 2722 arrival time associated with top detonation is a direct result of the early expansion and 2723 the un-spherical propagation of products and shocks associated with the decomposition 2724 at the top of the charge. This then re-adjusts when the detonation wave reaches the 2725 bottom of the charge, effectively releasing all of the potential energy and the remaining 2726 detonation products begin to radially expand. This results in mach stems formation and 2727 thus a superposition of waves resulting in standard friedlander pressure-time histories at 2728 greater scaled distances. This finding provides clear explanation as to why experimen-2729

tally the peak pressure values are lower than KB predictions for top detonated charges presented in Figures 4.3a. This does however reveal a systematic error in the majority of the presented data within this thesis, in that for near-field scenarios the complex interaction of the shock wave and detonation products results in increased uncertainty of the data.

Taylor^[167,168,169] discussed in great detail the theory behind how blast waves form and hypothesised an instantaneous release of energy from an infinitely small point in space resulting in radial expansion of the products and shock. Whilst the data presented for the far-field scaled distances agree with equivalency scaling of spherical shock wave parameters, the smaller scale distances highlight a greater sensitivity of resulting blast parameters. This has been related directly to the variable detonation mechanics in shaped charges alongside detonation position and orientation.

The presence of the gauge plate clearing effect discussed in Section 3.2.2.3, shows that with near-field conditions, the reduction in the peak specific impulse value is significant when comparing numerical simulations directly to KB predictions. Whittaker et al.^[179] ran numerical simulations to quantify the effects clearing has in this scaled distance region and showed that when $Z < 1.6 \text{m/kg}^{1/3}$ clearing can be effectively omitted. The 1.25m simulation outlined in Figure 3.16 falls very close to this region and therefore it important to only consider the trends where clearing has been effectively ignored.

When removing the clearing effect from the 1.25m numerical model, the peak pressure for 2751 a bottom detonated trial over predicts that of a top detonated shot whilst the impulse 2752 values resort to comparing with the KB predictions remarkably well. The danger in com-2753 paring purely numerical analysis to the KB predictions is that the numerical models, and 2754 their corresponding EOS's were developed using far-field data, $Z > 3 m/kg^{1/3}$. In this 2755 region the expanding fireball is no longer effecting the detached shock front. The model 2756 replicates an energy released instantaneously which results in a friedlander-like shock wave 2757 rather than one affected by the ongoing chemistry of the fireball. It would therefore be 2758 incorrect to suggest at this scale, the real-world physical mechanisms from the detonation 2759 mechanics and fireball is accurately captured. 2760

2761

2742

The results presented in Figures 4.3b are processed using the curve-fitting method presented in Section 3.2.1.1, which does its best attempt at omitting the clearing effects from purely experimental data. This raises the question as to why an increase in the specific impulse is seen in comparison to KB predictions. This can be used to further explain the narrative of why the semi-empirical method becomes inaccurate for the near-field scenarios tests. Considering Figure 4.3b, the under-prediction of impulse suggests that the energy released from these high explosives is higher than TNT within the fireball region. This difference suggest one single TNT equivlency factor cannot be definitively assigned across all scaled distances.

2771

The experimentally established positive phase duration, shown in Figure 4.3d, presents lower values to those evaluated by KB predictions by up to 15%. The large spread in the experimental recordings is directly related to the difficulty in determining this parameter, as discussed previously. This generally becomes more difficult with increased scaled distance as: (a) signal:noise is typically lower, and (b) the gradient of the latter stages of the positive phase is shallower, as can be seen in Figure 3.5.

2779 4.2.1.3 Time of Arrival Variability

Despite the visibly low levels of variability shown in both Figure 3.10a and 4.3c, shock front time of arrival, t_a , is a somewhat overlooked parameter when compared to peak pressure and peak specific impulse despite its qualitative comparison to KB predictions. The arrival time of a blast wave can be used to evaluate the resulting pressures and impulses using Rankine-Hugoniot principles which presents a utility of arrival time as a parameter for blast design purposes. The main aim of this section is to investigate and quantify the variability of shock wave arrival times, and investigate how it varies with scaled distance.

Due to the consistency of the results presented across all three high explosives tested, 2788 it was decided that arrival time of PE4 would be assessed due to having a much larger 2789 data set, with multiple repeat shots at each scaled distance. To evaluate the precision 2790 and repeatability of the data set, the relative standard deviation (RSTD) was calculated 2791 from the pressure-gauge arrival time data (from the historic and current tests presented 2792 in this thesis: 157 in total). The results of which can be used to assess variations in the 2793 measurements from this particular experimental method with respect to scaled distance, 2794 presented in Figure 4.4. 2795

To provide a more generalised relationship of arrival time variability with respect to scaled 2797 distances it was important to assess results which had enough repeat trials to represent 2798 real physical behaviours. Of all the scaled distances tested, there was a variety in which 2799 at least 5 nominally identical tests were conducted and so should provide a reasonable 2800 approximation to the general variability behaviour. These groups are shown in Figure 4.4 2801 as solid markers, whilst the hollow markers presented show the remaining scaled distances 2802 tested which had less than 5 nominally identical results. Overlaid on the plot is an ex-2803 ponential trend connecting the groupings with 5 or more trial, which when considering 2804 the same qualitative behaviour is seen in the hollow markers, decreasing variability with 2805 increasing scaled distance, is believed to be a physical representation of how variability in 2806 arrival time changes with scaled distances specifically for top detonated charges. It has 2807 been assumed however that the same behaviour would be experienced by bottom deto-2808 nated charges as a result of fluid dynamic instability formation, however to magnitude of 2809 the RSTD would be lower for equivalence scaled distances. 2810

2811

It is important to note the curve has been extrapolated for larger scaled distance values, 2812 $Z > 12 \text{m/kg}^{1/3}$, but not for near-field conditions, $Z < 3 \text{m/kg}^{1/3}$. The assumption made 2813 here is that for far-field scenarios, the propagating shock wave is unaffected by anything 2814 other than the medium it travels through, and therefore a similar relationship of variability 2815 is expected. For the near-field recordings it is however assumed the data would be affected 2816 by the sensitive detonation mechanics and to the idea of instabilities in the shock front 2817 forming and diminishing, in the intermediate range of scaled distances. The exponential 2818 relationship has been defined for the region of scaled distances tested and extrapolated as 2819 a guideline prediction outside these ranges. Future works will undertake more testing in 2820 near-field conditions, $Z < 3 \text{m/kg}^{1/3}$, in the hope to show a reduction in arrival time vari-2821 ability associated with a smooth shock front before instabilities start to form at extreme 2822 near-field in the support of the hypothesis of shock wave instability regions $^{[173]}$. It could 2823 however be that the magnitude of arrival time variability presented in Figure 4.4 would 2824 reduce if systematic detonation errors are omitted within the methodology. 2825 2826



Figure 4.4: RSTD in shock wave arrival time with respect to scaled distance, from historic and current pressure gauge data

The main point to address from this analysis is that quantifying arrival time, t_a , variability 2827 with respect to scaled distance, which the parameter itself can be chosen with little ambi-2828 guity, provides a further insight into the development of a shock front and the formation of 2829 any un-spherical nature, especially in top detonated scenarios. Current predictive methods 2830 provide discrete blast parameters for a given scaled distance an explosive is away from a 2831 target. Through understanding the spread of experimentally measured t_a , improvements 2832 can be made to fast running predictive methods to provide probabilistic blast parameters 2833 within the uncertainty range for a given distance. 2834

2836 4.2.2 Numerical Simulation

2835

The pressure gauge results presented within this Chapter, begin to build a coherent fundamental understanding of the nature of experimentally recorded far-field loading from a given charge composition, shape and mass. The importance of these findings provides a starting point to establish characteristics of more challenging blast loading conditions ²⁸⁴¹ both in the near-field and those in complex environments, knowledge of which can be ²⁸⁴² supplemented with high-fidelity numerical modelling.

2843

Whilst experimental data is beneficial for understanding the real world yield and subsequent effects of a particular explosive detonation, both the costs and safety concerns related to blast trials create a need for high fidelity numerical simulations which are able to capture the behaviours within any scenario.

2848

Understanding the mechanisms and magnitudes of blast loading on targets from both near-field detonations of high explosive, and those in complex environments, is of key importance for the analysis and design of the response of protective structures. However, there is little definitive experimental data on the measurement of these loads and consequently the predictions of numerical models of near-field blast loading are largely unvalidated.

2855

The experimental results presented with Chapter 4 have been used to validate far-field numerical models for PE4, PE8 and PE10, using the methodology outlined in Whittaker et al.^[179]. The intention was to implement the developed equations of state (EOS) for each explosive, into much more complex numerical simulations to produce validated and accurate predictions.

2861

It is important to note that the numerical modelling discussed within this thesis is collaborative work between the University of Sheffield, Blastech LTD and DSTL, which together are attempting characterise explosives with high levels of accuracy in order to map out the effects a given charge composition, mass and shape may have in a prescribed environment to better plan and protect civilian infrastructure. Whilst DSTL have conducted the numerical simulation, the author has undertaken all experimental data capture and comparative studies.

2869

2870 4.2.2.1 Model Description

The baseline numerical model consisted of 250g hemispherical charges placed on the floor which were centrally detonated (of an equivalent sphere) to match the experimental procedures adopted with the testing regime. A reflective boundary was set at the edge of the model used to represent the reflective wall (be that the bunker or the blockwork wall) with a size of 2.2m in height and 4.4m in width to prevent any clearing effects within the positive phase of the reflected shock. An additional reflective boundary was set up along the ground surface to represent the concrete pad used during the explosive trials.

2878

Afterburn is included in these free-air models to show that thermochemical analysis can suitably parametrise numerical models rather than relying on experimental methods which are very expensive and time consuming processes. The EOS was generated in a few hours using a thermochemical code. Afterburn should be included in free-field models to achieve an accurate EOS. This is to show that the model behaves in a representative way when it is included for all scenarios, whether that is relatively small amounts in free-field or large amounts in confined scenarios.

2886

The numerical model was solved using APOLLO blastsimulator, which makes use of Adap-2887 tive Mesh Refinement (AMR), and zoom levels (distance-dependent AMR) to allow finer 2888 mesh resolution to be used within the complex regions of numerical analysis^[36,109]. AMR 2889 is based on a mesh which exhibits an inconsistent resolution globally. In regions of the 2890 domain which requires a more refined resolution (i.e the detonation point, the shock front 2891 etc), the mesh refines to make more precise predictions. Other area of the mesh will 2892 reduce in resolution to allow for simulations to be undertaken faster. As the simulation 2893 progresses, as do the refined areas, and therefore providing high resolutions in the area 2894 which require them. This has the benefit of saving the computational power for the ar-2895 eas that require it through reducing the computational demand from areas where it is 2896 not needed. The AMR process requires a user-defined zone length, corresponding to the 2897 coarsest cell size, and a maximum resolution level size which corresponds to the smallest 2898 allowable cell size. The software then refines and un-refines different zones within the 2899 model (based on differentials of pressure, material etc) to accurately simulate the event 2900 while maximising efficiency. The model also uses "zoom levels" which allows a higher res-2901 olution level to be used for a fixed radius from the charge centre (e.g. a zoom level of 1 for 2902 200mm would increase the maximum resolution level by 1 until a disturbance is registered 2903 at 200mm, the model would then only allow the initial maximum resolution level to be 2904 achieved for the remainder of the model). As an example, the 2m models reviewed within 2905 the remainder of this document had the following zone lengths and resolution levels: 2906

2907	• Zone length = 200 mm, maximum resolution level = 5 .
2908	• Zoom level 3 for 200mm from charge centre.
2909	• Zoom level 2 for 600mm from charge centre.
2910	• Zoom level 1 for 1400m from charge centre.
2911	• Then maximum resolution level of 5 (6.25mm) for the remainder of the

The Explosive EOS parameters used in this study were generated using the thermochemi-2912 cal code Cheetah v7, which, due to export control reasons, are not available for publication. 2913 Therefore, an alternative thermochemical code, EXPLO5, was also used to determine the 2914 EOS for the explosives. These parameters have only been used for a complementary 2915 comparison to the Cheetah study and have not been fully assessed or validated, but are 2916 provided as representative values in Table 3.2. It is important to note the developed pa-2917 rameters were produced purely based on the explosive composition, correct density and 2918 a best guess of plasticiser material (finding the exact composition may improve the re-2919 sults), all done using the same default methodology. No calibrating to experimental data 2920 or tweaking of technique or parameters to improve results was performed. The numerical 2921 model construction is also discussed in more detail within Section 3.2.2.1 which provides 2922 additional narrative to the discussion for reference. 2923

2925 4.2.2.2 Numerical Model Validation

Figure 4.5 presents a comparison between numerical and experimental pressure histories 2926 across a range of standoff distances for each ideal explosive tested. A high degree of 2927 similarity in the qualitative form of the pressure-time histories, for all three explosives, 2928 across the entire range of far-field stand off distances, provides confidence in the modelling 2929 approach and parameters. This finding alone gives rise to the hypothesis presented by 2930 Tyas^[173] that for at least far-field scenarios, $Z > 3 \text{ m/kg}^{1/3}$, explosive characterisation is 2931 deterministic with low levels of variability. The comparable results, when adopting a more 2932 realistic representation of the test conditions, highlights the synergistic nature of these 2933 two techniques. Numerical models have become powerful enough to not rely solely on 2934 experimental data for validation and can now be used to fault-find systemic flaws within 2935 experimental procedures. 2936

2937

2924

model (6ms).



Figure 4.5: A compilation of reflected overpressure-time history plots for the three explosives tested across three different stand-off distances compared to the corresponding validated and APOLLO model predictions

Interestingly what is exhibited across each numerical simulation displayed in Figure 4.5 is 2938 a much faster arrival of the secondary shock wave when compared to experimental trials. 2939 This feature can lead to artificially high specific impulse predictions with the secondary 2940 shock arrival coinciding with the positive phase of the primary shock event. As mentioned 2941 in Section 3.2.2.1, the secondary shock arrival time varies depending on how afterburn is 2942 modelled. The current understanding of the secondary shock is that it is intimately linked 2943 to the post-detonation pressure-volume-energy relations of the fireball, which currently is 2944 not captured accurately without manual tweaks to modelling parameters^[141]. 2945

2946

2947 4.2.3 The Negative Phase

To evaluate the findings in Rigby et al.^[133], which displayed comparable predictions of negative phase parameters to well-controlled experimental testing of PE4, the same methodology and analytical techniques were adopted again for the remaining ideal explosives of PE8 and PE10. The result of which have been scaled accordingly and are presented in Figures 4.6a-c.

2953



Figure 4.6: Compilation of scaled negative phase parameters results of 250g PE4, PE8 and PE10 hemispherical charges using the representative TNTe: a) Negative Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time Duration.

The variability in each negative phase parameter is visibly greater than the positive phase 2954 parameters presented in Figures 4.2a-d for the same explosive trials. This has been linked 2955 to the increased difficulty in prescribing parameters with lower magnitudes being sensitive 2956 to electrical noise and systematic experimental features. Despite this, the main conclu-2957 sions to be drawn from the data presented in the aforementioned plots is that the plastic 2958 explosives tested behave almost exactly in line with KB predictions for far-field scenarios 2959 when conducted under strict conditions. The same cannot yet be deduced across all scaled 2960 distances as the behaviour of near field loading conditions are yet to be investigated and 2961 will be part of future planned works. 2962

2964 4.2.3.1 Secondary Shock Data

Section 3.2.3.2 began the investigation into the secondary shock and its associated blast 2965 parameters for PE4 detonations. The study presented a consistent general behaviour 2966 with KB predictions across the far-field range of scaled distance. There was however 2967 significant discrepancies in terms of the magnitudes due to being compared directly to 2968 a primary shock. Whilst the KB predictive tools in there current form do not capture 2969 secondary shock waves accurately, the presented behaviours of the associated parameters 2970 could provide insights into the mechanisms involved in their development. This behaviour 2971 is believed to be essential for fundamentally predicting them. With this idea in mind, 2972 the secondary shock data from both PE8 and PE10 was analysed in the same way, using 2973 the corresponding TNTe values evaluated in Section 4.2.1.2 are presented in Figures 4.7a-d. 2974 2975

Across all three plastic explosives tested in the far-field range, the scaled secondary shock 2976 positive phase parameters compare remarkably well when compared to one another at 2977 each increment of scaled distance. The general increase in variability associated with each 2978 of the parameters, seen in Figure 4.2, has been associated with the chaotic detonation 2979 cloud medium the secondary shock has to propagate through. This, similarly to primary 2980 wave data, tends to reduce with an increase in scaled distance seen in Figures 4.7a and 2981 4.7c. This suggests that variations related to this changing medium are insignificant once 2982 measurements are far enough away from charge centre. 2983

A feature which is exhibited within the pressure data recorded for the secondary shock 2985 (Figure 4.7a), is an apparent plateau at $Z \simeq 10m/kg^{1/3}$ and an increase in pressure values 2986 experienced some distance afterwards. The plateauing behaviour is justified through the 2987 curtailment of pressure as distance increases until the wave effectively is obsolete, but the 2988 apparent rise in pressure holds no physical explanation. This visible increase is a system-2989 atic error within the data capture at these large scaled distances. Pressure magnitudes 2990 are so low for the secondary shocks that the assignment of parameters is extremely sen-2991 sitive. Using gauges that are rated to 70 times greater than these magnitudes is flawed. 2992 The inherent electrical noise in the system accounts for ± 1 kPa and so contributes to the 2993 spreads seen. It is difficult to improve this using this methodology as gauges are required 2994 to be higher rated to survive the pressure from the primary wave. 2995



Figure 4.7: Compilation of scaled secondary shock parameters resulting from visual analysis of 250g hemispherical charges of PE4, PE8 and PE10 using the representative TNTe values: a) Negative Pressure, b) Scaled Negative Specific Impulse and c) Negative Phase Time Duration.

²⁹⁹⁷ Clearly the ideal explosives investigated within this thesis exhibit similar behaviours to a ²⁹⁹⁸ primary wave but are not captured by KB predictions when scaling the results based on ²⁹⁹⁹ the original charge mass and established TNT equivalency values.

3001 4.2.3.2 Secondary Shock Delay Predictor

The delay in time between the arrival of both the primary and secondary shocks is a feature which has been previously investigated success to quantify equivalent TNT yields ^[129]. Figure 4.8 presents the scaled secondary shock delay data across the three ideal explosives considered in this thesis. Although exhibiting a consistent behaviour with scaled distance, this could be related to the fact PE4, PE8 and PE10 have been almost identical across each parameter investigated. Rather than assuming this behaviour is consistent for all ideal explosives, it was therefore important to compare these results to historical data, providing confidence in the presented data within this thesis alongside the predictive tool developed by Rigby and Gitterman^[129].



Figure 4.8: Scaled secondary shock delay with respect to scaled distance for all three ideal explosives using representative TNTe values

Through manipulation of the data, presented in Figure 2.8, by dividing the secondary shock parameter, τ_{ss} (derived by Equation 4.1), by scaled distance squared, the parameter becomes dimensionless and therefore required no physical justification. The result of this data manipulation is displayed in Figure 4.9 with a log-polynomial fit represented by Equation 4.2.

3017

$$\tau_{ss} = \delta t_{ss} V_{od} / Z^2 (\rho W)^{1/3} \tag{4.1}$$


Figure 4.9: Dimensionless secondary shock delay parameter evaluated for all ideal explosives scaled accordingly compared with polynomial fit to historical data

Plotted alongside the historic data are the three ideal explosives investigated in this thesis, 3018 showing high levels of consistency when compared to all the experimental data and the 3019 newly presented fit. It is important to note that whilst the scaling of these secondary 3020 shock parameters is based on some physical mechanism, the fundamental processes under-3021 pinning the secondary shock behaviour is not yet fully understood. The fact there is such a 3022 close relationship between all the explosives considered, despite differences in velocities of 3023 detonation, packing densities and TNT equivalences, suggests that there is a real physical 3024 process relating the secondary shock to these parameters. 3025 3026

$$log(\tau_{ss}) = 0.3682 - 0.0351 log_{10}(Z)^2 - 1.498 log_{10}(Z)$$
(4.2)

3027 4.2.4 Pressure Gauge Summary

This section clearly validates the analytical and experimental techniques discussed in Chapter 3 for pressure gauge type recordings across the far-field range for three plastic explosives with ideal behaviours. Alongside this, there is definitive evidence that with well-controlled experimental trials, data only exhibit high levels of consistency but both positive and negative phase blast parameters are captured remarkably well by KB predictions. With this finding, it is hoped that the industry will recognise that for far-field regimes, the yield of explosives is not inherently variable and steps can be made to improve the fundamental understanding of blast wave mechanics.

3036

Detailed analysis into the secondary shock phenomena was undertaken in the attempt 3037 to understand the physical mechanisms behind the subsequent wave propagation and at-3038 tempt to both quantify and characterise its behaviour. The work developed in this chapter 3039 provides a reasonable and logical assessment of explosive blast wave features and presents 3040 a validated prediction tool which could potentially be integrated into numerical simula-3041 tions to better capture its behaviour. Whilst the fundamental mechanisms are yet to be 3042 captured accurately for the secondary shock features, these developments can hopefully 3043 drive improvements to the knowledge. 3044

3045

Future experimental data is required from explosives which exhibit widely different TNT equivalency values to distinguish whether the trends seen through Figures 4.7a-d are consistent across explosive composition, mass and distance. If the resulting data was consistent, considerations into a more appropriate way of scaling the results extracted from secondary shock data would be required to either agree with KB predictions of a primary wave or to develop a set of new empirical curve to supplement the established well validated predictive tool.

3053

³⁰⁵⁴ 4.3 High Speed Video Data

This section will begin to consider the data captured using high speed cameras during far-field testing, tracking specifically the propagating shock wave in real time away from the explosive centre. With this technique of analysis being relatively new for the blast industry, it has not been fully explored. The tools developed in Sections 3.3.1.1 and 3.3.1.3 have been tested against the three ideal explosives discussed in this chapter. Comparisons have been made directly to corresponding pressure gauge data to both further validate the methods developed and to provide greater insights into the shock wave phenomena.

3062

3063 4.3.1 Time of Arrival Variability

With arrival time being the main feature captured during HSV recordings, it was im-3064 portant to assess how the parameter varied both spatially and temporally during the 3065 spherical expansion of the shock wave. Implementing the shock wave edge detection and 3066 arrival time interpolation tools for far-field high speed video recordings, as described in 3067 Sections 3.3.1.1 and 3.3.1.3 respectfully, arrival time, t_a , values were established at every 3068 $0.1 \text{ m/kg}^{1/3}$ scaled distance along each virtual 'spokes' which start at the charge centre 3069 and plot radially outwards, in increments of 1°. The data captured through this analysis 3070 allows for a direct comparison to pressure gauge recordings which records pressure-time 3071 histories at discrete locations. The 3,163 data points as a result of implementing these 3072 methods on 10 HSV recordings of PE4 far-field detonations, 4,313 data points for PE8 3073 from 6 recordings, and 3,639 PE10 data points from 4 recordings, were collated with re-3074 spect to each increment of scaled distance. The RSTD was calculated similarly to that 3075 done for the gauge recordings seen in Figure 4.11. 3076

The standardised range of interpolated HSV arrival time results are compared directly to pressure gauge variation of PE4 trials, with respect to scaled distance, presented in Figure 4.10. As lens distortion was not accounted for during these trials, the videos were not used as a group of collated data, and only those with the same test set up and explosive composition were compared. Regardless of this, the relative variability of arrival time recordings at specific scaled distances held fairly consistent between groupings of tests when compared to the relationship pressure gauge data had with scaled distance.

3085



Figure 4.10: RSTD in shock wave arrival time with respect to scaled distance, when comparing pressure gauge and HSV data

A significant reduction in the variability of processed arrival times across the entire range 3086 of tested distances is experienced when using high speed video for PE4 detonations. In 3087 part, this reduction in variability is associated with the volume of data points created 3088 through the interpolation at each scaled distance. However, some of the scaled distances 3089 in question had a similar benchmark number of data points as the pressure gauge results. 3090 That being said, for the entire range tests, the two extremes had a low number of record-3091 ings established and yet there is still a noticeable reduction in processed t_a variability 3092 as scaled distance increases. This alone provides clear justification for the use of video 3093 recordings during explosive trials to enhance the precision and repeatability of blast pa-3094 rameters between tests. 3095



Figure 4.11: Logarithmic RSTD in shock wave arrival time as a function of scaled distance for both pressure gauge and high speed video recordings of 250g hemispheres of PE4

One thing to note is the substantial volume of interpolated data from just 10 processed PE4 videos when compared to 157 different pressure gauge recordings. The larger data set (3,163 recordings), alongside the clear improvement in repeatability and accuracy from just 10 explosive trials, presents a more cost-effective solution to experimental testing of high explosives.

3102

The interpolated values from HSV recordings of PE8 and PE10 detonations also experience the same behaviour of reduced variability as scaled distance increases. The reason gauge data boundaries have not been presented in Figure 4.11 is due a lack of data to extract a reasonable estimate of arrival time variation with distance. Comparisons to that for PE4 are made instead to facilitate the discussion. The videos for PE10 were by far the hardest to analyse, with the lighting conditions when conducting these trials making extracting shock wave data difficult. That being said the 4 videos which data could be used provided similar levels of variation from 157 PE4 pressure gauge trials, highlighting the efficiency of this testing method. With an increase in the number of videos available, a reduction in the variability is experienced when looking at the results from the 6 PE8, and then finally the 10 PE4 videos.

3114

The significance of Figure 4.11 is the comparable relationship between t_a variation with 3115 respect to scaled distance for both HSV and pressure gauge recordings. This is shown 3116 on a logarithmic scale to enable a clear comparison between the processed results from 3117 both methods of recording. A clear exponential reduction in t_a variability is seen with 3118 an increase in scaled distance across both methods of experimental analysis. The typical 3119 variations in the HSV data are approximately an order of magnitude lower than those in 3120 the pressure gauge data. The speculation that blast parameters exhibit high levels of in-3121 consistency across the far-field range is disproved with these findings, explicitly suggesting 3122 far-field regimes and the corresponding blast parameters are deterministic. 3123 3124

3125 4.3.2 Derivation of Explosive Yield from Arrival Time Data

To consider arrival time data as a metric for forensic explosive analysis, it is important to validate it against empirical data alongside quantifying the variability in the parameter. Rigby et al.^[131], Stennett et al.^[158] and Dewey^[39] all present methods of quantifying the explosive yield of a real-world accidental explosion through arrival time data analysis with respect to best estimations of stand-off from the explosive centre. Their findings presented clear agreement of explosive yield and thus the TNT equivalence factor of the explosive detonated.

3133

To verify the shock wave tracking and interpolation algorithm as an accurate means of gaining an understanding of how arrival time varies spatially across a full range of scale distances, the method was tested to estimate the apparent yield of the explosive used during the tests, which is known to be 250g PE4.

3138

Figure 4.12 shows how the HSV-measured values of arrival time compare to a variety of different sized TNT charges and their corresponding KB predictions. It is important to note that the axes have been scaled down to visualise a clear distinction between the predictive TNT curves due to modest changes in charge mass. The HSV data shows excellent agreement with the curves for TNT between 290-320g, equating to a TNT equivalence of 1.16-1.28. The minimum mean absolute error is associated with a TNT mass of 305g, i.e. an equivalence of 1.22, which is very close to the value of 1.20 found in related studies^[132]. This suggests that the optical technique presented is a reliable method for determining the TNT equivalence of explosives.



Figure 4.12: Interpolated and unscaled HSV shock wave arrival time from a 250 g PE4 hemispherical charge at 5 m stand-off compared with KB predictions for TNT hemispherical charges with different charge mass

Whilst the spread in TNT equivalence extracted from the HSV data is not significant, this could be vastly improved when considering what position on the shock wave you take to be the definitive front. The algorithm discussed in Section 3.3.1.1 makes use of image subtraction which results in clusters of pixels exhibiting change. Despite best efforts of the edge detection method, variations are therefore recorded in the shock wave position. The Abel transformation relates a spherically-symmetric 3D field to a two-dimensional projection^[34,91] which has been adapted for use in blast wave tracking through inversion of the process for tiny charges in well-controlled lab conditions^[172]. The inversion however requires refraction angles obtained through effective lens calibration which was not conducted during this testing regime. Future tests should consider the use of the Abel transformation inversion to improve the accuracy of shock wave position extrapolated from a 2D video of a 3D spherical expansion.

3162

3163 4.3.3 Capturing Secondary Shock Data

The secondary shock parameter has been shown to be as deterministic as the primary shock in Section 3.2.3.2, provided the right assumptions are made when attempting to characterise it. However, what has yet to be established is whether secondary shock data can be captured using HSV techniques which could help provide a more fundamental understanding of the phenomena.

3169

Adopting the same methods discussed in Sections 3.3.1.1 and 3.3.1.3 proved successful for capturing the propagating subsequent shock provided that lighting conditions were favourable and the explosive was not located too far out of the camera field of view. As the secondary shock is much weaker, the shock discontinuity is a lot more challenging to extract and therefore a lot of the videos provided unextractable data.

3175

Despite the difficulty in extracting secondary shock data across each explosive, Figure 4.13 3176 presents the overall secondary shock delay parameter, as discussed in Section 3.2.3.2, 3177 against the unscaled compiled pressure gauge data presented in Figure 4.8. The first 3178 thing to notice is the comparison in behaviours of the HSV extracted data to the pressure 3179 gauge data. This relationship provides enough evidence to support the validity of the 3180 ext extraction methodology for secondary shock data. The HSV data however seems to 3181 exhibit a smaller delay parameter across the explosives analysed. This is believed to be 3182 directly related to the HSV data tracking incident wave data throughout its duration for 3183 both primary and secondary shocks, where as the pressure gauges record at a discrete 3184 instance of distance. This means the secondary shock would be forced to expand against 3185 a reflected wave, decelerating its propagation and thus increasing its time of arrival when 3186 compared to the HSV data. 3187

3188



Figure 4.13: Interpolated and unscaled HSV secondary shock delay time from 250 g hemispherical ideal charges compared with pressure gauge recordings of PE4, PE8 and PE10

A learning point from early testing analysis of PE4 and PE10 was highlighted when the extracted secondary shock propagation data was either unusable or varied considerably, as seen in Figure 4.13. This knowledge was considered for the PE8 trials which were only conducted within favourable conditions resulting in all 8 shots providing credible data as opposed to only 5 of 20 trials in total for PE4 and PE10 combined.

3195 4.3.4 High Speed Video Summary

This section makes efforts at implementing the tools developed in Chapter 3 to explore the other data which can be extracted on the three ideal explosives tested. Highlighted is the requirement for recording conditions to be considered prior to a test if only recording data using cameras. If lighting conditions are unfavourable most of the videos become difficult to extract data from without artificially editing image brightness which induces a margin of doubt in what data is being considered.

Importantly, the HSV methods have shown to produce highly accurate results for explosive yield and secondary shock delay when compared with known experimental features and the corresponding pressure gauge recordings respectively. With the secondary shock is not fully understood, work of this kind which shows clear differences between incident and reflected delay data provides further insights which can be developed to fully characterise the physical process.

3208

3209 4.4 Future Research of Explosive Characterisation

3210 4.4.1 Near-Field Loading

Whilst already conducted is an in-depth and rigorous analysis of ideal explosives within far-field regimes, there is limited published work considering near-field loading conditions. Even fewer of these contain experimental-based evidence for the definitive mechanisms resulting in variability of near field blast parameters. The fireball of detonation products in this region is still expanding and driving the shock wave and so interacts with a structure in unison. KB predictions in this region are poorly defined, with limited experimental data of which exhibits significant scatter and divergence to physics-based numerical models^[150].

To establish the root cause of the discrepancies between numerical simulation and the KB predictions, it is essential to record experimental data of both spatial and temporal blast parameter distribution in near-field regions. In doing so, insights into how energy is released during the initial stages of detonation can be made helping to characterise the near field effects on a composition basis.

3224

With developments in near-field loading measurements discussed in Barr et al.^[10], a rigorous test plan should be undertaken in the future to characterise the temporal and spatial behaviour of detonation within close-proximity of a reflective surface to measure localised loading conditions. The experimental trials will require high levels of precision with blast parameters showing considerable sensitivity inaccuracies in detonator placement within close proximity of the charge. This data will be used to expand the bank of data used to establish the KB predictions and hopefully provided insights into the discrepancies between that and numerical models. Future work should also build on that presented by Rigby et al.^[130], which looks at implementing similar HSV techniques but for near-field fireball expansion tracking.

3235

3236 4.4.2 TNT Equivalence

Despite the vast quantities of published literature on TNT equivalence across a range 3237 of explosive compositions, there still holds discrepancies between researchers as to what 3238 realistic values are. This can only be a result of a general lack of consistency in exper-3239 imental processes and analytics. What has never been fully justified in literature is the 3240 idea that TNT equivalence varies with scaled distance. Within near-field regimes where 3241 the propagating shock wave is sensitive to fireball thermodynamics, the statement that 3242 TNT equivalence varying may be valid. Compositions will decompose and combust at 3243 different rates which should result in variations to energy release when compared to that 3244 of TNT. However, in far-field regimes, the explosive detonation can be considered as a 3245 point source energy release^[167] and therefore once the shock wave detaches from the fire-3246 ball, the localised differences in detonation thermodynamics can be ignored. Effectively 3247 at these greater scaled distances, shock waves are comparable based on the speed in which 3248 they propagate through free-air and thus is believed to exhibit a constant TNT equivalence. 3249 3250

The techniques developed in Chapter 3 when used on a variety of ideal explosives demon-3251 strates highly consistent blast parameter data in the far-field range which compare well 3252 to KB predictions for TNT. This provides justification and validation of developing tech-3253 nical procedures for data capture and analysis which considers the fundamental physical 3254 principles of shock wave propagation, relating to Objectives 2 and 3. With this in mind, 3255 the benefit of understanding how to improve our recorded data can be adopted to re-3256 characterising other ideal explosives, attempting to quantify their effects and compare 3257 with KB predictions to establish realistic and consistent TNT equivalence values across 3258 the far-field range.^[164] undertook well-controlled blast trials using PE4 across a range of 3259 mass scales, and showed general consistency of shock wave parameters regardless the mass 3260 tested. Although these masses tested are beyond what is possible for the University of 3261 Sheffield testing site, the fact that ideal explosives behave consistently both in mass and 3262

distance in the far-field range provides justification for this work. In doing so, more optimised numerical simulations can be developed to better quantify the effects these explosive compositions could have in more complex environments.

3267 4.5 Summary

With experimental blast parameters providing the primary source of evidence to supplement the fundamental understanding of shock loading conditions on a structure, it is of paramount importance to characterise and quantify these effects resulting from a variety of compositions across a range of distances.

3272

3266

Stress-testing the tools developed in Chapter 3 using a large data set of small-scale hemispherical PE4 detonations against other explosives of similar idealistic behaviour was the main aim of this Chapter. Presented is a rigorous investigation into the effects various ideal explosives have on structures across the far-field range. The data was collected using both pressure gauges and high speed video recordings to further validate the methods and results through comparison of nominally identical shots.

3279

The findings within Chapter 4 highlight the strength of KB predictions for both positive 3280 and negative phases of free-air shock wave parameters, specifically for far field scenarios, 3281 alongside the high consistency in output data from consistent well-controlled experimen-3282 tal trials. Despite only testing 250g hemispheres, the findings from $^{[164]}$ provide enough 3283 evidence that the results of consistency will transfer across mass and distance with the 3284 far-field range when considering ideal explosives of spherical shape. The methods of data 3285 capture and analysis have the potentially to be tested further when considering other non-3286 ideal explosives, charge shape effects and near-field loading conditions. 3287

3289 Chapter 5

Non-Ideal Explosive Blast Characterisation

3292 5.1 Introduction

Chapters 3 and 4 present validated experimental methodologies and analytical tools for 3293 accessing the far-field blast parameters from small scale ideal explosives in free-air, which 3294 have shown to improve the repeatability of recorded data and provide confidence in deter-3295 ministic predictions of far-field detonation yields. Although having a fundamental under-3296 standing of ideal explosives is required, in reality, common explosive threats are home-made 3297 due to the relative ease and low costs associated with acquiring their constituents. This 3298 has led to a critical need to understand the effects of detonating non-ideal explosives to 3299 improve civilian safety against potential terror attacks in more realistic situations. 3300 3301

This Chapter will exercise the validated methods of conducting experimental work, and 3302 the corresponding data analysis, discussed in Chapter 3, to explore the yields of small 3303 scale ANFO (Ammonium Nitrate 94% and Fuel Oil 6% mixtures). The overall aim is to 3304 characterise the composition across a range of scaled distances at a smaller mass range 3305 to quantify any differences in the behaviour between that and large scale charges. The 3306 processed data will be compared to numerical simulations to access the validity of the 3307 underlying physics assumed within standard JWL equations of state. An assumption that 3308 non-ideal explosives vary on mass as well as scaled distance has been made, meaning a 3309 single value for TNTe can not be assumed. If proven correct within the findings of this 3310

chapter, it would result in discrepancies between simulated non-ideal detonations and the
results from experimental trials, motioning a requirement for characterisation revisions
of non-ideal explosives to capture realistic physical mechanisms ongoing in small scaled
charges.

3315

3316 5.2 Experimental Setup

In the attempt to quantify the effects of small scale ANFO detonations a variety of experimental techniques were conducted to investigate the non-ideal behaviour which may be exhibited. This section outlines the basis of these trials making using previously validated methodologies in Chapter 3 for far-field studies but introducing a new technique of analysis for rate-stick trials.

3322 5.2.1 Far-Field Trials

A total of 37 far-field experiments were performed at the University of Sheffield (UoS) Blast and Impact Laboratory in Buxton, UK. These trials were conducted using surface detonated hemispherical charges with mass varying between 250-1000g comprising of two different chemical compositions (Ammonium Nitrate Fuel Oil (ANFO): 35 tests and Ammonium Nitrate (AN): 2 tests). Both explosives were commercially purchased from EPC-UK to provide comparable studies both of which presented material properties as seen in Table 5.1 quoted by the supplier.



Parameter	Ammonium Nitrate + Fuel Oil (ANFO)	Ammonium Nitrate (AN)
Composition	92.5 - 95% AN, 5.0 - 7.5% FO	99% AN, ${\sim}1\%$ Moisture
Density	$0.8 g/cm^3$	0.73 - $0.89 \ g/cm^3$

Table 5.1: EPC-UK material properties of ANFO and AN which have proven useful for this body of research and article

The charges were boosted with a 3g sphere of PE10 to ensure reliable shot-to-shot detonation^[112], and were done so at standoff distances of 1–9m from gauge instrumentation. It is important to note that a secondary objective from these trials considered the position of the booster/detonator and their effects on non-ideal explosive yield. With this in mind, 16 of the trials were top detonated and 21 bottom detonated. Figure 5.1 is a schematic displaying the different booster and detonator positions adopted for this testing regime. For each of the far-field trials, clear plastic sheets were heated and vacuum-formed around a 3D printed hemispherical mould, to provide a lightweight casing to facilitate negligible confinement of the ANFO prill whilst keeping a consistent shape. This was implemented to compare the results with the large bank of ideal explosive data available within the literature^[49]. A small circular cut was made in the top of the vacuum formed plastic casing to enable a consistent method of filling the charge with pril.



Figure 5.1: Schematic of the charge and booster locations used throughout this testing regime

The far-field experimental methodology for the non-ideal tests mirrors that discussed in 3344 Chapter 3. The explosive charges were detonated at varying stand-off distances, R_a and 3345 R_b in Figure 3.3, perpendicular to two rigid reflective surfaces in the form of a reinforced 3346 concrete bunker and a blockwork wall, separated exactly 10.0 m apart. Data was recorded 3347 using the same collection of Kulite HKM-375 piezo-resistive pressure gauges as were used 3348 for the recording of the ideal explosive detonations. The gauges were threaded through, 3349 and made flush to the surface of a small steel plate (approximately $110 \times 150 \times 10$ mm) which 3350 was fixed to these walls. The charges were placed on a small steel plate $(150 \times 150 \times 25 \text{ mm})$ 3351 prior to detonation, in order to avoid repeated damage to the concrete testing pad. 3352 3353

For bottom detonated trials, the steel anvil had a machined hole through the centre to allow for the detonator to be in contact with the PE10 booster. The pressure was recorded using a 16-bit digital oscilloscope and TiePie software, with a average sampling rate of 195 kHz at 16-bit resolution. The recording was triggered automatically using TiePie's 'out window' signal trigger on a bespoke break-wire signal, formed by a wire wrapped around the detonator. The 'out window' trigger initiated with a voltage drop outside the normal electrical noise experienced in the break-wire. This coincides with the detonation of the charge breaking the circuit.

3362

Data was recorded using the same collection of piezo-resistive pressure gauges as were used for the recording of the ideal explosive detonations. It is important to note that 30 of the ANFO trials were undertaken as part of a separate research project funded by CPNI (Centre for the Protection of National Infrastructure) and DSTL (Defence Science and Technology Laboratory) that has been granted permission of use in this thesis and hence denoted throughout.

3369



Figure 5.2: Top detonated arrangement for hemispherical ANFO charges boosted with 3g PE10 sphere; the yellow tubes are installed as guides for the detonator to be positioned vertically into the booster

The Photron FASTCAM SA-Z high speed video camera, fitted with a Tamron SP AF70 70-200mm zoom (F2.8) lens, and a zebra board which ran perpendicular to the blockwork and bunker walls, was again utilised to capture far-field shock propagation. In conjunction to this, a Shimadzu ultra high speed video camera was used to record detonation wave propagation and fireball breakout of the explosive to provide insights in the early stages of the event.

3376

3377 5.2.2 Rate Stick Trials

As an attempt to characterise ANFO small scale shots across a whole range of parameter 3378 metrics, there was a need to establish the velocity of detonation (VOD) of ANFO and 3379 how it develops within a charge. To evaluate this, 6 rate stick trials were undertaken 3380 making use of two Shimadzu ultra high speed cameras. ANFO prill was contained within 3381 300mm long, 3mm walled clear acrylic/PMMA (Polymethyl-Methacrylate) pipes which 3382 had varying diameters in the attempt to establish the critical diameter of ANFO and the 3383 explosives corresponding VOD. The three internal diameters of pipe tested were 50mm, 3384 75mm and 102mm which correspond to ranges quoted within published literature for the 3385 critical diameter of $ANFO^{[20,23,24,47,97]}$. 3386

3387



Figure 5.3: General arrangement of the rate stick trials using a 3mm wall thickness PVC clear tube, a 3D printed end cap which allows for detonator and booster placement and a reference measurement guide to enable distance tracking in the high speed videos

The pipes were sealed using a 3D printed detonator holder at one end and a lightweight fibreglass material at the other to provide minimal confinement at the pipes extents as seen in Figure 5.3. To trigger the camera, a breakwire system was wrapped around the detonator so that upon detonation a voltage drop is experienced, triggering the camera to record. The general arrangement of the detonator assembly can be seen in Figure 5.4. Five out of the six trials utilised a 3g PE10 booster to initiate the detonation process to be comparable with the data collected within the far-field studies. The final test looked at a non-boosted 50mm diameter rate stick trial.



Figure 5.4: General arrangement of the rate stick trials using a 3mm wall thickness PVC clear tube, a 3D printed end cap which allows for detonator and booster placement and a reference measurement guide to enable distance tracking in the high speed videos

³³⁹⁷ 5.3 Pressure Gauge Results

3398 5.3.1 Positive Phase

Having little knowledge on the yield and characteristics of small scale ANFO charges, it was essential to establish an understanding on the general qualitative behaviour recorded during testing. The aim of this is to assess if non-ideal explosives behave as consistently as ideal explosives, as seen in Figure 3.5.

3403

Presented in Figure 5.5 are 18 individual pressure gauge recordings as a result from 250g hemispherical ANFO detonations. These were conducted across a variety of standoff ranges tested alongside varying detonator position between top and bottom detonated. For data recorded between 2–9m, it is evident that although a discrepancy in the arrival times is consistently recorded (discussed further in Section 5.3.2), the overall trends in the

positive phase of the pressure-time histories show considerable agreement. This ultimately suggests that within far-field regions, the detonator position is irrelevant. A similar level of consistency is also to be experienced between non-ideal and ideal explosives. The traces at 1m standoff do present variability in the overall peak overpressure recorded. This has been directly linked to the spherical uniformity and irregularity of the detonation cloud breakout related to bottom and top detonated tests respectively.

3415



Figure 5.5: Compilation of raw data set of 250g ANFO hemispherical ground bursts, comprising of both top and bottom detonated charges, across the entire range of standoff distances tested in this regime. Positive phase is presented only.

To establish the behaviour small scale ANFO explosives exhibit when compared to TNT, it 3416 was important to adopt the same experimental analysis tools, validated for ideal explosives. 3417 This is undertaken to assess how the tools perform for non-ideal explosive detonations. 3418 Since Friedlander-like behaviours are presented in Figure 5.5, the curve fitted method was 3419 used to process the small scale ANFO data. The caveat is that this accounted for the gauge 3420 plate ringing (the phenomena discussed in Section 3.2.2) as the blast arena amendments 3421 had not been made prior to these trials being conducted. The output blast parameters 3422 resulting from the curve fitting method were collated. A TNT equivalency assessment 3423 made using an MAE analysis, comparing the ANFO data set to semi-empirical predic-3424 tions based on varying masses of TNT. As per the findings of Section 3.2.1.1, the positive 3425 phase duration exhibited higher levels of variability when assigning a specific value to the 3426 parameter. This was directly linked to noise in the signal, making the true point at which 3427 conditions return briefly back to atmospheric difficult to precisely determine. In common 3428 practice, an inaccurate time duration can be remedied by tailoring the decay coefficient 3429 in the Friedlander equation such that the specific impulse is preserved. With this noted, 3430 positive phase duration was omitted from the MAE analysis in line with the previous 3431 assessment on ideal explosives. 3432



Figure 5.6: Compiled scaled blast parameters from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.395, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration

To be in line with variability regions hypothesised Tyas^[173], the MAE analysis was per-3434 formed on all AN-based tests within the definitive far-field range. The aim was to attribute 3435 a TNTe factor at which the shock wave is no longer affected by ongoing fireball chemistry, 3436 instabilities and detonation cloud propagation. To establish the effects of detonator po-3437 sition and charge mass, the MAE analysis was undertaken for the data when separated 3438 into both nominally identical tests alongside the full data set. The results from the MAE 3439 analysis of peak reflected pressure and specific impulse converged on a TNTe = 0.3953440 across the entire range of scaled distances, for both charge mass and detonator position 3441 groupings. Arrival time however, presented a TNTe = 0.28 and 0.295, for bottom and top 3442 detonated trials respectively. This suggests that the shock waves resulting from small scale 3443 ANFO detonations propagate slower than an equivalent TNT mass with approximately 3444

40% of the mass of the detonated ANFO charge. This offset in arrival time, is visually represented in Figure 5.5, and will be discussed in detail in Section 5.3.2. The arrival time of the shock waves will however be treated with caution for discussions relating directly to explosive yield.

3449

3471

To assess the explosive yield alone, the TNTe = 0.395 was applied to each of the recorded 3450 blast parameters and presented in Figures 5.6a-d which show a striking agreement between 3451 each experimentally recorded blast parameter (expressed as a TNT equivalent mass), and 3452 the KB predictions. It is important to note that there were 2 preliminary trials which 3453 resulted in much lower explosives yields related to not using a PE10 booster, which have 3454 been removed from the presented data to avoid speculative comparison of different testing 3455 regimes. This finding does however provide enough evidence to suggest that small scale 3456 ANFO charges cannot be reliably detonated without the presence of a booster charge. 3457 3458

Interestingly to note is the behaviour of the peak pressure and specific impulse values in 3459 near field scenarios, $Z < 3m/kq^{1/3}$, when comparing top and bottom detonate shots in 3460 Figures 5.6a and 5.6b. The top detonated peak pressure values recorded in the exper-3461 imental trials seem When comparing peak pressure and specific impulse values, the top 3462 detonated trials exhibit different evaluated TNTe factors when compared directly to KB 3463 predictions. The bottom detonated trials present agreement in TNTe for both parame-3464 ters with KB predictions. This suggests that ANFO small scale charges are sensitive to 3465 detonator position in the near-field due to differences in the detonation product mechan-3466 ics occurring on breakout in line with the findings presented in Figure 5.5. It can be 3467 concluded that the energy release of an explosive, and therefore the specific impulse, is 3468 independent of detonator position. The peak pressure however is directly related to the 3469 fireball breakout and propagating shock wave shape. 3470

What can be deduced from this finding however is that specific impulse provides a more representative TNTe across all explosives and scaled distances regardless of whether a 'Friedlander' shock wave has fully formed. Specific impulse loading is directly related to the total energy released from detonation rather than pressure which is time-dependant based on shock wave forming. For the near-field it is important which parameter is considered but far-field can make use of both to establish equivalency in line with findings presented by Bogosian et al.^[16]. 3479

The results presented in Figures 5.6a-d contradict quoted values of TNTe for ANFO be-3480 ing around 0.82 across all scaled distances and masses, therefore posing implications for 3481 numerical modelling which have incorporated these assumptions within simulations. To 3482 assess the variability of the data set, it was scaled by mass alone and compared to vary-3483 ing KB prediction curves using a TNTe = 0.3-0.5, presented in Figure 5.7. A TNTe = 3484 0.395 ± 0.1 does agree with the results presented in Figure 2.14 by Figuli et al.^[52], sug-3485 gesting that a $\pm 10\%$ spread about the MAE evaluated TNTe could be related to inherent 3486 variability in ANFO trials as result of a combination of the factors mentioned in Section ??. 3487 3488



Figure 5.7: Compiled mass scaled blast parameters from ANFO explosive trials as a function mass scaled distance, compared with KB predictions, using a $TNTe=0.395\pm0.1$ to present variability bounds, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse

Across a variety of experimental trials, it would become evident if the gauge data was invalid, especially where gauges were swapped out depending on their pressure rating and where the charge was situated, providing confidence in the recorded and processed blast parameters. The confidence in the data provides us with enough evidence to suggest that non-ideal explosives are not scalable across all masses and standoff distances and therefore KB predictions may not hold as much credibility when assessing these types of explosives.

For ANFO in particular, larger charges masses (i.e a greater self-confinement and longer distance for detonation wave to travel without energy loses) foster the full detonation and

combustion of both AN and FO components of the composition, but in smaller charges 3498 a percentage of the energy is not fully released prior to the propagation of the air shock. 3499 The question which begins to be highlighted is why ANFO is described to exhibit a TNTe 3500 of around 0.82 across all scale distances and little further experimental work undertaken 3501 to assess the robustness of this factor across a range of masses and scaled distances other 3502 than that presented in Figure 2.14. The implication this has on the fundamental under-3503 standing of non-ideal explosives is significant and will result in any numerically modelled 3504 simulation of ANFO of low charge mass will result in over predictions in the behaviour. 3505 The contents of this chapter will make efforts at assessing the robustness of KB predictions 3506 against small mass-scale ANFO charges whilst making comparisons to the historical data 3507 captured from large scale charges. 3508

3510 5.3.2 Arrival Time Offset

Using the findings from the MAE analysis on peak reflected pressure and specific impulse, KB predictions of the positive phase, using a TNTe = 0.395, were overlaid on the raw data to evaluate whether the equivalency factor provided qualitatively similar trends in Figure 5.8. Whilst both the pressure and impulse trends are captured reasonably well, the arrival of the recorded shock waves is much later than an equivalent TNT blast.

With further inspection, the MAE analysis for arrival time highlighted TNTe being 0.28 3517 and 0.295 as providing more comparable scaled arrival time values to TNT predictions for 3518 both bottom and top detonated trials respectively which equates to on average ~ 0.3 ms 3519 delay in the arrival time in comparison to the TNTe establish for pressure and impulse. 3520 This suggests that despite exhibiting TNT equivalences of around 0.395 for energy related 3521 parameters, time-based shock wave parameters from small scale ANFO charges are equiv-3522 alent to even weaker detonations and therefore arrival later. It is has been hypothesised 3523 that the delay in arrival time to be a result of a combination of different factors, of which 3524 will be discussed further. 3525

3526



Figure 5.8: Compiled raw data from both top and bottom detonated trials at 2m, 4m, 6m and 8m standoff distance compared to KB predictions assuming a TNTe=0.395: Pressure-time history (Top) and Impulse-time history (Bottom), showing only positive phase

3527 5.3.2.1 Mesostructure of ANFO prill

The heterogeneity of small scale ANFO charges, when compared to homogenous cast TNT 3528 explosives used to develop the KB prediction tools, is a factor which could affect the ve-3529 locity of the detonation wave and therefore resulting blast parameters. Zygmunt and 3530 Buczkowski^[183] investigated the influence of ANFO prill characteristics on detonation ve-3531 locities and energy release and found that the prill structure and the size in these types 3532 of charges are massive influencers. Salyer et al.^[140] compared the detonation velocities 3533 of two commercial ANFO types which have vastly different prill sizes and mesostructures 3534 when prepared. The results suggested that the small prill resulted in much more ideal 3535 detonation behaviours relating directly to reduction in air voids allowing for a more stable 3536

3537 expansion of the detonation wave.

3538

Petes et al.^[112] discusses this inhomogeneity characteristic as being the potential reasoning for non-spherical propagation anomalies in the shock wave and fireball. This results in quoted blast parameter variability spreads of $\sim 7\%$ when comparing nominal trials detonating cast TNT, which is endorsed by^[9] who discusses instability formation relating to imperfections in the charge surface and homogeneity.

3544

Considering large scale ANFO charges, it is highly likely the bulk density increases due 3545 to more centrally located prill layers exhibiting void collapse through self-weight compres-3546 sion. Petes et al.^[112] detailed that an increased bulk density will result in faster detonation 3547 velocities and thus the resulting blast parameters exhibiting larger yields for large scale 3548 charges. McKay et al.^[99] and Dobrilovic et al.^[41] both experimented with reducing the 3549 density of ANFO by removing prill and exchanging it with polystyrene balls to assess the 3550 changes to the velocity of detonation in rate stick trials. Zygmunt and Buczkowski^[183] 3551 showed that increasing the density of ANFO charges using ground prill much higher deto-3552 nation velocities were experienced, which with alongside the aforementioned articles show 3553 agreement with the theory stated by Petes et al. [112]. 3554

3555

Conversely, the works presented by Fabin and Jarosz^[47] undertook analytical studies in 3556 trying to improve the explosive yield of ANFO charges and discovered the morphology 3557 and prill size distribution did not necessarily follow the same theory. A dependence on 3558 FO absorption features of AN has shown to result in lower detonation velocities for higher 3559 density ANFO, therefore inducing variability in detonation mechanics. Sadwin and Swis-3560 dak^[139] reinforced these ideas when it was reported that layer-to-layer density differences 3561 were measured throughout their large scale ANFO charge through varying detonation 3562 velocities and pressures. Consequentially to these density regions, hydrodynamic insta-3563 bilities would develop leading to a considerable amount of internal turbulence and thus 3564 a degree of detonation wave propagation impedance when compared to cast TNT, all of 3565 which would result in spreads in explosive yield. 3566

3567

For these small scale charges, where the mass itself is not enough to provide reasonable compaction to induce full/ideal detonation of the ANFO, the air voids between each prill are believe to have a impedance influence on velocity of detonation. It is assumed that cellular disturbances of the detonation wave are generated when propagating through the
prill structure, fostering multiple interactions within the complex mesostructure and disrupting the smooth isentropic expansion of the detonation wave and products.

- ³⁵⁷⁵ Mi et al.^[102] numerically modelled the shock-to-detonation transition in nitromethane, a ³⁵⁷⁶ non-ideal heterogeneous explosive, when incorporating different arrangements of air voids ³⁵⁷⁷ and applying varying energy shocks to the medium to induce initiation. This model pre-³⁵⁷⁸ sented delays during the initiation process when cavities were present in comparison to ³⁵⁷⁹ a homogeneous mixture. This provides further understanding to the complexity of the ³⁵⁸⁰ detonation process and some validation to the delays seen in Figure 5.8a-b.
- 3581

3574

Numerical simulations undertaken by Baer et al.^[6] demonstrated that heterogeneous ma-3582 terials, like ANFO, which undergo shock loading, do not exhibit one jump state as de-3583 picted in ideal explosives but consist of a distribution of states. In the early stages of 3584 being shocked, ANFO behaves elastically, with temperature and stress corresponding to 3585 those defined by the shock hugoniot of ammonium nitrate. As the the shock wave travels 3586 through the complex mesostructure, the distribution of states show elastic and plastic de-3587 formation effects, corresponding to induced ANFO prill pore and air void collapse behind 3588 the shock front. Thereafter, when all available void space is filled, compression waves 3589 traverse through the materials that eventually equilibrate to a spatially-uniform stress 3590 state which was also hypothesised by McKay et al.^[99]. When directly comparing this to 3591 a ideal homogeneous explosive, which jumps states effectively instantaneously, the time 3592 difference between those reactions could also have an effect on the offset seen in the small 3593 scale charges. 3594

3595

The ANFO used in these trials had a bulk density of 0.824g/cm³ measured using a known 3596 volume and mass container, which is significantly lower than an individual prills density, 3597 quoted as between $1.2 - 1.4 qg/cm^{3}$ [138]. Density, or air voids percentage, is documented as 3598 having a direct relationship with the detonation velocity and thus the resulting shock wave 3599 parameters^[154]. Adopting rudimentary calculations, the ratio between the bulk density of 3600 a given amount of ANFO and an individual prill results in around 60% - 70%, suggesting 3601 30 - 40% is attributed to the air voids which is in line with quoted amounts by Cetner 3602 and Maranda^[24]. If the ratio of measured charged density to potential density is applied 3603 to the TNTe factor established for the best fit of reflected pressure and specific impulse, 3604

141

a new $TNTe \simeq 0.246 - 0.328$ is established, which is in line with the MAE analysis for arrival time when compared to KB predictions.

3607

The arrival time delay could be attributed to the complex mesostructural interaction between detonation wave, ANFO prill and the air voids. This phenomena will be much more prominent in small scale charges, with a lack of self-compaction, when compared to homogeneous TNT charges.

3612

3613 5.3.2.2 Detonator Position

Comparisons between top and bottom detonated charges were undertaken to establish the delay in the shock wave arrival time related to detonator position. Using the TNTe value of 0.395, the scaled distances and arrival times for the small scale ANFO trials were calculated, and through the use of interpolation, the corresponding KB prediction of arrival time could be established. The difference between the recorded scaled arrival times and the KB predictions was the offset recorded and presented in Figure 5.9.

3620

Interestingly the findings, when comparing top and bottom detonated arrival time offset, 3621 show a consistently larger offset value attributed to bottom rather than top detonated 3622 charges, whilst also exhibiting a smaller degree of variability. This finding suggests that 3623 top detonated charges result in shock waves which travel faster than a bottom detonated 3624 charge. The velocity of detonation in ANFO has been shown to increase with charge ra-3625 dius^[12,43,80,98] up to a maximum value and thus in top detonated charges, the detonation 3626 wave has more explosive to pass through prior to breakout. The correct orientation of the 3627 detonator when used in the top detonated scenario was subjected to human error due to 3628 being free-standing in the testing methodology. Conversely, the bottom detonated charges 3629 passed through a hole in a steel anvil, only large enough for the detonator to fit, therefore 3630 improving the directionality and thus showing a higher degree of consistency in the offset 3631 parameters at each given scaled distance seen in Figure 5.9. 3632



Figure 5.9: Scaled time of arrival from experimental work offset from KB predictions based on a TNTe=0.395, against scaled distance for top and bottom detonated tests with reference best fit lines

Figure 5.9 does highlight that the offset in arrival time compared to KB increased with scaled distance for both top and bottom detonated charges. It is hypothesised that this is a feature of the ANFO shock wave de-accelerating faster than an equivalent TNT explosive based on the 39.5% equivalency. Despite detonator position making slight differences to the arrival time offset, this is second order mechanism and a more fundamental process causes the discrepancy in arrival time data.

3640

3641 5.3.2.3 Proportionality in the Velocity of Detonation with Charge Radius

The offsets in arrival time tends to increase with scaled distance in both scenarios of detonator position. This suggests for small scale ANFO charges the shock wave velocity is decaying faster than what a TNT charge scaled accordingly would. This finding is indicative of the relationship presented in Figure 5.6c which suggests that the decay of shock wave velocity is on a different gradient to what is experienced in TNT.

3647

3648 The factors mentioned above all contribute to the main overarching reason for the arrival

time offset but these are believed to be second order to the real mechanism resulting in the 3649 magnitudes of offset exhibitted. TNT has a detonation velocity of around 6940m/s when 3650 compared to the published figure of approximately between 4250-4800m/s for ANFO, again 3651 related to large scale trials. However, TNT reaches this quoted maximum speed effectively 3652 instantaneously due to its ideal-like detonation characteristics. ANFO detonations on the 3653 other hand requires a specific amount of time in which the charge is sustaining, and not 3654 losing energy through propagation of products (i.e., similarly to being confined), allowing 3655 for a steady-state detonation to occur exhibiting the quoted velocity. It is therefore a rea-3656 sonable assumption that comparing the internal conditions of small scale ANFO charges 3657 to TNT will result in slower detonation velocities at the instant of initiation, with the gap 3658 closing as charge diameter increases. 3659

3660

3671

Figure 5.10 displays a schematic of what is hypothesised to be occurring in the detonation 3661 procedure of ANFO when compared to TNT. Upon the detonation of TNT, the velocity 3662 of the shock wave travelling through the explosive is fairly constant until breakout. At 3663 this point the propagation of the detonation products and air shock results in progressive 3664 energy loss and reductions in speed. Conversely for ANFO, the maximum velocity is not 3665 achieved instantaneously with detonation, but instead ramps up based on the secondary, 3666 non-ideal combustion of the FO component of the charge which occurs over a longer time 3667 scale. Depending on charge size, the breakout of detonation products could happen any-3668 where along the curve ramping up to the maximum velocity of detonation of ANFO and 3669 then will behave similarly to TNT as a free air shock, just at a lower velocity. 3670

In the experimental trials presented within this thesis, the ANFO charges would fall into 3672 smaller scale behaviours meaning that the when comparing the trend to TNT, it is clear 3673 that the velocity of the shock reduces faster in the ANFO detonation. This would there-3674 fore create an artificial offset to arrival time data as the TNT shock wave travels faster 3675 for longer. Eventually the offset would level off when the changes in velocity with respect 3676 to time are almost the same (i.e. when then curves begin to plateau and converge). The 3677 larger the ANFO charge, the closer to the maximum detonation velocity and therefore 3678 less of an offset would be induced. The initial acceleration of velocity in ANFO would 3679 result in some error arrival time within a close proximity to the charge which begins to 3680 even out at greater scaled distances. This exact feature is seen in Figure 5.6b, from the 3681 large scale ANFO trials that exhibits recordings in arrival time which are greater than KB 3682

³⁶⁸³ predictions in near-field scaled distances.

3684



Figure 5.10: Theoretical schematic of different detonation and shock wave velocities with respect to scaled distance for TNT (Blue) and ANFO charges of various sizes (Red), with reference to the times at which detonation breakout occurs respectively to one another.

The initial offset is something which can be quantified using evaluated shock wave data for a TNT charge from KB prediction. If a velocity at detonation breakout can be recovered from these small scale ANFO charges then so can a time in which TNT would take to reach that same velocity. This would provide an initial offset at small scale distances and will be revisited in Section 5.4.1. Quantification of the increasing offset seen in Figure 5.9 is only possibly through understanding the behaviours of the shock wave from the moment it detonates up to far-field ranges.

3692

3693 5.3.2.4 Summary of Arrival Time Offset

Whilst all of the above offer a reasonable hypothesis as to why the captured arrival time data holds discrepancies to KB predictions, it is important to test these through other methods of analysis to provide further validation. Whilst varying detonator positions in a robust testing plan would be of interest to assess the variability of explosive yields within the near field, the results would not produce a significant progression in the characterisa³⁶⁹⁹ tion of small scale ANFO charges.

3700

Ensuring the exact formation and prill-to-prill interactions between tests is difficult for ANFO charge and therefore variations related to this are accepted as inherent to the heterogeneity of composition. With strict control measures the differences in prill size, charge density and oil absorption could be considered but it is believed to be a second order mechanism when establishing why the offset in arrival time for ANFO charges is so large.

3707

The proportionality in the velocities of detonation between TNT and ANFO, and their general trend prior to detonation product breakout are essential for understanding the arrival time offset. HSV techniques can be used to track the velocity of both the fireball expansion and the resulting shock wave propagation from the ANFO charges which is discussed further in Section 5.4.1.

3713

3714 5.3.3 Disagreement to Published TNT Equivalence

The fact this small scale testing regime resulted in a generally low TNT equivalence (TNTe 3715 $\simeq 0.4$) for ANFO is a contradiction to the widely accepted figure of approximately 0.80 3716 within the available published literature. Giglio-Tos and Reisler^[61] undertook a experi-3717 mental research consisting of the detonation of three large scale, 20-100 Ton, hemispherical 3718 ANFO charges which recorded blast parameters using pressure transducers and magnetic 3719 tape recording systems, resulting in a TNTe = 0.83. Petes et al.^[112] expressed the desir-3720 ability to use ANFO for explosive testing and provided a detailed compilation of historic 3721 testing results. These concluded on the idea that ANFO had approximately 80% of the 3722 energetic output of TNT. This thesis begins the discussion around why small scaled ANFO 3723 charges present a much lower energetic output than historically reported and what the 3724 real world implications of this are. The list below were the preliminary hypotheses based 3725 on the experimental results: 3726

3728 5.3.4 Was the composition of the explosive actually ANFO?

Findings from published literature details that purely ammonium nitrate detonation results in around $TNTe = 0.32-0.4^{[3,28,110,131,158]}$. This has led to considering the possibility the composition of ANFO being incorrect and fuel oil not being present as requested on purchase. With this in mind, the composition was tested using a gravimetric analysis, separating the substance using petane, resulting in a yield of $5.55\pm0.09\%$ and $94.45\pm0.09\%$ of the tested mass found to be fuel oil and ammonium nitrate respectively.

³⁷³⁶ During the detonation of ANFO consisting of 6% FO, theoretically an ideal and stoichio-³⁷³⁷ metrically balanced reaction occurs, meaning the oxygen molecules released as a result of ³⁷³⁸ the AN decomposition are enough to cause the full deflagration of FO. In our trials, with ³⁷³⁹ a lower percentage of FO at 5.5%, the detonation would result in a reduction in energy ³⁷⁴⁰ released $\simeq 5\%$ ^[92] through the development of nitrous oxides rather than full combustion ³⁷⁴¹ occurring. This however does not account for the 50% effective energy loss exhibited in ³⁷⁴² the recorded data. This finding led to the hypothesis being removed from consideration. ³⁷⁴³

37445.3.4.1Does the scale of the charge affect the chemical reactions occurring3745during detonation?

Due to the fact the FO constituent of the composition not being chemically bonded to the AN, there is a lag in the reaction time, related to reaction zone size. If the detonation wave is to reach the extent of the charge prior to this chemical reaction fully occurring, the potential energy release is considered to not be fully achieved.

3750

3758

In small scale charges, it was discussed whether the aforementioned reaction actually occurs at all, and therefore the yield of these tests is the result of only AN detonating. To test this hypothesis, Ammonium Nitrate prill was purchased from the same provider and tested under an identical methodology to the ANFO shots (250g hemisphere and boosted with a 1g sphere of PE10). In these trials no detonation occurred in any of the pure AN shots despite being boosted. This result was evidence to suggest the fuel oil oxygen reaction had to be occurring to sustain the detonation during the ANFO trials.

It was proposed that a percentage of the potential energy from the fuel oil was released 3759 from the ANFO prill directly surrounding the booster with the PE10 providing enough 3760 energy to near-instantaneously combust the FO in its immediate vicinity. However it was 3761 speculated, within the small sized charges, that the reaction of FO combustion could not 3762 sustain effectively when the reaction zone reached the edge of the charge where a lack of 3763 confinement results in pressure and temperature losses. This behaviour would result in 3764 the detonation of ammonium nitrate, with a tiny percentage of fuel oil, similar to the first 3765 hypothesis. 3766

3767

Numerical modelling of small scale AN charges was undertaken, using similar methods discussed in Section 4.2.2, to establish whether or not the reduced energy release from small scale ANFO charges was captured by simulating the detonation of AN. Both Figures 5.11ad and 5.12a-b represented experimental results for small scale ANFO trials when top and bottom detonated were compared with numerical simulations of 211.5g of AN detonation, established through removing the 5.5% FO composition and then an additional 10% mass for energy loses to the ground, in line with findings in Section 3.2.2.3.



Figure 5.11: Compilation of pressure-time and impulse-time histories from 1m standoff distances which related to top (red) and bottom (blue) detonated trials compared to APOLLO simulations of AN: a) Top P-T, b) Top I-T, c) Bottom P-T, and d) Bottom I-T.

The numerical simulations provide remarkable agreement with the experimental data de-3775 spite the fact a completely different explosive composition and corresponding JWL pa-3776 rameters have used to what is known to have been tested. The fact that the detonator 3777 position effects are captured effectively by the models provides confidence that assuming 3778 the ANFO composition behaves like pure AN at these mass scales is valid. The question 3779 posed here however is at what point does modelling the explosive as AN become invalid. 3780 Future research would consider testing a wide range of ANFO masses in free-field blast en-3781 vironments to quantify at what mass specifically results in a doubling of the yield through 3782 the fuel oil reaction occurring effectively. 3783

3784

Johansson^[82] presented the numerical modelling schemes of small scale ANFO charges which were validated using experimental work extracted from the literatures which detailed a lack of accuracy when using standard JWL parameters for capturing the behaviour on ANFO. The reason for this is because in a JWL EoS, there is an assumption of instantaneous energy release which for non-ideal explosives it is known not to be the case. Presented is an Ignition and Growth (I&G) EoS which when adopted for the same simulations, captures the behaviour of experimental ANFO detonation rather accurately. Future numerical simulation will consider the I&G EoS for non-ideal explosives in the attempt to capture their behaviours across a whole range of mass scales, alongside identifying at which regions are JWL parameters valid.

3795



Figure 5.12: Compilation of pressure-time and impulse-time histories from 1m standoff distances which related to top (red) and bottom (blue) detonated trials: a) Top P-T, b) Top I-T, c) Bottom P-T, and d) Bottom I-T.

37965.3.4.2Is the energy equivalence reduction related to unreacted ANFO prill3797projectiles?

The findings from the previous two hypothesis tests lead to a further theory that the overall explosive yield reduction, compared to quoted values in literature, could be directly linked to the quoted reaction zones of non-ideal explosives being anywhere from in 10-100mm^[29]. A rudimental analysis assessed the effect this radius of ANFO being un-reacted would have on the TNT equivalence for a variety of hemispherical charge sizes tested as seen in Figure 5.13.

3804

The analysis assumed a constant reaction zone size of 13mm and a TNTe = 0.82 to compute a mass ratio of ANFO for the reduced mass based on the reaction zone being un-reacted compared to the actual mass tested. The ratio was multiplied by the TNTe factor to assume an actually reacted TNTe factor in these small scale trials which is displayed by the plotted curve in Figure 5.13. This plot outlines both the charge masses tested in this series, which would result in a range of TNTe = 0.3 - 0.5, closely matching the spread seen for the experimental data conducted within this series (denoted by the red and blue markers), and charge masses up to those tested by Petes et al.^[112]. Based on these assumptions, to achieve the TNTe = 0.82 based on this mechanism alone, a charge mass of 10,000kg would be required.

> 1 Range of considered mass Masses tested in this regime 0 Top Detonated Pressure TNTe 0 Top Detonated Impulse TNTe Bottom Detonated Pressure TNTe Bottom Detonated Impulse TNTe È Petes et al. (1983) Carton (2018) Figuli et al (2014) 0 10⁻² 10⁶ 10⁰ 10^{2} 10⁴ Mass of original charge [kg]

Figure 5.13: Equivalent TNTe values resulting from applying a nominal 13mm reaction zone to a given ANFO charge and assuming that the region has not fully reacted and instead is fired off as a projectile compared with extract TNTe from experimental pressure and impulse data

It is important to note that the value of TNTe and size of reaction zone have been chosen based on published values and appropriate fits the available experimental data. The experimental recordings which are much lower than the quoted range of TNTe = 0.3 - 0.5are the result of being within a scaled distance of $Z < 1m / kg^{1/3}$, to which the top detonated position effects (see Figure 5.5) and fluid dynamic instabilities have a much greater influence on the recorded parameters and thus the inferred TNTe values, as discussed in Section 5.3.1.


3824 5.3.4.3 Additional Testing

Whilst a mechanism which captures the behaviour of the small scale charges, it is not necessarily the definitive physical process. The irony with the potential mechanisms considered in Section 5.3.4 is that both result in an effective yield reduction of around 50% for charges of this size, which agrees with the ratio between the recorded data and published values of ANFO yield, however, neither can be definitively confirmed.

It is actually hypothesised to be a combination of the above contributors which makes quantifying and characterising the fundamental process difficult. Further test were conducted using small scale charges but with a variety of ANFO/AN composition mixes. The idea behind these tests were to investigate and quantify the influence of FO has on the primary shock wave parameters and to establish which of the aforementioned mechanisms contributed to the over energetic output.

3837

The first lot of testing which was of interest was to vary the general composition of the 3838 AN/FO percentages to assess the effects this has for small scale ANFO charges. Petes 3839 et al.^[112] presented findings in large scales charge which suggested a drop in energy release 3840 when the FO percentage varied from being stoichiometric mix at 6%. To test this feature 3841 in small scale charges to establish whether the FO was making a difference in small scale 3842 charges was to change the composition by adding in a proportion of pure AN to reduce 3843 the global percentage of FO in each charge. A total of 10 tests (5 different FO% with a 3844 repeat test) were conducted recording the pressure-time history at two standoff distances 3845 resulting in 20 individual recordings. The data was analysed using standard methods dis-3846 cussed throughout this thesis, and an average TNTe factor was established for the tests 3847 at each FO percentage investigated, as seen in Figure 5.14. 3848

3849

What this investigation did prove was that even in these small scale charges, the percentage of FO does still play an effect on the overall explosive yield output from the detonation. This was enough evidence to suggest that during the detonation of ANFO in small quantities the mechanisms as to why a lower TNTe value is evaluated is not related to just AN detonating, and is a slightly more complicated phenomena. When no FO was present, the AN composition was unable to detonate, concluding that some FO is required and is part of the energy release process for small scale charges. 3857

It was therefore important to consider what would happen if the FO percentage was lower within the composition, but rather than a well mixed composition of ANFO with AN, having two distinct regions of AN and ANFO. This would investigate whether the reduced TNTe value seen for small scale ANFO is related to an unreacted shell of prill projecting away from the charge proportional to reaction zone sizes.





Figure 5.14: Extracted TNTe values from 250g hemispherical charge trials of ANFO varying the FO percentage by addition of pure AN

To test theories proposed in which only the FO in the direct vicinity of the booster charge 3864 is fully combusting and the remaining energy release is from the detonation of AN. To test 3865 this a double shelled hemisphere was used with the the inner shell containing ANFO and 3866 the outer shell consisting of pure AN both with 125g of the material in theory lowering 3867 the overall FO percentage down to 2.75%. With low levels of FO, it has been reported a 3868 incomplete reaction occurs and therefore lower energy releases and subsequentially slower 3869 detonation velocities^[183]. Obviously with a inner vacuum formed shell to keep the two 3870 compositions separate, an extra level of confinement, albeit minimal, is provided which 3871 could have resulted in additional combustion of the $FO^{[12]}$. 3872

3873

Figure 5.15a-d shows the results of a shelled hemisphere test of AN/ANFO mix when 3874 compared to a full 250g ANFO hemisphere measured at two different standoff distances. 3875 Considering the pressure-time history plots in Figures 5.15a and 5.15b, there is very little 3876 difference between the positive phases of the shelled trials and the full ANFO tests which 3877 alone suggests that the hypothesis that the outer layer of the charge provides very little 3878 to the initial primary shocks blast parameters. However, taking into account the specific 3879 impulse plots seen in Figures 5.15c and 5.15d, there is a clear reduction between the 3880 bench mark 250g ANFO and the hypothesis testing AN/ANFO shell. Whilst the 250g 3881 ANFO trial results in a TNTe $\simeq 0.36$, the shell trial exhibited a TNTe $\simeq 0.3$ assuming a full 3882 250g mass for both, suggesting there is a reduction in energy release but not what would 3883 be expected when removing 2.75% of the fuel oil which when looking at the trend seen in 3884 Figure 5.14, this composition would be expected to result in a TNTe $\simeq 0.23$. The question 3885 posed here is what the reason for an explosive with half the mass of ANFO and an outer 3886 shell of AN to provide a different behaviour to the same quantities of the material but 3887 evenly mixed. 3888



Figure 5.15: Compilation of pressure-time and impulse-time histories at 2m (red) and 8m (blue) standoff of 50/50 shells of ANFO/AN compared to 250g ANFO trials (black): a) 2m P-T, b) 8m P-T, c) 2m I-T, and d) 8m I-T.

It was considered whether the outer shell of the explosive exhibits detonation and/or com-3890 bustion in any of the tests conducted. The proof of some energy release in this region is 3891 exhibited through the differences in specific impulses when comparing the shelled tested 3892 to full ANFO in Figure 5.15, therefore it can be induced that the reactions are ongoing 3893 in the outer shell and cannot be fully assumed to be unreacted material projectiles. This 3894 leads on to the idea that close to the charge centre there is enough pressure, confinement 3895 and time for the ANFO to fully react prior to any energy loses, but the outer shell does not 3896 and therefore exhibits state changes but never fully reacted by the time breakout occurs. 3897 3898

A realistic conclusion to make from the results of the small scale ANFO tests, and the corresponding positive phase data, is that friedlander pressure-time histories are achieved similar to those resulting from ideal explosive detonation but for non-ideal explosives the reaction zone is the main mechanism which causes the reduction in TNTe and thus is not scalable with charge mass. The shelled tests exhibit specific impulse reductions when comparing to 250g ANFO shots which are directly related to the lack of FO in the final

section of the charge, and therefore no combustion could occur. It is assumed however that 3905 the outer shell of the charges only partially reacts, which is why only a small differences in 3906 the TNTe values extracted from the data is experience between the two trial types. With 3907 large charges, the reaction zone size becomes irrelevant when looking at its percentage of 3908 the whole charge mass and therefore the detonation fosters confinement, higher pressures, 3909 temperatures and more time for the reactions to occur, resulting in TNTe values close 3910 to the theoretical thermochemically derived value of TNTe=0.82. HSV work, discussed 3911 in Section 5.4, will look at quantifying a more realistic reaction zone size to improve the 3912 validity of the empirical curve derived in Figure 5.13. 3913

³⁹¹⁵ 5.3.5 Negative Phase

The negative phase of the small scale ANFO trials was of particular interest as again there is no previous literature which outlines its behaviour, and with the findings of discussed in Section 5.3.1 showing discrepancies between assumed knowledge and experimental data, further developments to understanding non-ideal detonation could be made. Figures 5.16ac represent the extracted and scaled negative phase parameters for the small scale ANFO trials which do not compare to KB predictions as well as the ideal explosives discussed in Figures 4.6a-c, which was somewhat expected.

3923

3914

Whilst Figure 4.6c presents a general consistency in the negative phase duration parameters extracted, the spreads observed are a consequence of the difficulty in prescribing the parameter generally, and within this low pressure region even more so. It is important to note that going forward the time duration of the negative phase will be omitted from further analysis in line with the notion presented within this thesis of it not providing truly valid data despite KB predictions capturing the parameter reasonably well.

³⁹³¹ Considered the negative pressure in Figure 5.16a, when comparing to KB predictions there ³⁹³² seems to be a much greater negative phase as a result of small scale ANFO detonations, ³⁹³³ resulting in a TNTe \simeq 0.82 providing a more appropriate fit. Needham^[107] discussed the ³⁹³⁴ phenomena of the negative phase and detailed the mechanism of the rising fireball creating ³⁹³⁵ lower pressure regions near the ground surface, which pulls the surround air towards the ³⁹³⁶ detonation point. This process further lowers the air density of the medium which has ³⁹³⁷ over-expanded during the shock waves propagation and therefore results in large negative phases within an energetic fireball. What this suggests for the small-scale ANFO trials is that the energy contained within the fireball, and subsequent shocks, is much greater than what is to be expected for standard ideal explosives, which has been related directly to the combustion of FO that was unable to occur during the initial detonation process.



Figure 5.16: Compiled scaled negative phase blast parameters from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.395, with increasing marker sizes to indicate the mass of charge: a) Reflected negative pressure, b) Reflected negative specific impulse, c) Scaled negative phase duration

Scaling all the negative phase data by a larger TNTe value based on the pressure data 3943 alone would result in a shift away from the KB predictions for the negative impulse in Fig-3944 ure 5.16b, which based on a TNTe=0.395 seems to be captured reasonably well. This led 3945 to question whether KB predictions were reasonable representations of ANFO, and other 3946 non-ideal explosives, for the negative phase as different TNTe values could be deduced 3947 for each parameter, which is unconducive when compared to how well ideal explosives be-3948 have against prediction tool across every considered parameter in far-field regimes. With 3949 ANFO still exhibiting ideal-like behaviours, but with a lack of scalability with mass, for 3950 each increment of mass scale there should be a valid TNTe value which works across the far-3951 field range and therefore a systematic error in the method of analysis has been highlighted. 3952 3953

The method of establishing the specific impulse values in Figures 5.16b and 4.6b, disregards the effect of the secondary shock during the calculation due it being so small in ideal explosives it could be omitted making minimal differences to the output results^[133]. Interestingly, small scale ANFO presents as if the secondary shock is more influential on the negative phase impulse as there is disagreement between the TNTe values required for KB predictions to capture the data. An investigation into the inclusion of capturing the secondary shock parameters when calculating the overall negative phase specific impulse. In doing so, a more appropriate value of a TNTe could be established which fits across each of the blast parameters in line with findings for ideal explosions in far-field scenarios seen in Chapter 4.

3976

With a more through examination of the data to account for the negative phase a stand 3965 alone feature of the primary blast wave by effectively omitting the effects of secondary 3966 shock was undertaken. As mentioned previously in Figure 5.16a, the negative pressure as-3967 sociated with small-scale ANFO seems to be better captured with a $TNTe \simeq 0.82$ which had 3968 been related to the FO combustion occurring within the confines of the fireball detonation 3969 cloud. It has been therefore assumed that all parameters which are extracted after the 3970 positive phase can be scaled accordingly with the idea that there is enough temperature, 3971 pressure and time for the full energy release from the partially reacted prill projectiles due 3972 to the confinement of the detonation cloud itself. Figures 5.17a-b present the negative 3973 phase parameters, scaled using a TNTe=0.82 when considering the behaviour as a perfect 3974 blast wave and removing effects of secondary shocks. 3975



Figure 5.17: Compiled negative phase blast parameters re-worked to include secondary shock capture from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.82, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse

³⁹⁷⁷ Clearly seen in both Figures 5.17a and 5.17b is a general improvement on how well KB

³⁹⁶⁴

predictions capture the negative phase experimental data. This finding provides justification the KB predictions capture blast parameters extremely well in the far-field regime when considering a perfectly ideal shock wave and thus the basis of future work which could look at the superposition of ideal primary and subsequent waves to establish accurate predictions for a real-world explosive event.

3983

3984 5.3.5.1 Secondary Shock Data

The scaled secondary shock data, when presented against KB predictions in Figures 5.18a-3985 d, again shows similar behaviour to the ideal explosives, with a large difference between 3986 predicted values of a primary wave but exhibiting considerable consistency across the en-3987 tire data set with respect to scale distance. The general behaviours of the data and the 3988 predictive curves are comparable which does give rise to the idea that secondary shock 3989 data is as deterministic as the positive phase and future work should consider the devel-3990 opment of similar empirical curves from a large quantity of secondary shock data resented 3991 within this thesis and published literature. 3992



Figure 5.18: Compiled scaled secondary shock blast parameters from ANFO explosive trials as a function scaled distance, compared with KB predictions, using a TNTe=0.82, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration

The issue currently faced is the idea that the secondary shock is highly dependent on the spatial and temporal characteristics of the fireball and therefore variations in the internal chemistry and energy release will increase the variation in extracted experimental data. Figures 5.19a-d present a compilation of all the secondary shock data collected within this thesis, scaled accordingly with the corresponding TNTe values.

Although the scaled data generally holds a level of comparison between the ideal and nonideal explosives there are some clear differences exhibited which could be key to further the understanding of small scale ANFO detonations and thus other non-ideal explosives. With reference to Figures 5.19b and 5.19c, the ideal explosives seem to exhibit less energy released in the form of specific impulse but have a time of arrival which seems to be smaller than that of the ANFO trials, suggesting that the secondary shock travels faster but is a much smaller quantity of energy associated with it. In reality this finding goes

back to the idea of the arrival time offset discussed in Section 5.3.2, which discussed the 4007 biggest influencer of arrival time offset to be the proportionality between the velocity of 4008 a ANFO shock wave, in comparison to one from an equivalent TNT mass. Interestingly, 4009 when approaching the near-field, $Z < 3m/kg^{1/3}$, the data for secondary shock arrival time 4010 tends towards the same point suggesting the offset between primary and secondary shock 4011 is consistent across all explosive types, related directly to the time in which it takes the 4012 secondary shock to begin to propagate. The data quickly trends away as the secondary 4013 shock in ANFO is travelling at a much lower velocity than that of the ideal explosives. 4014 The velocity proportionality theory could be explored in future research to acquire a re-4015 lationship between primary and secondary shock velocities for both ideal and non-ideal 4016 explosives to then quantify the offsets presented in Figure 5.19c in a robust manner. 4017 4018



Figure 5.19: Compiled scaled secondary shock blast parameters from all considered explosive trials as a function scaled distance, compared with KB predictions, using each corresponding TNTe value, with increasing marker sizes to indicate the mass of charge: a) Peak reflected overpressure, b) Scaled reflected peak specific impulse, c) Scaled arrival time, d) Scaled positive phase duration

It was important to test the dimensionless secondary shock delay prediction tool against small scale ANFO secondary shock data provided the knowledge that all parameters after

the primary wave is to be scaled with a TNTe=0.82. In order to express the secondary 4021 shock delay extracted from the data as dimensionless, there is a requirement to prescribe 4022 a velocity of detonation and packing density for the small scale ANFO. Whilst the packing 4023 density was measured pre-test to be approximately $820kg/m^3$, the velocity of detonation 4024 was uncertain from pressure gauge analysis alone. It was questioned whether the velocity 4025 of detonation used in this analysis associated to the primary shock, the secondary shock 4026 or the maximum velocity the detonation wave can achieve in the given composition. On 4027 closer inspection of the data presented within Rigby and Gitterman^[129] assumed the ve-4028 locity of detonation to be that associated with the maximum velocity of detonation the 4029 composition could achieve, meaning that regardless of mass scaling and the composition, 4030 the explosive secondary shock delay is normalised based on an ideal detonation. With 4031 that being said, the small scale ANFO data collected within this thesis was normalised 4032 using a velocity of detonation of 4,200m/s in line with values quoted in Petes et al.^[112], 4033 to which is presented in Figure 5.20. 4034

4035



Figure 5.20: Dimensionless secondary shock delay parameter evaluated for all explosive tested in this thesis, scaled accordingly, and compared with polynomial fit to historic data

4036 The clear comparable relationship between the normalised data and the fitted prediction

provides confidence in the tool across explosive composition mass and scaled distance. 4037 The concern however in considering small scale ANFO with a velocity of detonation of 4038 4,200m/s, similarly to large scale detonations, seems fragmented because the total energy 4039 released during detonation are different and thus the secondary shock behaviour should be 4040 too. It proposed that the energy which is not released during the development of the pri-4041 mary shock is gained during the propagation of the secondary shock, resulting in a halving 4042 of the blast parameters associated with the primary shock and doubling of the secondary 4043 shock parameters. This would explain why the delay time between primary and secondary 4044 shock arrival time is unaffected by this process as one the primary wave propagates slower 4045 and the secondary faster than they should when compared to large scale charges. This 4046 knowledge justifies the reason for assuming the maximum detonation velocity regardless 4047 of composition and mass scaling because even during non-ideal detonation the same quan-4048 tity of energy is released just over much lower time scales, and with understanding the 4049 two aforementioned parameters proportionality even if the energy is not captured by the 4050 primary wave, subsequent waves will. 4051

4052

4053 5.3.6 Pressure Gauge Summary

The section has considered the pressure gauge data recorded from the detonation of small 4054 scale ANFO charges with a thorough investigation into the mechanisms resulting in a 4055 TNTe=0.395 for primary shock wave positive phase parameters, and a TNTe=0.82 for all 4056 parameters subsequent to the breakout of the primary shock (i.e. negative phase of the 4057 primary wave and the secondary shock parameters). Discrepancies were exhibited in the 4058 TNTe of arrival time for both primary and secondary shocks which was related directly to 4059 the proportionality of velocity between small scale ANFO and TNT, which was not visible 4060 for ideal explosives discussed in Chapter 4, but in reality is probably a feature to consider 4061 during future analysis. 4062

4063

The pressure gauge analysis of small scale ANFO has provided insights into the behaviours of non-ideal explosives provided the reaction zone size is order of magnitudes larger than the explosive charges diameter. At each increment of mass, ANFO detonations result in friedlander shock wave behaviours which could be considered to be ideal, with a constant TNTe, across an entire range of standoff when compared to KB predictions. However, there is proportionality between mass and the associated TNTe, until a limit is reached 4070 where no amount of additional charge mass will effect the overall explosive yield. It is 4071 therefore paramount for a more robust mechanism of predicting non-ideal explosive be-4072 haviour.

4073

Interestingly, the findings for the secondary shock analysis suggest that of the total po-4074 tential energy of a given charge, there is a ratio of energy split between the primary and 4075 subsequent shocks. The amount of energy released during the primary shock development 4076 in small scale ANFO is approximately half than what was expected, however the devel-4077 opment of subsequent shocks encompassed around double the amount of energy. This 4078 idea has been speculated when considering the fact all the measured parameters which are 4079 confined within, and affected by, the detonation cloud for longer durations seem to exhibit 4080 far more energy in small scale ANFO than what is experienced in ideal explosives. 4081 4082

4083 5.4 High Speed Video Analysis

The methods discussed in Chapter 4 have been adopted for the far-field trials using hemi-4084 spherical ANFO charges to test their applicability to non-ideal explosives. The results from 4085 an individual trial at 5m standoff from a reflective wall was processed using the aforemen-4086 tioned methods and is presented in Figure 5.21. The data required a TNTe = 0.3 in 4087 order for the scaled arrival time data to replicate KB predictions. This is parallel to 4088 the findings from the MAE analysis undertaken on the pressure gauge data evaluating a 4089 lower TNTe factor (TNTe=0.28) for arrival time when compared to other blast parame-4090 ters (TNTe=0.395). This finding establishes confidence in the pressure gauge recordings 4091 triggering at the correct time and the time of arrival offset being a real physical feature 4092 of small scale ANFO charges. The reason for the offset in arrival time has vet to be fully 4093 established and therefore it is hoped that with the use of high speed video in conjunction 4094 with the theory of shock wave velocities presented in Figure 5.10, and their relationship 4095 to TNTe, an approximation for the offset could be deduced. 4096



Figure 5.21: Shock front arrival time from a bottom detonated 250g ANFO hemispherical charge placed at a 5 m stand-off, recorded using HSV and scaled using TNT equivalence factor of 0.3 to compare to KB predictions

4098 5.4.1 Fireball Breakout

Figure 5.22 displays two snapshot images taken from a bottom detonated hemispherical 4099 250g charge recorded at 1,000,000 fps. The average velocity of the detonation wave can 4100 be approximated using the known distance the wave has travelled in these tests, 53mm, 4101 divided through by the time taken to reach this position which was 28,000ns, resulting 4102 in a average velocity of $\sim 1900 \text{m/s}$. Considering Figure 5.10, it is a safe assumption that 4103 the velocity at breakout would be higher than this value due to the acceleration in ANFO 4104 detonation velocity from point source to charge extents and therefore is probably closer 4105 to a velocity of $\simeq 2700 \text{m/s}$, calculated from using the TNTe=0.395 established from pres-4106 sure gauges data analysis and multiplying it by the detonation velocity of TNT which is 4107 6950m/s. This finding is a reasonable approximation for supporting the notions regarding 4108 the lower TNTe value established from the far-field trials. 4109





Figure 5.22: Ultra high speed video footage of a bottom detonated 250g hemispherical trial displaying the comparison between charge diameter at the time of detonation and at the point in which the detonation wave reached the charge's extents and products began to expand; this is denoted by the charge size extending passed the green lines spaced 80pixels apart in both plots.

However, as discussed in Section 5.3.2, the lower TNTe value established from shock wave 4111 arrival time is when the data is compared to free-air shock propagation for TNT which 4112 during the early stage detonation process behaves very differently to ideal ANFO. It can 4113 be assumed that TNT from the moment it detonates, it does so with a velocity of around 4114 6950m/s across the entirety of its charge radius and then begin to decay when breakout 4115 occurs. As ANFO behaves differently, with an increasing velocity with charge radius, 4116 the best approximation which can be made for ANFO a average velocity of the detona-4117 tion wave across the radius to make it comparable to an almost perfect average velocity 4118 of 6950m/s in TNT. By making this assumption of average velocities, the difference in 4119 time it takes for a 250g TNT hemisphere to reduce down from 6950m/s to the average 4120 \sim 1900m/s would provide a reasonable theoretical approach to why an offset is recorded. 4121 4122

Figure 5.23 outlines the aforementioned theoretical approach and highlights an offset in 4123 arrival time of around 0.32ms between the detonation a 250g hemisphere of TNT and the 4124 time in which it begins to behave like a 250g hemisphere of ANFO based on HSV analysis 4125 of the fireball breakout. This offset value is similar to that presented in Section 5.3.2 when 4126 looking at the arrival time offset attributed to the pressure gauge data when comparing 4127 between the pressure and impulse evaluated TNTe=0.395 and the KB predictive curve, 4128 which gives justification towards this theory. Whilst ideal explosives exhibit similar veloc-4129 ity profiles to TNT, non-ideal explosive like ANFO need to be characterised differently, 4130 with shock wave arrival time being investigated based on the propagation dynamics of the 4131 detonation wave and subsequent shock wave. 4132





Figure 5.23: Shock wave velocity with respect to arrival time for a 250g TNT explosives evaluated through KB predictions with reference to the average vlocity extracted from the HSV of hemispherical ANFO detonation

4134 5.4.2 Variability Analysis

The same variability analysis undertaken in Section 4.3.1 to establish whether ANFO also 4135 behaves in a deterministic manner when relating the consistency of arrival time data to 4136 the scaled distance at which the recording was taken. Figure 5.24 shows arrival time vari-4137 ability across the top and bottom detonated (denoted by TD and BD respectively) ANFO 4138 hemispherical detonations with respect to scaled distance. The estimated gauge variation 4139 boundary (GVB) presented in Figure 4.11 for PE4 trials was used to test the confidence 4140 in the fit as a deterministic predictor for far-field free-air shock waves developed from 4141 different explosives. 4142

4143

The estimated GVB can be seen to generally hold credibility for the ANFO hemispheres tested and this provides confidence as this an upper bound for arrival time variability across the far-field range for all explosives. It is important to note that at the two extremities of the recording scaled distances, the variability in the data is higher based on
the shear lack of data points recorded. These positions correspond to the furtherest parts
of the cameras field of view and therefore are subject to lens distortion and can be omitted.

One finding that can be deduced which is in line with that of the pressure gauge data is that the variability of both bottom and top detonated shots are similar which gives rise to the consistency of each individual trial and the increase in variability as scaled distance enter the instability regions between $0.1 < Z < 3m/kg^{1/3}$ regardless of the differences in arrival time associated with detonator position discussed in Figure 5.9.



Figure 5.24: Logarithmic RSTD in shock wave arrival time of 250g hemispherical ANFO trials as a function of scaled distance for high speed video recordings, compared to empirical model detailed within Farrimond et al.^[49]

4156 5.4.3 Rate Stick Trials

The rate stick tests documented within this thesis were recorded using ultra high speed video cameras recording at between 250,000-500,000fps in order to capture the detonation wave propagation throughout each trial. The main reason for the variability of the frame rate is due to the filming capability of the camera used limited to a set number of frames, therefore in order to capture the fireball/shock wave propagation from the end of the cylinders a slower frame rate was required.

4163

The video recordings displayed in Figure 5.25 shows the general behaviour of the ANFO 4164 rate stick trials, which was consistent across all pipe sizes tested and therefore is not a 4165 diameter dependent feature within the bounds of this experimental regime. The first snap-4166 shot shows the 3g PE10 booster detonating and causing a preliminary flash to be seen 4167 percolate through the voids in the prill. As the snapshots progress through time intervals 4168 0.05ms, a clearly defined detonation wave can be seen to form, with a seemingly expanding 4169 bright region to which has been attribute to the ongoing chemical reactions attempting to 4170 find an equilibrium. The final snapshot shows the front of the reaction zone reaching the 4171 end of the pipe, at which point the bright zone succeeding it begins to compress until it 4172 reaches the end of the pipe too. The fireball/shock wave only begins to propagate away 4173 from the end of the tube when the bright zone is fully compressed which provides the 4174 understanding that the propagating pressure wave would be related to the position at 4175 which the cylinder begins to expand (the back of the bright zone) and the front face of the 4176 bright zone is a reaction wave which has effectively little-to-no pressure associated with it 4177 but induces decomposition of the explosive. The brighter region size of particular interest 4178 as it is speculated that this could be the reaction zone of ANFO which if quantified could 4179 be included in Figure 5.13 to both verify the projectile theory and the assumption of a 4180 13mm reaction zone for this sized charge. 4181

4182

Using similar methods discussed by Rigby et al.^[130] to track near-field blast loading, 4183 the displacement of the front and back faces of this bright region were tracked using the 4184 'Canny' edge detection in-built MATLAB function, as it was found to perform optimally 4185 for high contrast tracking. The back face of the bright region was defined by the position 4186 at which the cylinders began to laterally expand which provided to be more challenging to 4187 capture due to chaotic nature of the expanding detonation products. This was overcome 4188 by utilizing a threshold procedure to capture the brightest pixels, between a value of 0-255 4189 within each frame, and then assigning a range between the max value and a percentage 4190 (determined through trial and error) of the assigned pixel intensity, to which the edge 4191 detection function would consider. Anything outside of this threshold was omitted from 4192 the analysis, and assumed to be too dark to be the reacting region of the charge. To verify 4193

the assigned positions of the reaction zone, the tracked positions were plotted at regular intervals over the whole frame itself as seen in Figure 5.26.

4196

⁴¹⁹⁷ Using a pre-test photo taken from the high speed camera, displaying known dimensions ⁴¹⁹⁸ of the rate stick, the video was calibrated through assigning define boundaries of the pipe ⁴¹⁹⁹ external walls to achieve a real-world pixel size. The tracked positions from the source of ⁴²⁰⁰ detonation were calibrated to be a real-world distance travelled along the rate stick which ⁴²⁰¹ was also differentiated, with respect to time, resulting in the velocity of the propagation ⁴²⁰² of each front.

4203

Rather than viewing the whole pipe in its entirety with one analysis and the attempt to nullify any irregularities in the fronts bright regions behaviours, three randomly assigned box strips across the width of the rate stick were considered for the regions of analysis in the attempt minimise any curvature effects and irregularities across the entire front. These three independent processed data sets are to be used as self-validation of the results extracted from recordings.



Distance from End of Rate Stick [mm]

Figure 5.25: High speed video snapshots with 0.05ms intervals between each plot displaying the propagation of the detonation wave along a 300mm length 50mm diameter PMMA pipe



Figure 5.26: High speed video snapshots of 104mm internal diameter ANFO filled PMMA tube at t = 0.026, 0.052, 0.078 and 0.104ms after detonation, highlighting the reaction zone positions assigned (green lines) for the given region considered (green dashed lines) alongside the widths of the pipe (blue dashed lines).

⁴²¹¹ Figure 5.27 displays the same video recording as Figure 5.26 but only considering the

region defined by the green dashed lines. The reduced region of analysis results in a consistent reaction zone and therefore a definitive position can be established for each trial. The three regions of analysis were chosen at random between the confines of the rate sticks width, to establish a probabilistic catheterisation of reaction front position and velocity. These parameters were evaluated from both horizontal and vertical calibration pixel sizes across all three analysis regions and were compared to assess the accuracy and validity of the analytical data processing tool which can be seen in Figure 5.28.



Figure 5.27: High speed video snapshots of 104mm internal diameter ANFO filled PMMA tube at t = 0.026, 0.052, 0.078 and 0.104ms after detonation, zoomed into the area box region considered.

Figures 5.28a and 5.28b display the validation of the methodology process which considered the three different regions of analysis, all of which that are calibrated using both vertical and horizontal pixels sizes. The results from these different processes suggest not only is the calibration correct, resulting in accurate data, but the regional choices on the pipe result in a general consistency of both velocity and reaction zone size. It

is believed the initial flash duration discussed in Figure 5.25, corresponds to the time it 4225 takes before the measured reaction zone of the ANFO charges to visually appear without 4226 doubt through the illuminated prill. The initial flash from the detonator/booster reduces 4227 the precision of the visual interpretation of the ANFO detonation wave alone hence why, 4228 during the opening ~ 80 mm along the rate stick across both figures, spikes in the data is 4229 experienced which was a finding verified by Bohanek et al.^[17]. After this, the data begins 4230 to behave consistently and therefore can be considered to be credible and representative 4231 of the decomposition of ANFO, similar to the discussion made by Araos and Onederra^[4], 4232 until $\sim 200-250$ mm at which point, the data become corrupted by either detonation prod-4233 uct breakout or systematic experimental oversights of securing tape blocking the view of 4234 the reaction zone. With this in mind, all subsequent plots discussing the rate stick trials 4235 will be confined to these limits of distance along the pipe to avoid discussing the inefficacy 4236 of unverified data. 4237





Figure 5.28: HSV tracking results from a 50mm internal diameter rate stick trial, calibrated both vertically and horizontally, smoothed using a 15 point moving average to present: a) Detonation front velocity and b) Reaction zone length with respect to distance travelled along the pipe.

4239 5.4.3.1 Compiled Results

The results from the six different conducted rate stick trials subjected to the aforementioned analytical procedure are presented in Figures 5.29a and 5.29b for the lengths along the rate sticks which provide valid data which is representative of the decomposition an detonation of ANFO. When considering the smallest diameter pipes (50mm internal) which made use of a PE10 booster charge, denoted by the grey coloured lines, all exhibit consistency in velocity and reaction zone size across three nominally identical shots, providing confidence in the level of repeatability in the analytical methods developed between test, therefore verifying its application for the remaining tests to be qualitatively compared.



Figure 5.29: HSV tracking results from all ANFO rate stick trials conducted within this thesis, smoothed using a 15 point moving average to present: a) Detonation front velocity and b) Reaction zone length with respect to distance travelled along the pipe.

The non boosted 50mm diameter pipe shot presented much lower overall velocities and 4249 reaction zone than the boosted trials, with only a slight general increase in both with 4250 respect to distance along the rate stick. This finding is thought to infer the critical di-4251 ameter of ANFO to be around that of this pipe used in these trials due to the fact the 4252 energy loses due to the expansion of detonation products almost equals the energy released 4253 through detonation. What this does begin suggest is that the minimum bright zone size 4254 required to detonate ANFO successfully is represented by around 12mm which begins to 4255 point towards the theory proposed within Figure 5.13. 4256

4257

4258 The interesting finding when considering the 50mm internal diameter pipes is that upon

exhibiting behavior representative of ANFO detonation, a velocity of detonation measure-4259 ment of 1000m/s and 1200-1400m/s has been extracted for the non-boosted and boosted 4260 trials respectively. The latter of which reaches steady state detonation recording a velocity 4261 of $\sim 1700-1800$ m/s which is much lower than the quoted value for ANFO (~ 4200 m/s). The 4262 non-boosted 50mm rate stick test results in a consistent velocity of ~ 1000 m/s, due to the 4263 lack of additional initial energy provided by the booster to induce the chemical reaction 4264 process within the confinement of the charge prior to any detonation product expansion. 4265 The 50mm diameter rate sticks clearly are large enough to sustain the detonation reaction 4266 but the energy losses through the lateral fireball and product expansion is enough to freeze 4267 out any further energy gained from the decomposition of the ANFO. With these values 4268 in mind, a direct comparison can be made to the quoted value which results in a ratio of 4269 between $\simeq 25-43\%$ depending on the values chosen which is believed to be further evidence 4270 to the reduced yield from small scale ANFO charges when to large charge trials conducted. 4271 4272

The larger diameter rate stick trials (74mm and 104mm internal diameters) exhibited a 4273 much higher initial velocity which has been initially tracked $\sim 2300 \text{m/s}$, both increasing at 4274 similar rates to peak values of around 2800m/s after a 200mm run along the rate stick but 4275 no levelling off like what is exhibited in the 50mm diameter pipes. This is related to the 4276 fact the large diameter pipes induce a longer duration of confinement and therefore the 4277 energy loss through lateral expansion of these rate stick was no longer enough to restrain 4278 a minimum steady-state velocity but instead result in an increase in energy released and 4279 front velocity with respect to distance along the rate stick. 4280

4281

Considering the trajectory of these velocities, it is approximated that a rate stick of around 4282 500mm long is required to exhibit the quote velocities of large scale ANFO, assuming no 4283 plateauing occurs at these charge diameters. The 74mm and 104mm internal diameter 4284 pipes show similar patterns of behaviour for both reaction zone length and velocity devel-4285 opment which highlights the fact that the energy loss through lateral expansion of these 4286 rate sticks was no longer enough to restrain steady-velocities of the recorded fronts but 4287 instead resulted in an increase in energy release and velocity. This begins the debate as 4288 to whether the definition of the critical diameter of an explosive is the minimum size at 4289 which a cylindrical charge has to be to sustain a steady-state detonation is correct for 4290 non-ideal explosives and whether this could be the reason for a variety of different critical 4291 diameters quoted within published literature. 4292

4293

Qualitatively, the 104mm pipe seems to result in an increasing velocity at a greater rate 4294 than those recorded in the 74mm pipe. This is logical if less energy is being lost later-4295 ally whilst simultaneously gaining energy from the decomposition of ANFO but there is 4296 a larger surface area associated with the 104mm diameter pipe which will result in larger 4297 energy losses. This finding could be an artefact of the 15 point moving average applied 4298 to the raw data and should be treated with caution, assuming that the general physical 4299 mechanisms are similar. It is expected that with an increased minimum radius until det-4300 onation product breakout, the quicker the rise time in velocity to maximum theoretical 4301 value for ANFO. Using the data presented, this finding is not something which can be 4302 concluded on and would require a much more extensive rate-stick test plan across a range 4303 of pipe sizes and lengths with multiple repeats to establish its validity. 4304 4305

The measured reaction zone sized across all trials conducted with a booster exhibits an 4306 increase with distance travelled along the rate stick. As discussed previously, it is posited 4307 that as the ANFO detonates, under optimal conditions of confinement, the reaction zone 4308 length will increase in size. With the detonation cloud expansion only starting to occur 4309 when the back face of the zone reaches the charge extents, it is a reasonable suggestion 4310 that the larger the measured reaction zone, the more decomposition of ANFO occurs. This 4311 would result in a greater efficiency in the energy release of the composition as there would 4312 be more time and confinement for the deflagration of FO to occur. With this in mind, 4313 there key measurement of the reaction zone is at the beginning of the rate stick prior to 4314 any increase in length as this will identify the the amount of ANFO which could in theory 4315 will not react in any detonation. 4316

4317

It was hypothesised that the reaction zone measured in the rate stick trials could infer the 4318 range in size the zone could be depending on the test-to-test variability in the charges, 4319 directly relating to prill form and their macrostructural arrangement. Taking the non-4320 boosted 50mm trials presented in Figures 5.29a and 5.29b, a near steady-state detonation 4321 is displayed and therefore the trial was close to the critical diameter of non-boosted ANFO. 4322 With this in mind, it would suggest the constant behaviour in the measured reaction zone 4323 length of between 9-17mm, taking the range recorded, is the minimum size required to 4324 detonate ANFO and therefore the size in which quantifies the amount of ANFO which 4325 may be unreacted on breakout of the detonation products and the primary shock wave. 4326

4327

Undertaking a similar analysis presented in Figure 5.13, the TNTe values were calculated 4328 for effective masses of ANFO resulting from the reaction zone sizes of 9mm and 17mm in 4329 line with the aforementioned findings and is presented in Figure 5.30. What can instantly 4330 be deduced from this plot is the fact that almost all the collected data, both from this 4331 research and historical is captured by the theoretical mechanism proposed and therefore 4332 provides justification to the theory of unreacted prill projectiles. Whilst there is agree-4333 ment, the definitive mechanism is still to be established and future experimental testing 4334 should consider both the attempt of capturing this mechanism using high speed video and 4335 investigate the mass range which minimal data is presented for between 1-50kg, to verify 4336 if a general increase in TNTe is recorded in line with theoretical prediction. 4337 4338



Figure 5.30: Equivalent TNTe values resulting from applying a nominal 13mm reaction zone to a given ANFO charge and assuming that the region has not fully reacted and instead is fired off as a projectile compared with extracted TNTe values from experimental pressure and impulse data, making reference to the reaction zone range recorded Figure 5.29b.

4339 5.4.4 High Speed Video Summary

The validated HSV data processing tools developed within this thesis have been compared to the non-ideal explosive ANFO, in the attempt to characterise the mechanisms underlying the lower explosive yields associated with small scale charges and provide both theoretical and empirical quantifications to support the hypotheses made.

4344

4348

The results from using the originally developed tools provided confidence than small scale A346 ANFO charges at each increment of mass behave with ideal-like characteristics, exhibiting the ability to be scaled by a single given TNTe value in far-field ranges.

The use of KB velocity relationships provided further insights into why the arrival time of 4349 small scale ANFO charges do not have a directly comparable relationship to TNT when 4350 comparing to other blast parameters extracted. The development of detonation velocity 4351 within the ANFO composition was not measured as part of these tests, but an average 4352 velocity from detonation to breakout was inferred which allowed comparison to the be-4353 haviour of an ideal explosive and therefore TNT. Implementing this theoretical approach 4354 resulted in arrival time offset which closely matched the pressure gauge data when com-4355 pared to KB predictions. 4356

4357

Rate stick trials were undertaken in the attempt to further understand the internal det-4358 onation mechanisms and processed within smaller scale ANFO charges. An automated 4359 tracking algorithm was developed and self-validated in terms of its accuracy of tracking 4360 and the consistency in the test data through comparing three nominally identical shots 4361 which resulted in highly consistent data. The remaining trials were the conducted using a 4362 variety of pipe diameters and non-boosted charges. Through the analysis there is a clear 4363 relationship presented between confinement and/or charge diameter with the development 4364 of velocity. 4365

4366

One rate stick trial which was at quoted values of the critical diameter of ANFO (50mm internal diameter) and was not boosted, resulted in near steady state conditions, which not only verified the critical diameter but also presented the minimum conditions to achieve detonation. The reaction zone measurement for this trial was utilised to improve the mechanism of unreacted ANFO projectile prediction presented in Figure 5.30, which jus4377

tified the behaviour of both small and large scale ANFO trials and presents ranges of
potentially TNTe fluctuations based on the uncontrollable variables associated with heterogeneous prilled ANFO detonation. Whilst reasonable justification for these mechanisms
have been presented, a much larger and rigorous testing regime for ANFO, across mass
scales is required to help further validate the hypothesis presented.

4378 5.5 Future Research into Non-Ideal Detonations

The investigation into small scale ANFO has provided a significant gap in the current 4379 understanding of non-ideal explosive characterisation and the mechanisms which result in 4380 there effective and overall potential explosive yields. Whilst there are studies which at-4381 tempt to quantify a range of explosives which exhibit non-ideal behaviours, a distinct lack 4382 of thorough investigation is presented within published literature to quantify yields based 4383 on both mass and distance. The implication of assuming non-ideal explosives exhibit the 4384 same chemical processes during detonation as ideal explosives across an entire mass range 4385 is a general over prediction of the explosive output. If numerical models are not able 4386 to capture the yield of particular composition accurately across a full range of masses, 4387 a uncertainty within design regimes occur with the knock on effect of over-engineering 4388 each element of protection. Conducting well-controlled experiential trials for a number of 4389 commonly used home made explosives, varying both mass and standoff distance, will en-4390 able a global understanding of explosive loading conditions which can be integrated within 4391 probabilistic load characterisation for optimised protective schemes of element design. 4392 4393

In addition, this compilations of experimental data can be used to develop more robust numerical modelling schemes through the validation of thermochemical code values developed for EoS of each explosive. The method presented within this thesis makes use of the JWL EoS for small scale but adjusted to model AN alone which is known to be incorrect despite the accuracy of the simulation across the far-field range. Further investigation into the use of Ignition and Growth (I&G) EoS should be undertaken to accurately capture the detonation mechanics of non-ideal explosives across a whole range of masses.

Future work should look at undertaking a quantitative analysis of shock wave velocity across a full range of distances as a result from small scale ANFO charges using timer pins within the composition itself, alongside tracking the wave using incident gauges and/or
HSV from detonation through to free-air propagation. In doing so, empirical comparisons
can be made between the recorded data and the KB derived shock wave velocities for TNT,
to further access the hypothesis suggested in Figure 5.10 and to attempt to quantify the
offset associated with the disproportional shock wave velocity of TNT and ANFO.

4410 Chapter 6

⁴⁴¹¹ Summary, Conclusions and Future ⁴⁴¹² Work

4413 6.1 Summary

This thesis has aimed to characterise and quantify the effects of a shock wave in far-field regimes resulting from the detonation of both ideal, and non-ideal, explosives using validated analytical data processing methods.

4417

Explosive detonation and the subsequent parameters which follow have been investigated 4418 for many decades but despite best attempts to understand their effects, a clear divide has 4419 been presented for the fundamental nature of shock wave dynamics and the variability 4420 exhibits. Whilst designing infrastructure to withstand extreme dynamic loading poses dif-4421 ficulty when considering where a charge may be in relation to the structure, alongside its 4422 composition and mass, making it harder is the uncertainty on how deterministic the yields 4423 of an explosive are. If explosives exhibit high levels of variability within simple scenarios, 4424 the engineer can have no confidence of ensuring designs are robust enough to withstand 4425 extreme loading. 4426

4427

If variability levels can be established with respect to the distance a given charge is away from a target, a more probabilistic approach can be undertaken by a designer which exhibits a higher level of safety confidence. It is therefore of high importance to assess current practices of experimental work to highlight reasons as to why explosive yields

are viewed as chaotic by some in the industry and provided a robust approach to un-4432 dertaken well-controlled trials to reduce the inconsistency in data. Chapter 2 provides a 4433 review of the current literature as well as background theory to blast wave phenomenol-4434 ogy alongside state-of-the-art predictive methods for explosive yields in free-air scenarios. 4435 Chapter 3 proposed the development of numerous data processing tools which are exposed 4436 to PE4 experimental data and undergo synergetic validation with numerical simulations 4437 to highlight systematic features within methodologies, their effects and how they can be 4438 mitigated. Chapter 4 exercises the tools on a large data set of three ideal explosives in 4439 the attempt to both validate the tools across a wide range of ideal explosives and to iden-4440 tify whether ideal explosives exhibit deterministic behaviours across the far-field range of 4441 scaled distances. The methods which were validated in the aforementioned chapters were 4442 the used in Chapter 5 to study their applicability to small-scale non-ideal explosives, such 4443 as ANFO. The results of which provided fundamental insights into the characterisation of 4444 non-ideal explosives. 4445

4446

Findings from the PhD thesis provide a robust and validated far-field data set across a 4447 number of small-scale explosive compositions which should be used as a benchmark, not 4448 only for the level of repeatability achievable from well-controlled far-field trials, but as a 4449 final highlight to the blast community that far-field parameters are deterministic and are 4450 captured remarkably well by semi-empirical KB predictions. The industry's more mod-4451 ern construct of explosive detonation exhibiting significant and inherent variability across 4452 the entire range of scaled distances is the result of probabilistic based regimes which col-4453 lated trial data which had systematic errors in their approach of conducting and analysing. 4454 4455

The investigation into the detonation of small scale non-ideal explosive, ANFO, has pro-4456 vided fundamental developments to the understanding of how detonation mechanics effect 4457 the overall charge yield. Despite non-ideal behaviour, when a composition exhibits deto-4458 nation, provided the minimum reaction zone size is smaller than the charge diameter, it 4459 will result in a Friedlander ideal-like pressure-time history but the equivalency to TNT 4460 will vary based on the minimum charge radius and therefore mass. Through a theoretical 4461 approach, validated with experimental data, a fast look up tool for ANFO detonations is 4462 provided to estimate the explosive parameters depending on mass scaling. 4463

4465 6.2 Conclusions

The resulting work documented within this thesis can be summarised in the following conclusions which are listed in chronological order of appearance within the thesis:

When considering the far-field range alone, well-controlled experimental trials result in highly deterministic blast parameters across both the positive and negative due to exhibiting low levels of variability from nominal identical testing regimes. This finding has been shown across both ideal and non-ideal explosives in Figures 3.10 and 5.6.

- The prediction curves developed by Kingery and Bulmash^[87] not only capture the results of ideal explosive detonation in far-field regimes remarkably well, but are a sign of incredible provess in both theoretical and empirical understanding of blast wave phenomenology during the times the trials were conducted.
- Systematic features, such as detonator position (Figure 3.16), gauge mounting apparatus (Figure 3.15) and so on, albeit seemingly negligible in the grand scheme of explosive detonation, present issues in acquiring deterministic behaviours as scaled distances reduce into near-field regimes due to detonation mechanisms and shock wave interactions being highly sensitive to small changes respectively.
- The secondary shock phenomena presents similar levels of consistency with scaled distance in the far-field regime as the primary shock and therefore prediction curves, similar to those presented by Kingery and Bulmash^[87], has been presented in Figure 4.7.
- The use of high speed video recordings and subsequent validated data processing methods has shown to result in comparable data to that recorded with pressure gauges (Figure 4.11), but providing parameters across a much broader range of scaled distances from a small number of recordings.
- Non-ideal explosives, although exhibit friedlander-like pressure-time histories, are
 not scalable with mass like ideal explosives. The small-scale ANFO detonation re sults in a much lower explosive yield than quoted TNTe values within published
 literature suggest, established from large scale trials, depicted in Figure 5.7.
- Small scale ANFO detonations exhibit a seemingly delayed arrival time when compared to equivalent TNT detonations in Figure 5.7. This has been related to the

detonation and shock wave velocity profile inconsistencies between an ideal explosive 4496 behaviour and that of ANFO. Upon detonation of an ideal explosive, the detonation 4497 wave is assumed to propagate as its maximum velocity until reaching the edge of the 4498 charge at which point a decay in the velocity occurs. ANFO however sees an increase 4499 in detonation wave speed with the distance it has to travel through the explosive 4500 charge. This results in a clear discrepancy between arrival time predictions across 4501 the smaller charge diameters tested, but becomes increasingly negligible in line with 4502 charge diameter, in line with Figure 5.10. 4503

The negative phase of small scale ANFO detonations present reasonably higher magnitudes of parameters, comparing better with quoted figures of ANFO TNTe=0.82
in Figure 5.17. This has been deduced to be the effect of any ANFO which did not have enough time to full detonated during the first pass of the primary detonation wave, releases its energy sometime after, creating a more vigorous and energetic fireball which in turns results in an increased suction effect at ground level and thus large negative phases pressures and more powerful secondary shock features.

The mechanism underlying the reason as to why small scale ANFO resulting in much
lower yield in for positive phase parameters has been directly linked to the behaviour
of the characteristic reaction zone size for ANFO, projecting away from the charge
effectively unreactive. The mechansim has been comprehensively compared against
test data from a range of scales and is found to encapsulate the data remarkably
well in Figure 5.30.

Non-ideal explosives can be predicted by both empirical prediction tools and numerical simulations, therefore exhibiting ideal-like behaviours at each increment of mass. It is therefore important to make use of a third dimension to prediction tools for non-ideal explosions which consider the characteristic reaction zone projectile mechanism for a given composition which can be established using rate stick trials.

4522 6.3 Evaluation and Future Work

⁴⁵²³ Chapter 3 made a distinct effort to develop data processing methodologies for standard ⁴⁵²⁴ free-air explosive trials in the attempt to assess the validity of deterministic regions of ex-⁴⁵²⁵ plosive yield presented by Tyas^[173]. An extensive data set, comprising of 144 recordings ⁴⁵²⁶ of small-scale hemispherical PE4 detonations over the far-field range, was utilised to verify

the processing tools ability to capture blast wave parameters and evaluate them through 4527 comparisons to Kingery and Bulmash^[87] semi-empirical predictions. The background to 4528 characterising explosive yield, particularly in the far-field regime, is lack of agreement 4529 in the consistency of recorded parameters. Borenstein^[18] state the reasons believed for 4530 a wide range of variability assumption have been made for explosive yields is down to 4531 the way each individual decided to assess the results. Extrinsic and intrinsic sources of 4532 variability were not completely outlined in each published article, with conclusions drawn 4533 from the data which may not have been scientifically accurate. This has led parts of 4534 the industry to believe explosive detonation is inherently variable, which fosters anoma-4535 lous, or widely varying, data to be accepted as given without a through critique being 4536 undertaken. Whilst a generalised understanding of explosive yield regardless of explosive 4537 size, shape, composition and separation distance from a target (extrinsic) is important for 4538 probabilistic-based analyses, as to is a more robust and scientific understanding of a defini-4539 tive situation is required for high confidence in prescribed loading for specific scenarios. 4540 Through establish well-controlled experimental methodologies, validated and improved 4541 through numerical simulation, clear improvements in the understanding of explosive vari-4542 ability has been established, with both positive and negative phase parameters not only 4543 exhibiting deterministic behaviours but are also captured remarkably well by the KB pre-4544 diction tools, agreeing with the works of $\text{Esparza}^{[45]}$ and Rickman and Murrell^[125] and 4545 verifying the hypothesis posed by $Tyas^{[173]}$. 4546

4547

In near-field regimes, where the blast wave parameters are driven by the expanding det-4548 onation products and fireball, higher levels of variability has been recorded. This ties in 4549 with the uncertainty in of KB predictions in this regime where physics-based numerical 4550 simulations are shown diverge rapidly as scaled distances are reduced Cormie et al.^[32]. 4551 Whilst preliminary work at the University of Sheffield has made attempts at capturing 4552 spatial and temporal variations of near-field loading^[51,134,174], there is still a lot of work 4553 required to provide a robust understanding of these extreme conditions. Barr et al.^[10] 4554 has developed a new capability which vastly improves the resolution of the data capture 4555 presented in the aforementioned articles. Through a rigorous testing regime using this 4556 capability of near-field scaled distances and explosive charge compositions, the results 4557 would be used to provide better guidance for explosive quantification and characterisation 4558 through the full detonation process. 4559

Non-ideal explosives are discussed within literatures as exhibiting varying rates of energy 4561 release, depending on homogeneity, with discussion into how detonation mechanics inter-4562 nally within the charge, measuring velocity of detonation, changes with charge diameter 4563 and/or confinement^[5,80]. There is little investigation into the characterisation of shock 4564 wave development from non-ideal explosives and with what is available consisting of pre-4565 dominantly large scale trials which has been taken as a given across all mass scales $[^{68}]$. 4566 This is contradictory to the aforementioned articles which finds significant variations when 4567 considering the release of energy from non-ideal explosives being across longer timescales. 4568 To exhibit full potential release, non-ideal explosives need confinement from either a sur-4569 rounding material or additional charge mass which results in enough time before breakout 4570 to exhibit the full chemical decomposition. Smaller scale charges by nature therefore result 4571 in partial energy releases and cannot be defined by a single value of TNTe in line with 4572 the theories presented for ideal explosives. Chapter 5 has proven this finding by adopting 4573 the same well-controlled methodologies and validated data processing tools whilst deto-4574 nating small scale ANFO charges which resulted in much lower TNTe values than what 4575 has historically been published. Whilst a mechanism for the reduction in yield has been 4576 presented, it is important to test this theory with future larger scale trials, in the attempt 4577 to categorise at which mass scales do normal TNT equivalency rules apply, in which a 4578 non-ideal explosive exhibits ideal-like behaviours, and where the explosive yield becomes 4579 highly dependent on the mass. 4580

4581

Although ANFO was the only non-ideal explosive tested in this thesis, it is not the only one of interest or threat. Future works will consider the effects of other non-ideal explosive compositions to see if they too exhibit behaviours similar to ANFO with another dimension of scaling with mass. A more comprehensive dataset of non-ideal detonations across both mass and distance scales is required to provide confidence in the ability to not only understand explosive events but to capture them accurately with numerical simulation.

The conclusions made throughout the entirety of this thesis should provide evidence to the idea of deterministic blast wave features across a number of explosives in particular for far-field scenarios, and therefore any other suggestion should be put down to either systematic errors in data acquisition or results reporting extrinsic variability. The findings should ultimately be taken forward into the analysis of near-field, where the fundamental quantification is lacking, to see if similar characterisation methods can be adopted.
Bibliography

- [1] Akhavan, J. [2011], *The Chemistry of Explosives: Edition 3*, The Royal Society of
 Chemistry, Cambridge.
- [2] Ammann, O. and Whitney, C. [1963], 'Industrial engineering study to establish safety
 design criteria for use in engineering of explosive facilities and operations'. Report
 for Picatinny Arsenal. New York: Ammann and Whitney.
- [3] Aouad, C. J., Chemissany, ., Mazzali, P., Temsah, Y. and Jahami, A. [2021], 'Beirut
 explosion: TNT equivalence from the fireball evolution in the first 170 milliseconds',
 Shock Waves 31, 813–827.
- [4] Araos, M. and Onederra, I. [2017], Rectangular and Circular Explosive Charges Detonation Study using High-Speed Video, *in* '9th World Conference on Blasting
 and Explosives', Stockholm, Sweden.
- ⁴⁶⁰⁸ [5] Araos, M. and Onederra, I. [2019], 'Preliminary detonation study of dry, wet and
 ⁴⁶⁰⁹ aluminised ANFO using high-speed video', *Central European Journal of Energetic*⁴⁶¹⁰ *Materials* 16(2), 228–244.
- [6] Baer, M. R., Gartling, D. K. and DesJardin, P. E. [2012], 'Probabilistic models for
 reactive behavior in heterogeneous condensed phase media', *Combustion Theory and jodelling* 16, 75–106.
- 4614 [7] Baker, W. E. [1973], *Explosions in air*, University of Texas Press: Austin.
- [8] Baker, W. E., Cox, P. A., Westine, P. S., Kulesz, J. J. and Strehlow, R. A. [1983], *Fundamental Studies in Engineering 5: Explosion hazards and evaluation.* **URL:** http://deepblue.lib.umich.edu/handle/2027.42/25541
- ⁴⁶¹⁸ [9] Balakrishnan, K., Genin, F., Nance, D. V. and Menon, S. [2010], 'Numerical study
 ⁴⁶¹⁹ of blast characteristics from detonation of homogeneous explosives', *Shock Waves*⁴⁶²⁰ **20**, 147–162.

- [10] Barr, A. D., Rigby, S. E. ., Clarke, S. D., Farrimond, D. G. and Tyas, A. [2023], 'Temporally and Spatially Resolved Reflected Overpressure Measurements in the Extreme
 Near Field', Sensors 23(964).
- [11] Bdzil, J. B., Aslam, T. D., Henninger, R. and Quirk, J. J. [2003], 'High-Explosives
 Performance', Los Alimos Science 28, 96–110.
- [12] Boganek, V., Suceskka, M., Dubrilovic, M. and Hartlieb, P. [2022], 'Effect of confinement on detonation velocity and plate dent test results for anfo explosive', *Energies*15(4404), 1–9.
- [13] Bogosian, D., Ferritto, J. and Shi, Y. [2002], Measuring uncertainty and conservatism
 in simplified blast models, *in* '30th Explosives Safety Seminar', Atlanta, GA, USA,
 13-15 August.
- [14] Bogosian, D., Powell, D. and Ohrt, A. [2019], Consequences of Applying Objective
 Methods for Selecting Peak Pressure from Experimental Data, *in* 'International Symposium of the Interaction of Effects of Munitions with Structures (ISIEMS)', Panama City, Florida, 21-25 October, p. 11.
- [15] Bogosian, D., Yokota, M. and Rigby, S. E. [2016], TNT equivalence of C-4 and PE4:
 a review of traditional sources and recent data, *in* '24rd international symposium on
 military aspects of blast and shock (MABS)', Halifax, Nova Scotia, Canada, 19-23
 September.
- [16] Bogosian, D., Yu, A., Dailey, T. and Ohrt, A. [2014], Statistical Variation in Reflected
 Airblast Parameters from Bare Charges, *in* '23rd international symposium on military
 aspects of blast and shock (MABS)', Oxford, England, 7-12 September.
- [17] Bohanek, V., Tumara, B. S., Serene, C. H. Y. and Suceska, M. [2023], 'Shock initiation and propagation of detonation in anfo', *Central European Journal of Energetic Materials* 16, 1–13.
- ⁴⁶⁴⁶ [18] Borenstein, E. [2009], Sensitivity analysis of blast loading parameters and their trends
 ⁴⁶⁴⁷ as uncertainty increases, PhD thesis, The State University of New Jersey, USA.
- ⁴⁶⁴⁸ [19] Brode, H. L. [1955], 'Numerical simulations of spherical blast waves', *Journal of* ⁴⁶⁴⁹ Applied Physics **26**(6), 766–775.

- [20] Buczkowski, D. [2014], 'Explosive Properties of Mixtures of Ammonium Nitrate(V)
 and Materials of Plant Origin Danger of Unintended Explosion', *Central European Journal of Energetic Materials* 11, 115–127.
- [21] Canny, J. [1986], 'A Computational Approach to Edge Detection', *IEEE Transactions*on Pattern Analysis and Machine Intelligence 8(6), 679–698.
- [22] Carton, E. [2018], Air Blast Mitigation Using Water Foam Coverage, *in* '25nd Military
 Aspects of Blast and Shock Symposium (MABS)', The Hague, Netherlands, 24-27
 September.
- ⁴⁶⁵⁸ [23] Catanach, R. A. and Hill, L. G. [2002], 'Diameter effect curve and detonation front ⁴⁶⁵⁹ curvature measurements for anfo', *AIP Conference Proceedings* **620**, 906–909.
- ⁴⁶⁶⁰ [24] Cetner, Z. and Maranda, A. [2014], 'Selected parameters of heavy-ANFO explosive
 ⁴⁶⁶¹ materials', *High Energy Materials* **T.6**, 31–37.
- [25] Chabia, A. J., Bass, R. C. and Hawk, H. L. [1965], Measurements of wave fronts in
 earth, air and explosive produced by a 500-ton hemisphere of the detonated on the
 surface of the earth, Technical Report SC-RR-64-442, Sandia National Laboratories,
 Albuquerque, New Mexico, USA.
- (26) Chapman, D. L. [1899], 'On the rate of explosions in gases', *Philosophical Magazine* 4667 47(284), 90–104.
- ⁴⁶⁶⁸ [27] Chiquito, M., Castedo, R., Lopez, L. M., Santos, A. P., Mancilla, J. M. and Yenes,
 ⁴⁶⁶⁹ J. I. [2019], 'Blast Wave Characteristics and TNT Equivalent of Improvised Explosive
 ⁴⁶⁷⁰ Device at Small-scaled Distances', *Defence Science* 69, 328–335.
- ⁴⁶⁷¹ [28] Cochrane, K. [2006], Moranbah Ammonium Nitrate Project, Technical report, Dyno
 ⁴⁶⁷² Nobel Asia Pacific Limited, Salt Lake City, Utah.
- [29] Cook, M. A. [1968], 'Explosives—a survey of technical advances', Industrial and Engineering Chemistry 60, 44–55.
- [30] Cooper, P. W. [1990], Comments on TNT Equivalence, in '20th Internation Pyrotechnics Seminar', Colorado Springs, Colorado, July 24th-29th.
- 4677 [31] Cooper, P. W. [1996], Explosives Engineering, VCH Publications, New York.
- [32] Cormie, D., Mays, G. and Smith, P. [2019], Blast effects on buildings 3rd Edition,
 Vol. 3, ICE Publishing.

- ⁴⁶⁸⁰ [33] Cranz, C. [1926], Lehrbuch der Basllistik, Springer Germany, Berlin.
- ⁴⁶⁸¹ [34] Dasch, C. J. [1992], 'One-dimensional tomography: a comparison of Abel, onion-⁴⁶⁸² peeling, and filtered backprojection methods', *Applied Optics* **31**(8), 1146–1152.
- [35] Davis, V. W., Goodale, T., Kaplan, K., Kriebel, A. R., H.B, M., Melichar, J. F.,
 Morris, P. J. and Zaccor, J. N. [1973], Nuclear weapons blast phenomena, volume
 4685
 4: Simulation of nuclear airblast phenomena with high explosives, Technical Report
 4686
 1200-4, DASA, Washington DC, USA.
- [36] Dennis, A. A., Pannell, J. J., Smyl, D. J. and Rigby, S. E. [2021], 'Prediction of blast
 loading in an internal environment using artificial neural networks', *International Journal of Protective Structures* pp. 1–28.
- [37] Dewey, J. M. [1964], 'The air velocity in blast waves from t.n.t. explosions', Proceed-*ings of the Royal Society of London. Series A. Mathematical and Physical Sciences* **279**(1378), 366–385.
- [38] Dewey, J. M. [2005], 'The tnt equivalence of an optimum propane-oxygen mixture',
 Journal of Physics D: Applied Physics 38, 4245–4251.
- [39] Dewey, J. M. [2021], 'The TNT and ANFO equivalences of the Beirut explosion',
 Shock Waves **31**, 95–99.
- [40] Dobbs, N., Cohen, E. and Weissman, S. [1968], 'Blast pressures and impulse loads
 for use in the design and analysis of explosive storage and manufacturing facilities',
 Annals of the New York Academy of Sciences 152.1, 317–338.
- [41] Dobrilovic, M., Bohanek, V. and Skrlec, V. [2013], 'Influence of the initiation energy
 on the velocity of detonation of anfo explosive', *Central European Journal of Energetic Materials* 10, 555–568.
- [42] Edwards, T. Y. [1977], Proceedings of the dice throw symposium, Technical Report
 DNA 4377P-1, Defence Nuclear Agency, Santa Barbara, California, USA.
- [43] Esen, S., Souers, P. C. and Vitello, P. [2005], 'Prediction of the non-ideal detonation
 performance of commercial explosives using the dene and jwl++ codes', *International Journal for Numerical Methods in Engineering* 64, 1889–1914.
- [44] Esparza, E. D. [1986*a*], Airblast measurements and equivalency for spherical charges
 at small scaled distances, *in* '22nd Department of Defence Explosive Safety Seminar',
 Anaheim, California, USA, 26-28 August, pp. 2029–2057.

- ⁴⁷¹¹ [45] Esparza, E. D. [1986*b*], 'Blast measurements and equivalency for spherical charges at ⁴⁷¹² small scaled distances', *International Journal of Impact Engineering* **4**(1), 23–40.
- [46] Esparza, E. D. and Moroney, J. J. [1979], Reflected blast measurements at small scaled
 distances for m26e1 propellant, Technical Report Contractor Report ARLCD-CR79010, Southwest Research Institute, San Antonio, Texas.
- ⁴⁷¹⁶ [47] Fabin, M. and Jarosz, T. [2021], 'Improving ANFO: Effect of Additives and Ammo-⁴⁷¹⁷ nium NitrateMorphology on Detonation Parameters', *Mqterials* **14**(5745), 1–12.
- ⁴⁷¹⁸ [48] Fan, Z. [2009], Shock Waves Science and Technology Reference Library, Vol. 4, ⁴⁷¹⁹ Springer.
- [49] Farrimond, D. G., Rigby, S. E., Clarke, S. D. and Tyas, A. [2022], 'Time of arrival as a
 diagnostic for far-field high explosive blast waves', *International Journal of Protective Structures* pp. 1–24.
- [50] Farrimond, D. G., Woolford, S., Tyas, A., Rigby, S. E., Clarke, S. D., Barr, A.,
 Whittaker, M. and Pope, D. J. [2023], 'Far-field positive phase blast parameter characterisation of RDX and PETN based explosives', *International Journal of Protective*Structures pp. 1–38.
- ⁴⁷²⁷ [51] Fay, S., S. Clarke, J. A. W., Tyas, A., Bennett, T., Reay, J., Elgy, I. and Gant,
 ⁴⁷²⁸ M. [2013], Capturing the spatial and temporal variations in impulse from shallow
 ⁴⁷²⁹ buried charges, *in* '15th International Symposium on the Interaction of the Effects of
 ⁴⁷³⁰ Munitions with Structures (ISIEMS)', Potsdam, Germany, 17-20 September, pp. 1–9.
- ⁴⁷³¹ [52] Figuli, L., Kaviky, V., Jangl, S. and Ligasova, Z. [2014], Analysis of field test results
 ⁴⁷³² of ammonium nitrate fuel oil explosives as improvised explosive device charges, *in*⁴⁷³³ '13th International conference of Structures under shock and impact (SUSI XIII)',
 ⁴⁷³⁴ New Forest, UK, 3-5 June.
- ⁴⁷³⁵ [53] Fisher, E. M. [1950], Spherical Cast TNT Charges Air Blast Measurements, Technical
 ⁴⁷³⁶ Report NOLM-10780, Naval Ordnance Laboratory, White Oak, Maryland , USA.
- ⁴⁷³⁷ [54] Fisher, E. and Pittman, J. F. [1953], Air blast resulting from the detonation of small
 ⁴⁷³⁸ TNT charges, Technical Report NAVORD Report 2890, Naval Ordnance Laboratory,
 ⁴⁷³⁹ White Oak, Maryland, USA.
- ⁴⁷⁴⁰ [55] Forbes, J. W. [2013], Shock Wave Compression of Condensed Matter: A Primer ⁴⁷⁴¹ (Shock Wave and High Pressure Phenomena), Springer.

- ⁴⁷⁴² [56] Formby, S. A. and Wharton, R. K. [1996], 'Blast characteristics and TNT equiva⁴⁷⁴³ lence values for some commercial explosives detonated at ground level', *Journal of*⁴⁷⁴⁴ Hazardous Materials 50, 183–198.
- ⁴⁷⁴⁵ [57] Freidlander, F. G. [1946], 'The diffraction of sound pulses. I. Diffraction by a semi⁴⁷⁴⁶ infinite plate', *Proceedings of the Royal Society of London. Series A. Mathematical*⁴⁷⁴⁷ and Physical Sciences 186, 322–344.
- ⁴⁷⁴⁸ [58] Fried, L. E. [1994], Cheetah 1.0 users manual, Technical Report LLNL Report:
 ⁴⁷⁴⁹ UCRL-MA-117541, Lawrence Livermore National Laboratory, Livermore, CA, USA.
- [59] Gerasimov, S. I., Mikhailov, A. L. and A. Trepalov, N. [2017], 'Shock wave distribution
 in an explosion of an explosive material with plastic filler', *Combustion, Explosion*and Shock Waves 53, 689–695.
- [60] Gerasimov, S. I. and Trepalov, N. A. [2019], 'Video Recording of an Air Blast Wave
 Resulting from Initiation of a Light-Sensitive Explosive Composition', *Combustion*, *Explosion and Shock Waves* 55(5), 606–612.
- ⁴⁷⁵⁶ [61] Giglio-Tos, L. and Reisler, R. E. [1970], Air blast studies of large ammonium ni⁴⁷⁵⁷ trate/fuel oil explosions, Technical Report Memorandum No. 2057, Ballistic Re⁴⁷⁵⁸ search Laboratories, Aberdeen Proving Ground, Maryland, USA.
- [62] Gitterman, Y. and Hofstetter, R. [2012], 'Gt0 explosion sources for ims infrasound
 calibration: Charge design and yield estimation from near-source observations', *Pure*and Applied Geophysics 171(3-5), 599–619.
- [63] Glass, I. I. [1974], Shock Waves and Man, University of Toronto Institute of Aerospace
 Studies.
- ⁴⁷⁶⁴ [64] Goodman, H. J. [1960], Compiled free-air blast data on bare spherical pentolite, Tech⁴⁷⁶⁵ nical Report No. 1092, Ballistic Research Laboratories, Aberdeen Proving Ground,
 ⁴⁷⁶⁶ Maryland, USA.
- [65] Goodman, H. J. and Giglio-Tos, L. [1978], Equivalent weight factors for four plastic
 bonded explosives: PBX-108, PBX-109, AFX-103, and AFX-702, Technical Report
 ARBRL-TR-0205, Ballistic Research Laboratories, Aberdeen Proving Ground, Maryland, USA.

- [66] Granstrom, S. A. [1956], Loading characteristics of air blast from detonating charges,
 Technical Report No. 100, Transactions of the Royal Institute of Technology, Stockholm, Sweden.
- ⁴⁷⁷⁴ [67] Grisaro, H. Y. and Edri, I. E. [2017], 'Numerical investigation of explosive bare charge ⁴⁷⁷⁵ equivalent weight', *International Journal of Protective structures* **8**(2), 199–220.
- ⁴⁷⁷⁶ [68] Grisaro, H. Y., Edri, I. E. and Rigby, S. E. [2020], 'TNT equivalency analysis of
 ⁴⁷⁷⁷ specific impulse distribution from close-in detonation', *International Journal of Pro-*⁴⁷⁷⁸ tective structures 12(3), 315–330.
- ⁴⁷⁷⁹ [69] Groves, T. K. [1962], Surface burst 100-ton tnt hemispherical free field air blast
 ⁴⁷⁸⁰ overpressure, Technical Report No. 269, Defence Research Establishment Suffield,
 ⁴⁷⁸¹ Ralston, Alberta.
- [70] Hargather, M. J. and Settles, G. S. [2007], 'Optical measurement and scaling of blasts
 from gram-range explosive charges', *Shock Waves* 17(4), 215–223.
- ⁴⁷⁸⁴ [71] Hargather, M. J. and Settles, G. S. [2010], 'Natural-background-oriented schlieren
 ⁴⁷⁸⁵ imaging', *Experiments in Fluids* 48(1), 59–68.
- [72] Hobbs, M. J., Barr, A. D., Woolford, S., Farrimond, D. G., Clarke, S. D., Tyas,
 A. and Willmott, J. R. [2022], 'High-Speed Infrared Radiation Thermometer for the
 Investigation of Early Stage Explosive Development and Fireball Expansion', *Sensors*22(6143).
- [73] Hoffman, A. J. and Mills, S. N. [1956], Air blast measurements about explosive charges
 at side-on and normal incidence, Technical Report 988, Ballistic Research Laboratories, Aberdeen Proving Ground, Maryland, USA.
- ⁴⁷⁹³ [74] Hopkinson, B. [1915], British ordnance board minutes, 13565 edn, The National ⁴⁷⁹⁴ Archives, Kew, UK.
- ⁴⁷⁹⁵ [75] Horie, Y. [2009], Shock Waves Science and Technology Reference Library, Vol. 3,
 ⁴⁷⁹⁶ Springer.
- ⁴⁷⁹⁷ [76] Hyde, D. W. [1988], 'Users' Guide for Microcomputer Programs CONWEP and FUN⁴⁷⁹⁸ PRO Applications of TM5-885-1'. US Army Waterways Experimental Station,
 ⁴⁷⁹⁹ Vicksburg, MS, USA.
- ⁴⁸⁰⁰ [77] Hyde, D. W. [1991], 'Conventional weapons program (ConWep)'. US Army Water⁴⁸⁰¹ ways Experimental Station, Vicksburg, MS, USA.

- [78] Igra, O. and Seiler, F. [2016], Experimental methods of shock wave research, Springer
 International Publishing, Switzerland.
- ⁴⁸⁰⁴ [79] Institute for Economics and Peace [2022], 'The 2022 global terroism index'.
- [80] Jackson, S. I. and Short, M. [2015], 'Scaling of detonation velocity in cylinder and slab
 geometries for ideal, insensitive and non-ideal explosives', *Journal of Fluid Mechanics*773, 224–266.
- [81] Jeremc, R. and Bajic, Z. [2006], 'An approach to determining the TNT equivalent of
 high explosives', Scientific Technical Review LVI(1), 58–61.
- [82] Johansson, L. [2011], Numerical Study of Non-Ideal Explosive Detonations, PhD
 thesis, Lulea University of Technologu.
- [83] Johnson, O. T., Patterson, J. D. and Olson, W. C. [1957], A simple mechanical
 method for measuring the reflected impulse of air blast waves, Technical Report Memorandum no.1088, Ballistic Research Laboratories, Aberdeen Proving Ground,
 Maryland, USA.
- [84] Jouguet, E. [1905], 'On the propagation of chemical reactions in gases', Journal de
 Mathématiques Pures et Appliquées 6(2), 5–85.
- [85] Kennedy, W. D. [1946], Explosions and explosives in air, *in* 'Effects of Impact and
 Explosions. Summary Technical Report of Div. 2, NDRC, Vol.1, Washington, DC,
 AD 221 586'.
- [86] Kingery, C. N. [1966], Air blast parameters versus distance for hemispherical tht
 surface bursts, Technical Report 1344, Ballistic Research Laboratories, Aberdeen
 Proving Ground, Maryland, USA.
- [87] Kingery, C. N. and Bulmash, G. [1984], Airblast parameters from TNT spherical air
 ⁴⁸²⁵ burst and hemispherical surface burst, Technical Report ARBRL-TR-02555, Ballistic
 ⁴⁸²⁶ Research Laboratory, Aberdeen Proving Ground, Maryland, USA.
- [88] Kingery, C. N. and Coulter, G. [1982], Tht equivalency of pentolite hemispheres, Tech nical Report ARBRL-TR-02456, Ballistic Research Laboratories, Aberdeen Proving
 Ground, Maryland, USA.
- [89] Kingery, C. N. and Pannill, B. F. [1964], Peak overpressure vs scaled distance for tht
 surface bursts (hemispherical charges), Technical Report Memorandum No. 1518,
 Ballistic Research Laboratories, Aberdeen Proving Ground, Maryland, USA.

- ⁴⁸³³ [90] Kinney, G. F. and Graham, K. J. [1985], *Explosive Shocks in Air*, Springer-Verlag
 ⁴⁸³⁴ Berlin Heidelberg.
- [91] Kolhe, P. S. and Agrawal, A. K. [2009], 'Abel inversion of deflectometric data: comparison of accuracy and noise propagation of existing techniques', *Applied Optics*4837 48(20), 3894–3902.
- ⁴⁸³⁸ [92] Konya, A. and Konya, C. J. [2019], 'Blasting mechanics revisited: Characteristics of explosives', https://www.pitandquarry.com/blasting-mechanics-revisited ⁴⁸⁴⁰ characteristics-of-explosives.
- ⁴⁸⁴¹ [93] Kucera, J., Anastacio, A. C., Selesovsky, J. and Pachman, J. [2017], Testing optical
 ⁴⁸⁴² tracking of blast wave position for determination of its overpressure, *in* '6th Inter⁴⁸⁴³ national Conference on Military Technologies (ICMT)', Brno, Czech Republic, 31st
 ⁴⁸⁴⁴ May 2nd June, pp. 70–73.
- ⁴⁸⁴⁵ [94] Lozano, E. [2020], Reactive Burn Modelling of Non-Ideal Explosives, PhD thesis,
 ⁴⁸⁴⁶ Colorado School of Mines.
- ⁴⁸⁴⁷ [95] Lutzky, M. [1965], Theoretical Versus Experimental Results for Air Blast From One⁴⁸⁴⁸ Pound Spherical TNT and Pentolite Charges at Sea Level Conditions, Technical
 ⁴⁸⁴⁹ Report NOTLR 65-57, Naval Ordnance Laboratory, White Oak, Maryland , USA.
- ⁴⁸⁵⁰ [96] Lyons, S. [2012], Characterisation of Blast Wave Variability, PhD thesis, The Uni⁴⁸⁵¹ versity of Newcastle, Australia.
- [97] Maranda, A., Paplinksi, A. and Galezwski, D. [2010], 'Investigation on detonation
 and thermochemical parameters of aluminized ANFO', *Journal of Energetic Materials*21, 1–13.
- [98] Matyas, R., Zeman, S., Trzcinski, W. and Cuziloi, S. [2008], 'Detonation performance
 of tatp/an-based explosives', *Propellants, Explosives and Pyrotechnics* 33(4), 296–
 300.
- ⁴⁸⁵⁸ [99] McKay, M. W., Hancock, S. L. and Randall, D. [1974], 'Development of a low-density
 ⁴⁸⁵⁹ ammonium nitrate/fuel oil explosive and modelling of its detonation properties', *Tech-*⁴⁸⁶⁰ nical Report DNA 3351 F. Physics Internation Company, San Leandro, California.
- ⁴⁸⁶¹ [100] Meshkov, E. E. [1969], 'Instability of the interface of two gases accelerated by a ⁴⁸⁶² shock wave', *Fluid Dynamics* 4(5), 101–104.

- [101] Meyer, R., Kohler, J. and Homburg, A. [2011], Explosives Sixth, Completely Revised
 Editions, Wiley VCH Verlahshesellschaft, Weinheim, Germany.
- [102] Mi, X., Michael, L., Loannou, E., Nikiforakis, N., Higgins, A. J. and Ng, H. D.
 [2019], 'Meso-resolved simulations of shock-to-detonation transition in nitromethane
 with air-filled cavities', *Journal of Applied Physics* 125, 1–22. 245901.
- ⁴⁸⁶⁸ [103] Mizukaki, T., Wakabayashi, K., Matsumura, T. and Nakayama, K. [2014],
 ⁴⁸⁶⁹ 'Background-oriented schlieren with natural background for quantitative visualiza⁴⁸⁷⁰ tion of open-air explosions', *Shock Waves* 24(1), 69–78.
- ⁴⁸⁷¹ [104] Murphy, M. J. and Adrian, R. J. [2010], 'PIV space-time resolution of flow behind ⁴⁸⁷² blast waves', *Experiments in Fluids* **49**, 193–202.
- [105] National Academies of Sciences, E. and Medicine [2018], Reducing the Threat of
 Improvised Explosive Device Attacks by Restricting Access to Explosive Precursor
 Chemicals, Washington, DC: The National Academies Press.
- ⁴⁸⁷⁶ [106] Needham, C., Brisby, J. and Ortley, D. [2020], 'Blast wave modification by detonator ⁴⁸⁷⁷ placement', *Shock Waves* **30**, 615–627.
- ⁴⁸⁷⁸ [107] Needham, C. E. [2010], *Blast Waves*, Springer Germany, Berlin.
- [108] Ohashi, K., H.Kleine and Takayama, K. [2001], Characteristics of blast waves generated by milligram charges, *in* '23rd International Symposium on Shock Waves', Fort
 Worth, USA, 22-27 July, pp. 187–193.
- [109] Pannell, J. J., Panoutsos, G., Cooke, S. B., Pope, D. J. and Rigby, S. E. [2021], 'Predicting specific impulse distributions for spherical explosives in the extreme near-field
 using a Gaussian function', *International Journal of Protective Structures* 12(4), 437–
 459.
- [110] Pasman, H. J., Fouchier, C., Park, S., Quddus, N. and Laboureur, D. [2020], 'Beirut
 ammonium nitrate explosion: Are not we really learning anything?', *Process Safety Progress* e12203, 1–18.
- [111] Paterson, S. [1995], 'The structure of the reaction zone in a detonating explosive',
 Symposium on Combustion 5(1), 672–684.
- [112] Petes, J., Miller, R. and McMullan, F. [1983], 'User's guide and history of anfo as
 a nuclear weapons effect simulation explosive', *Technical Report DNA-TR-82-156*.
 Kaman Tempo, Alexandria, Virginia.

- ⁴⁸⁹⁴ [113] Popper, K. R. [1963], Science as Falsification Conjectures and Refutations, Routledge and Keagan Paul.
- [114] Price, D. [1967], 'Contrasting patterns in the behavior of high explosives', Symposium
 (International) on Combustion 11, 693–702.
- [115] Rae, P. J. and McAfee, J. M. [2018], 'The Blast Parameters Spanning the Fireball
 from Large Hemispherical Detonations of C-4', *Propellants, Explosives, Pyrotechnics* **43**(7), 694–702.
- ⁴⁹⁰¹ [116] Randers-Pehrsons, G. and Bannister, K. A. [1997], 'Airblast loading model for
 ⁴⁹⁰² DYNA 2D and DYNA 2D', *Technical Report ARL-TR-1310*. Aberdeen Proving
 ⁴⁹⁰³ Ground, MD, USA.
- [117] Rayleigh [1882], 'Investigation of the character of the equilibrium of an incompressible heavy fluid of variable density', *Proceedings of the London Mathematical Society*s1-14(1), 170-177.
- [118] Reisler, R. E., Keefer, J. H. and Ethridge, N. H. [1995*a*], Measurement techniques
 and instrumentation: Volume 1 nuclear era (1945-1963), Technical report, Applied
 Research Associates Inc., Albuquerque, New Mexico.
- [119] Reisler, R. E., Keefer, J. H. and Ethridge, N. H. [1995b], Measurement techniques
 and instrumentation: Volume 2 the high explosives era (1959-1993), Technical report, Applied Research Associates Inc., Albuquerque, New Mexico.
- [120] Reisler, R. E., Keefer, J. H. and Giglio-Tos, L. [1966], Basic air blast measurements
 froma 500-ton tnt detonation: Project 1.1 operation snowball, Technical Report Memorandum No. 1818, Ballistic Research Laboratories, Aberdeen Proving Ground,
 Maryland, USA.
- [121] Reisler, R., Pettit, B. and Kennedy, L. [1976], Air blast data from height-of-burst
 studies in canada, vol 1: Hob 5.4 to 71.9 feet, Technical Report 1950, Ballistic Research Laboratories, Aberdeen Proving Ground, Maryland, USA.
- [122] Reisler, R., Pettit, B. and Kennedy, L. [1977], Air blast data from height-of-burst
 studies in canada, vol 1: Hob 45.4 to 144.5 feet, Technical Report 1990, Ballistic
 Research Laboratories Report 1990, Aberdeen Proving Ground, Maryland, USA.

- [123] Remennikov, A. M. [2003], 'A REVIEW OF METHODS FOR PREDICTING
 BOMB BLAST EFFECTS ON BUILDINGS', Journal of Battlefield Technology
 6(3), 1–6.
- ⁴⁹²⁶ [124] Richtmyer, R. D. [1960], 'Taylor instability in shock acceleration of compressible ⁴⁹²⁷ fluids', *Communications on Pure and Applied Mathematics* **13**(2), 297–319.
- [125] Rickman, D. D. and Murrell, D. W. [2007], 'Development of an improved methodology for predicting Airblast pressure relief on a directly loaded wall', *Journal of Pressure Vessel Technology, Transactions of the ASME* 129(1), 195–204.
- ⁴⁹³¹ [126] Rigby, S. [2014], Blast Wave Clearing Effects on Finite-Sized Targets Subjected to
 ⁴⁹³² Explosive Loads, PhD thesis, University of Sheffield, UK.
- [127] Rigby, S. E. [2021], Blast wave time of arrival : A reliable metric to determine
 pressure and yield of high explosive detonations, Technical Report 079, Fire and
 Blast Information Group.
- [128] Rigby, S. E., Fay, S. D., Tyas, A., Warren, J. and Clarke, S. D. [2015a], 'Angle of incidence effects on far-field positive and negative phase blast parameters', *International Journal of Protective Structures* 6(1), 23–42.
- [129] Rigby, S. E. and Gitterman, Y. [2016a], Secondary shock delay measurements from
 explosive trials, *in* '24th International Symposium on Military Aspects of Blast and
 Shock (MABS)', Halifax, Nova Scotia, Canada, 18-23 September.
- [130] Rigby, S. E., Knighton, R., Clarke, S. D. and Tyas, A. [2020a], 'Reflected Nearfield Blast Pressure Measurements Using High Speed Video', *Experimental Mechanics* **60**(7), 875–888.
- [131] Rigby, S. E., Lodge, T. J., Alotaibi, S., Barr, A. D., Clarke, S. D., Langdon, G. S.
 and Tyas, A. [2020b], 'Preliminary yield estimation of the 2020 Beirut explosion using
 video footage from social media', *Shock Waves* **30**(6), 671–675.
- ⁴⁹⁴⁸ [132] Rigby, S. E. and Sielicki, P. W. [2014], 'An investigation of TNT equivalence of ⁴⁹⁴⁹ hemispherical PE4 charges', *Engineering Transactions* **62**(4), 423–435.
- [133] Rigby, S. E., Tyas, A., Bennett, T., Clarke, S. D. and Fay, S. D. [2014b], 'The
 Negative Phase of the Blast Load', *International Journal of Protective Structures*5(1), 1–20.

- [134] Rigby, S. E., Tyas, A., Clarke, S. D., Fay, S. D., Reay, J. J., Warren, J. A., Gant,
 M. and Elgy, I. [2015b], 'Observations from Preliminary Experiments on Spatial and
 Temporal Pressure Measurements from Near-Field Free Air Explosions', *International Journal of Protective structures* 6(2), 175–190.
- [135] Rigby, S. E., Tyas, A., Fay, S. D., Clarke, S. D. and Warren, J. A. [2014a], Validation
 of Semi-Empirical Blast Pressure Predictions for Far Field Explosions Is There
 Inherent Variability in Blast Wave Parameters?, *in* '6th International Conference on
 Protection of Structures Against Hazards', Tianjin, China, 16-17 October, pp. 1–9.
- [136] Robbe, C., Nsiampa, N., Oukara, A. and Papy, A. [2014], 'Quantification of the
 uncertainties of high-speed camera measurements', *International Journal of Metrology*and Quality Engineering 5, 201–209.
- [137] Rudlin, L. [1963], On the origin of shockwaves from spherical condensed explosions
 in air part 1: Results of photographic observations of pentolite hemispheres at
 ambient conditions, Technical Report NOTLR 62-182, Naval Ordnance Laboratory,
 White Oak, Maryland , USA.
- [138] Sadwin, L. D. and Swisdak, M. M. [1970*a*], 'An/fo charge preparation for large scale
 tests', *Technical Report NOLTR 70-205*. United States Naval Ordnance Laboratory,
 White Oak, Maryland.
- ⁴⁹⁷¹ [139] Sadwin, L. D. and Swisdak, M. M. [1970b], 'Blast characteristics of 20 and 100
 ⁴⁹⁷² ton hemispherical an/fo charges, nol data report', *Technical Report NOLTR 70-32*.
 ⁴⁹⁷³ United States Naval Ordnance Laboratory, White Oak, Maryland.
- ⁴⁹⁷⁴ [140] Salyer, T. R., Short, M., Kiyanda, C. B., Morris, J. and Zimmerly, T. [2010], Ef⁴⁹⁷⁵ fects of Prill Structure on Detonation Performance of ANFO, *in* '14th International
 ⁴⁹⁷⁶ Detonation Symposium', Coeru D'Alene, Idaho, 11-16 April.
- [141] Schwer, L. and Rigby, S. E. [2017], Reflected Secondary Shocks: Some Observations
 using Afterburning, *in* '11th European LS-Dyna Conference 2017', Salzburg, Austria.
- ⁴⁹⁷⁹ [142] Scott, D. G. [2019], Small-Scale Characterization of Shock Sensitivity for Various
 ⁴⁹⁸⁰ Non-ideal Explosives Based on Detonation Failure and Behaviour, PhD thesis, Purdue
 ⁴⁹⁸¹ University, Indiana.
- [143] Shear, R. E. and Day, B. D. [1959], Tables of thermodynamic and shock front parameters for air., Technical Report Memorandum Report 1206, Ballistic Research
 Laboratories, Aberdeen Proving Ground, Maryland, USA.

201

- [144] Shear, R. E. and Wright, E. Q. [1962], 'Calculated peak pressure-distance curves
 for pentolite and tnt', *Ballistic Research Laboratories Memorandum Report 1423*.
 Aberdeen Proving Ground, Maryland, USA.
- ⁴⁹⁸⁸ [145] Shelton, F. H. [1988], *Reflections of a Nuclear Weaponeer*, Shelton Enterprises.
- [146] Sherkar, P., Shin, J., Whittaker, A. and Aref, A. [2016], 'Influence of Charge Shape
 and Point of Detonation on Blast-Resistant Design', *Journal of Structural Engineering*142, 1–11.
- [147] Shi, Y., Wang, N., Cui, J., Li, C. and Zhang, X. [2022], 'Experimental and numerical
 investigation of charge shape effect on blast load induced by near-field explosions', *Process Safety and Environmental Protection* 165, 266–277.
- ⁴⁹⁹⁵ [148] Shin, J., Whittaker, A. and Aref, A. [2019], 'Influence of Charge Shape and Point of ⁴⁹⁹⁶ Detonation on Blast-Resistant Design', *Journal of Structural Engineering* **145**, 1–15.
- [149] Shin, J., Whittaker, A. S. and Comie, D. [2015], 'TNT Equivalency for Overpressure
 and Impulse for Detonations of Spherical Charges of High Explosives', International
 Journal of Protective Structures 6, 567–579.
- [150] Shin, J., Whittaker, A. S. and Comie, D. [2015b], 'Incident and Normally Reflected
 Overpressure and Impulse for Detonations of Spherical High Explosives in Free Air',
 International Journal of Protective Structures 141(12), 567–579.
- [151] Shirbhate, P. A. and Goel, M. D. [2021], 'A Critical Review of TNT Equivalence
 Factors for Various Explosives', *Recent Advances in Computational Mechanics and Simulations* 103, 471–478.
- [152] Simoens, B. and Lefebvre, M. [2011], 'Influence of different parameters on the tnt equivalent of an explosion', *Central European Journal of Energetic Materials* 8(1), 53–
 67.
- [153] Simoens, B. and Lefebvre, M. [2015], 'Influence of the shape of an explosive charge:
 Quantification of the modification of the pressure field', *Central European Journal of Energetic Materials* 12(2), 195–213.
- [154] Sitkiewicz-Wolodko, R., Maranda, A. and Paszula, J. M. [2019], 'Modification of anfo
 detonation parameters by addition of ground of ammonium nitrate (v) and aluminium
 powder', Central European Journal of Energetic Materials 16(1), 122–134.

- [155] Smale, W. R. and Sigs, R. C. [1961], Surface burst of 100 ton the hemispherical
 charge, Technical Report No. 205, Defence Research Establishment Suffield, Ralston,
 Alberta.
- [156] Smith, P. D., Rose, T. A. and Saotonglang, E. [1999], 'Clearing of blast waves from
 building facades', *Proceedings of the Institution of Civil Engineers: Structures and*Buildings 134(2), 193–199.
- [157] Sochet, I., Gardebas, D., Calderara, S., Marchal, Y. and Longuet, B. [2011], 'Blast
 Wave Parameters for Spherical Explosives Detonation in Free Air', Open Journal of
 Safety Science and Technology 1, 31–42.
- [158] Stennett, C., Gaulter, S. and Akhavan, J. [2020], 'An Estimate of the TNTEquivalent Net Explosive Quantity (NEQ) of the Beirut Port Explosion Using
 Publicly-Available Tools and Data', *Propelants, Explosives, Pyrotechnics* 45, 1675–
 1679.
- [159] Stimac, B., Skrelec, V., Dobrilovic, M. and Suceska, M. [2021], 'Numerical modelling
 of non-ideal detonation in anfo explosives applying wood-kirkwood theory coupled
 with explo5 thermochemical code', *Defence Technology* 17, 1740–1752.
- ⁵⁰³¹ [160] Stoner, R. G. and Bleakney, W. [1948], 'The attenuation of spherical shock waves ⁵⁰³² in air', *Journal of Applied Physics* **19**, 670.
- ⁵⁰³³ [161] Suceska, M. [2018], Explo5 user's guide, Technical report, OZM Research S.R.O.,
 ⁵⁰³⁴ Hrochův Týnec , Czechia.
- ⁵⁰³⁵ [162] Sultanoff, M. and McVey, G. [1954], Shock pressure at and close to the surface of
 ⁵⁰³⁶ spherical pentolite charges inferred from optical measurement., Technical Report 917,
 ⁵⁰³⁷ Ballistic Research Laboratories, Aberdeen Proving Ground, Maryland, USA.
- [163] Swisdak, M. [1975], Explosion effects and properties. Part 1: Explosion effects in
 Air, Technical Report NSWC/WOL/TR-65-116, Naval Ordnance Laboratory, White
 Oak, Maryland , USA.
- [164] Tang, L., Bird, D., Rigby, S. E., Tyas, A. and Warren, J. [2017], Reflections on Variability of Blast Pressure Measurement at Different Scales, *in* '17th international symposium on the interaction of the effects of munitions with structures', Bad NeuenahrAhrweiler, Germany, 16-20 October.

- ⁵⁰⁴⁵ [165] Tang, L., Rigby, S. E. and Tyas, A. [2018], Validation of Air3D for scaled experimen⁵⁰⁴⁶ tal pressure and impulse data, *in* '25th International Symposium on Military Aspects
 ⁵⁰⁴⁷ of Blast and Shock (MABS)', The Hague, Netherlands, 24-27 September.
- [166] Tarver, C. M. and Urtiew, P. A. [1997], Theoretical and computer models of detonation in solid explosives, Technical Report LLNL Report: UCRL-JC-128755,
 Lawrence Livermore National Laboratory, Livermore, CA, USA.
- [167] Taylor, G. I. [1950a], 'The formation of a blast wave by a very intense explosion
 I. Theoretical discussion.', Proceedings of the Royal Society of London. Series A.
 Mathematical and Physical Science 201, 159–174.
- [168] Taylor, G. I. [1950b], 'The formation of a blast wave by a very intense explosion II.
 The atomic explosion of 1945', Proceedings of the Royal Society of London. Series A.
 Mathematical and Physical Science 201, 175–186.
- ⁵⁰⁵⁷ [169] Taylor, G. I. [1950c], 'The dynamics of the combustion products behind plane and
 ⁵⁰⁵⁸ spherical detonation fronts in explosives', *Proceedings of the Royal Society of London*.
 ⁵⁰⁵⁹ Series A. Mathematical and Physical Science **200**, 235–247.
- [170] Taylor, G. I. [1950d], 'The instability of liquid surfaces when accelerated in a di rection perpendicular to their planes. I', Proceedings of the Royal Society of London.
 Series A. Mathematical and Physical Sciences 202(1068), 81–96.
- [171] Thiboutot, S., Brousseau, P. and Ampleman, G. [2015], 'Deposition of petn fol lowing the detonation of seismoplast plastic explosive', *Propellants, Explosives and Pyrotechnics* 40, 329–332.
- [172] Tobin, J. D. and Hargather, M. J. [2016], 'Quantitative Schlieren Measurement of
 Explosively-Driven Shock Wave Density, Temperature, and Pressure Profiles', Pro *pelants, Explosives, Pyrotechnics* 41, 1050–1059.
- ⁵⁰⁶⁹ [173] Tyas, A. [2019], Blast loading from high explosive detonation: What we know and
 ⁵⁰⁷⁰ don't know, *in* '13th International Conference on Shock and Impact Loads on Struc⁵⁰⁷¹ tures (SILOS)', Guangzhou, China, 14-15 December, pp. 65–76.
- ⁵⁰⁷² [174] Tyas, A., Reay, J. J., Fay, S. D., Clarke, S. D., Rigby, S. E., Warren, J. A. and
 ⁵⁰⁷³ Pope, D. J. [2016], 'Experimental studies of the effect of rapid afterburn on shock
 ⁵⁰⁷⁴ development of near-field explosions', *International Journal of Protective Structures*⁵⁰⁷⁵ 7(3), 452–465.

- ⁵⁰⁷⁶ [175] Tyas, A., Warren, J. A., Bennett, T. and Fay, S. [2011], 'Prediction of clearing effects ⁵⁰⁷⁷ in far-field blast loading of finite targets', *Shock Waves* **21**(2), 111–119.
- [176] US Department of Defence [2008], 'Structures To Resist the Effects of Accidental
 Explosions'. UFC 3-340-02. US DoD, Washington, DC.
- [177] von Neumann, J. [1942], Theory of detonation waves, Technical report, Institute
 for Advanced Study. Nation Defence Research Committee of the office of Scientific
 Research and Development.
- [178] Weibull, W. [1950], Explosion of spherical charges in air: Travel time, velocity of
 front, and duration of shock waves, Technical Report X-127, Ballistic Research Lab oratories Report, Aberdeen Proving Ground, Maryland, USA.
- [179] Whittaker, M. J., Klomfass, A., Softley, I. D., Pope, D. J. and Tyas, A. [2018],
 Comparison of Numerical Analysis with Output from Precision Diagnostics during
 Near-Field Blast Evaluation, *in* '25th International Symposium on Military Aspects
 of Blast and Shock (MABS)', The Hague, Netherlands, 24-27 September.
- [180] Wu, C., Fattori, G., Whittaker, A. and Oehlers, D. J. [2010], 'Investigation of Air Blast Effects from Spherical-and Cylindrical-Shaped Charges ', International Journal
 of Protective Structures 1(3), 345–362.
- [181] Xiao, W., Andrae, M. and Gebbeken, N. [2020], 'Effect of Charge Shape and Initia tion Configuration of Explosive Cylinders Detonating in Free Air on Blast-Resistant
 Design', Journal of Structural Engineering 146, 1–13.
- [182] Zukas, J. A. and Walters, W. [1998], Explosive Effects and Applications Shock
 Wave and High Pressure Phenomena, Springer-Verlag, New York.
- [183] Zygmunt, B. and Buczkowski, D. [2007], 'Influence of ammonium nitrate prills
 properties on detonation velocity of anfo', *Propellants, Explosives and Pyrotechnics* **32**(5), 411–414.