Using Genetic Programming to Learn Predictive Models from Spatio-Temporal Data

by

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Abstract

This thesis describes a novel technique for learning predictive models from non-deterministic spatio-temporal data. The prediction models are represented as a production system, which requires two parts: a set of production rules, and a conflict resolver. The production rules model different, typically independent, aspects of the spatio-temporal data. The conflict resolver is used to decide which sub-set of enabled production rules should be fired to produce a prediction. The conflict resolver in this thesis can probabilistically decide which set of production rules to fire, and allows the system to predict in non-deterministic situations. The predictive models are learnt by a novel technique called Spatio-Temporal Genetic Programming (STGP). STGP has been compared against the following methods: an Inductive Logic Programming system (Progol), Stochastic Logic Programs, Neural Networks, Bayesian Networks and C4.5, on learning the rules of card games, and predicting a person’s course through a network of CCTV cameras.

This thesis also describes the incorporation of qualitative temporal relations within these methods. Allen’s intervals [1], plus a set of four novel temporal state relations, which relate temporal intervals to the current time are used. The methods are evaluated on the card game Uno, and predicting a person’s course through a network of CCTV cameras. This work is then extended to allow the methods to use qualitative spatial relations. The methods are evaluated on predicting a person’s course through a network of CCTV cameras, aircraft turnarounds, and the game of Tic Tac Toe.

Finally, an adaptive bloat control method is shown. This looks at adapting the amount of bloat control used during a run of STGP, based on the ratio of the fitness of the current best predictive model to the initial fitness of the best predictive model.
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Declarations

Some parts of the work presented in this thesis have been published in the following articles:


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Chapter 1

Introduction

1.1 The problem domain

This thesis investigates learning predictive models from non-deterministic spatio-temporal data. Predictive models can be used to predict future spatio-temporal data; or to recognise events or activities from past or current observations. The research in this thesis fits into the wider research area of behaviour modelling of multiple objects. Behaviour modelling can be applied to a wide variety of domains including: city centres, airports, stations, motorway networks, office buildings, homes, and hospitals. Figure 1.1 shows two of these domains: a city centre and a motorway network. Typical applications of behaviour modelling in a motorway network include: predicting traffic flow; recognising road accidents; and detecting traffic offences. Typical applications of behaviour modelling in a city centre include: recognising fights, predicting the flow of people through the streets; and recognising theft.

Behaviour modelling is a complex and only partially solved problem for a number of reasons: Firstly, there are multiple interacting objects in the domains, which create complex datasets to predict, and learn from. For example, in the city centre domain multiple people in the scene might affect the temporal order of information referring to each person (which may be difficult to identify as individuals over time), and a model using this information needs to be able to cope with this variation. Secondly, the objects behave in a non-deterministic manner. For example, in the motorway domain at a road
Advances in this research area will help to improve systems that automatically monitor these domains. These systems could be improved in the following ways. Firstly, they could predict or recognise the actions of multiple objects more accurately, for example at a station where there are large numbers of interacting people. Secondly, they could predict or recognise over an extended period of time, or recognise events; for example the junction a car might take could be based on the route it took over the last 200 miles. Finally, they could use more complex probabilistic models to more accurately recognise, or predict from non-deterministic data. For example, in the last example, the likelihood of the car taking the junction would need to be computed based on the likelihood of it taking specific junctions at each point on its journey, which in practice is a complex conditional probability distribution. The work in this thesis aims to contribute to these three areas.

1.2 A system to model and learn object behaviour

Figure 1.2 shows the four main components required for a system to learn and predict or recognise the behaviour of objects: data generation; data representation; model learning; and recognition or prediction.

1.2.1 Data generation and representation

To acquire data on objects requires identifying the locations of objects of interest over the entire domain. There are two main approaches to identifying the locations of objects in
domains covering a wide area. One approach is to use a network of cameras, where each object is tracked individually over the cameras. Tracking algorithms come from the field of Computer Vision [119]. They analyse the video produced by the cameras frame by frame to locate and track objects. There are many problems with this approach: cameras can be expensive to buy and maintain; the tracking algorithms are not always reliable; and it can be hard to place cameras to cover every part of the domain, due to ethical or legal issues. An alternative approach is to use a network of sensors. Each sensor outputs when it detects movement or some other factor has occurred along with the length of time it has happened. There are a number of benefits of sensors over using cameras: they are cheap; they are reliable; and they can be placed in almost every part of the domain. The downside is that, unlike using cameras combined with a tracking algorithm, the output is just a set of movement states, and the system might not know which object has caused them. This is known as the data association problem [32]. In the motorway network and city centre domains it is expensive to place cameras over the entire space. Cameras are also affected by the weather, and the tracking algorithms will fail to track people and cars when they become occluded by other objects. Placing movement sensors under the road or pavement can be cheaper; can be more reliable for tracking occluded people and cars; and are less affected by the weather.

Once a set of object data has been identified it needs to be described in an appropriate representation. A representation needs to both describe the properties of each of the objects, and relations (i.e. spatial or temporal) between the objects. The representation chosen must represent the data accurately, and must be easy to learn a model from.
1.2.2 Model learning and prediction

A model contains a set of components which each perform a specific task to aid the model when it is making a prediction, or recognising an event. A learning algorithm then attempts to find the best representation for the components in the model and the values for its parameters, such that it best predicts from, or recognises a set of data. Once the model has been learnt it can then be used to predict, or recognise unseen data.

This thesis investigates how predictive models can be learnt from non-deterministic spatio-temporal data, and what is the best representation for their components. This thesis represents predictive models using a production system. This contains a set of production rules represented in first order logic, and a conflict resolver to decide which production rules to use when multiple production rules make a prediction. The production rules contain a condition section that represents a pattern to find in the spatio-temporal data, and the action section represents a prediction or event to recognise. In this context, this thesis attempts to investigate the following questions:

1. Does representing the components of the predictive models using first order logic, produce more accurate results on non-deterministic spatio-temporal data than using standard machine learning representations?

2. Does using a probabilistic conflict resolver produce more accurate predictive models on non-deterministic spatio-temporal data than other conflict resolution approaches?

3. Does using evolutionary search techniques to learn production rules produce more accurate results on non-deterministic spatio-temporal data than using a deterministic (greedy) search?

4. Does learning the production rules and the parameters of the conflict resolver simultaneously produce more accurate results on non-deterministic spatio-temporal data than learning them sequentially?

5. Does use of qualitative temporal relations within the components of the predictive models make them robust to changes in the temporal structure of the non-deterministic spatio-temporal data?

6. Does use of qualitative spatial relations within the components of the predictive models make them robust to changes in the spatial structure of the non-deterministic spatio-temporal data?
1.3 Thesis overview

The structure of this thesis is as follows:

- Chapter 2 is a literature review of the following subjects: spatio-temporal data acquisition, and representation; and spatio-temporal predictive model learning.

- Chapter 3 firstly describes how spatio-temporal data is represented. Secondly, an architecture of the novel spatio-temporal modelling scheme is described. Finally, a method to evaluate predictive models on the spatio-temporal data is described.

- Chapter 4 describes how predictive models are learnt using a novel Genetic Programming based technique called Spatio-Temporal Genetic Programming (STGP). Techniques to build the initial population of predictive models, the fitness function, and the genetic operators are described. The system is evaluated against standard machine learning algorithms, and the Inductive Logic Programming system; Progol. Experiments are done using deterministic, and non-deterministic datasets with varying amounts of noise. Finally, experimentation with the different parameters for STGP is presented.

- Chapter 5 describes an approach for incorporating temporal relations into predictive models. A set of novel temporal relations to relate the time range of an object to the current prediction time is described. This is tested on a handcrafted game of Uno, and real-world CCTV datasets. A comparison with predictive models using, and not using, the temporal relations is given. The system is then compared against the alternative methods from the previous chapter. Finally, experimentation with some of the parameters of STGP is presented.

- Chapter 6 describes an approach for incorporating spatial relations along with the temporal relations from Chapter 5 into predictive models. This is evaluated using a real-world CCTV dataset, the game of Tic Tac Toe, and recognising events from an aircraft apron. A comparison is presented comparing predictive models containing, and not containing spatial relations. Again, a comparison is performed with the alternative methods from Chapter 4, along with experimentation with some of the parameters for STGP.

- Chapter 7 describes a method to automatically vary the amount of bloat (downward pressure on the size of the predictive models) using the Tarpeian method [22] during a run of STGP. Experiments and results using the datasets from the previous chapters is given.
• Chapter 8 summarises the conclusions of the thesis, investigates how well the thesis has answered the raised shown in the previous section of this chapter, and proposes potentially fruitful further directions for this research.
Chapter 2

Background

2.1 Introduction

This thesis investigates the learning of predictive models from non-deterministic spatio-temporal data. In this thesis the spatio-temporal data is typically generated from video. Once a predictive model has been learnt it can then be used to predict future spatio-temporal data, or recognise a particular event from past spatio-temporal data. An example will now be introduced that will be used to explain in more detail how predictive models are learnt, and how this relates to the rest of this chapter. The example will be used throughout this chapter to explain the different techniques and methods. A video has been taken of a set of people walking along a path. The path contains a junction where a person can take either the right or left fork. Figure 2.1 shows a set of frames taken from the video.

Figure 2.1: A set of frames from a video of a person walking along a path.
To learn a predictive model from this video requires four stages (Figure 2.2). Firstly, a set of spatio-temporal data has to be generated from the video. This is performed by identifying objects in the scene, in this case the people and the path; and then extracting properties on the objects for example their: speed; colour; and relationships between the other objects. Secondly, the spatio-temporal data must be stored within the computer. This requires an appropriate representation that should both: describe the spatio-temporal data accurately; and be suitable for use with a predictive model. Thirdly, once a set of spatio-temporal data has been generated it can be used to induce or learn a predictive model. A predictive model contains a set of components [111] that aid the predictive model when it is making a prediction or recognising an event, for example there might be one component to predict the person will take the left fork, and another component to predict the person will take the right fork. Each component is described by a separate representation. To learn a predictive model involves finding best representation and parameters for its components such that it best predicts or recognises from a set of spatio-temporal data. Fourthly, once a predictive model has been learnt it may be applied to a set of spatio-temporal data to predict future occurrences, or to recognise an event. In the example the input data could be the location of a person along the path, and the prediction could be how likely the person is to take the left or right fork.

The stages outlined in Figure 2.2 have been used to structure the rest of this chapter. Section 2.2 presents an overview of techniques for processing video to locate its objects and produce a set of basic properties or features on each object for example: its colour; speed; or position. Section 2.3 firstly describes the different spatial and temporal relations
that can be defined between objects, and the various representation schemes that can be used to describe spatio-temporal data. Frames are explained which are used to represent the spatio-temporal data in this thesis. First order logic is also explained which is used to represent the production rules in this thesis. Section 2.4 describes methods for learning predictive models from spatio-temporal data, and reviews techniques that can firstly deal with variable length spatio-temporal data, and secondly non-deterministic spatio-temporal data. Section 2.5 describes production systems which are the architecture used to represent the predictive models used in this thesis. Production systems contain a set of production rules, and a conflict resolution strategy to decide how to apply the production rules to predict in different contexts. Section 2.5.1 outlines different techniques to learn production rules represented in first order logic from a set of spatio-temporal data. Section 2.5.2 explores different conflict resolution strategies, and Section 2.5.3 present an overview of techniques to allow production rules to deal with non-deterministic data. To learn the production rules in this thesis an evolutionary search technique called Genetic Programming is used. Section 2.6 describes this technique in more detail. Finally Section 2.7 describes some existing systems that learn predictive models, represented in first order logic, from spatio-temporal data.

2.2 Generating spatio-temporal data from video

The first stage to produce a set of spatio-temporal data from video is to process the video to find the objects in it. Once a set of objects have been located then the properties from each of the objects and the relations between the objects can be computed. There is a large set of different properties that could be extracted from an object including: its average colour; texture; speed; orientation; position; and the time range it appears in the video. There are two main types of relations between objects. Firstly, how objects are related to each other over time (or temporal relations), and secondly how objects are related to each other in the space they exist in (or spatial relations). These will be covered in more detail in Section 2.3. The remainder of this section will look at the different techniques to locate objects in video.

2.2.1 Locating objects in video

There are three main approaches for locating objects in a video. The first uses a prior model of the object to be found. A model is fitted (for example using edge information) to the set of video frames to find the location of the object. There have been object
models produced for tracking humans [7, 47], and vehicles [28, 56]. Figure 2.3 shows a very simple model of a human based on four rectangles, and some example results of how it might match the three frames shown in Figure 2.1.

The approach works well when there is a known object to be found and a prior model of it can be produced in advance. This approach will fail firstly when the object to be found has a large amount of variation in its appearance, preventing it from fitting to its object model. Secondly, it will fail in situations where it is hard to decide a priori the specific objects that will appear in the scene for example in an airport terminal. Here a large number of different objects can appear: passengers, luggage and trolleys etc; and it would be hard to find prior models for all the possible objects.

The second approach is to identify coherently moving regions that appear in the foreground of the video. These regions are then assumed to be objects, (or parts of objects). This approach does not require a detailed prior object model, and so can work in videos where it is difficult to define the types of objects that might appear. This was the approach used to produce some of the datasets used in this thesis, shown in Chapter 4, as it allowed the method described in this thesis to be quickly applied to a large variety of situations.

A background model is learnt over time. Any regions that are not modelled by it are seen as foreground regions. A background model is learnt in the following manner. Firstly, the background is modelled at the pixel level by separately modelling the colour distribution at each pixel over time. A new pixel value is seen as a foreground pixel if it is assigned a low probability by its colour distribution. Foreground pixels are then typically grouped into regions using connected component analysis [119]. These regions need to be associated to a set of objects, and these objects need to be tracked over time. One approach is to use a Kalman filter [51]. This is a stochastic linear predictor where the likelihood of an object’s location is a linear function of its previous location; and a noisy observation based on the location of a region within the current frame. The Kalman filter is used in three stages: prediction; data association; and correction. The prediction stage...
linearly predicts the location of the object in the next frame by using its previous location. The location of the object is further refined by using the location of a region detected in the current frame. The data association stage finds a region whose location is the most likely match to the predicted location of an object. The correction phase then uses this region to refine the location of the object. New objects are then created for any unmatched regions. Typically, if an object does not find a matching region for a number of frames it is removed.

This approach has been applied to tracking vehicles [68, 124], and people [124, 132], and groups of people [42, 74]. Figure 2.4 shows the detected foreground regions (shown in white) representing the person walking along the path. There are two main problems with this approach. Firstly, it assumes the objects will move in a linear manner; if they move in a non-linear manner, for example if a person changes direction sharply they may be failed to be tracked. Secondly, objects can become fragmented if parts the object to be tracked match the background model. The datasets used in Chapter 4 do not have these problems as the objects are well segmented from the background, and they move in a linear manner.

The final approach uses feature points extracted from the frames. Objects are located by grouping up sets of points having similar properties (e.g. having similar motion). This approach can deal with occluding objects, because some of the feature points on each of the objects are still visible. Beymer [8] uses this approach to track cars along a motorway. The cars are tracked from a user defined detection region at the bottom of the frame, to a hand defined exit region at the top of the frame. In the detection region a corner detector is applied to extract corner feature points. The position and velocity of these feature points are then tracked over time by using a Kalman filter. To group up the feature points a graph based approach is used. The vertices are the tracks of the feature points, and the edges group up feature points that move in the same manner. Initially a feature is connected to all feature points within a specific radius. Over time these edges are removed if the
amount of relative motion between the tracks of two feature points is above a pre-defined threshold. This approach assumes that the objects will move in a linear manner, and as explained previously, if the object moves in a non-linear manner it might fail to be tracked properly. Also it assumes that the object will not change its shape, or appearance once it leaves the detection region. A large number of objects e.g. people, can have variation in their appearance, and so would not be tracked well by this approach.

2.3 Representing spatio-temporal data

The previous section discussed the techniques used for locating and extracting information relating to objects in video, in order that a set of spatio-temporal data may be produced. The spatio-temporal data contains data on the individual objects, and data on relations between objects over time. The spatio-temporal data needs to be described in an appropriate representation. The representation is on two levels. The first level is how to represent each of the object’s properties and relations between objects. The second level is how to represent data on multiple objects. The appropriate representation chosen depends on the task to be performed. The representation must integrate well with the system that is using the data, in this case of this thesis a predictive model. It must also accurately describe the data given the task the system is performing; in the case of this thesis predicting or recognising events from spatio-temporal data.

There are two possible types of representations for describing properties of an object, or relations between objects: quantitative representations, and qualitative representations. Quantitative representations describe a property or relation based on a specific quantity like seconds or metres; for example “Bob’s height is 2 metres.”, or “Andy is 2 metres to the left of Colin”. Qualitative representations describe a property or relation using a particular quality or categorisation like short, or long; for example “Bob is tall.”, or “Andy is behind Colin”.

There are two main approaches to representing data on a set of objects: a fixed length representation, or a variable length representation. A fixed length representation uses a predefined number of attributes, where each attribute has a name and predetermined type and set of values. This allows properties of an object to be easy represented, but it is often difficult to efficiently describe multiple objects, and their relations. For example, Galata et al. [34] produced a system that can learn the interactions between cars on a road for example overtaking, and following. They use a fixed length input vector, that is limited to describing interactions between two cars. To extend the system to model the interactions of more than two cars would require a different fixed length vector to be produced that is
specialised to that number of cars. Many standard machine learning algorithms require a fixed length vector, but there are some solutions to allow variable length data to be described as a fixed length vector. These are detailed in Section 2.4.2.1. A variable length representation, however, does not require the number of possible objects and their relations to be predefined, so it can be used in situations where an unknown number of objects might appear. There is also no redundancy in the representation as only actual relations between objects need to be stored. For example, Needham et al. [89] produced a system that could learn the rules of basic card games. A variable length representation based on first order logic was used to describe the cards. This did not place any limits on the number of cards that could be represented both in each scene, or over the length of a game.

The remainder of this section will firstly explain two types of qualitative object relations: qualitative spatial relations, and qualitative temporal relations which are used in Chapters 5 and 6. Subsequently, two approaches, used in this thesis to represent variable length spatio-temporal data: frames, and first order logic will be presented.

### 2.3.1 Qualitative spatial relations

Cohn and Hazarika [13] give an overview of work in qualitative spatial relations. There are two main types of qualitative spatial relations: relations based on regions and relations based on points.

The first approach uses a set of regions, and looks at how each of the regions relate to one another. Region Connected Calculus (RCC-8) [105] is a topological spatial calculus to represent the possible spatial relations between two regions. There are 8 possible relations (Figure 2.5) which describe concepts like two spatial regions touching, or overlapping. Maillot et al. [69] uses RCC-8 as part of a system to build a visual concept ontology.

The second approach assumes objects are points in space, and relates the position of an object to the position of a reference object. Orientation relations [45] relate the orientation of a primary object based on a reference object and a frame of reference (Figure 2.6). The line representing the frame of reference passes through the reference object, and the primary object’s orientation is based on which side of the line it is located. The simplest orientation relation is a level 1 orientation relation. It only uses one frame of reference, and therefore is a binary relation based on which side of the line the object is located. Figure 2.7 shows two level 1 orientation relations: one allowing an object to be east or west of the line, and the other allows the object to be north or south of the line. To
allow more complex orientation relations the two previous level 1 orientation relations are combined together and rotated by 45 degrees forming a level 2 orientation relation. This then allows four different orientations: North$_2$, South$_2$, East$_2$ and West$_2$. Level 3 orientation relations can then be defined, to allow more fine grained orientations by combining, and rotating the level 2 operation relations. The level 3 orientation relations are: North$_3$, South$_3$, East$_3$, West$_3$, North-east$_3$, North-west$_3$, South-east$_3$, South-west$_3$. Orientation relations are used in Chapter 6 to describe the orientation and location of virtual movement sensors placed on a video of people walking along a path.

Other approaches include work by Fernyhough et al. [27] who use a grid based spatial relation to relate a reference object to an object close to it. This is used to automatically learn event models from road scenes. Needham et al. [88] uses a local cardinal system to

Figure 2.5: The RCC-8 relations from [105].

Figure 2.6: An orientation relation where the primary object’s orientation is based on the position of the reference object, and the orientation of the frame of reference.
describe the location of objects. Each object defines its own cardinal reference frame and this is used to describe objects around it. Siskind [117] uses a force-dynamic model that describes how objects are attached to each other over time. The output from the model is combined with a set of event definitions which recognise the actual events that have occurred for example picking up an object.

2.3.2 Qualitative temporal relations

There are two main ways to represent time: as a set of points, or as a set of intervals. Situational Calculus [70] and the work of McDermott [71], represent the world as a sequence of states. Each state describes the world at an instantaneous point in time. Another approach is to represent time by periods or intervals. Allen’s Interval Calculus [1] describes temporal interactions between two time periods as a set of thirteen temporal relations. These relations are calculated on the start and end time of each of the time periods and they are only valid when both time periods have a valid start and end time. Figure 2.8 shows Allen’s intervals which are: meets, met-by, starts, started-by, finishes, finished-by, during, contains, before, after, overlaps, overlapped-by, and equals. Allen’s intervals are used in Chapters 5 and 6. Chapter 5 also defines a novel set of temporal state relations which can deal with time ranges that do not have an end time. Vilain [128] extends Allen’s Interval Calculus by combining the point, and period time representations. This is done by adding point-to-point, and point-to-interval temporal relations to the calculus.

2.3.3 First order logic

This section gives an overview of first order logic which is used within the predictive models described in Chapter 3. The first part of the section shows how the spatio-temporal data, and predictive models can be represented in first order logic. The second part looks at how inference is performed on spatio-temporal data using the predictive models to make
Chapter 2  

Figure 2.8: The thirteen Allen’s intervals [1].

A prediction. The learning of first order logic production rules is explained in Section 2.5.1, and combining first order logic with probability is explained in Section 2.5.3. The examples used in this section are based on the Path example shown in Section 2.1. This section will only describe the first order logic required for the work in this thesis, for a fuller explanation please refer to Norvig et al. [111].

2.3.3.1 Spatio-temporal data

Spatio-temporal data is based on a set of objects. In first-order logic objects are represented by constants for example: Path, Andrew, or Anna. The objects have properties, and relations can exist between them. In first order logic predicates, and functions are used to represent object properties and relations. Predicates represent logical relationship between one or more objects. Unary predicates (just containing one object) are typically used to describe properties of an object for example Red(Andrew) represents that Andrew is Red. Binary predicates (containing two objects) describe relations between two objects for example LeftOf(Anna, Andrew) represents that Anna is to the left of Andrew. Some relations are better represented as functions. Functions represent a mapping from an object, or a tuple of objects to a specific object, for example Position(Andrew) represents applying the object Andrew to the function Position and returning its location. A term is a logical expression that refers to an object; functional expression (i.e. a function with a set of arguments), constants and variables (explained in the next section) are all terms. Terms and predicates can be combined to form atomic sentences. An atom is a predicate followed by a parenthesized list of terms, for example LeftOf(PositionOf(Andrew),PositionOf(Anna)) represents that the Andrew’s position is above Anna’s position.
2.3.3.2 Predictive models

The type of predictive models used in this thesis, described in Section 2.5, use a set of production rules. This section will explain how the production rules are represented in first order logic. Firstly, the production rules need to represent more complex logical sentences than the ones described in the previous section. This is achieved by using the logical connectives (shown in Table 2.1) with the atomic sentences, for example $\text{LeftOf}(\text{Anna}, \text{Andrew}) \land \text{LeftOf}(\text{Andrew}, \text{Bob})$ represents that Anna is to the left of Andrew and Andrew is the left of Bob.

<table>
<thead>
<tr>
<th>Name</th>
<th>Symbol</th>
<th>Returns</th>
</tr>
</thead>
<tbody>
<tr>
<td>And</td>
<td>$X \land Y$</td>
<td>$\text{if } X = t \text{ and } Y = t \text{ then } t \text{ else } f$</td>
</tr>
<tr>
<td>Or</td>
<td>$X \lor Y$</td>
<td>$\text{if } X = f \text{ and } Y = f \text{ then } f \text{ else } t$</td>
</tr>
<tr>
<td>Not</td>
<td>$\neg X$</td>
<td>$\text{if } X = t \text{ then } f \text{ else } t$</td>
</tr>
<tr>
<td>Implies</td>
<td>$X \Rightarrow Y$</td>
<td>$\text{if } X = t \text{ and } Y = f \text{ then } f \text{ else } t$</td>
</tr>
<tr>
<td>BiImplies</td>
<td>$(X \Leftrightarrow Y)$</td>
<td>$X \Rightarrow Y \land Y \Rightarrow X$</td>
</tr>
</tbody>
</table>

Table 2.1: The first order logical connectives.

Secondly, the production rules need to generalise from the spatio-temporal data. The logical sentences in the previous section used constants which meant they could only apply to specific objects. These constants can be replaced with variables to produce generalised sentences, where the value of a variable ranges over the set of terms. To control how a variable is used within a sentence two quantifiers are used. Universal quantification ($\forall$, “for all”) states that the sentence must be true for every possible value for the variable, otherwise the sentence is false. Existential quantification ($\exists$, “there exists”) states that the sentence must be true for at least one value of the variable, otherwise it is false. The previous example can be generalised as $\forall x ((\text{LeftOf}(\text{Anna}, x) \Rightarrow \text{LeftOf}(x, \text{Bob}))$ which represents that for each object in the world if Anna is to the left of it then the object must be to the left of Bob.

A production rule has an action section, and a condition section. The condition section matches a pattern in the spatio-temporal data, and the action section predicts the spatio-temporal data to occur next. In first order logic this is represented by a clause. A clause is a disjunction of literals, and a literal is an atom, or negated atom. The production rules in this thesis have a similar representation to a special type of clause: the Horn clause which is a clause that only has at most one positive literal. All variables used in Horn clause are universally quantified. The head of a Horn clause is the positive literal, and the body of a clause if the set of negative literals. The head represents the action section, and the body represents the condition section. The spatio-temporal data described in the previous
section can be represented as a fact which is a clause that has no body. Horn clauses are restricted class of first order logic sentences, this makes them easier to learn and perform inference on than full first order logic. The learning of Horn clauses will be explained in Section 2.5.1. The production rules used in the predictive models, explained in Chapter 3, have a similar representation to Horn clauses. Horn clauses are typically written using implication, where the negative literals imply the positive literal. Equation 2.1 shows a Horn clause which states that if a person is at the junction on the path at time \( t \) then they will take the left hand fork. The head of this Horn clause is \( \text{Movement(LeftFork,} t) \).

\[
\text{Person}(x) \land \text{Time}(t) \land \text{AtJunction}(x,t) \Rightarrow \text{Movement(LeftFork,} t) \tag{2.1}
\]

To specialise a Horn clause a substitution can be used to change the variables to constants. A substitution \( s = \{v_1/t_1, v_2/t_2\} \) contains a set of variables \( v \), and a set of terms \( t \) that will replace the variables. When a substitution is applied to a logical sentence all variables in the sentence that match one of the variables in the substitution are replaced by its accompanying term. For example the substitution \( \theta = \{x/\text{Anna}, y/\text{Andrew}\} \) applied to \( \text{LeftOf}(x,y) \) gives the following result: \( \text{LeftOf(Anna, Andrew)} \). A ground term is a term that does not contain any variables, and a ground atom is an atom that does not contain any variables. Unification typically finds the most general substitution that makes two logical sentences equal. Substitutions and unifications as shown in the next section are used to perform inference. A sentence \( S_1 \theta \)-subsumes a sentence \( S_2 \left(S_1 \preceq S_2\right) \) if \( S_1 \theta \subseteq S_2 \), or every atom in \( S_1 \) is in \( S_2 \). This can then be used to give a specific to general ordering for a set of sentences. This is used within the techniques to learn first order sentences (described in Section 2.5.1) to decide how to search the space of possible sentences.

### 2.3.3.3 Inference

The previous sections have shown how to represent spatio-temporal data and predictive models in first-order logic. This section will present how predictive models can be applied to the spatio-temporal data to make a prediction. To do this a check must be performed to see if the spatio-temporal data logically matches or entails the condition section of each production rule. A logical inference procedure is used to do this. One approach is to enumerate over all possible configurations of the world. If the spatio-temporal data, and the condition section are true in the same world configurations then the spatio-temporal data entails the condition section, and its action section can be used for the prediction.

To produce the world configurations the Herbrand universe and the Herbrand base must be computed. The Herbrand universe is the set of all ground terms created from
combining the function and constant symbols together and the *Herbrand base* is the set of all possible ground atoms. Each world configuration is described by a *Herbrand interpretation* which assigns a true or false value to each possible ground atom. An interpretation which makes a logical sentence true is called a *model*. Sentence $S_1$ entails $S_2$ ($S_1 \models S_2$) if in every model that $S_1$ is true in $S_2$ is also true.

The only problem with enumerating every world configuration is that when there is a large number of constants and predicates it can be computationally expensive to perform. An alternative approach is to use the resolution algorithm [109]. This is a proof based technique that tries to match every literal in the condition section of the production rule with some spatio-temporal data. To use the algorithm the spatio-temporal data, and the condition section must be converted into conjunctive normal form (CNF), which is a conjunction of clauses. Then they are both are standardised apart (so that variables do not have the same names). Then one literal is unified to the complementary of the other. This process repeats until the empty clause is found, or no more unifications can be done. If the empty clause is found then the spatio-temporal data entails the condition section. A simpler resolution algorithm, called forward chaining [111] can be used, if the production rules are represented as Horn clauses. In forward chaining spatio-temporal facts are unified with literals in the Horn clause. Once all the literals in the body of the Horn clause are unified the head of the Horn clause is returned and can be used for a prediction.

### 2.3.4 Frames

Frames [78] can be used to represent the properties of objects, and temporal and spatial relations between objects. There are two types of frames: a class frame, and an instance frame. A class frame describes a specific type of object. It contains a number of slots which describe different properties or attributes of the object. A slot can have a default value, and a set of facets which constrain the possible values the slot can contain. Multiple values can be assigned to a slot. A class frame can inherit slots and default values from a parent frame creating a hierarchy amongst the class frames. Figure 2.9 shows a class frame for a Person. It contains three slots: the name of the person, their speed and their position. An instance frame uses a class frame to store information on a specific object, by filling in the values of the slots. Figure 2.9 show an instance frame for a person. They are called Bob, are at position (40,50), and are moving a medium speed. Frames are used in Chapter 3 to represent the history of spatio-temporal object data.

The frame data in this thesis is stored using the Extensible Markup Language (XML) [10], as explained in Chapter 3. This is a meta-language that places a tag around data.
items. A tag has a name, and often a set of attributes, and is used to give a semantic description of the data it encloses. An XML schema is used to formally define the tags and their structure. XML is human readable, but it is quite verbose, and can often greatly increase the size of the data it is representing. List and Fisher [64] use XML to represent their Computer Vision Markup Language (CVML). This allows data from a vision system to be represented in a common format that can be easily shared. Their approach can describe features on objects like their position, bounding box, and type; and can group up sets of objects. There is, however, no way to describe spatial or temporal relations between objects.

2.4 Learning predictive models of spatio-temporal sequences

This section will firstly give an overview of predictive model learning, and then will show previous learning approaches.

2.4.1 An overview of predictive model learning from spatio-temporal sequences

To produce a predictive model requires: a sequence of spatio-temporal data; a representation to describe the predictive model, and its associated parameters; and a learning algorithm. Each point in the sequence produces an example where the input is the past spatio-temporal data, and the output is the future set of spatio-temporal data. There two main ways to represent the spatio-temporal data with the main ones being fixed length and variable length vectors, as described in Section 2.3. The predictive model is represented by a set of components. A component [111] performs a specific task which aids the predictive model when it is making a prediction, for example it could use a set of object information to predict that a particular event will happen, or recognise that a particular event has occurred. There is a variety of representations used for the components includ-
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ing: graphs, trees, linear functions, and logical statements. These will be explained in more detail in the following sections. A learning algorithm then attempts to find the best representation for the components in the model and the values for its parameters, such that it best predicts a set of examples. Structure learning is used to find the optimal representation for the components, and parameter learning is used to find the optimal values for the model parameters.

More formally an example \((x, f(x))\) is a set of input data \(x\), and an output \(f(x)\) produced by applying the input data to an unknown function \(f\). Given a set of examples generated using \(f\) induction is performed to find a hypothesis or model that best approximates \(f\). A good model will generalise, or predict well from unseen examples. If the unknown function has a continuous output then inducing a model of it is called regression, and when the output is discrete it is called classification.

Model selection is the task of selecting the model, from the set of all possible models, that best predicts the examples. The model has to satisfy two criteria. Firstly it must predict well from the examples, and secondly it must not be too complex. A complex model is likely to specialise on, or overfit the examples, and noise within the examples. This makes it less likely to generalise or predict from the unseen examples.

A learning algorithm performs the task of model selection, by searching through the space of possible models to find the model that best predicts the examples. A search technique is used to explore the space of possible models. It is typically guided by an explicit fitness function that provides feedback to the search technique, by computing a score, based how on the current best model predicts the examples. Some search techniques use an implicit fitness measure where the fitness is included within the search technique. There are a wide variety of search techniques, and fitness functions which are described in the following sections.

Minimum description length (MDL) [107] is one approach to prevent overfitting. It is an information based fitness score (Equation 2.2). The fitness is calculated by computing the amount of information to code the model \(I_{\text{model}}\); the amount of information to code the parameters of the model for a particular instance \(I_{\text{params}}\); and the amount of information to code the residual \(I_{\text{residual}}\), which is the difference between the model predictions and reality. The best model can be found by minimising this score.

\[
I_{\text{total}} = I_{\text{model}} + I_{\text{params}} + I_{\text{residual}}
\]  

(2.2)

Another approach is to use \(k\) fold cross validation. This divides a set of examples into \(k\) sections. Each of the \(k\) sections are then used as a test set, and the remaining examples
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as a training set. The training set is used to induce a model, and the test set is used to see how well it predicts from unseen examples. Models that overfit the training examples, will predict poorly from the test examples. In this thesis 10 fold cross validation is used as described in Chapter 4.

2.4.2 Previous techniques for learning predictive models

This thesis presents novel approaches for learning predictive models from non-deterministic spatio-temporal data from visual scenes. The visual scenes themselves can contain a variable number of objects, and the events within them can last over a variable length of time. This means the input data is a variable length vector which can vary in size, both spatially and temporally. This section will cover techniques that can firstly learn models from variable length data, and secondly learn models of non-deterministic data.

2.4.2.1 Learning predictive models from variable length data

Most standard model learning techniques like neural networks, decision trees [99] and support vector machines (SVMs) [127] require a fixed length input vector. This vector often needs to be defined by hand, and as explained in Section 2.3 can only describe a set number of objects over a specific range of time. For example Xu and Hogg [133] learn a neural network to predict the position and size of a person walking through a scene. Neural networks produce a prediction by passing the input through a set of linear classification functions called neurons which are connected together into a set of layers. The approach uses a fixed length input vector, so assumes that only one person will be walking through the scene, and only a fixed length history will be used for the prediction.

One approach to allow a variable length vector to be used within a fixed length vector is to produce a histogram on the number of types of elements in the variable length vector. In natural language processing this approach is called bag of words [50], where a histogram is produced on the number of different words appearing in a document. To apply the bag of words approach to digital images and videos a set of visual [118] or video [90] words needs to be produced. To produce a set of visual words, image patches are extracted from a set of training images, and these patches are clustered based on their similarity. The prototypes found, which represent the centre of the clusters, are then used as the visual words. Video words are produced in a similar manner except that the patches use data from the current, and previous frames. This approach has been successfully applied to learning the categories of natural scenes [24], objects [17, 118], and human actions [90].
Similar approaches have been applied when producing kernels that can use variable length input vectors. Kernels are used to map a set of data points into a high dimensional space, and are used with linear classifiers like SVMs to allow them to deal with non-linearly separable datasets. Grauman and Darrell [39] use a pyramid match kernel which uses a set of histograms each using progressively larger bin sizes. At each histogram information from each example that occur in the same bin are matched together. Each example can contain a different number of data items. The weighted sum of differences of the number of matches between each subsequent histogram level is then computed. The downside with all these approaches is that spatial or temporal relations between the data items are lost when the statistics are produced. If this is important then a poor model will be produced.

An alternative technique to deal with variable length vectors in situations where the number of objects is fixed, but the history for events is variable, is use a predefined function to compute the value of the object configuration over time, for example computing its average value. Sumpter and Bulpit [125] use this approach when learning a neural network to predict the position and shape of a virtual robot sheep dog and a set of animals. The object information at each point in time is represented by a set of learnt clusters. The values of the clusters are modelled over time by a set of leaky neurons, where each cluster is modelled by a single neuron. The activation level of each neuron is based on the running average of its current level, and its cluster’s value.

### 2.4.2.2 Learning models of non-deterministic data

The methods in the previous section assumed that the data is deterministic and the model needs to make a non-probabilistic prediction. The remainder of this section will explain techniques to deal with non-deterministic data, and probabilistic predictions.

Bayesian Networks graphically represent the full joint probability distribution between a set of variables as explained in Section 2.5.3.1. They still rely on a fixed sized input vector, but can describe the likelihood of a particular prediction, and can deal with missing data. Bayesian Networks typically have a fixed number of random variables so will work in situations where the number of objects that might occur is known a priori, and the length of history that is required.

Dynamic Bayesian Networks (DBNs) are Bayesian Networks that can probabilistically model a set of observations over time, for example object configurations, and can deal with variable length histories. Each point in time is represented by a slice containing a set of evidence variables, that describe observations from the world; and a set of hidden state variables that describe the current state of the world. Three probability distributions
are also used: the prior distribution over hidden states, the transition model that gives the likelihood of the hidden state given a set of previous hidden states, and the sensor model that represents the likelihood of the evidence given the current hidden state. Given a set of observations a DBN is created by unrolling [111], where the slice is replicated until all the observations are covered.

Once a DBN has been created there are four main inference tasks: filtering, prediction, smoothing, and most likely explanation. Filtering computes the likelihood of the current hidden state, given a set of observations. Prediction computes the likelihood of a set of future states. Smoothing computes the likelihood of a previous hidden state using current and previous observations. Most likely explanation finds the set of hidden states that best describe a set of observations.

Hidden Markov models (HMMs) [102] are a popular DBN. Each slice is a simplified DBN as it only contains one state variable, and one observation variable. It also uses a simplified transition model based on a first-order Markov process where the likelihood of the current hidden state is only based to the previous hidden state. These simplifications are important as they allow for some efficient inference algorithms to be used. HMMs have been used for producing high-level models of human tasks from video, where the observations are image features extracted from the video frames, and the states are the possible human actions. The key reason to use a HMM for this task is that often the observations are noisy, so it can be hard to make a prediction just using their values. The HMM deals with the observation noise by probabilistically modelling the observations over time to determine which set of hidden states best matches the observations. HMMs have been successfully used for sign language recognition [123] and recognising human movement [11].

There are three main issues with HMMs: the observation variable must use a fixed number of dimensions; only one state variable can be used; and the likelihood of the current hidden state is only based on the previous hidden state. The remainder of this section explains solutions to these problems.

Firstly, the observation variable in a HMM must use a fixed number of dimensions, so typically it can only describe a fixed number of objects. This will not allow the HMM to deal with scenes where there is a varying number of objects. One approach to solve this problem is to use the representations described in Section 2.4.2.1 to represent the observation variable. Kettnaker and Brand [54] propose another solution by representing the observation model as a Gaussian mixture model (GMM) over the variable length observation. A GMM approximates a probability distribution by using a set of weighted Gaussian distributions. Each observation is applied to the GMM and the results are mul-
tiplied together. It was successfully applied to learn the behaviour of vehicles at a traffic intersection. The downside of this approach is that it does not easily represent relations between observations, as each of the Gaussian distributions used in the GMM requires a fixed number of dimensions.

Secondly, HMMs can only use one hidden state variable, which makes it hard to describe interactions between multiple objects. Coupled Hidden Markov Models [92] are a DBN which can represent two objects interacting. Each slice has a hidden state and observation variable for each of the two objects. The likelihood of each hidden state is related to each of the previous hidden states from the two objects, and so can model interactions between the objects. This approach is limited to a maximum of two interacting objects, as above this number there only exists approximate inference techniques.

Thirdly, HMMs only base the likelihood of the current hidden state on the previous hidden state, so cannot explicitly model higher order temporal dependencies, although the structure of the HMM does allow them to be implicitly modelled. Variable Length Markov Models (VLMMs) [35] are an efficient way to describe the number of previous states required to predict a new state. VLMMs use a sequence of states based on symbolic observations, and use this to learn a model that can probabilistically predict the next symbol. This is performed by finding the optimal number of previous symbols that is required to predict each symbol. The observations at each point in time are represented by a fixed length vector. To produce a symbolic sequence the observations must be converted to a symbolic sequence. This can be performed by clustering the observations to produce a set of prototypes. A symbolic stream is formed by replacing each observation by the name of its closest prototype. VLMMs have been applied to modelling traffic interactions [34], and human behaviour [35]. There are two main problems with VLMMs: firstly there is no way to assign probabilities to the observations, so they cannot model uncertain data; and secondly the model has limited ability to deal with noise.

2.5 Production systems

Production systems are the architecture used to represent the predictive models and the spatio-temporal data used in this thesis. They require a set of production rules, a knowledge base, and a conflict resolution algorithm [66].

Production rules are of the form: IF condition THEN action. Within the context of predictive spatio-temporal models the condition section represents a pattern to find in the spatio-temporal data, and the action section represents the set of spatio-temporal data to occur next. The production rules in this thesis have a similar representation to Horn
clauses (explained in Section 3.3.1). Each production rule typically models a different aspect of the spatio-temporal data. An alternative approach to describe the production rules is to use a stochastic context free grammar (SCFG). A SCFG contains a set of production rules written in propositional logic, each labelled with a probability. Each production rule contains a non-terminal symbol in the condition section, and a list of terminal and non-terminal symbols in the action section. They have been successfully used to model poker games [80], and activities within a car park [49]. The main problem of using SCFGs over first order logic is that the production rules used in SCFGs use propositional logic which cannot contain variables and therefore are unable to generalise. Production rules represented in first order logic can use variables and are therefore able to generalise.

The knowledge base represents the history of past spatio-temporal data. In this thesis frames are used to represent this spatio-temporal data, as described in Section 2.3.4. To evaluate the production rules on the knowledge base the condition-act cycle [66] is used. This applies all the condition sections of the production rules to the knowledge base. A conflict-set is produced of all production rules that successfully match the knowledge base. In a traditional production system a conflict resolution algorithm is then used to select one of the production rules. Its action section is then fired, and the output is added back into the knowledge base. In this thesis the conflict resolution algorithm is slightly modified. As the spatio-temporal data used in this thesis is non-deterministic there might be multiple possible predictions, so the conflict resolution algorithm might return more than one production rule. The action sections of the selected production rules are fired, producing a prediction. This prediction, however, is typically not added back into the knowledge base because in this thesis the production rules only base their prediction on the history of past spatio-temporal data (Section 3.4).

The following sections will firstly describe how first order logic production rules are learnt from spatio-temporal data. Secondly, the different conflict resolution strategies that can be used to decide which production rules to use when making a prediction will be described. Finally, techniques to allow production rules to deal with non-deterministic data will be described.

2.5.1 Learning first order logic production rules

This section will review techniques for learning first order logic production rules represented by Horn clauses. In the methods described in this section the head of the Horn clause represents the action section of the production rule, which describes the next set
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of spatio-temporal data; and the body represents the condition section of production rule, which contains a set of literals representing a particular pattern in the spatio-temporal data. Firstly supervised learning techniques to learn Horn clauses will be described, subsequently unsupervised learning techniques will be covered.

Inductive Logic Programming (ILP) [82, 100] is a supervised learning technique to induce a set of Horn clauses. It requires a set of examples, and a set of background Horn clauses. The background Horn clauses describe unlabelled data from the world. The set of examples represents labelled data from the world that needs to be learnt. The set of induced Horn clauses should be able to correctly predict the examples using the background Horn clauses. For example a set of Horn clauses might be learnt to predict if a person will go left or right at the fork in the path. The background Horn clauses represent the spatio-temporal information of a person’s position on the path over time. The examples describe when a person took the left or right fork. The Horn clauses that are learnt should accurately predict the fork the person took based on their previous positions along the path. More formally there is a set of positive \( E^+ \) and possibly negative examples \( E^- \), along with a set of background clauses \( B \). In this thesis only positive examples are used, as the videos are from real-world domains where it is hard to generate negative examples. The aim is to learn a hypothesis \( H \) containing a set of Horn clauses that entail the positive examples given the background, but does not entail the negative examples given the background (Equation 2.3).

\[
(B \land H \models E^+) \land (B \land H \not\models E^-)
\] (2.3)

There are two approaches to supervised learning of a set of Horn clauses: learn them in a sequential manner or learn them concurrently. These will now be explained in more detail.

2.5.1.1 Supervised learning of a set of Horn clauses in a sequential manner

To learn a set of Horn clauses sequentially a covering method like the AQ algorithm [76] is used. The covering method works in the following manner. An example will be chosen and a Horn clause that entails the example will be learnt. This is then added to the hypothesis. Then all other examples that are entailed by the Horn clause are removed, and the process repeats until there are no more examples left.

FOIL [100] uses the AQ algorithm to learn a set of Horn clauses. It starts its search for a Horn clause by creating one with an empty body. It then uses a greedy search to find the best Horn clause. At each stage the current best Horn clause is specialised by either
adding a new literal, or adding an equality measure between two variables. A fitness function using an information gain metric based on the number of positive and negative examples matched by the Horn clause is used to find the best specialisation. The search stops when a Horn clause is found that does not cover any of the negative examples. FOIL cannot learn just from positive examples, and must either have negative examples, or a closed world assumption.

Progol [82, 85] also uses the AQ algorithm, but can learn just from positive examples. It is used in this thesis as a comparison method to the methods presented in Chapters 4 to 6. To find a Horn clause the search space is bounded by the most specific Horn clause which entails the example. All Horn clauses found must subsume the most specific Horn clause. To learn the most specific Horn clause a positive example and a set of mode declarations are used. There are two types of mode declarations: head, and body. Head declarations limit the constants and variables used in the head of the Horn clause; and body declarations to limit the literals that can be used in the body of the Horn clause. To find the best scoring Horn clause an A* search [111] is used, which performs a general to specific search over the lattice of subsumptions from the most specific Horn clause. A* search is a best first search, which uses a heuristic function, in this case based on the number of positive and negative examples the Horn clause has entailed and how many more literals are required to produce a solution. The search starts with an empty Horn clause which is then refined by adding new literals to it such that it still subsumes the most specific Horn clause. The search stops when a Horn clause is found which has a fitness score that cannot be improved by any refinements.

The two previous techniques use a greedy search methods to learn Horn clauses. Using a greedy search method to find clauses has the problem that it might find locally optimal solutions. An alternative technique is to use stochastic search methods which can look at different areas of the search space concurrently making it less likely to find local optima. One approach is to use random restart search. This starts by randomly generating a Horn clause, and adding it to the current list of active Horn clauses. A Horn clause is then selected from the active list either randomly, or by picking the best scoring Horn clause. Refinements to the Horn clause are added to the active list, and the process repeats. This will continue until a set number of Horn clauses have been evaluated, at which point the search is restarted. This process will then continue until an overall number of Horn clauses have been evaluated, when the search will stop. Železný et al. [129] present a large study of random restart methods compared with deterministic search techniques. They conclude that random restart methods have a lower search cost than deterministic search techniques. Muggleton and Tamaddoni-Nezhad [87] use random restart search
in their quick generalisation technique. This finds consistent Horn clauses in the search space. These are Horn clauses which entail at least one of the examples. It has been used to provide Horn clauses in Progol’s A* search algorithm, and as a seed to a genetic algorithm (GA). Genetic algorithms are described in more detail in Section 2.6. When there were few consistent Horn clauses in the search space it was found that QG seeded GA was more efficient, both in runtime and Horn clauses evaluated, than the A* and unseeded GA techniques.

Nezhad and Muggleton [126] use a GA [37] to search for a single Horn clause. A novel binary representation is used which represents the variable bindings (variables in the head and body that are the same), in the most specific Horn clause. Through the use of genetic operators specific variable bindings could be allowed or disallowed, creating a more specific, or more general, Horn clause which still subsumes the most specific Horn clause. The technique was implemented using a simple GA, and replaced the A* search used in Progol to find the best Horn clause. The results showed that the GA based search performed better than A*. The SIA01 algorithm [4] uses a GA binary representation based on the selected example. The system then learns a Horn clause that generalises from this example by using crossover and mutation operators that generalise predicates, change constants, and replace constants with variables. A fitness function based on the consistency, completeness, and syntactic generality of the Horn clause is used. Individuals are added to the new population if they have a better score than the worst individual in the new population. When the score of the current population has not changed for a number of generations the best individual is returned. Stochastic clause selection [122] randomly selects a fixed number of Horn clauses from the search space that guarantee a Horn clause will be found that is good enough for the solution. It was shown to give better results than Progol, both on the time to find a Horn clause, and the accuracy of the Horn clause.

The methods reviewed in this section show that stochastic search techniques can find good Horn clauses in a shorter time than greedy search techniques. This was one of the reason a stochastic evolutionary search approach was chosen to learn the production rules in this thesis (Chapter 4).

2.5.1.2 Supervised learning of a set of Horn clauses concurrently

The methods described in the previous section induce Horn clauses sequentially until all the examples have been covered. There has also been work on learning the complete set of Horn clauses concurrently. A comparison of the different systems is shown in [23]. One of the first systems to do this was REGAL [36]. It used a distributed GA system. The system is divided into a set of nodes each running a separate GA. The nodes learn
a Horn clause that covers a specific set of the examples. These nodes are controlled by a central supervisor node. The supervisor node decides which subset of examples to send to each GA node, and forms the overall set of Horn clauses by combining together the best Horn clauses from each of the GA nodes. A hand defined language template is used to represent the possible terms and variables that could appear in the Horn clause. Figure 2.10 shows an example language template and its associated binary encoding. The

Figure 2.10: An example showing the language template and binary encoding used in REGAL. Each box can contain a binary value, which indicates if the literal, or constant should be used within the clause. The binary encoding shown in the diagram represents the clause \( \text{colour}(y,r), \text{colour}(x,g) \).
subsumes it. If this is the case then most general Horn clause of the two is then removed from the IAS. If this check fails the Horn clause is removed from the IAS and added to the final answer set. This repeats until there are no more Horn clauses left in the IAS. The clauses in the final answer set are then ranked by the number of times each clause subsumes (or is subsumed by) the rest of the clauses, and only the most specific clauses are kept. When compared on how the Horn clauses (that should be learnt) were ranked, the technique ranked them high than Progol did.

In both REGAL and G-NET the supervisor node must combine the Horn clauses learnt from the nodes to form the overall set of Horn clauses. A better approach is to allow the system to find the most optimal set of Horn clauses by evolutionary search, rather than learning individual Horn clauses. DOGMA [46] again uses a GA, and learns a set of Horn clauses on two levels. The first level is similar to REGAL and G-NET. The Horn clauses are represented using the same fixed binary template as REGAL and the same set of genetic operators are used to evolve the Horn clauses. On the second level a set of families are used which group up the Horn clauses to form the overall set of Horn clauses. A separate set of genetic operators are used to join, and break up families. This approach was shown to be better than FOIL with low to medium noise levels in the training examples.

To avoid the limitation of using a fixed length GA to represent the set of Horn clauses a variable length structure for example a tree could be used. Genetic Logic Programming System (GLPS) [131] represents the set of Horn clauses as a forest of AND-OR trees. Each tree represents a set of Horn clauses that all have the same head. The leaves of the tree contain literals, and the nodes can either represent AND, or OR. The forest of AND, or OR trees can be accessed on 4 different levels. The first level is the entire forest, the second level is an individual AND-OR tree, the third level is a sub-tree within an AND-OR tree, and the fourth level is a leaf node within an AND-OR tree. The only operator used to evolve the forests of AND-OR trees is a modified crossover operator. It selects two forests of AND-OR trees, by fitness proportionate or tournament selection, then two elements both on the same level are selected. These elements are then swapped over and both forests of AND-OR trees are added to the new population. The system was combined with the output from FOIL and was found to be more noise robust than just using FOIL alone.

This section has presented evidence that inducing a set of Horn clauses at the same time, produces better results than learning Horn clauses sequentially. This was one of the reasons the production rules were learnt at the same time (Chapter 4).
2.5.1.3 Unsupervised learning of sets of Horn clauses

The previous sections used supervised learning to induce a set of Horn clauses. An alternative set of approaches called rule discovery systems use an unsupervised learning approach where the learner is not given any labeled examples, but finds interesting Horn clauses that cover the unlabeled examples, where interestingness is based on some criterion. This allows a wider range of clauses to be found because there is greater flexibility on what is an optimal Horn clause is given a specific context. It is useful in situations where it is hard to provide complete set of labeled examples. For example with the path example, it might be hard to have an example of every action the humans perform in the scene, so an unsupervised learning approach could be used to learn novel actions in the scene.

Rule discovery systems maintain a list of clauses. A clause is then selected from the list by using a specific search technique. Then the clause is removed from the list, and checked to see if it is valid on a specific set of unlabeled examples. If the clause is valid it is added to the overall hypothesis. If the clause is not valid then a refinement operator is applied to the clause, to produce a set of new clauses which are added to the list. The approach repeats until the list is empty.

CLAUDIEN [103] uses a language bias to limit the possible set of clauses, and the possible refinements to a clause. The validity of a clause is based on whether the percentage of the unlabeled examples that it models is above a preset threshold. A best first search is used to select clauses, with a search heuristic based on the minimum description length principal, using the number of positive and negative grounding substitutions a clause has, along with the length of the clause. Tertius [29] again uses a best-first search to select the clauses. The search heuristic applies a set of sampled grounding substitutions to a clause, and records the number of times the head and body are satisfied by each substitution. The refinement operator can add a new literal to the body of the clause, unify two variables, or change a variable into a constant. They are ordered to ensure a specific clause is only generated once during the search.

HR [15] is a rule discovery system used to learn mathematical theories. It induces a theory containing a set of classification rules represented as range-restricted predicates, and a set of association rules represented as range-restricted clauses. The refinement operator uses a set of unary, and binary production rules. A production rule takes a single clause, or two clauses, and changes them; for example removing variables from the head of the clause, or composing two clauses together. The success sets (the data the clauses match) for the new clauses are then calculated. If the success set is empty then association rules representing a non-existence hypothesis are derived. If there is an existing clause
with the same success set then association rules representing an equivalence hypothesis are derived. If the success sets are unique then a new classification rule is derived, and association rules are also derived. A application based comparison of HR with Progol is made in [14] which found that HR is more likely to find clauses that cover concepts with fewer positive examples than Progol. Santos et al. [112] presents a comparison of Progol and HR on a cognitive vision task. They concluded that both methods performed well with different noise levels in the data, but overall Progol performed slightly better than HR. HR found a larger number of clauses, and took longer to find a solution than Progol.

The techniques described in this section have been used to provide the input to some of the learning methods explained in the following sections. They have not been incorporated into the method described in this thesis, as this relies on a supervised learning approach. It could be done as future work to try and broaden the range of production rules the method could search over.

### 2.5.2 Conflict resolution strategies

There are many different strategies that are used to perform conflict resolution in expert systems. These include: using the first production rule that appears in the conflict set, applying priority values to the production rules, and using meta-rules which decide which kinds of production rules are more important than others [66]. Similar approaches are used when a set of Horn clauses is used to predict an unseen example. The Horn clauses are ordered typically from most specific to most general. Then each Horn clause is applied in order, until one is found which entails the example. It is often hard to learn a set of Horn clauses where some of the clauses do not match some of the negative examples. This will then cause problems with predicting unseen examples as it might get the wrong prediction. A more accurate approach is to use all clauses and to form a consensus when making the prediction.

Pompe and Kononenko [97] use the ILP-R [96] method to induce a set of clauses from a set of training data. These clauses are then used as features within a Naïve Bayes classifier. To predict the class of an unseen example the classifier uses how well each clause covers the unseen example, and the conditional likelihood that the clause will predict a specific class. The conditional likelihood is estimated from a set of labelled training examples. A comparison was done with a procedural approach (where the clauses were applied to an unseen example in order, and the class of the first matching clause was used). The results showed that the Naïve Bayes approach will still work when the procedural approach fails to return the correct classification.
Flache and Lachiche’s 1BC [30] system takes a similar approach except that the instead of using an ILP method to induce the clauses from data the rule discovery system Tertius [29] is used. The system is asked to find clauses that only contain one literal that relates to a property of an object, and the rest of the literals must be related to relations between objects. This ensures that all the clauses will be independent when used as features within the Naïve Bayes classifier.

Another technique for improving the accuracy of classification is to use boosting to learn a set of clauses. Boosting [115] combines a set of weak classifiers to produce a strong classifier. A weak classifier makes a classification which performs just better than random guessing. A weak learner is used to produce the weak classifiers by repeatedly training itself on a weighted training set. On each run a weak classifier is generated. The error of this weak classifier on the training set is then calculated. This is used to weight the weak classifier when the final classifier is produced. The weights on the training set are then updated based on how well the weak classifier predicted each data item, including weights at poorly classified items. To produce the final classification a weighted majority vote over all the weak classifiers is performed. Quinlan [101] applies boosting to the FFOIL system, which is a variant on FOIL [100] designed to learn functional relations. The standard boosting algorithm is changed in two ways. Firstly a weighted re-sampling technique is used to generate the data set to learn each new clause. This is performed by sampling the training set based on the weights on the data items. Secondly the weight on each learnt clause is the same. The results showed that the boosting version of FFOIL produced more accurate results than the non-boosted version.

Muggleton et al. [86] use a SVM to decide the class of an unseen example based on a set of clauses which entail it. The Progol ILP system is used initially to find a large number of clauses (typically around 1500 - 2000) which correctly cover a pre-defined percentage of the training data. The clauses are then applied to each example in the training set, and it is recorded if the clause can correctly entail the example. A kernel is used that compares the similarity of two examples based on the set of clauses which entail them. This kernel can then be used with a SVM to predict the class of an unseen example based on the set of clauses which entail it. A comparison was done using a structured toxicology dataset, and it was shown that this technique is more accurate than Progol, and standard SVM methods.

The previous set of methods work in two stages: firstly the Horn clauses are learnt using a standard ILP algorithm, and the parameters of a conflict resolver are learnt, which compute its most likely class of an unseen example based on which clauses entail it. This next set of methods presented here use a combined approach where both the Horn clauses...
and parameters of the conflict resolver are learnt at the same time. This then ensures that more accurate predictive models can be learnt.

Davis et al. [19] use a greedy learning algorithm called Score As You Use (SAYU). Firstly the Aleph ILP system [121] is given an example, and used to find a clause that generalises the example. The clause is learnt in a greedy manner where a clause with the highest m-estimate is used. This clause is then added as a binary feature to a Bayesian Network. The structure and parameters of the Bayesian Network are then learnt. The score of the Bayesian Network is then calculated by using the area under its precision-recall curve. If the score is worse than the previous score the clause is removed. The algorithm was tested on both a Naïve Bayes classifier (described in the next Section 2.5.3.1), and with a Tree Augmented Naïve Bayes (TAN). A TAN is similar to a Naïve Bayes classifier but can allow a feature to be dependent on one other feature. The technique was only tested on binary classification problems, and was found to use fewer clauses, and shorter clauses than using a two-stage approach.

Landwehr et al. [61] use similar ideas by integrating Naïve Bayes into FOIL. The covers, and score functions in FOIL are re-written. The covers function determines whether an example is predicted by a hypothesis given some background information. The score function returns a score based on how well a hypothesis covers the set of examples given some background information. The changed covers function used a Naïve Bayes classifier to return the probability of a hypothesis predicting an example given some background information. The score function was changed to return the probability of a hypothesis predicting a set of examples given some background knowledge. The separate and conquer approach to learn examples used in FOIL (where examples that are covered by a learnt clause are removed from the training data), is removed. The system uses a beam search for clauses, which keeps a set of the $n$ best clauses found so far, and will stop learning clauses when there is no change in the score between adding two separate clauses to the hypothesis. The approach was shown to be more accurate than using standard ILP.

The novel approach to conflict resolution presented in this thesis is similar to the two previous methods [19, 61]. A combined approach is used to learn the production rules, and the probability distribution for the conflict resolver (Chapter 4). However unlike the methods described in this section the conflict resolver returns a set of production rules rather than a particular classification. To produce a prediction the action sections of these production rules are fired creating a set of spatio-temporal data. This is the same as how a conflict resolver in an expert system works, and allows the predictive models to generalise from a set of spatio-temporal data, as shown in Section 3.3. A full Bayesian Network (Section 3.3), is used to represent the conditional probability distribution used within the
conflict resolver as opposed to Naïve Bayes or TAN used in the methods in this section. This allows for better modelling of the dependencies between different production rules when deciding which production rules to use to predict the next set of spatio-temporal data.

### 2.5.3 Applying first order logic production rules to non-deterministic spatio-temporal data

This section presents a review of methods for combining first order logic with probability. These methods allow the first order logic production rules to be used with non-deterministic spatio-temporal data, and allow the outcome of a first order logic production rule to be uncertain. Firstly probability will be defined, then Bayesian Networks and finally techniques to combine first order logic and probability will be shown.

#### 2.5.3.1 Probability

Probability may be used to represent/model how likely particular events are to occur in the world. This section will give a brief overview of probability related to this thesis, for a fuller explanation please refer to [111]. The world is made up of a set of random variables that each describe particular parts of the world. Each random variable $X$ can either be continuous or have a set of discrete states $x_i$. An event describes if a particular occurrence might occur in the world, and assigns a state to each of the random variables. A probability value between 0 and 1 is then assigned to the event to describe how likely it is to happen. The probabilities of all possible mutually exclusive events in the world must sum to 1. The full joint probability distribution represents the probability for every possible combination of states over the random variables.

The prior probability distribution (Equation 2.4) represents probability of a random variable $X$ being in state $x_1, \ldots, x_n$ when there is no other information about the state of the world. The conditional probability distribution (Equation 2.5) is used when there is some information on the state of the world that is relevant to determining some other state. It is the probability of variable $A$ being in state $a_i$ conditioned on the fact that variable $B$ is in state $b_j$.

$$P(X = x_i)$$

$$P(A = a_i | B = b_j) = \frac{P(A = a_i, B = b_j)}{P(B = b_j)}$$

The product rule shown in Equation 2.6 is a rearranged version of the conditional probability distribution, but is a key equation used to build Bayesian Networks. Bayes
The product rule (Equation 2.7) is used to invert the conditional probability distribution in cases where there is information on random variable Y, but little information on random variable X.

\[
P(A = a_i, B = b_j) = P(A = a_i|B = b_j)P(B = b_j)
\]

Equation 2.8 shows the condition that the random variable X is independent of Y. Conditional independence (Equation 2.9) states that given random variable Z the conditional probability of random variables X and Y can be broken down into independent conditional probability distributions where each random variable X and Y are conditioned on Z. Conditional independence is an important concept which is used within the Naïve Bayes classifier (shown in Equation 2.10) where the set of boolean features \( F = \{ f_1, ..., f_n \} \) are each assumed to be conditionally independent given the class variable C.

\[
P(X|Y) = P(X)
\]

\[
P(X,Y|Z) = P(X|Z)P(Y|Z)
\]

\[
P(C,F) = P(C) \prod_i P(f_i|C)
\]

### 2.5.3.2 Bayesian Networks

The simplest way to represent the full joint probability distribution for discrete variables is to use a table. This can quickly require lots of memory as the number of variables is increased, often requires a lot of data to estimate making it hard to compute, and is very poor at generalising. Using the product rule and conditional independence assumptions the full joint probability distribution can be broken down into a set of conditional probability distributions for each random variable \( X_i \) based on a set of parent nodes \( Pa_i \) it is directly influenced by (Equation 2.11).

\[
P(X_1, ..., X_i) = \prod_i P(X_i|Pa_i(X_i))
\]

This can then be represented by a Bayesian Network (also called a Belief network) [94] by using a directed acyclic graph (DAG). The random variables represent the nodes of the graph, and the edges represent the links to each node’s parents. An example DAG
is shown in Figure 2.11. To perform exact inference over the Bayesian Network can be intractable when it is a multiply connected (when there is more than one undirected path between any two nodes in the network). An alternative approach is to approximate by sampling from the Bayesian Network. The Markov Chain Monte Carlo (MCMC) algorithm [75] is a popular sampling technique, which uses a transition probability to jump between variable states. If the algorithm is run long enough the time spent in each of the variable states will approximate to the actual distribution.

![Figure 2.11: A simple Bayesian Network involving four variables: $X$, $A$, $B$, and $C$. $X$ has three parent nodes it is directly influenced by: $A$, $B$, and $C$.](image)

There are two key problems with learning Bayesian Networks: Parameter learning, and structure learning. Parameter learning relates to estimating the conditional probability distribution for each random variable in the Bayesian Network. Structure learning relates to computing the optimal set of edges between the random variables so that the underlying full joint probability distribution is well modelled, or approximated. A complete dataset has a value for each of the random variables in every example. An incomplete dataset has examples where some of the random variables are not assigned a value. When the structure is already predefined and there is a complete dataset the parameters of the Bayesian Network can be estimated directly from the dataset. When there is a complete dataset, but the structure and parameters are undefined there are a variety of approaches including genetic algorithms [62] and greedy algorithms [16, 44].

The structure of a Bayesian Network can often be simplified by introducing extra random variables into the network called hidden nodes. When the structure of the network containing these hidden nodes is fixed the problem is to estimate the parameters of the network. In the previous case this problem was easy because the parameters could be directly estimated from the dataset, as the network now contains hidden nodes an estimation of what these parameters could be needs to be found from the dataset. The EM (Expectation Maximization) algorithm [20] can be used to solve this problem. It uses an incomplete dataset where the data for the hidden variables is unknown. The parameters
are computed in two steps. Firstly the expectation step uses the current parameters and the incomplete dataset to compute the possible distribution of values for the hidden variables. Secondly, in the maximisation step each the possible values for the hidden variables are used to create a complete dataset, which is used to update the parameter values.

### 2.5.3.3 Combining first order logic and probability

Section 2.5.2 looked at predicting, or classifying an example by using a set of first order logic production rules. Here it was assumed that the examples were deterministic, and there was no way to assign a probability to how likely the prediction or classification was. This section will review methods for assigning probabilities to examples, and production rules, so that the likelihood of a prediction, or classification can be computed.

Early techniques to solve this problem come from the area of expert systems. Here the likelihood of a prediction or classification produced by a production rule is based on the likelihood of the production rule, and the likelihood of the examples used in the rule. Bayes rule [43] and certainty theory [116] have been used to represent this probability. The probabilities are typically hand-defined, and the technique only allows the probability of production rule to be based on a sub-set of examples it uses from the knowledge base.

An alternative approach comes from Probabilistic Logic Learning [104] which combines probability, logic, and learning techniques. Probabilistic logic learning upgrades, or generalises, standard probabilistic representation techniques to incorporate logical clauses. The previous approaches only allowed the likelihood of a single production rule to be estimated based on a sub-set of examples it matches. Probabilistic logic learning however allows the likelihood to be computed of a set of production rules based on how well they match or predict a set of examples.

Haddawy [40] describes a Bayesian Network using first order logic sentences. A knowledge base is used to store the structure of the network. Each sentence has its own conditional probability table that relates its value to the values of its parent sentences. Checks are performed to ensure that the sentences will build a valid Bayesian Network. To perform inference over the knowledge base a set of examples in the form of ground logic statements and a grounded query term are required. A network generation algorithm uses the knowledge base to backward chain from the query until a grounded Bayesian Network is produced that includes the examples. Inference is then performed over the grounded Bayesian Network to produce the probabilistic likelihood of the query. This approach uses a hand defined set of logical sentences to describe the Bayesian Network. Kersting and De Raedt [53] developed an approach called Bayesian Logic Programs (BLP), where both the logical clauses, and their parameters can be learnt. Bayesian Logic Programs require a set
of Bayesian clauses, a set of conditional probability distributions, and a set of combining rules. A Bayesian clause is the same as a range-restricted Horn clause except each of the atoms and predicates have a finite domain, defined by the states of random variables. Each Bayesian clause has an associated conditional probability distribution representing the probability of the state of the head, given the state of the body. Combining rules are used to combine the conditional probability distributions of two Bayesian clauses that have different bodies, but the same head. Structure learning is performed by applying a greedy structure learning method to the initial results from the knowledge discovery system CLAUDIEN [103]. This adds and deletes atoms from each of the clauses and keeps the one which keeps the network acyclic and has the best results. This repeats until there is no change in the score.

Similar approaches have been used by Koller and Pfeffer to combine frame based systems [57], and relational databases [33] with Bayesian Networks. In [57] each class frame has a set of slots added to it which describe its values, its parent frames, and a conditional probability distribution that computes the likelihood of its value based on the values of its parents. A knowledge based model construction method is then used to take a set of frame instances and build a Bayesian Network. This work is extended in [33] to relational databases where a probabilistic relational model (PRM) is used to represent the probability distribution. A greedy search method is used to learn the structure and parameters of the PRM.

Markov Logic Networks [106] generalise Markov networks. A Markov network (also called a Markov random field) models the joint probability distribution of a set of random variables. It uses an undirected graph and a set of potential functions. Each variable is a node in the graph, and each potential function scores the value for a specific clique (group of neighbouring nodes) in the graph. The joint probability is computed by setting each variable to a specific value, and then multiplying together the values for the cliques. This value is then normalised by summing joint probability for every possible combination of values for the variables. A Markov Logic Network uses a first order knowledge base containing a set of constants, and a set of first order sentences where each sentence is assigned a real number. This is used to produce a Markov network where each node is a grounded predicate. The potential functions are replaced by using the exponential sum of the number of true groundings for each first order sentence in a specific world weighted by its real number. To compute the joint probability of the Markov network it is assigned a specific world. Each world assigns a true or false value to each of the grounded predicates. Then the probability of this world over all other worlds is computed. Markov Logic Networks can be learnt by using a greedy beam search [55], but this can get trapped
in local optima. Biba et al. [9] overcomes this problem by using an iterative local search technique.

Stochastic Logic Programs [18, 83] are a generalisation of stochastic context-free grammars and HMMs. Stochastic Logic Programs are used in this thesis (Chapters 4 to 6). A stochastic logic program (SLP) contains a set of first order range-restricted definite clauses, where each clause has a value associated with it. Range-restricted means that every variable that appears in the head of the clause must appear in the body. A pure SLP is one where all the clauses have values, and an impure SLP is one where some of the clauses have values. A normalised SLP is one where the values for clauses having the same head sum to 1, and an un-normalised SLP is one where the values do not sum to 1. The probability distribution over SLPs is defined using the set of derivations of a particular query. From this three probability distributions can be produced. The probability distribution over the set of derivations, the probability distribution over the set of refutations (these are successful derivations), and the probability distributions over atoms (this is based on the outcome from the refutations). Muggleton [84] describes a two-phase approach to learn SLPs. Firstly a set of Horn clauses are learnt using Progol, and then parameters for each clause is computed by looking at the probability of each clause based on to the frequency with which the clause is involved in the proofs of the positive examples. The failure-adjusted maximisation (FAM) [18], can also be used to estimate the parameters for normalised SLPs. FAM is based on the EM algorithm with an adjustment made for failure derivations. Muggleton shows in [81] an analytical solution to learn the parameters and structure of the SLP at the same time, however there is no current implementation of the approach. A comparison with BLPs is made in [98] where it was shown that BLPs can encode the same information as SLPs, and by applying combining functions to SLPs they can encode the same information as BLPs.

This section has showed techniques that combine logic and probability, so that the likelihood of a set of production rules over a set of examples can be computed. The method described in Chapters 3 and 4 predicts the possible sets of spatio-temporal data by using the first sub-set of the history the production rules match, so only computes the possible set of predictions based on a sub-set of examples rather than over all examples. This makes it similar to approaches from expert systems explained at the start of this section. The technique in this thesis could be expanded by finding all possible matches for the production rules in the history, and then producing a distribution over all predicted spatio-temporal data. This is not explored in this thesis, but could be investigated in future work.


2.6 Evolutionary search

Evolutionary search is based on Darwin’s theory of natural selection and the survival of the fittest. It works well in search spaces with a large number of local minima, or maxima, where local or greedy search techniques will often fail to find the correct solution. This section will first give an overview of evolutionary search, then it will talk about two main evolutionary searches: genetic algorithms and genetic programming. A variant on genetic programming is used in this thesis to learn the predictive models (Chapter 4).

2.6.1 Overview of evolutionary search

Evolutionary search works in the following manner, see Figure 2.12. Firstly, a population of randomly generated individuals is produced. Next a fitness function is used to assign a fitness value to each individual of the population. Then individuals of the population are selected based on their fitness and a set of genetic operators is used to combine them, which creates a new population. The individuals are then scored again, and a check is made to see if a specific number of generations have passed, or an individual of a specific fitness has been found. If this is the case then the fittest individual from the population is returned, otherwise the process is repeated.

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The next few sections will look at different techniques to represent individuals in the population, different fitness and selection methods, different genetic operators, methods
to reduce the complexity of the final solution and finally methods to prevent bloat and improve population diversity.

### 2.6.2 Representation

The two main techniques to represent the individuals in the population are binary strings, or trees. Genetic Algorithms (GA) [37] use a binary string which is typically of a fixed length and Genetic Programming (GP) [58] (with a good overview in [95]) uses a tree based representation. Some other representations include [52] which uses a linear sequence of instructions, and [77] which uses an indexed graph.

In GAs the binary string encodes the possible solutions. To create the initial population a random set of binary strings is generated. In GP trees are made up of terminals and functions. Terminals can be constants, variables, or functions with no arguments, and they appear in the leaf nodes of the tree. Functions are standard computer programming functions for example +, AND, or SIN and they appear in the nodes of the tree. A leaf node is a node which does not have any child nodes. A root node is a node which does not have any parent nodes. The depth of a node is defined as the number of edges that are traversed from the root node to the node. The maximum depth is defined as the depth of the deepest leaf node. Figure 2.13 shows a GP program representing the equation \(1 + x^2\).

![GP tree](image.png)

**Figure 2.13:** An example GP binary tree which is representing the function \(1 + x^2\).

The function nodes are * and +, and the terminal nodes are 1, and \(x\). The root node is +, and the depth to the 1 node is 1, and the maximum depth is 2. The trees evaluated in a depth first manner.

In Koza’s original research work on GP [58] all the functions used in the tree had to exhibit a property called closure. This is the ability for a function to be able to handle arguments of any datatype and any value. The key idea behind closure is that a tree can still be evaluated using any arbitrary set of functions. This creates two main problems. Firstly each function must be written to handle the output of every other function, which
can often make it hard to write. Secondly, there is a large set of possible ways to combine
the functions which produces a large set of possible trees some of which are nonsensical.
An alternative approach is to impose a typing to the tree; this only allows functions and
terminals to connect together if the function can handle the data produced by the terminal
or function, reducing the size of the search space. Strongly Typed Genetic Programming
[79] assigns a hand defined type to each terminal, and to each function it assigns a hand
defined a type for each of its arguments, and the type of data it returns. Checks are
performed when the tree is initially generated, or altered to ensure that for all functions
the type of its child nodes match the type of its arguments.

There are two techniques that can be used to produce the initial trees: the Full method,
and the Grow method. The Full method ensures the depth of the terminals in the tree are
all at the maximum depth. This is achieved by only using functions at all depths other
than the maximum depth. At the maximum depth only terminals can be used. In the
Grow method either a function or a terminal is used at every depth other than maximum
depth. Again, at the maximum depth a terminal is picked. To produce an initial population
containing a large range of tree depths and structures Ramped half and half [58] is used.
This generates trees from a hand defined minimum depth to a maximum depth using both
the Full and Grow methods in equal proportion.

2.6.3 Fitness methods

To assign a fitness to individuals in the population a fitness function is required. This
assigns a score to each individual in the population based on how well it solves the task to
be completed. Koza [58] describes four fitness methods: raw fitness, standardised fitness,
adjusted fitness, and normalised fitness. Raw fitness is in terms of the problem to be
solved. It compares the individual against a number of fitness cases, or examples. For
example with the path example there will be a number of different situations of a person
walking along the path, and the raw fitness will be the number of times an individual in
the population correctly predicts which fork the person will take. Raw fitness is typically
based on error. This is produced by computing for each example the difference between
the example’s output and individual’s output; and then summing the results. Raw fitness is
used in this thesis, described in Section 4.7, scores how well the predictive models predict
from a set of history. To compute the fitness the predictive model is applied at each point
in the history to produce a prediction. This prediction is compared against the data at the
next time point in the history to produce a predictive match score. The fitness is produce
by computing the average predictive match score over the history.
Standardised fitness changes the raw fitness so that a lower value is better than a higher value, where a value of 0 is best. This is shown in Equation 2.12 where $r_{\text{max}}$ is the largest possible raw fitness value, and $r(i)$ is the raw fitness of individual $i$.

$$s(i) = r_{\text{max}} - r(i) \quad (2.12)$$

Adjusted fitness (shown in Equation 2.13) emphasizes small changes in standardised fitness, this allows greater separation of the fitness of individuals when the fitness starts to converge in later generations.

$$a(i) = \frac{1}{1 + s(i)} \quad (2.13)$$

Normalised fitness is computed from the adjusted fitness (Equation 2.14). It is the individual’s adjusted fitness, normalised by the total adjusted fitness for the population. Normalised fitness assigns a larger value to individuals with higher fitness, and can be used by fitness proportionate selection described in the next section.

$$n(i) = \frac{a(i)}{\sum_{k=1}^{M} a(k)} \quad (2.14)$$

### 2.6.4 Population sampling methods

Population sampling methods, as described in Section 2.6.1, are used to select individuals from the population based on its expected value. The *expected value* of an individual is the expected number of times the individual will be selected to reproduce and is based on the individual’s fitness. These individuals will then be given to the genetic operators (described in the next section) to produce a new population. It is important that the population sampling method does not sample excessively from the very fit individuals, which would create a new population dominated by these individuals. This will reduce diversity (explained in Section 2.6.7) causing the population to prematurely converge. Conversely, if the population sampling method does not sample enough from the fitter individuals of the population it will take a long time to find an optimal solution.

In fitness proportionate selection [48] the “expected value” of an individual is based on its fitness divided by the total fitness of all individuals in the population. Individuals with higher fitness will have a higher expected value, and therefore will reproduce more. There are two methods to implement fitness proportionate selection: roulette wheel sampling, and stochastic universal sampling (SUS). Roulette wheel sampling is equivalent to allocating space on a circular wheel based on the fitness of each individual. The wheel
is then virtually spun to select an individual. This repeats until the number of individuals required for the new population are selected. In roulette wheel an individual can be selected a large number of times more than its expected value. This could cause a very unfit or very fit individual to dominate in the new population. Stochastic Universal Sampling [6] is an approach to solve this problem. Instead of spinning the roulette wheel \( n \) times based on the individuals required for the new population the wheel is spun once, but has \( n \) equally spaced pointers on it which are used to select the individuals. The main problem both of these fitness proportionate selection methods is that they are biased to pick fitter individuals in the population in early generations. These fitter individuals will then dominate the population, reducing diversity and ultimately causing the evolutionary search to prematurely converge.

There have been a number of methods to solve these problems, which scale the raw fitness of an individual to an expected value. Sigma scaling [31] keeps the selection pressure at a constant value for the entire run. The selection pressure is the how much of the population is dominated by highly fit individuals. An individual’s expected value is based on the its fitness, and the mean and standard deviation of the population. Boltzmann selection [38] allows the selection pressure to vary during the run. A temperature is used to control the selection pressure where a high temperature means a low selection pressure. Over the run the temperature is lowered which increases the selection pressure, allowing the population to focus on the fitter individuals.

Alternative techniques to using fitness proportionate selection are: tournament selection, and rank selection. Tournament selection [37] picks \( n \) individuals at random from the population, and returns the one with the best fitness. Larger values for \( n \) cause the method to sample more often from the fitter individuals in the population. Rank selection bases the expected value of an individual on its rank rather than its actual fitness. This is performed by sorting the individuals by their fitness and assigning them a number from 1 to the size of the population. In this thesis tournament selection is used (Chapters 4 to 7). Rank selection [5] prevents highly fit individuals from dominating the population, but it can slow down the search.

### 2.6.5 Genetic operators

In a Canonical GA [130] the sampling method is firstly used to create an intermediate population which is the same size as the current population. Subsequently two binary strings are selected at random, without replacement, from the intermediate population. One point crossover [37] is used to change the two binary strings. A cut point on the
binary string is selected, and each binary string has the contents past the cut point swapped over with the contents from the other binary string. If crossover is not performed the binary strings are left unchanged. Mutation is performed on the two binary strings with a small probability each bit in the binary string is randomly changed. The two binary strings are then added to the new population. This process repeats until the intermediate population is empty.

GP uses similar genetic operators, but does not use an intermediate population, and it does not combine the operators together. The crossover operator [58] selects two trees from the population, and randomly picks a sub-tree on each program: these two trees are swapped over and are added to the new population. Figure 4.5 shows crossover performed on two trees. The mutation operator [58] selects one tree from the population, randomly picks a sub-tree on it, and replaces it with a randomly generated sub-tree. Figure 2.15 shows mutation performed on a single tree. The reproduction operator [58] selects a tree from the population and adds it to the new population.

![Crossover diagram](image1.png)

**Figure 2.14: Crossover performed on two trees.**

![Mutation diagram](image2.png)

**Figure 2.15: Mutation performed on a tree.**
2.6.6 Reducing the complexity of evolving solutions in Genetic Programming

Normally in GP the program is represented as one tree. However, to solve many problems repeated use of the same code is required. To do this with one tree requires GP to evolve the repeated pieces of code separately in the correct parts of the tree, which can often be difficult for large problems. A better solution is to break up the tree so that it has sub-trees that represent the repeated pieces of code, and a result sub-tree that uses the code sub-trees when it is evaluated. Koza et al. [59] use this approach by replacing the tree with a result producing branch and a set of Automatically Defined Functions (ADFs). The ADFs represent different pieces of repeated code, and the result producing branch is used to call them (Figure 2.16). Different function and terminal sets can be given to each of the ADFs, and the result producing branch which allows the ADFs to evolve different pieces of repeated code. The number of ADFs for each individual is fixed. A change is made to the crossover operator to only allow sub-trees from the same ADF or result producing branch to be swapped over. To allow GP to automatically learn how many ADFs to use Koza [60] introduced architecture altering operations. These allowed ADFs to be created, and deleted within an individual, but there was no method to copy ADFs between individuals. Evolutionary pressure will then decide the optimal number of ADFs to use. Chapter 4 shows similar approach to represent the predictive models used in this thesis, where each ADF is a production rule, and the result producing branch is a conflict resolver to decide how to use the production rules to predict in a specific context. This chapter also introduces operators that can add and replace production rules from different predictive models.
Instead of forcing the architecture of the trees to contain sub-trees representing the repeated code another approach is to use one GP tree, but to freeze sub-trees within a tree so they cannot be changed. Evolutionary Module Acquisition (EMA) [2] randomly picks a GP tree and compresses a random sub-tree, replacing it with a function call. This allows the code within the sub-tree to be preserved. EMA can also expand functions back to their original sub-trees. Roberts et al. [108] takes a different approach. They store information on all the sub-trees in the population in a database. Initially the GP system is run multiple times. The sub-tree database for the best run is analysed and the set of \( n \) best sub-trees are added as terminals to the terminal set. Then GP is performed again using this changed terminal set. Encapsulated Genetic Programming [65] introduces pointers into the GP tree, which can point to any sub-tree within the tree. The pointers are preserved with crossover. This allows code reuse and a graph like structure to evolve.

Instead of trying to find common code within the trees, another approach is to break the population into groups of individuals that each solve a separate sub-problem. To produce a result the best individual in each group is run, and the results combined to produce an overall result. This has been successfully applied to classification problems. McIntyre et al. [73] applies niching which has been successfully used in genetic algorithms, and multi-objective optimisation [72] where individuals are ranked by their pareto-fitness. Lichodzijewski [63] uses first and second price auctions, where individuals in the population bid for classifying a class. In first price auctions the individual with the highest bid is selected, and it must pay its bid to the system. If the individual correctly predicts the class it receives a reward. In second price auctions the individual with the highest bid is again selected. If it does not correctly predict the class its bid is paid to the system. If it does predict correctly then it receives a reward, and must pay to the system the highest bid from the individual that predicted incorrectly. This incorrectly predicting individual must also pay its bid to the system. In experimentation second price auctions were found to work the best.

### 2.6.7 Bloat and diversity

Bloat and diversity are key issues when using GP. Bloat happens when trees in the population contain sub-trees that do not contain any useful code, ie. if the sub-trees were removed the tree would evaluate in the same way and get the same fitness score. Diversity looks at the range of different individuals in the population. To control bloat the size of the individuals in the population is restricted, but this can effect diversity. To allow GP to find good solutions a population of high diversity is required, but this is also more
likely to provide solutions having bloat. By controlling bloat and diversity an optimal set
of individuals can be potentially found. A comparison of bloat control methods is given
in [67]. An analysis of diversity with fitness is given in [12].

Different techniques can be used to control bloat. The simplest is to use a parsimony
term on the fitness function. It can often be hard to set how much of the fitness should be
based on the score of the tree, and how much should be based on its size. Soule [120] de-
scribes when parsimony pressure can be successfully used to control bloat. Rochat [110]
uses dynamic population sizes to control diversity and bloat. The best fitness of the cur-
rent individual is related to the initial best fitness to decide how many individuals should
be removed, or added to the population. The Tarpeian bloat control method [22] stochasti-
cally removes a percentage of the individuals at each generation that are above the average
size. This method is not as strict as parsimony pressure, and allows GP to still use larger
individuals in later generations. The Tarpeian method is used to control bloat in the our
learning technique, described in Chapter 4. The percentage of individuals removed from
the population is fixed for each run. Chapter 7 describes a technique to automatically vary
the percentage of individuals removed at each generation. An alternative bloat methods
is the waiting room [93] where individuals wait to be added to the population based on
their size. To adaptively control diversity Ekart [21] uses a fitness sharing approach that
changed the niche size based on the change in population diversity, and fitness of the best
individual in the population. The diversity metric is based on the weighted arithmetic
mean between individuals in the population.

2.7 Complete systems for learning predictive models from
video

Fern et al. [26] looked at learning event definitions from video of people picking up
and putting down a set of blocks. A raw video of a scene is converted into a polygon
representation by segmenting and tracking the blocks. The polygons are then applied
to a force-dynamic model which describes how the blocks in the scene are in contact
with each another. The scenes are temporally represented using And-Meets-And (AMA)
propositional logic. A specific-to-general learner is then used to generalise from the AMA
formulas to learn the event definitions.

Fern and Givan [25] look at learning the force-dynamic relations from the same videos
as the previous paper. An object tracker is applied to videos which outputs low-level
information on the blocks for example the distance between them and their speed. These
are then stored as a sequence of observations. A sequence of states is also produced representing the force-dynamic relations. The mapping between the observation sequence and the state sequence is then learnt using CLAUDIEN [103]. Two types of rules are used for the mapping: o-rules, and s-constraints. The o-rules map observations to a specific state. The s-constraints are used as constraints on the set of states. To produce a set of states from a sequence of observations, each of o-rules is applied to the sequence. The resulting set of states is then has the s-constraints iteratively applied to it.

Most closely to the work in this thesis is the work of Needham et al. [89] in which Horn clauses to describe the protocols of basic card games are learnt from video. The cards in the video are tracked using a blob tracker [68]. When a card was stationary for a number of frames it is assumed to be part of the game. Features from the card including texture (calculated from Gabor wavelets, and Gaussians applied at various orientations and scales), colour (calculated from a binned histogram of hue, and saturation), and position were produced. Each colour, and texture feature was independently clustered using agglomerative clustering. The clusters were then used to train a vector quantisation based nearest neighbour classifier. One of the players had their voice recorded during the games. The energy of the speech signal was analysed using a fixed length window. When the energy was over a fixed threshold spectral analysis was performed on the window, and the result was histogrammed. K-means clustering was then performed on the speech samples, to find clusters of similar speech sounds. A set of temporal facts representing the cards, and the speech sounds spoken during the game was produced. Progol was used to learn Horn clauses that could predict the speech sounds based on the properties of a set of cards. The technique cannot deal with probabilistic datasets, and has a very simple conflict resolution strategy that can cause it to predict the wrong outcome. In Chapter 4 the datasets and the technique from this paper are compared against the novel techniques described in this thesis.

Santos et al. [112] apply the same video analysis technique from the previous paper to videos of dice games. Temporal facts describing the properties of the dice were then produced. These were input into Progol and HR to learn a set of rules describing the game. As explained in Section 2.5.1.3 both methods performed well with different noise levels in the data, but overall Progol performed slightly better than HR. Again, like the previous paper the technique does not deal with probabilistic datasets.

Santos et al. [114] learn a set of rules from video to decide where best to place a camera in a scene to observe a visual task. Videos of coloured blocks being stacked in various combinations were taken. The blocks in the video were tracked using the same blob tracker from the previous papers [89]. The colour of the blocks was extracted from
the video, and a local cardinal system is used to represent their location. In a local cardinal system each object defines its own cardinal reference frame which is used to represent the location objects around it. The block data is then described as a set of symbolic relations. Progol was used to learn a set of Horn clauses from this data. The system assumes that the data is deterministic and will not be able to learn or apply non-deterministic rules.

2.8 Conclusions

This chapter has reviewed current work on learning predictive models from non-deterministic spatio-temporal data. The spatio-temporal data is generated from videos containing variable numbers of objects. The predictive models are then used to predict future spatio-temporal data, or to recognise events.

It has been shown that to represent spatio-temporal data that contains variable numbers of objects a variable length representation would be advisable. Chapter 3 shows the use of Frames to represent the spatio-temporal data used in this thesis. The spatio-temporal data describes properties of the objects, and relations between objects. In this thesis qualitative relations are used to describe object relations. Chapter 6 shows the use of both region based, and point based qualitative spatial relations. It was explained that Allen’s interval calculus can only be applied when both time intervals have a valid start and end time. Chapter 5 introduces a novel temporal relation that can represent intervals that do not have a valid end time.

The predictive models in this thesis are represented as a production system. A production system contains a set of production rules, and a conflict resolver, which decides which of the production rules to use for the prediction. Production rules in this thesis are represented in first order logic. There are multiple approaches to learn first order production rules with the best results from using stochastic search techniques, and inducing multiple production rules concurrently. Both of these conclusions have been incorporated into the approach described in this thesis (Chapter 4).

Most approaches to learning the parameters of the conflict resolver, and the first order logic production rules use a two stage approach where the first order logic production rules are learnt, and then the parameters of the conflict resolver are estimated. Recent techniques have improved on the results from the two-stage approach by learning both the parameters of the conflict resolver and the production rules simultaneously. The same idea has been used to learn the production rules, and the conflict resolver in this thesis (Chapter 4). The probability distributions used within the conflict resolvers use simple Bayesian Networks, the technique described in Chapter 4 uses a full Bayesian Network.
This allows for a better modelling of dependencies between the production rules.

A genetic programming based approach is used to learn the predictive models. A similar idea to ADFs is used where the result producing branch represents the conflict resolver and each ADF represents a production rule. However, unlike ADFs, production rules may be swapped or added to different production rules. The Tarpeian bloat control method is used in this thesis to control the size of the individuals in the population. The Tarpeian bloat control method uses a fixed Tarpeian value for the entire of the run. Chapter 7 investigates a technique to vary the amount of downward pressure on the size of the predictive models in the population over the course of the run.
Chapter 3

An Architecture for Representing, and Modelling Spatio-Temporal Data

3.1 Introduction

This chapter outlines an approach for representing and modelling spatio-temporal data. Chapter 4 will then explain how a predictive model can be learnt from spatio-temporal data based on this approach. Figure 3.1 shows the architecture that has been developed within this work. It is broken down into two parts: a observation history data representation (for the rest of this thesis it will be called history), and the predictive model representation. A history represents the previous and current set of spatio-temporal data relative to the current time. The history is input into a predictive model, which predicts the most likely set of spatio-temporal data that will occur after the current time. The predictive model is based on a production system described in Section 2.5. The production rules describe the different possible patterns in the history and their possible outcomes. A conflict resolver then decides how to use the production rules to predict in different contexts.

Section 3.2 explains in more detail how the history is represented. Section 3.3 explains how the predictive model is represented. Finally, Section 3.4 explains an inference procedure to allow a predictive model to predict from a set of history.
Figure 3.1: An architecture to represent and model spatio-temporal data. It has three parts: a history; and a predictive model which is input the history; and produces a prediction. The predictive model is broken down into two parts: a set of production rules, and a conflict resolver.

3.2 History representation

The history represents the set of previous and current spatio-temporal observation data. The spatio-temporal data contains entities, and relations. Entities represent objects, groups of objects, or parts of objects. Relations represent any relations between entities for example spatial or temporal. Section 2.3 described two main representation techniques for spatio-temporal data: fixed length, and variable length. A fixed length representation would not be appropriate here, because the datasets used in this thesis contain variable numbers of objects and object relations that last for variable lengths of time. To solve this problem Frames [78] (described in Section 2.3.4) are used to represent the history in this thesis. Each of the entities and relations require a definition represented by a class frame. Entities or relations that appear in the history are instances of these definitions with constant properties, represented by an instance frame. Properties represent the phys-
Practical properties of an entity or relation, for example its speed, height or colour. These also require a definition, and instances are produced when the entities and relations using the properties appear in the history. These concepts are described in more detail in the following sections.

### 3.2.1 Properties

*Properties* are used to describe physical properties of an entity, or relation. In this work they are defined globally, and are not associated with a particular type of entity, or relation. This allows the properties of different types of entities or relations to be easily compared.

Properties consist of a set of attributes. An *attribute* stores data on a property, for example the property *position* might have two attributes *x* and *y* that store the actual position of the object. Firstly attributes will be explained, and then properties will be explained.

An attribute must first be defined by using a class frame. All attribute class frames contain the following slots: Name, Type, Value and Probability. The Name slot contains the instance name of the attribute (which is used as an identifier), the Type slot contains the data type of the attribute, the Value slot contains the value of the attribute, and the Probability slot contains the likelihood of this value. The Type slot can take one of three values: symbolic, integer, and float. To control which data the Value slot can contain the facet ValueRange is used. For the symbolic type this is a list of the symbols, and for the float, and integer types it is a range of possible values. In each attribute class frame, the value for the type slot is completed, along with the ValueRange facet. The remaining slots are left blank and are completed when an instance of the attribute class frame is created.

Properties are defined in a similar manner. All properties are defined using their own class frame. This class frame contains a Name slot, which stores the instance name of the property, and slots for each of the attributes the property uses. The attribute and Name slots are initially blank, and are completed when an instance of the property class frame is produced. An example will now be introduced that will be used throughout the rest of this section to explain the different concepts. The example extends the path example given in Section 2.1 by allowing both people and cars to appear on the path. Information on the *x*, *y* position of the cars and people is recorded, along with the colour of the people and the cars. Figure 3.2 shows three attribute class frames: *X*, *Y* and *ColourName*. The *X* and *Y* attributes are both of type integer, and the range of values they can take is from 0 to 255. The *ColourName* attribute is of type symbolic, and can only have values Green, Red, or Blue. These attributes are used by two properties: Position and Colour.
Chapter 3 An Architecture for Representing, and Modelling Spatio-Temporal Data

<table>
<thead>
<tr>
<th>Class</th>
<th>X</th>
<th>Class</th>
<th>Y</th>
<th>Class</th>
<th>ColourName</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td></td>
<td>Name</td>
<td></td>
<td>Name</td>
<td>Symbolic</td>
</tr>
<tr>
<td>DataType</td>
<td>Int</td>
<td>DataType</td>
<td>Int</td>
<td>DataType</td>
<td></td>
</tr>
<tr>
<td>Value</td>
<td></td>
<td>Value</td>
<td></td>
<td>Value</td>
<td>Symbolic</td>
</tr>
<tr>
<td>ValueRange</td>
<td>[0 - 255]</td>
<td>ValueRange</td>
<td>[0 - 255]</td>
<td>ValueRange</td>
<td>Green, Red, Blue</td>
</tr>
<tr>
<td>Probability</td>
<td></td>
<td>Probability</td>
<td></td>
<td>Probability</td>
<td></td>
</tr>
</tbody>
</table>

Figure 3.2: Property and attribute examples. The top row shows the class frames for the attributes: X, Y, ColourName. The bottom row shows the class frames for the properties: Position and Colour.

The Position property’s class frame has slots the X and Y attributes, and the Colour property’s class frame has a slot for the ColourName attribute.

3.2.2 Entities

Entities describe objects, collections of objects, or collections of object parts. This section will firstly cover how entities are defined by using entity class frames, and then it will describe entity instances represented by instance frames.

3.2.2.1 Entity definition

All entity definitions are described by an entity class frame. All entity class frames have the slots: Name and Time. They also have slots to store the properties that the entity uses. An entity class frame may also inherit (in an object oriented sense) from other entity class frames. The Name slot stores the name of the entity instance, and the Time slot is used to describe the temporal scope of an entity instance over which its properties are constant.

Table 3.1 shows the four possible types of values the time slot can contain: Point, Period, AllTime, and Incomplete. The Point time type is used to represent an entity existing for an instantaneous period of time, which could represent a quantised time period. The Period time type is used to represent an entity instance that exists for a range of time. The range is described by the start and end time of the entity or relation instance. The AllTime type is used to represent an entity instance that always exists in the history. It therefore exists from the beginning of time (−∞) to the end of time (∞). Finally, the Incomplete time type represents an entity instance that exists, but the end time is unknown. The end time is...
represented by *Unknown*. This is used when an entity instance still exists at the current time.

<table>
<thead>
<tr>
<th>Time type</th>
<th>Temporal range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Point</td>
<td>([t_s, t_s + \delta])</td>
</tr>
<tr>
<td>Period</td>
<td>([t_s, t_e])</td>
</tr>
<tr>
<td>AllTime</td>
<td>([-\infty, \infty])</td>
</tr>
<tr>
<td>Incomplete</td>
<td>([t_s, Unknown])</td>
</tr>
</tbody>
</table>

Table 3.1: The four time types: Point, Period, AllTime and Incomplete. They are defined by temporal ranges. Variable \(t_s\) represents the start time of the entity or relation instance, and \(t_e\) represents the end time of the entity or relation.

Initially all slots are blank, and are completed when an instance of the entity class frame is produced. Figure 3.3 shows two entity class frames one for a *Car*, and the other for a *Person*. They both use the same set of properties: *Colour* and *Position*.

<table>
<thead>
<tr>
<th>Class</th>
<th>Car</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td></td>
</tr>
<tr>
<td>Time</td>
<td></td>
</tr>
<tr>
<td>Colour</td>
<td></td>
</tr>
<tr>
<td>Position</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Person</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td></td>
</tr>
<tr>
<td>Time</td>
<td></td>
</tr>
<tr>
<td>Colour</td>
<td></td>
</tr>
<tr>
<td>Position</td>
<td></td>
</tr>
</tbody>
</table>

Figure 3.3: Two example entity class frames, which use the properties shown in Figure 3.2. The first class frame is for a *Car*, and the second is for a *Person*.

### 3.2.2.2 Entity instance

Entity instances are represented by entity instance frames which are instances of a specific entity class frame. The values for the *Name* and *Time* slots are completed along with creating instance frames of the property, and attribute class frames that the entity uses. The property slot values in the entity instance frame are then completed with the instance name of the property instances. Figure 3.4 shows two entity instance frames, one for a *Person*, and the other for a *Car*. The *Car* entity instance frame is an instance of the *Car* class frame. It existed between times 0 to 8. During this time it was in position (200,700) and had a colour of Green. The *Person* entity instance frame is an instance of the *Person* class frame. It existed between times 4 to 8. During this time it was in position (250,350) and had a colour of Blue.
**Attribute instance frames**

<table>
<thead>
<tr>
<th>Class</th>
<th>X</th>
<th></th>
<th>Class</th>
<th>Y</th>
<th></th>
<th>Class</th>
<th>ColourName</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>X1</td>
<td></td>
<td>Name</td>
<td>Y1</td>
<td></td>
<td>Name</td>
<td>ColourName1</td>
</tr>
<tr>
<td>DataType</td>
<td>Int</td>
<td></td>
<td>DataType</td>
<td>Int</td>
<td></td>
<td>DataType</td>
<td>Symbolic</td>
</tr>
<tr>
<td>Value</td>
<td>200</td>
<td></td>
<td>Value</td>
<td>700</td>
<td></td>
<td>Value</td>
<td>Green</td>
</tr>
<tr>
<td>ValueRange</td>
<td>[0 - 255]</td>
<td></td>
<td>ValueRange</td>
<td>[0 - 255]</td>
<td></td>
<td>ValueRange</td>
<td>Green, Red, Blue</td>
</tr>
<tr>
<td>Probability</td>
<td>100%</td>
<td></td>
<td>Probability</td>
<td>100%</td>
<td></td>
<td>Probability</td>
<td>100%</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>X</th>
<th></th>
<th>Class</th>
<th>Y</th>
<th></th>
<th>Class</th>
<th>ColourName</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>X2</td>
<td></td>
<td>Name</td>
<td>Y2</td>
<td></td>
<td>Name</td>
<td>ColourName2</td>
</tr>
<tr>
<td>DataType</td>
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<td></td>
<td>DataType</td>
<td>Int</td>
<td></td>
<td>DataType</td>
<td>Symbolic</td>
</tr>
<tr>
<td>Value</td>
<td>250</td>
<td></td>
<td>Value</td>
<td>350</td>
<td></td>
<td>Value</td>
<td>Blue</td>
</tr>
<tr>
<td>ValueRange</td>
<td>[0 - 255]</td>
<td></td>
<td>ValueRange</td>
<td>[0 - 255]</td>
<td></td>
<td>ValueRange</td>
<td>Green, Red, Blue</td>
</tr>
<tr>
<td>Probability</td>
<td>100%</td>
<td></td>
<td>Probability</td>
<td>100%</td>
<td></td>
<td>Probability</td>
<td>100%</td>
</tr>
</tbody>
</table>

**Property instance frames**

<table>
<thead>
<tr>
<th>Class</th>
<th>Position</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>Position1</td>
</tr>
<tr>
<td>X</td>
<td>X1</td>
</tr>
<tr>
<td>Y</td>
<td>Y1</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Position</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>Position2</td>
</tr>
<tr>
<td>X</td>
<td>X2</td>
</tr>
<tr>
<td>Y</td>
<td>Y2</td>
</tr>
</tbody>
</table>

**Entity instance frames**

<table>
<thead>
<tr>
<th>Class</th>
<th>Car</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>Car1</td>
</tr>
<tr>
<td>Time</td>
<td>Period (0,8)</td>
</tr>
<tr>
<td>Colour</td>
<td>Colour1</td>
</tr>
<tr>
<td>Position</td>
<td>Position1</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Person</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>Person1</td>
</tr>
<tr>
<td>Time</td>
<td>Period (4,8)</td>
</tr>
<tr>
<td>Colour</td>
<td>Colour2</td>
</tr>
<tr>
<td>Position</td>
<td>Position2</td>
</tr>
</tbody>
</table>

Figure 3.4: Two entity instance frames, which are instances of the entity class frames from Figure 3.3. Firstly the attribute, and property instance frames that the entity instance frames use are shown, and then the entity instance frames are shown.
3.2.3 Relations

Relations describe relationships that exist between multiple entities for example spatial or temporal relations. Firstly the relation definitions, represented by relation class frames, will be described; and secondly the relation instances, represented by instance frames, will be described.

3.2.3.1 Relation definition

Each relation definition requires its own class frame. All relation class frames have the following slots: Name and Time. The Name slot stores the name of the relation instance, and the Time slot stores the amount of time the relation instance existed for. The Time slot is represented in the same way as for entity definitions and entity instances (described in Section 3.2.2.1). Slots are also added to store the entity instances the relation uses. Facets are added to each entity slot to store which types of entities the relation can use. Property slots can also be added to store information on the relation. Relation class frames can also inherit from other relation class frames. Figure 3.5 shows the relation class frame for relation Left Of. It requires two slots to store the entity instances the relation uses, and two facets Type1, and Type2 which control the type of entities the relation can use, in this case Car and Person.

<table>
<thead>
<tr>
<th>Class</th>
<th>Left Of</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td></td>
</tr>
<tr>
<td>Time</td>
<td></td>
</tr>
<tr>
<td>Type1</td>
<td>Car</td>
</tr>
<tr>
<td>Type2</td>
<td>Person</td>
</tr>
<tr>
<td>Entity1</td>
<td></td>
</tr>
<tr>
<td>Entity2</td>
<td></td>
</tr>
</tbody>
</table>

Figure 3.5: The Left Of relation definition. The relation represents that a car is to the left of a person.

3.2.3.2 Relation instance

A relation instance is an instance of a particular relation definition. It is stored in an instance frame and created by using the relation class frame and filling in the values for the Name, Time and Entity slots. Figure 3.6 shows an example relation instance for the Left Of relation. It is an instance of the Left Of relation class frame. It existed between time values 4 to 9 and used entities Carl and Person1.
## System implementation

To implement the history representation within the computer requires two elements: a file format, and a memory representation described in the sections below.

### File format

XML [10] was chosen as the file format, because it is easy to parse, is human readable, and there is a large body of tools for analysing and displaying data written in XML. Figure 3.7 shows the Person1 entity instance from Figure 3.4 represented in XML. The probability and attribute instance frames are stored as sub-frames within the entity instance frame rather than describing them separately. This allows for a more compact and easy to read representation.

### Memory representation

To read the XML datafiles into the computer requires an XML parser and a memory representation. There are two main memory representations that can be used. The first is to use a fixed time unit like seconds, or hours. The state of the history at each time unit is then stored. The problem with this representation is that the unit needs to be decided a priori. If a large scale time unit (like days) is used it can lead to loss of data, and if a small scale time unit (like milliseconds) is used data can be duplicated. The second representation takes a different approach. Instead of representing the history at specific time points it represents it by changes in its state. A state change is caused by adding, removing or changing an entity or relationship instances in the history. The possible reasons an entity or relation instance will change its state are: changing its properties, or changing it time range. This is a more compact representation because duplicated data is merged together, and data cannot be lost as every history state change is represented.
Figure 3.7: An example of the Person1 entity instance from Figure 3.4 represented in XML.

representation was used in this thesis.

3.3 Predictive model representation

A predictive model uses a set of spatio-temporal history data to predict the most likely set of spatio-temporal data to occur next. More formally it uses a set of history data $H_{1:T} = \{h_1, ..., h_T\}$ where each history item $h_t = (K_t, L_t)$ is a tuple containing a set of entities $K_t$ and a set of relations $L_t$ that exist at time $t$; and computes the probability of a set of spatio-temporal data $h_{t+1}$ occurring at the next time step as shown in Equation 3.1.

$$P(h_{t+1} | H_{1:T})$$ (3.1)

In this thesis the predictive models are represented using a production system (as described in Section 2.5). This requires two elements: a set of production rules, and a conflict resolver. Each production rule contains a condition section that matches a specific subset of the history, and an action section that represents a new entity or relation. The production rules are explained in more detail in Section 3.3.1. To make a prediction the production rules are applied to the history. A conflict resolver is used to decide
which of the production rules matching the history to use for the prediction. The conflict resolver used in this thesis uses a conditional probability distribution (Equation 3.2), where \( r_i \) is a boolean random variable that represents if production rule \( p_i \) is enabled on the history \( (r_i = enabled(H_{1:T}, p_i)) \), \( n \) is the number of production rules, and \( u_i \) is a boolean random variable that represents if production rule \( i \) should be fired. The production rules that should be fired are used to produce the prediction at the next time step \( (h_{t+1} = fire(u_1, ..., u_n)) \). The probability distribution is represented by a Bayesian Network, and can produce multiple sets of predictions each with an associated probability. This allows the conflict resolver to predict from non-deterministic data.

\[
P(h_{t+1}|H_{1:T}) = P(u_1, ..., u_n|r_1, ..., r_n) 
\]

(3.2)

To illustrate how this approach works let’s introduce an example based on a simplified version of the children’s card game Uno. This example will be used throughout the rest of this chapter to illustrate the different concepts with the predictive models.

The game is played by two people each having a set of cards containing different coloured pictures on them. In each round of the game each player puts down a card. If the cards both have the same picture, and colour then “Same” should be shouted out. If the cards have the same picture, but different colours then “Shape” should be shouted out. If the cards have the same colour, but different pictures then “Colour” should be shouted out. Finally if the two cards are different then “Nothing” is said.

A set of production rules that represents the game of Uno is shown in Figure 3.8 and the probability distribution for the conflict resolver is shown in Table 3.2. This only lists the entries that have a probability greater than zero. All other entries have a probability of zero, and therefore are not used to produce a prediction. Table 3.2 shows that, for example, if the only production rule \( r_1 \) matches the history than only its output \( (o_1) \) with probability 1.0 should be fired.

\[
\begin{align*}
\text{r1: } & \text{IF SHAPE(C1) == SHAPE(C2) AND COLOUR(C2) == COLOUR(C2) } \\
& \text{THEN SAME} \\
\text{r2: } & \text{IF SHAPE(C1) == SHAPE(C2) AND COLOUR(C2) != COLOUR(C2) } \\
& \text{THEN SHAPE} \\
\text{r3: } & \text{IF SHAPE(C1) != SHAPE(C2) AND COLOUR(C2) == COLOUR(C2) } \\
& \text{THEN COLOUR} \\
\text{r4: } & \text{IF SHAPE(C1) != SHAPE(C2) AND COLOUR(C2) != COLOUR(C2) } \\
& \text{THEN NOTHING}
\end{align*}
\]

Figure 3.8: A hand defined set of production rules for Uno.
This is a very simple example of how the conflict resolver works. In this case, only one production rule will be enabled on the history, and this production rule will be fired to produce a prediction. The conflict resolver, however, can deal with multiple production rules being enabled at the same time. This, as shown in the following example can, greatly simplify the complexity of the production rules required. It is used by the learning method (Chapter 4) in this thesis to reduce the size of the search space when learning predictive models, which makes it more likely an optimal solution will be found. In the Uno example the condition sections of Same and Nothing production rules ($r_1$ and $r_4$) use elements from the condition sections of the Shape and Colour production rules ($r_2$ and $r_3$), as shown in Figure 3.8. To reduce this reuse, the Same and Nothing condition sections can be represented using the Shape and Colour condition sections, shown in Figure 3.9, using the probability distribution shown in Table 3.3. The Nothing production rule is fired when the Shape, and Colour production rules are not enabled, and the Same and Nothing production rules are enabled. The Same concept is produced by firing the Same production rule, when all the production rules (Same, Shape, Colour and Nothing) are enabled.

\begin{verbatim}
r5: IF TRUE THEN SAME
r6: IF SHAPE(C1)==SHAPE(C2) THEN SHAPE
r7: IF COLOUR(C2)==COLOUR(C2) THEN COLOUR
r8: IF TRUE THEN NOTHING
\end{verbatim}

Figure 3.9: The combined production rules for Uno.

The rest of this section will show how the production rules are described, and how inference is performed on the history using a predictive model to predict future spatio-temporal data.
|   | r₅ | r₆ | r₇ | r₈ | u₅ | u₆ | u₇ | u₈ | P(u₅, u₆, u₇, u₈ | r₅, r₆, r₇, r₈) |
|---|----|----|----|----|----|----|----|----|-------------------------------|
| 1 | T  | T  | T  | T  | T  | F  | F  | F  | 1                             |
| 2 | T  | T  | F  | T  | F  | T  | F  | F  | 1                             |
| 3 | T  | F  | T  | T  | F  | F  | T  | F  | 1                             |
| 4 | T  | F  | T  | T  | F  | F  | F  | T  | 1                             |

Table 3.3: The probability distribution for the combined production rules in Figure 3.9.

### 3.3.1 Production rules

A production rule has a similar representation to a Horn clause. The condition section of the production rule is like the body of a Horn clause, as it can contain variables, statements describing objects and relations, and logical functions. The action section is the same as the head of the Horn clause. It can only contain one entity or relation, in the same way that the head can only contain one literal. To evaluate the production rule on a set of history the substitution $\theta$ is applied to the variables in the condition section ($b\theta$), which grounds the variables to a subset of the history data. If the condition section entails this data it will return back true, otherwise it will return false. Section 3.4 explains how to search for the substitution $\theta_T$, that causes the condition section to entail a specific subset of the history.

If the condition section returns true then the action section of the Horn clause is evaluated producing a new entity or relation instance. The evaluation is performed by grounding the variables in the action section using the same substitution that caused the body to evaluate true. The condition and action sections will now be more formally defined.

#### 3.3.1.1 Condition section

The condition section $b = \{F, \Lambda, C, X, E\}$ is represented by a set of functions $F$, a set of node parameters $\Lambda$, a set of constants $C$, a set of variables $X$. These are formed into a directed acyclic graph (DAG) where the nodes are constants, variables, and functions, and the edges $E$ represent links from constants to functions, variables to functions, or links between functions.

The DAG is arranged into three layers: an input layer; a processing layer; and a result layer. The input layer uses the set of variables to extract a subset of the history data. This data is presented to the processing layer containing the functions, and the constants which check if they match this data. The result layer again contains functions and returns a boolean result based on if this match was successful or not.

The variables and functions will now be more formally described. Variables are assigned an entity or relation at a specific point from the history. Each variable has a pre-
determined data type, and time range. They ensure that only entities or relations of the correct type, and within the desired time range relative to the current time can be assigned to the variable. This reduces the amount of history data that needs to be searched, and only the most relevant parts of the history are used in the processing layer.

A function \( f_i : (V_i, \lambda_i) \rightarrow v_r \) is used to compute the result \( v_r \) using the set of result values from its parent nodes \( V = \{v_1, ..., v_n\} \), and node parameters \( \lambda_i \). There are four kinds of functions: data functions, comparison functions, logical functions, and user defined functions as described below:

- **Data functions** these process the entities or relations returned from the variables. There are two functions: the \( \text{Get} \) function, and the \( \text{Exists} \) function. The \( \text{Get} \) function returns the value of a specific attribute from an entity or relation. The \( \text{Exists} \) function returns if the entity or relation instance is of a specific type.

- **Comparison functions** these produce a boolean result by performing a test on a specific attribute from an entity or entities. The standard comparison functions used are the numeric comparisons: \( \text{equal, not equal, less than, greater than, less than or equal to, and greater than or equal to} \); and the symbolic comparison: \( \text{equal} \) and \( \text{not equal} \).

- **Logical functions** these combine the results from the comparison functions to produce a boolean result. The standard logical functions defined in the system are: \( \text{And, Or and Not} \).

- **User defined functions** the user is also allowed to define their own processing functions. This can be used to add background knowledge to the condition section. The functions operate in the same way as the condition section. They are input a set of arguments, these are then processed using the same functions, and constants that can appear in the condition section, and then a result is returned.

To explain these concepts let’s use the example introduced in Section 3.3. The condition section for the Colour production rule (given in Figure 3.8) is shown in Figure 3.10. Equation 3.3 shows this written in first order logic.

\[
\text{NotEqual(GetTexture}(x)\text{, GetTexture}(y)) \land \text{Equal(GetColour}(x)\text{, GetColour}(y)) \quad (3.3)
\]

The input layer contains two variables (\( x \) and \( y \)). Each variable relates to a different card in the history. The processing section makes use of four functions: \( \text{And, Equal, Not Equal} \) and \( \text{Get} \). The \( \text{Get} \) function is used to get the colour, or the texture from the cards. The
Figure 3.10: The condition section for the Colour production rule from Figure 3.8.

The condition section uses the Equal function to check if the cards have the same colour, and the Not Equal function to check if the two cards have different textures. Finally, the And function uses the result from the Equal and Not Equal functions to check if the cards both have different textures and the same colour.

3.3.1.2 Action section

The action section of the production rule generates a new entity or relation if the condition section matches a subset of the history. To create a new entity or relation each of its properties and attributes has to be initialised. They can either be initialised to a constant; or to a variable from the condition section, along with a specific property. When the variable is grounded the property from its assigned entity or relation will be used to initialise the property in the new entity or relation. This then allows the action section to generalise from the history. The number of production rules to be learnt may be reduced because of this, which decreases the size of the search space, making an optimal solution easier to find.

In Figure 3.11 the action section for the Colour production rule is defined. It creates a new Event entity which has the value of Colour for the Speech attribute, and also has two
properties (Card1Shape and Card2Shape) representing the shape of the two cards that have been put down. The values for these properties will come from the history by using the entities assigned to the variables x and y. Equation 3.5 shows this written in first order logic, where n1 and n2 are the names of the name attributes, t1 and t2 are the textures, and p1 and p2 is the likelihood of the name attributes.

<table>
<thead>
<tr>
<th>Class</th>
<th>Speech</th>
<th>Class</th>
<th>Say</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>Speech1</td>
<td>Name</td>
<td>Say1</td>
</tr>
<tr>
<td>DataType</td>
<td>Symbolic</td>
<td>Speech</td>
<td>Speech1</td>
</tr>
<tr>
<td>Value</td>
<td>Colour</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ValueRange</td>
<td>Colour,Same,Nothing,Shape</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Probability</td>
<td>100%</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Event</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
<td>Event1</td>
</tr>
<tr>
<td>Time</td>
<td></td>
</tr>
<tr>
<td>Say</td>
<td>Say1</td>
</tr>
<tr>
<td>Card1 Shape</td>
<td>x.Texture.Name</td>
</tr>
<tr>
<td>Card2 Shape</td>
<td>y.Texture.Name</td>
</tr>
</tbody>
</table>

Figure 3.11: The action section for the Colour production rule. The text in a typewriter font shows that the value of the slot is a link to another instance frame. The Time slot is left blank, as it is filled in when the entity instance is used for a prediction.

\[
\begin{align*}
\text{Event} & (\text{Event1}, \text{Say}(\text{Say1}, \text{Speech}(\text{Speech1}, \text{Colour}, 100))), \\
\text{Card1Shape} & (\text{Texture}(x, \text{Name}(n1, t1, p1))), \\
\text{Card2Shape} & (\text{Texture}(y, \text{Name}(n2, t2, p2)))
\end{align*}
\]

### 3.4 Inference

Once a model has been produced an inference procedure is required so that it can be applied to a set of data to produce a prediction. This section describes an inference procedure for the predictive models on a set of history. More formally given a prediction model M inference needs to performed using a set of history Ht to produce a set of possible outputs \( W = \{w_1, \ldots, w_n\} \) occurring at time \( t + 1 \), where \( n \) is the number of (mutually exclusive) outputs, \( w_i = (o_i, p_i) \), and \( o_i \) is a possible output having a probability \( p_i \). The predict function \( \text{predict} : (M, H) \rightarrow W \) is used to perform this inference. The function
works in the following stages:

1. For the condition section $b$ of each production rule $s \in S$ search for the substitution $\theta_{Ts}$ that causes the condition section to entail a subset $h \in H$ of the history $H$, $(b\theta_{Ts} \models h)$.

2. The enabled set $r$ (describing how each of the production rules evaluated on the history) can then be input to the conflict resolver producing a set of possible firing sets $U = \{u_1, \ldots, u_n\}$.

3. The set of possible outputs $W$ can be computed by keeping every firing set $u_i = \{u_{i1}, \ldots, u_{iS}\}$ where $P(u_i|r) > 0$. Then $w_i$ is computed for each remaining $u_i$ by setting:
   - $o_i = \{a_{is}\theta_{Ts} \mid u_{is} = \text{true}\}$
   - $p_i = P(u_i|r)$

The possible output $o_i$ is produced by taking a firing set $u_i$, and for every production rule $s$ that should be fired (i.e. $u_{is} = \text{true}$) its action section $a_{is}$ is grounded on the substitution $\theta_{Ts}$ that caused its condition section to entail a subset of the history $(a_{is}\theta_{Ts})$. The likelihood of this output $P(u_i|r)$ is found by looking it up in the probability distribution for the conflict resolver.

To search for $\theta_{Ts}$ is a hard problem for two reasons. Firstly, it is a large search space and this can quickly get large as the size of the history, and number of variables in the production rule increases. Secondly, there are multiple possible values for $\theta_{Ts}$ and the one needs to be chosen that will be best to predict the new output.

To solve these problems the exhaustive search for $\theta_{Ts}$ initially uses history data only at the current time ie. $H_t$. If this is unsuccessful the history is extended to include the previous history items ie. $H_{t-1}$. This process is repeated until a value for $\theta_{Ts}$ is found, or the history size is above a predefined threshold. The pseudo-code for this algorithm is shown in Figure 3.12.

To explain the predict function an example from the game Uno, shown in Figure 3.13 is be used. The history contains two cards at time 1: Card 1 has a black triangle, and Card 2 has a black circle. The first stage of the function uses the predictive model for the Uno dataset, and computes which of the condition sections from the production rules will entail the history. If we use the Uno production rules from Figure 3.9 it can be seen that the production rules that apply to this history are the Colour, Same and Nothing production rules. The $\text{FindBestSubstitution}$ algorithm is applied to the condition section of
Input: Condition section ($b$), History ($H$)

Output: The best substitution ($\theta_T$) which is a list of tuples where each tuple is a mapping from a variable in $b$ to an object in $H$.

Function FindBestSubstitution

For $s = 1$ to max history size
  Assign $h$ to a subset of $H$ of size $s$
  Foreach variable $v$ in $b$
    Find all objects in $h$ that have the same type as $v$,
    and occur within its time range.
  End Foreach
  Foreach substitution $\theta$ in the set of possible variable to object assignments
    If $b\theta$ =true Then
      Return $\theta$
    End If
  End Foreach
End For

Figure 3.12: The FindBestSubstitution algorithm.

Figure 3.13: An example game of Uno.

these production rules to find where they match the history. For example by applying the FindBestSubstitution algorithm to the condition section of the Colour production rule (shown in Figure 3.10) the value for $\theta_T$ is $\{x/\text{Card1}, y/\text{Card2}\}$. This means that $x$ refers to Card 1 and $y$ refers to Card 2.

The second stage of the function uses the conflict set to decide which production rules to use for the overall prediction. The production rules enabled on the history were the Colour, Nothing, and Same production rules which produces the following enabled set: $r_5 = T$, $r_6 = F$, $r_7 = T$, $r_8 = T$. By looking this up in the probability distribution given in Table 3.2 it can be seen that there is only one possible firing set of production rules that can be used to create the prediction: $u_5 = F$, $u_6 = F$, $u_7 = T$, $u_8 = F$. This means that the
only production rule to be used for the prediction will be the Colour production rule. The third stage of the function uses the set of production rules that should be fired to produce the prediction. In this example there is only one production rule, which comes from the Colour production rule. To generate the output the action section of the Colour production rule (shown in Figure 3.11) is fired by grounding it using the substitution $\theta_f$. This creates a new Event entity shown in Figure 3.14. The prediction is that Colour should be said next (at time 2) with a probability of 1.0.

![Table 1](image1)

Figure 3.14: The Event entity instance, along with its property and attribute instances produced by the action section of the Colour production rule. The text in a typewriter font shows that the value of the slot is a link to another instance frame.

### 3.5 Discussion

This chapter has presented a method to represent and store the history data within the system. It has also shown how the predictive models are represented and inference performed on the history. A frame based representation is used to describe the history. The predictive models are based on a production system, and contain a set of production rules, and a conflict resolver.

Typing is used both within the history to describe different classes of entities and relations, and within the production rules to only allow them to access specific subsets of the history. This allows domain knowledge to be incorporated into the history, and the predictive models. It also reduces the possible space of predictive models, and prevents invalid predictive models from being produced. As the types of the entities and relations are defined by the user, it makes the history representation potentially applicable to a wide
range of spatio-temporal domains. The use of inheritance also allows the definition of the entities and relations to be produced in a hierarchical manner.

The use of the conflict resolver firstly allows the predictive model to deal with multiple production rules entailing the history. The production rules can be combined together to make the prediction which simplifies the complexity of the predictive model. Secondly, the conflict resolver can produce multiple outputs, allowing it to predict from non-deterministic data. Finally, the condition section of the production rules can be extended by allowing users to add their own functions. The following chapter will look at how these predictive models can be learnt from data.
Chapter 4

Learning Predictive Models of Spatio-Temporal Data

4.1 Introduction

Chapter 3 described: a method for representing spatio-temporal data; an architecture for representing predictive models; and an inference technique, to allow them to predict from spatio-temporal data. This chapter presents methods for automatically learning predictive models from spatio-temporal data. The novel method described in this chapter, called Spatio-Temporal Genetic Programming (STGP), is used to learn predictive models. Firstly, Section 4.2 explains why a stochastic search approach was used to learn the predictive models. Then in Sections 4.3 to 4.8 a formal description of the STGP method is given. Finally, in Sections 4.9 and 4.10 a comparison of STGP with Progol [82], Pe (an implementation of the FAM algorithm [18] for SLPs), Neural Networks [111], Bayesian Networks [94] and C4.5 [99] is performed, along with an experimentation with the parameters for STGP.

4.2 Learning predictive models

To learn a predictive model requires finding the set of production rules $S$ and the conflict resolver $c$ that best models the set of history $H$, (i.e. find the predictive model that gets
the best accuracy when it predicts from the history) as shown in Equation 4.1.

$$\text{argmax}_{S,c}(P(S,c|H))$$  \hspace{1cm} (4.1)

Predictive model learning in the context of this thesis can be broken down into two parts: structure learning, and parameter learning [111]. Structure learning is on two levels. Firstly, the optimal number of production rules needs to be found, and secondly the optimal number of functions, variables, and constants, along with their connectivity needs to be found for each production rule. Parameter learning involves computing a conditional probability distribution for the conflict resolver (described in Section 3.3). This distribution does not contain any hidden variables, and the history data is complete, so there is a closed form solution for calculating its parameters.

There are various approaches to perform structure and parameter learning. Section 2.5.1 reviewed different approaches to learning first order logic production rules, represented by Horn clauses. There were two main conclusions. Firstly, using stochastic or evolutionary search finds good Horn clauses in a faster time than using greedy search [4, 87, 122, 126, 129]. Secondly, learning a complete set of Horn clauses simultaneously produces better results than sequentially learning a set of Horn clauses [3, 36, 46, 113, 131]. These techniques have been incorporated into the approach described in this thesis: an evolutionary search technique is used to learn the individual production rules and sets of production rules simultaneously. Section 2.5.2 looked at techniques for learning the parameters of the conflict resolver. It was shown in [19, 61] that learning both the production rules, and the parameters together, rather than using a two stage process produced better results. These ideas have again been introduced into the approach described in this thesis where both the production rules, and the parameters of the context chooser are learnt simultaneously. The following section will give an overview of the approach.

### 4.3 Spatio-Temporal Genetic Programming

Figure 4.1 gives an overview of Spatio-Temporal Genetic Programming (STGP) the novel method to learn the predictive models presented within this chapter. It is based on Genetic Programming (GP), and uses the same set of steps that are used in GP, and Genetic Algorithms (GA). The numbered set of steps below shows a run of STGP in more detail.

1. **Initialise the structure of the predictive models:** create a population of predictive models which each contain a randomly generated number of production rules.
2. **Compute parameters for the predictive models**: For each predictive model the parameters for its conflict resolver need to be computed from the history.

3. **Compute fitness value for each of the predictive model**: Use a fitness function to assign a fitness value to each of the predictive models.

4. **Check stopping criteria**: Check if the run has reached the maximum number of generations allowed, or there is a predictive model in the population which has an optimal fitness score. If so stop the run, and return the predictive model with the best (maximal) fitness score.

5. **Apply structure altering operations to the population of predictive models**: Apply structure altering operators to the population of predictive models to try and improve their fitness.

6. **Go back to step 2.**

The following sections will explain these steps in more detail. Firstly, Section 4.4 describes the structure learning techniques including: initialisation techniques, and structure altering operators. Next, Section 4.6 shows the parameter learning technique. Finally, Section 4.7 describes the fitness function.
4.4 Initialising the population of predictive models

To initialise STGP a population of randomly generated predictive models is produced. The process of generating a predictive model involves randomly creating a new production rule. To create a new production rule involves randomly generating its condition, and action sections. It is important that the population of predictive models is as diverse as possible, as explained in Section 2.6.7. A population with high diversity initially provides STGP with a wide range predictive models, which makes it more likely it will find the correct solution, and less likely to converge on a sub-optimal solution. Population diversity and how it is affected by the different STGP parameters is explored in Section 4.10.3. Initialisation of both the production rules and predictive models will now be described in more detail.

4.4.1 Predictive model initialisation

Predictive models consist of a set of one or more production rules. When a new predictive model is created, it is initialised with one randomly generated production rule. The Ramped half and half method [58] (Section 2.6.2) is used to generate the condition sections of the production rules. This ensures that the population of predictive models has production rules with condition sections that contain a variety of structures and depths.

4.4.2 Production rule initialisation

To create a new production rule involves firstly randomly creating the condition section, and then randomly creating the action section.

4.4.2.1 Condition section initialisation

Section 3.3.1.1 showed how the condition section is defined. It contains a set of functions, a set of variables, and a set of constants arranged in a Directed Acyclic Graph (DAG). Two things are required to create a new condition section: firstly a method to constrain the structure of the DAG so that it is always valid; and secondly a technique which uses the structural constraints to build a valid condition section.

Given a set of functions, constants and variables there is a large number of DAG structures that can be formed. However, not all structures will be valid, and these cannot be evaluated on a particular history. Figure 4.2 shows two invalid condition sections. The first condition section is evaluating whether the symbol Red is less than the symbol Green; and the second condition section is evaluating if the number 1 is equal to the...
symbol Green. To solve this problem constraints are placed on the composition of the DAG. This ensures that all DAG structures are evaluable, gives a good initial start point to the structure learning algorithm, and reduces the search space of possible structures. Strongly Typed Genetic Programming [79] is used to control the structure of the DAG. It assigns a type to every function, constant, variable and function argument. A DAG is only “valid” if for every function used in the DAG its argument types match the types of its parent nodes. The possible types used in this thesis are: Int, Float, String, Boolean, or Time.

![Invalid condition sections.](image)

The structural constraints described are used when generating a new condition section. The user defines a maximum depth of the DAG. This allows the maximum complexity and time to evaluate the condition section to be controlled. There are two possible ways to build the condition section: the Full method, and the Grow method [58]. This thesis will use the versions of the Full and Grow methods from [79], where the root node of the DAG must have a Boolean type. Two changes are made to these methods so that they can be used to produce production rules.

Firstly, if a function requires a variable as an argument STGP must use an existing one, or generate a new one of the correct type. The entity or relation type of the variable is defined in the sub-type of the argument. Firstly, STGP checks to see if there are any variables matching the desired entity or relation type. If there is a set of variables, then STGP can either decide to pick a random variable, or to generate a new variable. The likelihood of picking an existing variable $P(t)$ is shown in Equation 4.2. The equation makes it increasingly hard to generate new variables as the number of them increases.

$$P(t) = \frac{N_t}{N_t + 1}$$  

A new variable is generated when the maximum number of variables for a specific type has not been exceeded. This limits the complexity of the condition section, and prevents
STGP from producing predictive models that are overly complex. To generate a new variable requires completing its entity type, and time range. The time will be randomly chosen from either AllTime, Period time, or Point time. For Point and Period time, a time range is also randomly generated. Period time is not used in any of the runs in this thesis, but a discussion is given about how it could be used at the end of Chapter 5.

Secondly, to prevent condition sections from being generated that always evaluate true (or false) a restriction is added to the Grow, and Full methods. This occurs when the condition section contains sub-trees that either just contain constant value terminals, or variables which are the same. When nodes are assigned to a function’s arguments a check is performed to make sure they are not all constant value symbols, or use the same variable. If this is the case another assignment is found.

An example of the Full method will now be shown, based on the Uno example from Section 3.3. The following functions will be used: And (having a Boolean type, and a Boolean type for the its arguments), Get-Colour (having a String type, and an argument containing a variable of type Card), Equal (having a Boolean type, and a String type for its arguments), and Not Equal (having a Boolean type, and a String type for its arguments). The following terminals will be used Red, Green, and Yellow. All the terminals have a String type. The variables will all be of type Card. The stages of the example are shown in Figure 4.3. The maximum depth is set to 3. The Full method initially picks a function with a Boolean type. There are three possible options: And, Equal, and Not Equal; and And is chosen. The type for And’s arguments is Boolean, and as the method is not at the maximum depth a function with a Boolean type is chosen; this time it is Equal. The argument type for Equal is String, and as the method is now at the maximum depth only terminals of type String can be chosen. Get-Colour and Red are chosen. Get-Colour also requires a variable, in this case the variable \(x\) of type Card is used. Next, the second argument for the And node is found, and Not Equal is selected. Again the argument type for the Not Equal node is String and as the method is at the maximum depth only terminals of type String can be picked. Get-Colour and Yellow are selected. Again, Get-Colour requires a variable this time the variable \(y\) of type Card is used.

The functions and terminals which can be used in the condition section must be defined before STGP is run. These can be manually defined, or generated from the property, entity, or relation definitions. Some of the functions and terminals (described in Section 3.3.1.1) need extra parameters when they are defined. The Get function needs to have the entity type, property, and attribute it will use. The Exists function needs to have the entity or relation type. The Symbol terminal needs the symbol it will use. The Numeric terminal
4.4.2.2 Action section initialisation

To generate a new action section STGP selects a random entity, or relation definition, then for each property selects either a random number; symbol; or an existing variable in the condition section, and property to use.

4.5 Altering the predictive models

A set of structure altering operators is used to modify the current set of predictive models, to create a new population of predictive models. A population sampling method is used to select predictive models from the current population. In this thesis tournament selection and roulette wheel are used, as described in Section 2.6.4. These predictive models are then altered either by modifying which production rules are used in the predictive models, or by modifying the structure of the individual production rules in the predictive models. Then the predictive models are added to the new population. This is shown in Figure 4.4.
The following sections will explain how the predictive models and the production rules are altered in more detail.

### 4.5.1 Altering the set of production rules

There are four kinds of operators to change the set of production rules in the predictive models. These are: *reproduction*, *adding in a new production rule*, *replacing* an existing production rule, and *removing* a production rule. A set of probabilities are used to control how much each operator is used. Which operator is used is selected randomly based on a probability distribution $P_o$. The operators have been inspired by Koza’s work on architecture altering operations [59], as described in Section 2.6.6. The operators will now be described in more detail.

**Reproduction** copies the predictive models unchanged into the new population.

**Adding in a production rule from another predictive model** This requires two predictive models. A production rule from the first picked predictive model is randomly selected, and added to the second. This second predictive model is then included in the new population.

**Replacing a production rule** This requires two predictive models. A production rule from the first predictive model is replaced by a production rule randomly selected
from the second. The first predictive model is then included in the new population.

**Removing a production rule** A randomly selected production rule is removed from a predictive model. The predictive model is then included in the new population.

### 4.5.2 Altering the composition of the individual production rules

Two operators are used to change the composition of individual production rules, *crossover* and *mutation* [58].

#### 4.5.2.1 Crossover

Crossover is used to swap over parts of two different production rules. Two kinds of crossover are used with the production rules: condition section crossover, and action section crossover.

Condition section crossover uses the condition sections of two production rules and is based on the crossover technique used in [79]. To perform crossover a random node in the first condition section is selected. The same probabilities as used in [58] are used to select nodes in the DAG. With probability of 10% a terminal node is picked, and with probability of 90% a function node is picked. Nodes in the second condition section which match the node’s type and sub-type are then found. If there are no matching nodes then a new node in the first condition section is selected, and the process repeats. When a set of matching nodes in the second condition section has been found, a node in this set is randomly selected. The node and its sub-tree in the first condition section is then swapped with the selected node and its sub-tree in the second condition section. This can be seen in Figure 4.5.

In action section crossover, if the action sections are both entities or both relations then entity or relation crossover can be performed. To perform entity crossover a random property from the entity’s definition is selected, and then a random attribute from the property is selected. Then the values from each of these attributes in each entity are swapped over. In relation crossover one of the entity types used in the relation’s definition is chosen. Then the id value for this entity type within each relation is swapped over. If one action section is a relation and the other is an entity then the action sections are just swapped over.
4.5.2.2 Mutation

There are two possible types of mutation used in this thesis: condition section mutation and action section mutation. Condition section mutation, is based on the mutation operator described in [79]. It selects a random node within the condition section of the production rule and replaces it and its children with a randomly generated DAG which has a root node that matches the type of the randomly picked node. The Grow method is used to produce the new DAG. The DAG’s depth is randomly chosen such that it does not exceed the maximum depth of the DAG. Figure 4.6 shows a node (highlighted in black) being selected, and a new DAG replacing it and its children. In action section mutation a random property is selected from the entity and its value is replaced with a randomly generated value.

4.6 Conflict resolver parameter learning

Once a set of production rules have been produced the next stage is to compute the parameters for the conflict resolver. It is represented by a discrete conditional probability distribution $P(U|R)$, as described in Section 3.3. The distribution probabilistically decides which set of enabled production rules should be fired to produce a prediction.

Calculation of $P(U|R)$ has a simple closed form solution and is computed in two stages. Firstly evaluate each of the production rules at each point in the history. Secondly fire the action sections of each enabled production rule. Then record which of the outputs successfully matched the actual output at the next point in the history. The probability
distribution can be computed as shown in Equation 4.3 by recording the number of times $(N_r)$ the set of production rules have been enabled, or not enabled $r = (r_1, ..., r_N)$, $r_i \in \{true, false\}$ when applied to the history; and the number of times $(N_{ur})$ when the action sections of the enabled production rules were fired their outputs matched the actual output at the next time step $u = (u_1, ..., u_N)$, $u_i \in \{true, false\}$, $u_i$ is true if there is a match and false otherwise.

$$P(U = u|R = r) = \frac{P(U = u, R = r)}{P(R = r)} = \frac{N_{ur}}{N_r}$$  \hspace{1cm} (4.3)

The probability distribution is computed over all occurring combinations of enabling/not enabling the production rules, and output matches/mismatches. In theory this could be large, but in practice the number of combinations is limited, so sparse storage solutions can be used. The method used to compare the output from a production rule with the actual output $H$ is described by Equation 4.4. It finds the entity or relation $h$ from the actual output that best matches the production rule output. The matching is done using the Match function (shown in Figure 4.7) which computes the proportion of properties in the entity or relation which have the same values to the output from the production rule.

$$MS(p, H) = \max_{h \in H}(\text{match}(p, h))$$  \hspace{1cm} (4.4)

The computation for $P(U|R)$ can now be described more formally. At each point $t$ in the history $H$ the set of production rules $S$ are evaluated and the results $r$ are stored where $r_i$ is true if the condition section $b_i$ of production rule $i$ entails the subset of the training
Input: Entity or relation \(O\) produced from the action section of a production rule and an entity or relation \(C\) from the history to compare it to.

Output: The fraction of properties that match.

<table>
<thead>
<tr>
<th>Function Match</th>
</tr>
</thead>
<tbody>
<tr>
<td>If (O) and (C) have the same types</td>
</tr>
<tr>
<td>Foreach property (p) in (O)</td>
</tr>
<tr>
<td>If (O) and (C) have the same value for property (p)</td>
</tr>
<tr>
<td>(s = s + 1)</td>
</tr>
<tr>
<td>(t = t + 1)</td>
</tr>
<tr>
<td>Return (s / t)</td>
</tr>
<tr>
<td>Else</td>
</tr>
<tr>
<td>Return 0</td>
</tr>
</tbody>
</table>

Figure 4.7: The pseudo code for the matching algorithm.

data \(h\) \((b_i\theta_T \models h)\) where \(h \in H\), and false otherwise. The algorithm described in Section 3.4 is used to find the substitution \((\theta_T)\) that causes the condition section of the production rule to entail a subset of the history. Next, the firing set \(u\) is formed where \(u_i = true\) if \(b_i\theta_T \models h\) and \(MS(a_i\theta_T) = 1\); and false otherwise. Finally the number of times in the history \(N_r\) a specific \(r\) occurs is computed, and the number of times \(N_{ur}\) a specific \(r\) occurs and specific \(u\) also occurs is computed, and used to compute \(P(U|R)\) (Equation 4.3).

Figure 4.8: A path containing three sensors numbered 1, 2 and 3.

Parameter learning will be illustrated with an example. Figure 4.8 show a path which has 3 sensors on it numbered 1, 2 and 3. People walk along the path passing over sensor 1, and then either take the left or right fork, passing over sensor 2 or 3 in the process. We do not consider any other routes in this simplified example. Figure 4.9 shows a predictive model for predicting which sensor the person will pass over next once they have passed over sensor 1. Production rule 1 states that sensor 2 will detect next, and production rule 2 states that sensor 3 will detect next. The problem now is to learn the parameters of the
R1: IF DETECT(SENSOR1, T) THEN DETECT(SENSOR2, T+1)
R2: IF DETECT(SENSOR1, T) THEN DETECT(SENSOR3, T+1)

Figure 4.9: The predictive model for the Path example.

<table>
<thead>
<tr>
<th>Time</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Detection history</td>
<td>{1}</td>
<td>{2}</td>
<td>{1}</td>
<td>{3}</td>
<td>{1}</td>
<td>{2}</td>
<td>{1}</td>
<td>{2}</td>
</tr>
<tr>
<td>r₁</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>r₂</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>u₁</td>
<td>T</td>
<td>F</td>
<td>F</td>
<td>F</td>
<td>T</td>
<td>F</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>u₂</td>
<td>F</td>
<td>F</td>
<td>T</td>
<td>F</td>
<td>F</td>
<td>F</td>
<td>F</td>
<td>F</td>
</tr>
</tbody>
</table>

Table 4.1: The prediction results for the Path model on a set of history. The history at each point in time represents the sensor numbers that have been detected. There is only one detection at each point in time because the condition sections of both of the production rules only use detections at the current time.

There are three possible situations that have occurred in this history, and these will be used to compute the probability distribution \( P(U|R) \):

1. Both production rules are enabled on the history, but only the output of production rule 1 matches the next detection (i.e. sensor 2 next), so only its action section should be fired. This occurs at time points: 1, 5, and 7.

   \[
P(u₁ = t, u₂ = f | r₁ = t, r₂ = t) = \frac{N_{u₁=t,u₂=f,r₁=t,r₂=t}}{N_{r₁=t,r₂=t}} = \frac{3}{4} = 0.75 \tag{4.5}
\]

2. Both production rules are enabled on the history, but only the output of production rule 2 matches the next detection (i.e. sensor 3 next), so only its action section should be fired. This occurs at time point 3.

   \[
P(u₁ = f, u₂ = t | r₁ = t, r₂ = t) = \frac{N_{u₁=f,u₂=t,r₁=t,r₂=t}}{N_{r₁=t,r₂=t}} = \frac{1}{4} = 0.25 \tag{4.6}
\]

3. None of the production rules were enabled on the history, and no output is predicted, so none of the action sections should be fired. This occurs at time points: 2, 4, 6 and 8.
\[ P(u_1 = f, u_2 = f | r_1 = f, r_2 = f) = \frac{N_{u_1=f,u_2=f,r_1=f,r_2=f}}{N_{r_1=f,r_2=f}} = \frac{4}{4} = 1 \quad (4.7) \]

There are other possible combinations, but these do not occur and so are not computed. This means out of a possible 16 combinations (4 enabled combinations * 4 fired combinations), only 3 are actually computed and stored.

### 4.7 Fitness function for scoring predictive models

The fitness function is used to produce a fitness score which represents how well a predictive model predicts a future set of history from a past set of history. To compute the fitness score the predictive model is applied at each point in the history to produce a prediction. This prediction is compared against the history at the next time point to produce a predictive match score. The fitness score is calculated by computing the average predictive match score over the history.

More formally given a predictive model \( M \) and a set of history \( H \) the predictive model predicts from the history \( H_{1:t} \) at each time point \( t \). This is performed by the prediction function described in Section 3.4 producing a set of predicted outputs \( W \). Each predicted output \( w_i \) is a tuple \((o_i, p_i)\) containing the output \( o_i \), and its likelihood \( p_i \). Equation 4.9 shows how the set of predicted outputs is compared with history at the next time step \( H_{t+1} \). To perform this comparison each \( o_i \) is compared against \( H_{t+1} \) using the \text{FindBestMatch} function (described below) and the result multiplied by \( p_i \). The best comparison score is then returned. This process repeats over the entire history, and the average comparison score is computed as shown in Equation 4.8.

\[
f(M, H) = \frac{1}{|H|} \sum_t \text{compare}(\text{predict}(M, H_{1:t}), H_{t+1}) \quad (4.8)
\]

\[
\text{compare}(W, D) = \text{Max}_i(l_i \times \text{FindBestMatch}(p_i, D)) \quad (4.9)
\]

The \text{FindBestMatch} function (shown in Figure 4.10) takes the actual history, and the predicted output, and firstly pads each of them out with blank entities or relations so that they are the same size. Then, for each item in the actual history, a unique match in the predicted output is found. For each of the matches a comparison is done between the two objects using the Match algorithm described in Section 4.6. An exhaustive search is then performed over all the possible combination of matches to find the best (maximal) matching score.
**Chapter 4**

**Learning Predictive Models of Spatio-Temporal Data**

**Input:** A set of Entity or relations \((P)\) predicted by the predictive model, a set of entities or relations \((H)\) describing history data at the next time point.

**Output:** The score on how well the prediction matches the history data.

---

**Function** FindBestMatch

| Fill the sets \(P\) and \(H\) with empty entities or relations such that they are the same length. \(best = 0\) |
| Foreach mapping \(m\) from objects in \(P\) to objects in \(H\) |
| \(s = 0\) |
| Foreach object \(p\) in \(P\) get its mapped object \(m(p)\) |
| \(s = s + \text{Match}(p, m(p))\) |
| If \(s > best\) |
| \(best = s\) |
| Return \(best\) |

---

Figure 4.10: The pseudo code for the FindBestMatch algorithm.

The fitness function will now be illustrated with an example. We will use the same predictive model, and conflict resolver from the previous section. This time the predictive model is applied to a different set of history as shown in Table 4.2. In the \(W\) row each tuple is the predicted sensor number, followed by its probability for example \((2, 0.75)\) is the prediction that Sensor 2 will detect next with the probability of 0.75. The underscore for the sensor number represents that there was no output. The bold items show which of the predicted outputs match the actual outputs. In the compare row the 1 in each calculation is the result from the compare function and shows that the predicted output exactly matched the actual output. The fitness score can then be computed as shown in Equation 4.10.

\[
f = \frac{(1 \times 0.75) + 0 + (1 \times 0.25) + 0 + (1 \times 0.25) + 0}{6} = 0.208 \quad (4.10)
\]

---

**4.8 Controlling the size of the predictive models**

To prevent the predictive models from overfitting the history, and getting too large, some form of size control is required. In GP this is called bloat and refers to excess code in the program trees that are not used. The Tarpeian method [22] is one of the methods in GP used to control bloat. It has been shown to perform well on standard GP datasets [67], therefore will be used in STGP to control the size of the predictive models. This method is described in Section 2.6.7. Section 4.10.3.2 shows results on how changing the Tarpeian value affects STGP.

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Table 4.2: The fitness results for the Path predictive model on a set of history data. Variables \( r_1 \) and \( r_2 \) represents that production rule 1 or 2 were enabled or not enabled on the history. Variable \( W \) represents the set of predictions, which each tuple is a prediction from a production rule containing an output, and its probability. The tuples in bold represent where the prediction matches the detection at the next time step. The variable \( \text{compare} \) represents how well the prediction matched the actual history.

4.9 Evaluation

A comparison was performed with STGP and five other methods: Progol [82], Pe (an implementation of the FAM algorithm [18] for SLPs), Neural Networks [111], Bayesian Networks [94] and C4.5 [99]. Five datasets were used for the comparison: Uno, Uno2, Paper Scissors Stone (PSS), CCTV and Play Your Cards Right (PYCR). Three of the datasets (Uno, Uno2, and PSS) were taken from the work of Needham et al. [89]. The other two datasets (CCTV and PYCR) are novel, and were produced for this thesis. Both of these datasets are non-deterministic and test how the different methods deal with learning from non-deterministic data. PYCR was also set as a grand challenge in the work of [89].

Section 4.9.1 will describe these datasets in more detail. Some of the datasets have training sets that are generated from video, Section 4.9.2 will describe how this was performed. Finally, Section 4.9.3 describes the representation used for each of the methods.

4.9.1 Overview of the datasets

This section gives a brief overview of the datasets: Uno, Uno2, PSS, PYCR, and CCTV.

4.9.1.1 Uno and Uno2

The card game Uno involves two players. Firstly one player says “Play” to signify both players should put down a card. Each player then puts down a card, and the first player who correctly shouts out how the two cards match picks up all the cards that have been
put down. If the cards both have the same picture, and colour then “Same” should be shouted out. If the cards have the same picture, but different colours then “Shape” should be shouted out. If the cards have the same colour, but different pictures then “Colour” should be shouted out. Finally, if the two cards are different then “Nothing” is said. This process repeats until a player cannot put down a card.

The game Uno2 works in a very similar manner; the only difference is that instead of one player saying “Play” and both players putting down a card, they just take it in turns to put a card down. The similarity is then based on the current and previous cards that were put down. The methods should learn predictive models from the Uno and Uno2 datasets that given the cards put down by each of the players should predict the result that should be said.

For both Uno and Uno2 six training sets were produced. One was from real world video, as described in Section 4.9.2.1. This contained 50 rounds of the game for both Uno and Uno2. The rest were hand crafted with different levels of noise. The noise levels were: 0% (clean), 5%, 10%, 20% and 30%. The noise was produced by changing or removing the speech outputs, or removing cards. The datasets contained 130 rounds of the game.

4.9.1.2 Papers scissors stone

Paper Scissors Stone is a card game again played by two people, each with three cards representing paper, scissors and stone. One player will say “Play”, and a card is selected by each player. Both cards are placed down face up at the same time. The game is played from the view point of player 1. If player 1’s card beats player 2’s card then “Win” will be heard. If player 1’s card is beaten by player 2’s card then “Lose” will be heard. If both players have put down the same cards then it is declared a draw and “Draw” will be heard. Scissors will beat paper; paper beats stone; and stone beats scissors. Table 4.3 shows the possible states.

<table>
<thead>
<tr>
<th>(Player 2)</th>
<th>(Player 1) Paper</th>
<th>Scissors</th>
<th>Stone</th>
</tr>
</thead>
<tbody>
<tr>
<td>Paper</td>
<td>Draw</td>
<td>Loose</td>
<td>Win</td>
</tr>
<tr>
<td>Scissors</td>
<td>Win</td>
<td>Draw</td>
<td>Loose</td>
</tr>
<tr>
<td>Stone</td>
<td>Loose</td>
<td>Win</td>
<td>Draw</td>
</tr>
</tbody>
</table>

Table 4.3: The result states for a game of Paper Scissors Stone between two players.

Again, the methods should learn predictive models that given the cards put down by each of the players should predict the result that should be said. Six training datasets were produced in a similar manner to Uno and Uno2. One dataset was generated from
real-world video, and the rest were handcrafted with the same levels of noise as the Uno and Uno2 datasets. The real world video training set contained 100 rounds of the game, and the handcrafted training sets contained 130 rounds of the game.

4.9.1.3 CCTV data of a path

A static camera was used to film a scene containing a path with a junction point in it. A frame of the video is shown in Figure 4.11(a), and Figure 4.12 shows the four possible movement patterns in the scene. The video is used to mockup a set of CCTV cameras over the image as shown in Figure 4.11(b).

Figure 4.11: Figure (a) shows a frame of the video with a person taking a decision at the junction point. Figure (b) shows the possible location of the virtual CCTV cameras in the image.

Figure 4.12: The four possible movement patterns in the CCTV scene.

The methods should learn a predictive model that can predict based on the CCTV cameras a person has been in previously which CCTV camera they will appear in next. The CCTV dataset tests if the different methods can learn from, and model, non-deterministic
data. Six training sets were produced in the similar manner to the PSS, Uno and Uno2 datasets. One dataset was produced from real-world video, and the rest were handcrafted. The same noise levels as previously described were used. Noise was added by removing regions and changing their numbers. The real world dataset contained 50 detections, and the handcrafted datasets contained around 120 detections.

### 4.9.1.4 Play your cards right

Play Your Cards Right (PYCR) is a card game played by a person and a dealer. The cards are numbered from 1 to 5 with 1 being the lowest, and 5 being the highest. Firstly the dealer says “Play” and puts down a card face up. Then the person must say if they predict the next card will be “Higher” or “Lower” than this card. The dealer will then put down the next card. If the person guesses correctly then the dealer says “Win”, otherwise they will say “Lose”.

The methods should learn a predictive model that should use the state of the cards put down to predict the spoken outcomes from the person and the dealer. PYCR, like the CCTV dataset tests if the different methods can learn from non-deterministic spatio-temporal data. Five handcrafted training sets were produced, having the same noise levels as the previous datasets. The noise was added by removing cards and speech outputs, and changing the speech outputs. The datasets contained 130 rounds of the game.

### 4.9.2 Spatio-temporal data acquisition

Four out of the five datasets (Uno, Uno2, PSS and CCTV) have a training set that is generated from video. Firstly, spatio-temporal data must be acquired from the videos, and then it must be represented within the different methods. This section describes data acquisition, and the next section describes data representation.

#### 4.9.2.1 Uno, Uno2 and PSS

The Uno, Uno2 and PSS videos will be that used in [89]. The datafiles from this paper are used for the experiments in this chapter, but the speech cluster labels are changed to be the actual speech (word) labels. The remainder of this section will explain how the datafiles were produced. The videos were taken of the game playing area, and objects moving in the area were tracked using a generic blob tracker [68]. When an object was stationary for a number of frames it is assumed to be part of the game. Features from the object including texture (calculated from Gabor wavelets, and Gaussians applied at various orientations and scales), colour (calculated from a binned histogram of hue, and saturation),
and position were produced. Each colour, and texture feature was independently clustered using agglomerative clustering. A graph was produced with data items as the nodes, and the feature clusters used to weight the edges. The graph was then partitioned to form clusters of data items. These clusters were then used to train a vector quantisation based nearest neighbour classifier. One of the players had their voice recorded during the games. The energy of the speech signal was analysed using a fixed length window. When the energy was over a fixed threshold spectral analysis was performed on the window, and a histogram of the result was produced. K-means clustering was then performed on the speech samples, to find clusters of similar speech sounds. In this thesis the previous step is changed by replacing the speech cluster labels by manually annotating them with the actual speech (word) labels.

### 4.9.2.2 CCTV

A 10 minute video of people walking along a path containing a junction was filmed. This was then used to mock up a network of CCTV cameras. Figure 4.11 shows a frame from the video. Virtual motion detectors, representing CCTV cameras, were hand placed over the video (Figure 4.11 right). Using frame differencing, and morphological operations the video was processed to determine the location of the motion. If the number of moved pixels in a region exceeded a fixed threshold then the virtual detector outputted that motion had occurred at that location. To prevent false detections the motion detection is implemented as a 2-state machine (where the states are motion/no motion). The state machine required a number of frames (normally 10) of stability to change state.

### 4.9.3 Representation

This section will show how the spatio-temporal data is represented in the different methods.

#### 4.9.3.1 Progol and Pe

In Progol a set of events occurring in a visual scene is represented as a sequence of states in which each state describes: the current state of the objects in the scene; an action associated with this state; the time the state occurs at; and how the state relates to previous state. Progol requires four elements as its input: a set of types; some background knowledge; some examples; and a set of mode declarations. The Uno dataset will be used to illustrate these elements. The rest of the datasets use similar elements. The same representation from [89] will be used for the Uno, Uno2 and PSS datasets.
Firstly, Progol needs some type declarations. Figure 4.13 shows the type declarations for the Uno dataset: texture, colour, position, and speech. No background information is required for any of the datasets.

\[
\begin{align*}
texture(f0). & \quad texture(f1). & \quad texture(f2). \\
colour(c0). & \quad colour(c1). & \quad colour(c2). \\
position(p0). & \quad position(p1). \\
speech(s_1). & \quad speech(s_2). & \quad speech(s_3). \\
speech(s_4). & \quad speech(s_5). & \quad speech(s_6). \\
speech(s_7). & \quad speech(s_8). & \quad speech(s_9). & \quad speech(s_{10}).
\end{align*}
\]

Figure 4.13: Type declarations for Progol on the Uno dataset.

Secondly, Progol requires a set of examples – Figure 4.14 shows some examples for the Uno dataset. The first example shows two cards being placed in the scene, and an appropriate response (action) being heard. The second example shows an empty scene, and an appropriate action being heard. Both examples have a similar structure. The \texttt{time} predicate represents the time the example occurred at. The \texttt{successor} predicate represents how this example temporally relates to a previous example. The \texttt{state} predicate is used to represent the visual scene. It either represents an empty scene, as shown in Example 2, represented by \([\text{}\]), or it represents a set of objects in the scene. In Example 1 the state of the world is: \([f1, c0, p0], [f0, c0, p1]\) which represents two objects, one with texture \(f1\) and colour \(c0\), at position \(p0\); and the other with texture \(f0\) and colour \(c0\), at position \(p1\). Finally the \texttt{action} predicate represents what spoken response has been heard.

Finally, Progol requires some mode declarations. Figure 4.15 shows the mode declarations for the Uno dataset. It shows that Progol needs to produce a clause which has an \texttt{action} term its head, and its body can contain the terms \texttt{successor} and \texttt{state}.

To convert the clauses learnt by Progol into a Stochastic Logic Program (Section 2.5.3.3) the likelihood of each clause needs to be calculated from data. Two approaches are used in this thesis to do this. Firstly, Pe (which implements the failure-adjusted maximisation algorithm from [18]) is used. Secondly, the clauses learnt by Progol are converted into a predictive model, and the parameters of its conflict resolver are estimated by STGP. This is performed by converting each Horn clause into a production rule, where the action section contains the appropriate entity or relation representing the head of the Horn clause, and the condition section represents the body of the Horn clause. Then, the algorithm described in Section 4.6 is used to estimate the parameters of the conflict resolver.
%Example 1
time(t_0).
time(t_15).
successor(t_0,t_15).
state([[f1,c0,p0],[f0,c0,p1]],t_15).
action(s_10,t_15).

%Example 2
time(t_15).
time(t_20).
successor(t_15,t_20).
state([],t_20).
action(s_9,t_20).

Figure 4.14: Examples of the Uno dataset which are used with Progol.

modeh(1, action(#speech,+time))
modeb(*, state([-texture,-colour,-position],
                [-texture,-colour,-position]),+time))
modeb(*, state([],+time))
modeb(1, +any = #any)
modeb(*, successor(-time,+time))

Figure 4.15: Mode declarations for Progol on the Uno dataset.

4.9.3.2 STGP

STGP requires the following: a set of property, entity and relation definitions; a datafile; and a set of terminals, and functions. These will now be explained by using the Uno dataset as an example. The other datasets use similar settings.

The representation used in the datafile is described in Section 3.2. The properties and entities used to learn the Uno dataset are shown in Figure 4.16. There are four property definitions: colour, texture, position, and speech, and two entity definitions: card (with properties: texture, colour and position), and action (with property speech).

Figure 4.17 shows the terminals used to learn the Uno dataset. There are colour symbols c0, c1; texture symbols f0, f1, f2; position symbols p0, p1; and speech symbols Same, Shape, Nothing, Play, Colour. Figure 4.18 shows the functions used to learn the Uno dataset. There are functions to check the existence of a card, or a talker entity in the world Exists(Card), Exists(Action). Also, there are functions to get property information from the cards, and talker entities Get(Card:Colour),

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Get (Card:Position), Get (Card:Texture), Get (Action:Speech). Finally, there are functions to compare symbolic data Equal, Not-Equal, and logical functions And, Or, Not.

```xml
<PROPERTY-DEFINITION NAME="COLOUR">
  <ATTRIBUTE NAME="NAME" TYPE="SYMBOLIC" VALUES="c0,c1,c2"/>
</PROPERTY-DEFINITION>

<PROPERTY-DEFINITION NAME="TEXTURE">
  <ATTRIBUTE NAME="NAME" TYPE="SYMBOLIC" VALUES="f0,f1,f2"/>
</PROPERTY-DEFINITION>

<PROPERTY-DEFINITION NAME="POSITION">
  <ATTRIBUTE NAME="NAME" TYPE="SYMBOLIC" VALUES="p0,p1"/>
</PROPERTY-DEFINITION>

<PROPERTY-DEFINITION NAME="SPEECH">
  <ATTRIBUTE NAME="NAME" TYPE="SYMBOLIC" VALUES="Shape,Colour,Nothing,Same,Play"/>
</PROPERTY-DEFINITION>

<ENTITY-DEFINITION NAME="CARD">
  <LEARNABLE VALUE="FALSE"/>
  <PROPERTY NAME="COLOUR"/>
  <PROPERTY NAME="POSITION"/>
  <PROPERTY NAME="TEXTURE"/>
</ENTITY-DEFINITION>

<ENTITY-DEFINITION NAME="ACTION">
  <LEARNABLE VALUE="TRUE"/>
  <PROPERTY NAME="SPEECH"/>
</ENTITY-DEFINITION>
```

Figure 4.16: Properties, and entity definitions for STGP on the Uno dataset.

c0, c1
p0, p1
f0, f1, f2
Same, Shape, Nothing, Play, Colour

Figure 4.17: Terminals for STGP used to learn the Uno dataset.
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Exists(Card), Exists(Action),  
Get(Card:Colour), Get(Card:Position)  
Get(Card:Texture), Get(Action:Speech)  
And, Or, Not-Equal, Equal, Not

Figure 4.18: Functions used to learn the Uno dataset

4.9.3.3 Bayesian Networks, Neural Networks, and C4.5

These methods were implemented using the WEKA machine learning system [41]. This requires a fixed length representation to describe the datasets. The representation will describe the current state of the scene, along with an associated action that needs to be learnt. Figure 4.19 shows an example representation for the Uno dataset. The first six attributes (Colour1, Position1, Texture1, Colour2, Position2, and Texture2) describe the properties of the cards in the scene, with cN, pN, fN representing that no card is present. The final attribute (Speech) represents the action associated with the scene. The first line of data indicates that no cards are in the scene and that play (s_play) was uttered. The second line of data represents that a card with colour c2, position p0, and texture f0, and a card with colour c2, position p1, and texture f1 are in the scene and that colour (s_colour) was said.

@RELATION Uno  
@ATTRIBUTE Colour1 {c0,c1,c2,cN}  
@ATTRIBUTE Position1 {p0,p1,pN}  
@ATTRIBUTE Texture1 {f0,f1,f2,fN}  
@ATTRIBUTE Colour2 {c0,c1,c2,cN}  
@ATTRIBUTE Position2 {p0,p1,pN}  
@ATTRIBUTE Texture2 {f0,f1,f2,fN}  
@ATTRIBUTE Speech {s_shape, s_play, s_same, s_colour, s_nothing, s_unknown}  

@DATA  
cN,pN,fN,cN,pN,fN,s_play  
c2,p0,f0,c2,p1,f1,s_colour

Figure 4.19: An example Uno dataset representation for Bayesian Networks, Neural Networks, and C4.5.
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4.10 Results

This section will firstly outline the evaluation criteria for the experiments. Then an analysis of the results from the different methods, and experiments with the different parameters for STGP will be presented.

4.10.1 Evaluation criteria

Two criteria were used to evaluate the predictive models produced by the different methods: coverage, and accuracy. Coverage \(c\) scores if the predictive model can correctly predict the history (i.e. the probability of correct prediction is greater than 0) and is the number of correct predictions \(n_c\) divided by the history size \(s\) (Equation 4.11). Accuracy \(a\) scores with what probability the correct prediction is made. It is calculated by taking the sum of the likelihoods \(l = \{l_1, ..., l_{nc}\}\) for each correct prediction, and dividing it by the history size, as shown in Equation 4.12. In non-deterministic scenarios this cannot be 100%.

\[
c = \frac{n_c}{s} \tag{4.11}
\]

\[
a = \frac{\sum l_i}{s} \tag{4.12}
\]

4.10.2 A comparison of STGP with current methods

Figures 4.20 - 4.27 show graphs comparing the coverage and accuracy of STGP with Bayesian Networks, C4.5, Neural Networks, and Progol on the five different datasets explained in Section 4.9.1. The graphs also show the results for estimating the probabilities of the clauses learnt by Progol using Pe, and STGP. Ten fold cross validation was used in all the experiments. In STGP the training folds are used in the following way: four folds are used to estimate the parameters of the conflict resolver, and five folds are used to score the predictive models. A windowed section (which moves at every generation) of the parameter fold, and the scoring fold is used for the calculations. Overall the results show that STGP had accuracy on all the datasets that was as good as, or better than the other methods.

On both Uno and Uno2 the maximum achievable result for these datasets was 100% accuracy, and 100% coverage (as they are deterministic). It can be seen in Figures 4.20 and 4.21 that STGP matches the expected result for the clean dataset, and keeps close to this result with noisy data. Combining Progol with STGP on both the Uno and Uno2 datasets produced more accurate results than all methods other than STGP. The Uno and
Uno2 datasets do not contain enough examples to describe every possible outcome that can occur within the game. C4.5, Neural Networks, and Bayesian Networks cannot produce generalised rules from the examples, and effectively rely on storing common examples and their outcomes. They fail to get 100% accuracy and 100% coverage (Figures 4.20 and 4.21), as they will have not learnt enough examples to correctly predict from all the test data. These methods are also affected by noise in the examples, which can be seen in the graphs. Progol and STGP which can learn generalised rules from the examples get better results because the generalised rules can still correctly predict test examples which have not occurred in the training data. Progol suffers from a clause evaluation problem that affects its coverage and accuracy results. This is caused by an incorrect ordering of the clauses it has learnt. As explained in Section 2.5.2 the clauses are applied in the order they are learnt until one clause entails the unseen example. In this thesis the clauses were applied in the order that Progol had learnt them. This often means that although Progol had learnt the correct set of clauses their ordering caused Progol to predict incorrectly. Figure 4.22 shows one of the results from the Uno Clean dataset. It can be shown that the correct number of clauses has been learnt, but when they are applied to the test fold it got 93% coverage and 93% accuracy. If the clauses were in the correct order it would have got 100% coverage and 100% accuracy. The problem is due to where the Same clause is located. In Figure 4.22 the Colour and Shape clauses are applied before the Same clause which means Progol will incorrectly predict a same event as a colour or shape event. By placing the Same clause above the Colour and Shape clauses this problem is solved, as shown in Figure 4.23.

Pe can be used to solve this clause ordering problem. It estimates the likelihood that a clause is used in a prediction. All the clauses are applied to the unseen example, and the likelihood of a prediction is based on the clauses that entail the unseen example. This approach improves Progol’s coverage results, but does not improve its accuracy due to some clauses clashing when they entail an unseen example. For example, the estimated probabilities from Pe for the clauses in Figure 4.22 are shown in Figure 4.24.

Using these probabilities the likelihood of the Same clause entailing an unseen example is based on the Same clause likelihood along with the likelihood of the Colour, Shape, and Nothing clauses because these also entail the unseen example. The probability of predicting the next event will be same is then $\frac{0.05}{0.1+0.1+0.05+0.23} = 0.1$. However, if the Shape, Colour and Nothing clauses were not included in the prediction, the prediction for same would have the correct probability of 1.0. Pe must output all clauses that match the data, unlike STGP which can prevent the action sections of some production rules from being output. This can be seen in the results as combining the clauses learnt by Progol
with STGP gets more accurate results than Progol, and Progol combined with Pe.

On the PSS dataset the optimal obtainable result is again 100% coverage, and 100% accuracy (as it is deterministic). STGP, as shown in Figure 4.25, gets the best accuracy results, and matches the optimal result on the clean dataset, and keeps close to this for the noisy datasets. C4.5 gets the same accuracy results as STGP on the clean dataset, but its accuracy reduces on the noisy datasets. Neural networks get good results (average accuracy 97%) on the clean datasets, but again this drops on the noisy datasets. Progol, Progol combined with Pe, and Progol combined with STGP got worse results than C4.5 and Neural Networks. The PSS datasets, however, are different to Uno and Uno2 in that no general rules are required to get good results on the training examples. The training data contain all the possible combinations of the game, so all that is required is to memorise these combinations. This explains why C4.5 and Neural Networks gets better results on this dataset than on the Uno and Uno2 datasets. Progol again suffers from the clause ordering problem described previously which affects its results. Pe solves the clause ordering problem, but the clashing clauses reduce the accuracy of the results. When the clauses from Progol are combined with STGP there is not enough training data to cor-

Figure 4.20: The mean accuracy and coverage for Uno Clean (top) and Uno 10% noise (bottom). The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
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![Graphs showing mean accuracy and coverage for Uno2 Clean (top) and Uno2 10% noise (bottom). The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.](image)

**Figure 4.21**: The mean accuracy and coverage for Uno2 Clean (top) and Uno2 10% noise (bottom). The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

- `action(s_play,A) :- state([],A).`
- `action(s_colour,A) :- state([[B,C,D],[B,E,F]],A).`
- `action(s_shape,A) :- state([[B,C,D],[E,F,D]],A).`
- `action(s_same,A) :- state([[B,C,D],[B,E,D]],A).`
- `action(s_nothing,A) :- state([[B,C,D],[E,F,G]],A).`

**Figure 4.22**: A result for Progol on the Uno dataset with the clauses in the wrong order.

- `action(s_play,A) :- state([],A).`
- `action(s_colour,A) :- state([[B,C,D],[B,E,D]],A).`
- `action(s_shape,A) :- state([[B,C,D],[B,E,F]],A).`
- `action(s_same,A) :- state([[B,C,D],[E,F,D]],A).`
- `action(s_nothing,A) :- state([[B,C,D],[E,F,G]],A).`

**Figure 4.23**: A result for Progol on the Uno dataset with the clauses in the correct order.

- `action(s_play,A) :- state([],A).`
- `action(s_colour,A) :- state([[B,C,D],[B,E,F]],A).`
- `action(s_shape,A) :- state([[B,C,D],[E,F,D]],A).`
- `action(s_same,A) :- state([[B,C,D],[E,F,G]],A).`

rectly estimate the parameters for the conflict resolver. This prevents it from correctly predicting all of the test data, which reduces its accuracy.

On the PYCR dataset STGP gets the best accuracy and coverage as shown in Figure
0.50::action(s_play,A) :- state([],A).
0.10::action(s_colour,A) :- state([[B,C,D],[B,E,F]],A).
0.10::action(s_shape,A) :- state([[B,C,D],[E,F,D]],A).
0.05::action(s_same,A) :- state([[B,C,D],[B,E,D]],A).
0.23::action(s_nothing,A) :- state([[B,C,D],[E,F,G]],A).

Figure 4.24: The estimated probabilities for the clauses in Figure 4.22 using Pe.

![Graph 1](image1)

![Graph 2](image2)

Figure 4.25: The mean accuracy and coverage for PSS Clean (top) and PSS 10% noise (bottom). The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

4.26. The optimal result for PYCR is 100% coverage, and 90% accuracy (as it has nondeterministic outcomes). This is based on playing the game where each possible game combination occurs in equal proportion. STGP is close to this for both the clean and noisy datasets. It does fail to get 100% coverage due to not learning rules for infrequent events in the training data. On the clean data, Bayesian Networks, C4.5 and Neural Networks got more accurate results than Progol, and Progol combined with Pe. However, on the noisy data the inverse is true, as can be seen in Figure 4.26.

Progol does not learn enough clauses to cover the possible cases in the game. When Progol is combined with either Pe, or STGP the accuracy does not improve due to the lack
of correct clauses. Progol’s fitness function is based on how well the clauses cover rather than predict the data. It looks at the number of positive examples to negative examples covered by a potential clause. The more negative examples a clause covers, the less likely Progol will be to use it. This can make it hard to learn clauses from non-deterministic data, where a particular state in the world can have multiple outcomes. If insufficient examples are available Progol sees multiple outcomes as noise, which can prevent it finding a clause.

![Graphs showing mean accuracy and coverage for PYCR Clean and PYCR 20% noise.](image)

Figure 4.26: The mean accuracy and coverage for PYCR Clean (top) and PYCR 20% noise (bottom). The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

The results for the CCTV dataset are shown in Figure 4.27. The expected results for CCTV are 100% coverage and 83% accuracy (as it has non-deterministic outcomes). This is based on the four actions from Figure 4.12 occurring in equal proportions in the data. STGP got the best results, but does not get 100% coverage, because it fails to learn infrequent changes between regions in the training data. In STGP for a predictive model to match a particular pattern in the training data the pattern must occur both within the window used the estimate the parameters of the conflict resolver, and in the window to score the predictive models. This is done to prevent STGP from learning from noise, and to help it generalise. Infrequent region changes that only appear in one of the windows will not be modelled, and are seen as noise. This is why some of the infrequent region
changes in the CCTV dataset were not modelled. This can be verified in the results as the predictive models learnt from different folds modelled different actions. Neural Networks, and Progol got results that were statistically the same on the clean dataset. Bayesian Networks, C4.5 and Progol combined with Pe got the worst results on the clean dataset. The methods get similar results with increasing levels of noise, except for STGP, and Progol combined with STGP. Progol fails to get good results, because the CCTV dataset is non-deterministic which affects its fitness function (explained previously). When Progol is combined with Pe accuracy is not improved. This is due to problems with clashing clauses, which effect Pe’s accuracy. By combining Progol with STGP its accuracy results are improved, and they are shown to be statistically similar to STGP (p-value on clean data is 0.03, with 5% noise is 0.0003, and with 10% noise is 0.01).

![CCTV Clean](image1.png) ![CCTV Clean](image2.png) ![CCTV 20% Noise](image3.png) ![CCTV 20% Noise](image4.png)

Figure 4.27: The mean accuracy and coverage for CCTV Clean (top) and CCTV 20% noise (bottom). The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

### 4.10.3 Parameter experimentation with STGP

This section presents results from experimenting with the different STGP parameters to see how they affect its performance on different datasets. The initial values for the param-
eters are shown in Table 4.4, these were based on typical parameter values from the GP literature. The rest of this section will show experiments varying each of the parameters in turn. The best results from each experiment are used in subsequent experiments.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Population Size</td>
<td>6000</td>
</tr>
<tr>
<td>Tarpeian value</td>
<td>None</td>
</tr>
<tr>
<td>Maximum number of generations</td>
<td>100</td>
</tr>
<tr>
<td>Initialisation generations</td>
<td>10</td>
</tr>
<tr>
<td>Selection method</td>
<td>Tournament selection using 6 individuals</td>
</tr>
<tr>
<td>Percentage of operators</td>
<td>Reproduction (10%), Delete (10%), Adding (40%), Replace (40%)</td>
</tr>
<tr>
<td>in initialisation generations</td>
<td></td>
</tr>
<tr>
<td>Percentage of operators</td>
<td>Reproduction (10%), Crossover (50%), Mutation (10%), Delete (10%), Adding (10%), Replace (10%)</td>
</tr>
<tr>
<td>in normal generations</td>
<td></td>
</tr>
<tr>
<td>Conflict resolver type</td>
<td>Probabilistic</td>
</tr>
</tbody>
</table>

Table 4.4: Initial settings for STGP.

### 4.10.3.1 Population Size

The following values were used for the population size parameter: 1000, 2000, 3000, 4000, 5000, and 6000. Figure 4.28 show the accuracy results on the clean versions of the datasets. The graphs show that by increasing population size this is not a statistically significant change in the average accuracy of the results. Similar results were seen on the medium and high noise datasets. The PSS and Uno2 clean datasets have a large amount of variance in the accuracy results for population size 1000, when compared with the other population sizes. To increase population diversity, and provide STGP with a greater range of predictive models when trying to find a solution it was decided to keep the population size at 6000 for all the datasets in this chapter. This allows STGP to deal with noisy datasets, and makes it more likely to converge to the correct solution.

### 4.10.3.2 Tarpeian value

In the population size experiments there were no constraints on the possible size of the predictive models. Figure 4.29 shows that the average size of the predictive models across all datasets typically increased a constant rate to the number of generations STGP had performed. This relationship is the same regardless of population size, and shows the predictive models suffer from bloat. As explained in Section 2.6.7 bloat causes the predictive models to contain redundant elements which could make them less general, and
Figure 4.28: The mean accuracy graphs for population size on the clean datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

slow down STGP’s search for a solution. To control bloat the Tarpeian method [22] was used. The amount of bloat control is based on the Tarpeian value that varies from 1 to 10. Two experiments were then performed. The first experiment applied Tarpeian bloat control over the entire run using the Tarpeian values in the integer range of 1 to 10. The second experiment delaying the Tarpeian bloat control until after the 10 initialisation generations had been performed, to see if the increased diversity in the initial generations of the run would produce better results.

To find the best Tarpeian value for each dataset requires finding the lowest value which
has an accuracy at least as good as the accuracy for the dataset with no Tarpeian control. This means finding on the accuracy graph the point where the mean accuracy begins to flatten out.

Figure 4.30 shows the accuracy values for the Tarpeian values on the clean datasets. Figure 4.31 shows the average model size for the different Tarpeian values. It can be seen that for CCTV and Uno2 a Tarpeian value of 3 will produce results with the same accuracy as without using bloat control, but the size of the predictive models is significantly reduced. For Uno and PYCR this value is 4, and for PSS this value is 5. PSS requires a more complex predictive model than the rest of the datasets which explains in its higher Tarpeian value. For all datasets a Tarpeian value of 2 did not get good accuracy results when compared to the accuracy results to not using bloat control. The medium noise accuracy results for the datasets show a similar picture. The accuracy results on the high noise datasets show they require slightly different Tarpeian values. PSS, Uno2, CCTV and PYCR require a Tarpeian value of 4; and Uno requires a Tarpeian value of 6.

Figures 4.32 and 4.33 show the accuracy and size results on the clean datasets when the Tarpeian bloat control is not performed for the initial 10 generations. It can be seen that there is no significant difference in the results when compared with using Tarpeian bloat control for the entire run. The same findings are found on the medium, and high noise datasets. It was therefore decided to apply Tarpeian bloat control for the entire length of the run.

The Tarpeian method controls the size of the population, which affects its diversity. The results show that a very low Tarpeian value decreases the diversity of the population too much, and prevents STGP from finding the correct solution. The datasets which require simpler predictive models like Uno, and Uno2 require a slightly lower Tarpeian values than the datasets which require more complex predictive models like PSS. Chapter 7 presents an adaptive Tarpeian method that varies the Tarpeian value during the run.
Figure 4.30: The mean accuracy results for the clean datasets on different Tarpeian values. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

of STGP. This stops the user from having to decide which Tarpeian value to use, and optimises the Tarpeian value depending on the current state of the population.

4.10.3.3 Tournament selection

Tournament selection (Section 2.6.4) is one technique to select individuals in the population, the next section will show another called Roulette wheel. It requires a value which determines how many individuals in the population will take place in the tournament. A low value will cause tournament selection to select more randomly from the population,
and higher values will cause it to select more from the fitter individuals in the population. To find the best value for the datasets an experiment was performed that tried out the following tournament selection values: 2,5,10,20,40,60,80,100,120,140,160,180, and 200.

Figure 4.34 shows how the different tournament selection values performed on the clean datasets. It can be seen that for the PYCR, Uno and PSS datasets an increased tournament selection value reduces the mean accuracy of the results (PSS p-value=0.004, PYCR p-value=0.05, Uno p-value=0.03; calculations based on tournament values 5 and
Figure 4.32: The mean accuracy results for the clean datasets on different Tarpeian values where Tarpeian bloat control starts after the first 10 generations. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

For the Uno2 and CCTV datasets a increased tournament selection value had no statistically significant change in the accuracy in the results (Uno2 p-value=0.35, CCTV p-value=0.43; calculations based on tournament values 5 and 200). Across all datasets a tournament selection value of 2 produced poor results. A similar pattern can be seen as with the medium noise datasets as with the clean datasets, with the exception that STGP gets worse accuracy results on the Path dataset with an increasing tournament selection value, and the accuracy results on the Uno dataset do not have a statistically significant (p-value 0.64) change as the tournament selection value is increased. On the datasets with
Figure 4.33: The mean size results for the clean datasets on different Tarpeian values where Tarpeian bloat control starts after the first 10 generations. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

High noise levels varying the tournament selection value has little change in the results apart from for PYCR where it got worse accuracy with an increasing tournament selection value. The variation in the results is due to population diversity. Larger tournament selection values force STGP to sample more from the fitter individuals in the population, which will reduce the population diversity. For some datasets like Uno, and Uno2 it has been shown that solutions can still be found even with reduced population diversity, but for the rest of the datasets this reduced diversity will not allow STGP to find the correct solution. Small tournament selection values on the other hand increase the population
Figure 4.34: The mean accuracy results for the clean datasets on different Tournament selection values. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

diversity, but force STGP to search randomly over the space of predictive models. This random search will take longer time to find the correct solution, and often results in STGP finding a locally optimal solution. A balance between using a tournament selection value which is too small, or too large needs to be found. It was decided to keep the tournament selection value at 6 for all datasets in the remaining experiments, which is a reasonable compromise based on the results shown.
4.10.3.4 Roulette wheel

Roulette wheel selection (Section 2.6.4) is analogous to allocating space on a circular wheel depending on each individuals fitness. A pointer is then virtually spun to select individuals. Figure 4.35 shows graphs showing the results of Roulette wheel and Tournament selection on the clean datasets. It can be seen that Roulette wheel selection does not produce very accurate results for all datasets. This can be explained in more detail by looking at the best value for the generations, as shown in Figure 4.36. These graphs show that the best score for the individuals using Roulette wheel either stays constant or increases (when it should go down). This shows that Roulette wheel selection is selecting too randomly from the population, and is not focusing on the fitter individuals in the population affecting the accuracy results. The same results can be seen on the medium noise datasets. On the high noise datasets there is not any statistically significant difference between Roulette wheel and Tournament selection on PYCR, and Uno2. It was decided to keep tournament selection as the selection method due to its the better accuracy results over Roulette wheel selection.

4.10.3.5 Maximum number of generations

To find out if increasing the maximum number of generations STGP is run for would increase the accuracy of the results an experiment was performed. STGP was run with the following values for the maximum number of generations: 150, 200 and 250. For all datasets there was no change in the results for by increasing the generation value from 100 generations. Figure 4.37 shows the average best value for each generation for the clean datasets It can be seen that STGP converges on a solution by 100 generations for all datasets, and that the average best value does not change by increasing the amount of generations. This explains why running STGP for more generations does not increase the accuracy of the results. A generation value of 100 was therefore chosen, to be used for all datasets.

4.10.3.6 Operators

The final parameter to investigate was the operators used to evolve the predictive models. In Table 4.4 the percentage of the adding and replacement operators is increased for the first 10 generations. Then the percentage of these operators was reduced, and the percentage of the crossover operator is increased. The idea behind this approach is to initially perform a global search to try and find the best number of production rules in the predictive models. Then a local search is performed to try and locally optimise the predictive
models. To see how this global search effects the results an experiment was performed. It looked into varying the number of generations the global search was performed for. The values were None, 10, 20, and 30.

Figure 4.38 shows the results on the clean datasets. STGP got the best score on Uno, PYCR and PSS by using 10 generations of the global search phase. For Uno and PSS STGP converged in half the number of generations by using 10 generations of the global search phase than for any other value. STGP found the best solution on the Uno2 dataset by using 20 generations of the global search phase. STGP converges on the solution for
Figure 4.36: The best fitness score for the predictive models for the clean datasets using Roulette wheel, and Tournament selection.
Figure 4.37: The best fitness score for the predictive models for the clean datasets with different values for the maximum number of generations.
the CCTV dataset so long as some form of global search phase is used. By not using the
global search phase it can be seen that it takes STGP longer to converge to a solution,
and on the Uno2 and PYCR datasets it fails to converge on the correct solution. Similar
comments can be applied to the results for the datasets with medium noise, as for the
clean datasets. STGP, however, converges fastest on the Uno2 dataset with a global search
period of 10 generations, but gets slightly better results with a global search period of 30
generations. A similar story can be applied to the results from the datasets with high
noise, apart from the Uno2 dataset the best global search period is 10 generations. For the
Uno2 dataset the best results are found with 20 generations for the global search period.

The results show that a period of increased adding and replacing of production rules in
the predictive models reduces the convergence time, and also makes it more likely to find
the correct solution. Solutions for the CCTV dataset can be found by just using global
search, but for the rest of the datasets a combination of the global search, and local search
are required to find the correct solution. This shows that for the CCTV dataset all the
production rules required for the solution are generated in the initial generation, and all
that is required is to find the correct combination of these production rules. For the rest of
the datasets finding the best combination of the production rules generated in the initial
generation allows STGP to find the correct area of the search space to locate the correct
solution. Then the crossover and mutation operators can be used to locally optimise the
production rules to find the correct solution.

The number of generations that the global search is performed for effects the number
of generations it takes STGP to convergence on the correct solution, and its ability to
find the correct solution. The results show that performing the global search for a larger
number of generations (e.g. 30) causes the value of the best predictive model to converge
during the global search, this value only starts to reduce when local search is performed.
Converging during the global search is bad for two reasons: it reduces the diversity in the
population, which might mean STGP will not find the correct solution; and it increases the
number of generations required to find the correct solution. The value of 10 generations
for the global search was chosen for all datasets.

4.10.4 Conflict resolver

The previous experiments all used the probabilistic conflict resolver described in Section
4.6. An experiment was performed to see what would happen if a very simple conflict
resolver was used, where every production rule that was enabled was fired to produce a
prediction. This was only performed on the deterministic datasets (Uno, Uno2, and PSS)
Figure 4.38: The fitness score results for the best scoring predictive models for the clean datasets where the number of generations performed on the global search is increased.
as the conflict resolver is unable to deal with non-deterministic data. The experiment was the same as the Tarpeian value experiments from Section 4.10.3.2. Figures 4.39 and 4.40 show the results on the clean datasets. It can be seen that the accuracy results on both: using bloat control for the entire run, and delaying bloat control by 10 generations is significantly worse than the accuracy results using a probabilistic conflict resolver (Section 4.10.3.2). These results showed that when a probabilistic conflict resolver was used the accuracy was close to 100% on the clean datasets. Similar results were observed on the medium and high noise datasets. For these reasons it was decided to use the probabilistic conflict resolver for all the datasets in this chapter.

The reason why the predictive models using the simple conflict resolver performed poorly (in terms of both coverage and accuracy) is down to one reason: a more complex search space. The search space when using the simple conflict resolver is full of local optima compared to one where a probabilistic conflict resolver is used. The search space contains many predictive models where the only way to get into the fitter part of the search space is to firstly find a less fit area of the search space. This is because to improve the fitness of a predictive model it must go through two states. Firstly some of its production rules must be enabled at the same time, but when fired they produce different predictions, which causes a conflict. Then the predictive model has to evolve to resolve this conflict. When the sub-models are conflicting the predictive model gets a lower fitness score than it currently has. Once the conflict has been resolved the predictive model gets a higher fitness score. STGP probabilistically selects fitter predictive models for use in the next population. This can mean that the evolution can get stuck in a local optima where the predictive models containing conflicting production rules are never picked and the run locally converges.

4.11 Conclusions

This chapter has described Spatio-Temporal Genetic Programming (STGP). This is used to learn the predictive models as described in Chapter 3. It has been compared with Progol, Neural Networks, Bayesian Networks, and C4.5; on five different datasets. Three were deterministic, and two were non-deterministic. STGP got the best results overall. Progol suffered from a clause clashing problem that effected both its coverage and accuracy. When Progol was combined with Pe it managed to improve Progol’s coverage, but due to clashing clauses it does not improve its accuracy. Combining Progol with STGP improved both Progol’s coverage and accuracy on all datasets. Bayesian Networks and C4.5 performed fairly well, but were limited due to their inability to learn generalised
rules from data.

STGP produces the best results with: some form of size control on the predictive models; the tournament selection sampling technique using a tournament selection value that favours the better scoring predictive models; and an increased amount of adding and replacement of production rules in the initial 10 generations of the run. The results on the maximum number of generations showed that STGP had converged on a solution by 100 generations. Work could be done to investigate diversity techniques (Section 2.6.7) to see
Figure 4.40: The mean accuracy and size results for the clean datasets on different Tarpeian values where a simple conflict resolver is used in the predictive models. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

if maintaining diversity for a larger number of generations improves the results.
Chapter 5

Learning Predictive Models Using A Qualitative Representation of Time

5.1 Introduction

In Chapter 4 the predictive models used a sequential approach for representing time. This is not very robust to noise and the presence of multiple objects, for reasons which will be discussed in Section 5.2. This chapter describes the use of qualitative relations to represent time, which solves this problem. Four novel temporal state relations are described, shown in Section 5.4. Section 5.6 firstly presents a comparison of STGP, with: Progol [82], Neural Networks [111], Bayesian Networks [94] and C4.5 [99] on learning predictive models containing temporal relations from an Uno dataset, and a CCTV dataset. Secondly, to see how the temporal relations allow a predictive model to deal with noise, and multiple objects the STGP results on the CCTV dataset from this chapter, and Chapter 4 are applied to two CCTV test sets one containing multiple people, and one containing random injection noise. Thirdly, results with experimenting with some of the parameters for STGP is presented.
5.2 Quantitative representation of time

Section 2.4.2.2 described Markovian approaches to temporal modelling include Variable Length Markov Models (VLMMs) [35] and Markov Chains. Each observation represents a state of the world at a specific time. The sequence of observation vectors are used to predict the most likely subsequent observations. Our work in Chapter 4 followed this principle: the variables in the condition section used a relative Point time representation to reference entity and relationship instances in the history. There are two main issues with this implicit representation of time. Firstly, when there is injection noise occurring in the data (i.e. noise occurs as extra items between the data items), and secondly when there are multiple objects in the scene. These both cause the sequence ordering to change. Any predictive models that rely on an explicit observation sequence ordering will then fail to recognise the observations, and will be unable to make a prediction.

To illustrate the problems with the sequential representation of time we take an example inspired by the CCTV domain in Chapter 4. Figure 5.1 shows a crossroads. On the crossroads are five circular regions numbered 1 to 5. When motion is detected in a region, the region will produce an output. An arrow represents a person walking through the crossroads going through regions 1, 2 and then 3. The motion through the crossroads can be represented using continuous time as shown in the graph in Figure 5.1. To be able to use this data with a sequential representation of time it must be converted into an observation sequence. This is normally done by temporal quantisation. There are two possible approaches: sample from the data at a fixed rate, or compress each of the constant property time ranges into a single sample, by sampling at one point per time range (for example the end, or start time) illustrated in Figure 5.1. Fixed sampling produces a far more detailed representation of the data, but often contains large amounts of repeated data. Compressing the time ranges reduces the amount of information that is represented (for example the length and absolute start and end times are lost), but it is a more compact representation which can be easier to learn from due to its lower complexity.

Figure 5.2 shows how injection noise might affect a predictive model. The same person is walking through the crossroads passing through regions 1, 2, and 3, but this time region 4 outputs incorrectly (for example due to camera noise). This can be seen as injection noise occurring between region detections at locations 1 and 2 in both the continuous time graph and in the observation sequence. This may cause problems if the model relies on an observation sequence occurring in a fixed ordering.

Figure 5.3 shows the same crossroads, but now two people are walking through at the same time. It will be used to show how multiple objects in the scene might affect the pre-
Figure 5.1: This diagram shows a person walking along a crossroads and passing through the circular regions numbered 1, 2 and 3. The movement in the scene is represented as a continuous time graph. Temporal quantisation is applied to the graph to produce a sequence of region detections.

Figure 5.2: This diagram shows a person walking along a crossroads and passing through the circular regions numbered 1, 2 and 3, and region 4 (shaded) firing erroneously.

dictive model. The first person follows the same route as in the previous example, and the second person walks through regions 4, 2 and finally 5. The motion in the crossroads is shown in the continuous time graph. The graph shows that the movement of the two people in the crossroads causes motion in different regions at the same time. The observation sequence in the first example (1, 2, 3) now has extra regions occurring in the middle of it. This will again cause problems if the predictive model relies on an observation sequence
occurring in a fixed ordering.

Tracking objects using a separate model per object is one solution to modelling multiple objects. However, this is not always possible or reliable: for example a person might get occluded by other people in the scene which would make it harder to constantly track them. Hidden Markov Models [102] (Section 2.4.2.2) are one approach to deal with random injection noise. These probabilistically map a set of observations to a set of states. They, however, cannot model interactions between multiple objects. Coupled Hidden Markov Model [92], are an approach to solve this problem, but approach is limited to a maximum of two objects, as above this amount there only exists approximate inference techniques.

5.3 Qualitative representation of time

The previous section showed that when a predictive model relies on a sequence of observations occurring in a fixed ordering it might fail to recognise the same observation sequence when it contains injection noise, or multiple objects (distractor noise). The predictive models for STGP in Chapter 4 used Point time to represent the position of the observations in the observation sequence. This is not robust to injection, or distraction noise. An alternative approach is to use interval time (Section 2.3.2) to describe the time of the observations, and to use a predictive model based on the qualitative relationships between different time intervals. The benefit of this approach is that it can be more robust.
to injection noise and multiple objects because a predictive model uses temporal relations, rather than using explicit positions in the observation sequence. The point time approach could work if it could be trained on every possible observation sequence ordering, but using a qualitative approach is potentially better because it can generalise from fewer example sequences.

Allen’s Interval Calculus [1] (Section 2.3.2), is a way to temporally represent the set of possible relationships between two time intervals. It provides a representation of time invariant to injection and distraction noise. The multi-person example from the previous section can be solved by modelling each person’s movement by a different set of Allen’s intervals. Clause 5.1 describes the first person’s movement through the crossroads. It shows that if there has been motion in region 1, which is before motion in region 2, and there has also been motion in region 2 before motion in region 3 then this was generated by Person 1.

\[
\text{Motion} (\text{Region}_1, t_1) \land \text{Motion} (\text{Region}_2, t_2) \land \text{Motion} (\text{Region}_3, t_3) \land \ \text{Before} (t_1, t_2) \land \text{Before} (t_2, t_3) \rightarrow \text{Person}_1(t_3)
\]

Clause 5.2 shows the second person’s movement through the crossroads. It shows that if there has been motion in region 4 before region 2, and there has been motion in region 2 before region 5 then it must have been caused by Person 2. Using these two clauses not only deals with the problem of injection, or distractor noise, but also allows the separation of the continuous time graph into each person’s movement.

\[
\text{Motion} (\text{Region}_4, t_1) \land \text{Motion} (\text{Region}_2, t_2) \land \text{Motion} (\text{Region}_5, t_3) \land \ \text{Before} (t_1, t_2) \land \text{Before} (t_2, t_3) \rightarrow \text{Person}_2(t_3)
\]

5.4 Temporal state relations

Allen’s Interval Calculus assumes that both of the time intervals have a start and end time. In this thesis when an object has been initially identified in a scene it will be given a time interval having a start time, but an unknown end time. An object will only receive the end time for its time interval when it cannot be identified in the scene anymore (for example by leaving the scene).

An object goes through four temporal states during the time it is in a scene. These are based on how the object’s start and end times relate to current time (Figure 5.4). Firstly, the object enters the scene: its start time is the same as the current time, but its end time
is unknown. Next, the object *exists* in the scene: its start time is less than the current time, but its end time is unknown. Next, the object is *leaving* the scene: its start time is less than the current time, and its end time is equal to the current time. Finally, the object has *left* the scene, where both its start and end times are less than the current time.

![Figure 5.4: The four temporal states, with respect to current time, an object can be in: entering, existing, leaving, and left. The dotted lines represent that we don’t know when the object will leave the scene.](image)

One possible approach to implement this is to use Allen’s intervals, but some changes have to be made. Firstly, a constant value (‘future’) must be assigned to the end time of a time interval which is unknown. Secondly, the current time must be transformed from a point time to an interval by making it exist for δ time (< currentTime, currentTime + δ>). This then collapses Allen’s intervals down from seven to four as shown in Figure 5.5. Temporal state Entering is then defined using Starts; Existing can be defined using During; Leaving can be defined using Finishing; and Left can be defined using Before.

Solving this problem by using Allen’s intervals does not seem the most logical solution because two parameters are still required (the time of the object, and the current time), increasing the size of the predictive models; and there is redundancy, as only four out of the seven relations are actually required. An alternative approach is to define a new set of temporal relations. Clauses 5.3 - 5.6 show the four temporal state relations for an object o by comparing its start time o_s, and end times o_e to the unknown time t_u, or the current time t_c. In STGP these are added as user defined functions to the condition section of the production rules. The advantage of using these temporal state relations over Allen’s intervals is they only require one parameter, rather than two. This reduces the search space, and makes finding solutions easier.
Figure 5.5: This shows how the four temporal states could be represented as Allen’s intervals. The diagonal lined filled box represents the current time, which has a time range \((\text{currentTime}, \text{currentTime} + \delta)\). The black filled box represents the object, where its unknown end time has been replaced with a constant. Temporal state Entering can be represented as Starts. Temporal state Existing can be represented as During. Temporal state Leaving can be represented as Finishing. Temporal state Left can be represented as Before.

\[
\begin{align*}
(o_s = t_c) \land (o_e = t_u) & \rightarrow Entering(o) \tag{5.3} \\
(o_s < t_c) \land (o_e = t_u) & \rightarrow Existing(o) \tag{5.4} \\
(o_s < t_c) \land (o_e = t_c) & \rightarrow Leaving(o) \tag{5.5} \\
(o_s < t_c) \land (o_e > t_c) & \rightarrow Left(o) \tag{5.6}
\end{align*}
\]

5.5 Evaluation

This section will present the datasets, and the representations used for STGP, Bayesian Networks, Neural Networks, C4.5 and Progol in the evaluation of the ideas presented in this chapter.
5.5.1 Overview of the datasets

5.5.1.1 CCTV

Two training datasets were produced: a real world dataset, and a clean dataset. The real
world dataset was generated from the real world CCTV video from Chapter 4 (Section
4.9.1.3). The scene analysis technique from this chapter (Section 4.9.2.2) was used to
produce the symbolic representation. It contained 80 region changing events. The clean
dataset was the same clean handcrafted dataset from Chapter 4 (Section 4.9.1.3). To see
how the use of temporal relations allows STGP to deal with noise three additional test
sets were produced: a clean test set, a multi-person test set, and a noise injection test
set. The clean test set was handcrafted and produced in the same manner as the clean
training set. It contained 135 region motion events. The multi-person dataset was on the
same scene used for the single person real world CCTV video, but there were multiple
people in the scene at one time. Figure 5.6 shows a screenshot from the multi person
video. The dataset contained various forms of noise caused by the overlapping people,
and contained 88 region motion events. The injection noise dataset was produced by
taking a hand crafted CCTV dataset and adding random injection noise between each
CCTV event. It contained 250 region motion events (125 were actual changes, and 125
were noisy changes).

![Figure 5.6: A screenshot from the video of a path containing multiple people.](image)

5.5.1.2 Uno

The handcrafted Uno dataset has a similar sequence to the Uno dataset from Chapter 4
(described in Section 4.9.1.1). The differences between the two datasets are the cards can
be in the scene for a range of time, and they leave the scene after, not before, the result is heard. The dataset is handcrafted and will now be described in more detail.

The computer initially sees a blank scene. Then “Play” is heard. Next two cards, each one having one of three possible coloured shapes on them, are placed down either at the same time, or one by one. If the two cards have the same coloured shape then “Same” is heard; or if they the same colour then “Colour” is heard; or if they have the same shape, “Shape” is heard; or if the cards are different then “Nothing” is heard. The cards are then removed either together, or one by one.

Two handcrafted training datasets were created: a non-noisy training set and a noisy training set. Each one contained around 50 rounds of Uno. Noisy data was prepared by adding 10% of noisy data to the non-noisy training data. The noise took the form of removing cards, removing the play state, and changing the output state.

5.5.2 Representation

5.5.2.1 STGP

The properties and entities used to learn the CCTV dataset are shown in Figure 5.7. There is one property definition Region, and this is used with the Object entity definition. The properties and entities used to learn the Uno dataset are shown in Figure 5.8. There are four property definitions: Colour, Texture, Position, and Speech, and two entity definitions: Card (with properties: Texture, Colour and Position), and Speaker (with property Speech).

<PROPERTY-DEFINITION NAME="REGION">
    <ATTRIBUTE NAME="NAME" TYPE="SYMBOLIC">
        VALUES="REGION-0, REGION-1, REGION-2, REGION-3"/>
    </PROPERTY-DEFINITION>

<ENTITY-DEFINITION NAME="OBJECT">
    <LEARNABLE VALUE="TRUE"/>
    <PROPERTY NAME="REGION"/>
</ENTITY-DEFINITION>

Figure 5.7: The property and entity definitions for the CCTV datasets.

Figure 5.9 shows the functions used to learn the CCTV dataset. There are the Allen’s intervals and the novel temporal state relations (Section 5.4). There are functions to check the existence of an object in the world Exists(Object), and functions to get property
Figure 5.8: The property and entity definitions for the Uno datasets.

information from the objects (Get(Object:Region)). Finally, as there are functions to compare symbolic data (Equal, Not-Equal), and logical functions (And, Or, Not). Figure 5.10 shows the terminals used to learn the CCTV dataset, which are constants representing the four regions.

Figure 5.11 shows the functions used to learn the Uno dataset. There are functions to check the existence of a Card, or a Speaker entity in the history (Exists(Card), Exists(Speaker)). Also, there are functions to get property information from the Cards, and Speaker entities (Get(Card:Colour), Get(Card:Position),
Exists(Object)
Get(Object:Region)
Get(Card:Texture), Get(Speaker:Speech)
And, Or, Not-Equal, Equal, Not
Enter, Leaving, Left, Existing
Before, Meets, Overlaps, Starts
During, Finishes, Time-Equal

Figure 5.9: The functions used in the CCTV datasets.
Region0, Region1, Region2, Region3

Figure 5.10: The terminals used in the CCTV datasets.
Get(Card:Texture), Get(Speaker:Speech). Next, there are functions to compare symbolic data (Equal, Not-Equal), and logical functions (And, Or, Not). Finally there are temporal state intervals, and the Allen’s intervals. Figure 5.12 shows the terminals used to learn the Uno dataset. There are colour symbols: c0, c1; texture symbols: f0, f1, f2; position symbols: p0, p1; and speech symbols: Same, Shape, Nothing, Play, Colour.

Exists(Card), Exists(Speaker),
Get(Card:Colour), Get(Card:Position)
Get(Card:Texture), Get(Speaker:Speech)
And, Or, Not-Equal, Equal, Not
Enter, Leaving, Left, Existing
Before, Meets, Overlaps, Starts
During, Finishes, Time-Equal

Figure 5.11: The functions in the Uno dataset.
c0, c1
p0, p1
f0, f1, f2
Same, Shape, Nothing, Play, Colour

Figure 5.12: The terminals in the Uno dataset.

Variables are used in the condition section of the production rules to reference entity or relationship instances in the history. In Chapter 4 the variables used Point time to constrain where in the history they could be assigned an entity or relationship instance.
Point time uses a single time value. This meant a variable was only able to be assigned entity or relationship instances associated with a specific point in the history relative to the current time. The production rules therefore could only then be evaluated at specific points in the history relative to the current time. If the objects that make the condition section of the production rule evaluate true move their location in the history (due to distractor, or injection noise) the variables in the condition section would not be able to be assigned to them, and the production rule would evaluate false. This would prevent the production rule from producing a prediction.

To allow STGP to take advantage of the temporal relations, and to deal with distractors, or injection noise the time type AllTime is used in this chapter to constrain where variables can be assigned entity or relationship instances in the history. AllTime allows the variables to be assigned entity or relationship instances anywhere in the history, within a defined time range. Section 5.6.3.2 performs an experiment to show how changing the length of this time range affects the coverage and accuracy of the predictive models. This means the production rule will be evaluated over the entire history rather than at specific points, which means that if the position of the entity or relationship instances (that causes the condition section of the production rule to evaluate true) move the condition section will still evaluate true.

5.5.2.2 Progol, and Pe

A similar representation to the one described in Section 4.9.3.1 was used for all the datasets in this chapter. The state predicate is replaced by an object data predicate that describes the properties of a specific object, and temporal predicates enter, existing, leaving, and left that describe its temporal state. To allow Progol to learn clauses that are robust to noise the successor predicate is replaced by a set of clauses representing Allen’s intervals. The same approach (described in Section 4.9.3.1) is used to convert the clauses learnt by Progol into a SLP.

5.5.2.3 C4.5, Neural Network, and Bayesian Network

The WEKA machine learning system [41] was used to perform the C4.5, Neural Network, and Bayesian Network algorithms. WEKA requires the input data to be a fixed length vector. A binary feature vector was used to record the state of the scene, along with an associated event. Each binary feature represents if a specific temporal relationship is held between a set of objects each having a specific type and set of attribute values, and position in the history. The binary feature vector represents all possible permutations of
temporal relations with objects and their states. This is typically a large set of possible features, with a large majority of them being redundant. To reduce the size of the feature vector a simple feature selection method was performed. Features were removed if they were always false, or always true, over the entire training set.

5.6 Results

This section will firstly show how the temporal relations introduced in this chapter make STGP robust to noise. Secondly it will show how STGP compares with Progol, Neural Networks, Bayesian Networks, and C4.5 on the datasets previously described. It will also show how estimating the likelihood of the clauses learnt by Progol by Pe and STGP affects the results. Finally, it will show experiments on the different parameters for STGP. Ten fold cross validation was used in all the runs, and the same evaluation criteria used in Chapter 4 (described in Section 4.10.1) was used.

5.6.1 Temporal noise robustness of STGP

Two experiments were performed to see how robust to noise the predictive models learnt in this chapter were. The experiments took the predictive models from Chapter 4 that were trained on the CCTV datasets, but did not use temporal relations; and compared them to the predictive models from this chapter that were also trained on the CCTV datasets, but used temporal relations. The first experiment compared them using the CCTV injection noise test set, and the second on the CCTV multi-person test set.

Figure 5.13 shows the coverage results for STGP on the clean test set, and the injection noise test set with, and without using temporal relations in the predictive models. The results show that predictive models are affected by injection noise when they do not use temporal relations, but if they use temporal relations they are unaffected by injection noise. This is because in the predictive models that do not use temporal relations the condition sections of their production rules assume that the entity and relationship instances that allow the condition section to evaluate true will only occur at specific positions in the history. When the injection noise affects the position of these objects in the history the condition section is unable to be assigned to them and it will evaluate false. Predictive models that use temporal relations are unaffected by the injection noise, because the use of temporal relations allows the condition sections of their production rules to be assigned entity or relationship instances from the entire of the history, which means they can still be assigned objects even if they have changed position in the history from the training set.
Figure 5.13: How the time used by the variables in condition section of the predictive models affects their ability to deal with injection noise. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

Figure 5.14 shows the accuracy results for STGP on the CCTV multi-person test set when the predictive models using, and not using temporal relations. The graphs show that using temporal relations is slightly more accurate than not using them when trained on the real world data (p-value=0.01), but when a clean training set is used the results for using and not using temporal relations are not statistically significantly different (p-value=0.35). There is not such a large difference in the results between using and not using temporal relations that was seen for the injection noise test set. This is due to two reasons. Firstly, the history used for predictive models using temporal relations has a fixed size, and sometimes it is not large enough to contain enough spatio-temporal data to make the correct prediction. Secondly, the combination of movement of multiple people can create ambiguous patterns in the history where it is unclear how many people are in the scene, making it hard to produce the correct prediction.

5.6.2 A comparison of STGP with current methods

Figure 5.17 shows the coverage and accuracy results on the CCTV dataset, and Figure 5.15 show the coverage and accuracy graphs for the Uno dataset. Overall the graphs show that STGP got accuracy results that were better than, or the same as the accuracy results for the other methods. There were no results for Neural Networks on the real world CCTV dataset, and the Uno Temporal datasets, because WEKA failed with a stack size error when learning from the training data. This indicates the set of possible relations was too large.

The optimal result for the Uno Temporal dataset is 100% coverage and 100% accuracy
Figure 5.14: How the time used by the variables in the condition section of the predictive models affects their ability to predict the actions of people from a multi-person dataset. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

(as the dataset is deterministic). It can be shown from the graphs (Figure 5.15) that STGP keeps close to this for both the clean and noisy data. The clauses learnt by Progol are too general, as shown in Figure 5.16. Here the clauses only use the temporal state and properties of one of the objects in the history. To predict most events in Uno requires the comparison of the properties of two cards from the history. As the learnt clauses only use one object the accuracy and coverage results for Progol are reduced. When the probability of these clauses is estimated by Pe there is no improvement in the accuracy because of the poor quality of the initial clauses. There is a slight improvement when the likelihood of the clauses are estimated by the conflict resolver in STGP. C4.5 and Bayesian Networks are unable to generalise from data and rely on storing common examples and their outcomes (Section 4.10.2). The results show that both of the methods were unable to learn enough examples from the training data to correctly predict from the test data.

The optimal result for the CCTV dataset is 100% coverage, and 83% accuracy. This is based on the four possible actions on the path occurring in equal proportions. The graphs show that STGP gets less than this on both accuracy and coverage for both datasets. This is due to not learning infrequent region changes in the training data. The reasons for this were explained in Section 4.10.2. Also the length of the history affects the results which will be explained in more detail in Section 5.6.3.2. The CCTV dataset is non-deterministic which is why Progol does not get good accuracy or coverage results. All the clauses learnt by Progol only make use of the properties of one region in the history, and they do not use Allen’s intervals to combine together to properties of different regions. Pe should improve the accuracy results, but this is not the case, and it shows that it is affected by Progol not learning the correct set of clauses from the training data. On the
real world CCTV dataset the results are improved by estimating the likelihood of the clauses by STGP which produces accuracy results that are as good as STGP. However, on the clean dataset the accuracy results are worse than just using Progol alone. C4.5, Neural Networks, and Bayesian Networks are unable to generalise and suffer from the same problems described for Uno Temporal, which affect their results.

```
action(s_play,A).
action(s_nothing,A) :- object_data(B,C,D,E), enter(B,A).
action(s_colour,A) :- left(B,A).
action(s_shape,A) :- left(B,A).
action(s_same,A) :- object_data(B,C,D,E), enter(B,A).
```

Figure 5.15: The mean coverage and accuracy results for the different methods on the Uno Temporal datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

Figure 5.16: An example set of clauses learnt by Progol on the Uno Temporal dataset.
5.6.3 Parameter experimentation with STGP

Section 4.10.3 showed experimentally that the values for all STGP parameters other than Tarpeian value either made little difference or were optimal over the datasets used in the chapter. For this reason, it was decided to use the best values for the parameters for all the STGP experiments in this chapter, and to experiment with the Tarpeian value parameter, and the history length parameter (which controls the length of history a variable of type AllTime can look for entities or relations). This section will show the results of these experiments.

5.6.3.1 Tarpeian value

To control the bloat the Tarpeian method [22] was used. Figure 5.18 shows the results from varying the amount of Tarpeian bloat control. For the real world CCTV dataset there was little difference in the accuracy results for the different Tarpeian values: they all got similar accuracy results to not using Tarpeian bloat control, and they all got significantly smaller predictive models than the results for not using bloat control. The clean CCTV
dataset did not get very accurate results below a value of 4 when compared to not using bloat control. The most accurate result was produced with a Tarpeian value of 6. The clean Uno dataset performed poorly on Tarpeian values below 6, when compared to not using bloat control. For values 6 and above the accuracy, and size of the results was the same as not using Tarpeian bloat control (for example the p-value for the similarity in mean size between a Tarpeian value of 6 and no bloat control is: 0.35, and the p-value for the similarity in mean accuracy is 0.79). On the noisy Uno dataset STGP got poor results for Tarpeian values below 6, and got the most accurate results for Tarpeian values 9 and 10, although these are very similar to the results for Tarpeian values 5 to 8. The size of the predictive models produced by using Tarpeian bloat control was slightly smaller than without using it (p-value=0.08).

The graphs show that for datasets that require predictive models containing simple production rules, like CCTV, a small Tarpeian value can be used. This is because STGP will typically find the correct solution in a small number of generations and will not be affected by the population diversity issues associated a small Tarpeian value. For more complex datasets like Uno a larger number of generations are required to find the correct solution. Small Tarpeian values greatly reduce the diversity of the population early on in the run, and cause STGP to converge on a sub-optimal solution. Larger Tarpeian values do not affect the diversity of the population as much, allowing STGP to find the correct solution, whilst keeping a control on its size. This is consistent with the findings from Chapter 4 (Section 4.10.3.2). Chapter 7 shows results of an adaptive Tarpeian method that varies the Tarpeian value during the run of STGP.

5.6.3.2 History length

To see how the size of the history affected STGP’s results on the Uno and CCTV datasets an experiment was performed using the history values 2 to 10. Figure 5.19 shows the results. For all datasets increasing the size of the history decreased the mean accuracy and coverage of the results. This is due to the fact that a longer history contains more complex patterns. In turn this requires learning a more complex predictive model. This increases the size of the search space, and makes finding predictive models harder.

5.7 Conclusions

This chapter has shown that using qualitative relations rather than sequence based approaches to model temporal history allows the predictive models to be robust to both
Figure 5.18: The mean accuracy and size results for the datasets using different Tarpeian values. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 5.19: The mean coverage and accuracy results for the datasets on different history length values. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
distractor, and injection noise. Four new temporal state relations have been defined, and have been successfully shown to be used on two datasets: CCTV, and Uno. STGP produced the most accurate predictive models for all datasets. Progol did not manage to learn clauses complex enough to correctly predict from the training data. The inability for Neural Networks, Bayesian Networks, and C4.5 to generalise from data affected the accuracy of their results. It was shown that using the temporal relations, rather than using a sequential approach allowed STGP to be robust to injection noise, and to be slightly more accurate when predicting from scenes containing multiple people. Finally, it was shown that the history size used by STGP affects the coverage and accuracy of the results. A possible extension to the work presented here is rather than using a fixed history size STGP could learn the best history size by using Period time in the variables. Period time takes a time range and would allow the data pointers to limit how much history, and where within the history it looked for entity or relationship instances. The time range could be learnt from the training data.
Chapter 6

Learning Predictive Models Using A Qualitative Representation of Space

6.1 Introduction

In Chapters 4 and 5 the location of the objects in the scene was described by a quantitative 2D location. If the absolute location of the objects changed (for example due to camera shift) then it is likely the predictive models would be unable to predict activities involving these objects. This chapter incorporates qualitative spatial relations into the predictive models. These look at the qualitative spatial difference between object locations. This allows the predictive models to be robust to changes in the structure of the scene, because the condition sections of the predictive models can look for patterns in the history using qualitative spatial relations between objects, rather than assuming that objects will appear in specific scene locations. Section 6.2 firstly explains this in more detail, and shows the reasons why using qualitative spatial relations to describe the location of the objects is robust to spatial noise. Section 6.4.1 shows the results of an experiment to see if using spatial relations makes STGP more robust to objects changing their spatial locations. Section 6.4 presents a comparison of STGP with Progol [82], Neural Networks [111], Bayesian Networks [94] and C4.5 [99] on three datasets: CCTV, aircraft turnarounds and Tic Tac Toe. Finally, Section 6.4.3 presents an experiment is performed on some of the parameters for STGP.
6.2 Qualitative representation of space

The positions of the objects in the datasets in Chapters 4 and 5 were represented by a quantitative 2D location. A predictive model trained on this data relies on the objects always appearing (qualitatively) at the same absolute image locations. If this is not the case then the predictive model may fail to predict correctly.

This can be explained by using an example from Section 5.2. Here there was an explicit mapping between the detector’s location and its symbolic label. The label of each detector is stored with the \((x, y)\) location of its centroid. To label a new set of detections their \((x, y)\) locations are compared to the \((x, y)\) locations of the stored detectors. If there is a match then the new detection is labelled with the stored detector’s label. On Figure 6.1 the detections from the crossroads are initially assigned to one set of stored detections. If the camera is moved (as is common with pan-tilt-zoom CCTV cameras) the detections are then assigned to a different set of stored detections. If a predictive model relies on a specific sequence of stored detections then it will fail to predict when there is image movement.

![Image movement](image.png)

Figure 6.1: This shows how movement in the scene affects detection labelling.

An alternative approach is to describe the location of the detections by how they spatially relate to each other. Section 2.3.1 presented an overview of qualitative spatial relations. A predictive model using spatial relations is more robust to noise because if the detections move but stay in the same relative spatial orientation it will still be able to make a prediction. The predictive model will often be more general and therefore be simpler because it only has to learn the spatial relations between detections rather than every possible combination of detection locations. The next section will show how spatial relations are used on three different datasets: CCTV, aircraft turnaround, and Tic Tac Toe.
6.3 Evaluation

This section will firstly present three different datasets which use spatial relations, and secondly the representations used for STGP, Bayesian Networks, Neural Networks, C4.5 and Progol.

6.3.1 Datasets

6.3.1.1 CCTV using spatial relations

The real-world single person CCTV video from Chapter 4 was used to produce the datasets. A similar scene analysis method to the one used in Chapter 4 (Section 4.9.2.2) was used to produce the symbolic representation. The method in this chapter has one difference: in Chapter 4 when a detector produced an output the scene analysis method produced a detection containing its symbolic name. In this chapter, the scene analysis method produces a detection containing its x,y location, and a relation describing how this detection spatially relates to the previous detection. Compass based level 2 orientation relations (Section 2.3.1) are used to describe how the detections spatially relate to each other. To calculate how the current detection relates to the previous detection the angle between the (x,y) image location of the current detection and the previous detection is calculated with respect to the direction of the y axis on the image. This angle is then quantised into one of four spatial regions: North, South, East and West. The training set contained 81 detections. To see how well STGP deals with detections changing their locations two test sets were produced: a handcrafted clean test set (containing 116 detections), and a similar handcrafted test set (containing 126 detections) where the locations of two of the detections were swapped over.

6.3.1.2 Aircraft turnarounds

The aircraft turnaround data was taken from the EU Co-FRIEND project. The airport apron was filmed using eight static cameras, with each camera having a different view of the scene. Figure 6.2 shows one of the camera views, where the different vehicles and people operating on the aircraft can be seen. The objects are tracked separately in each camera and the tracks from the different cameras are fused together to produce 3D data on each object. The tracking data is noisy due to the low quality of the videos, bad weather and variable lighting conditions. This causes problems including: objects not being tracked; objects being assigned different ids; or objects being assigned the

\[1\text{http://84.14.57.154/co-friend}\]
wrong object type. The tracking data is then converted into a relational description by using three of the RCC-8 relations (Section 2.3.1): surrounds, touches and disconnected. These describe how the objects in the scene spatially relate to each other, and how they also relate to static zones on the ground-plane (Figure 6.3), based on International Air Transport Association (IATA) specifications. Allen’s intervals (Section 2.3.2) are used to describe how the objects temporally relate to each other. A structured type hierarchy is used to describe the different classes of objects in the apron. This is used by the methods to produce more general predictive models from the training data.

The spatio-temporal data is hand labelled by experts in IATA protocols to describe the type and duration of events that have occurred in the apron, for example: refueling, baggage unloading, or loading the catering. To produce a set of training data the labelled spatio-temporal data is temporally compressed. This is done in two stages. Firstly, only
spatio-temporal data labelled with an event is kept, and non-labelled spatio-temporal data is removed. Secondly, for each labelled event only the spatio-temporal data occurring in a fixed length temporal window placed the end of the event is kept. Section 6.4.3.2 performs an experiment with STGP to see how the length of the window affects the results. Each event has a large amount of variation due to the noise in the tracking data. The training data set contains 70 events.

6.3.1.3 Tic Tac Toe

Tic Tac Toe is a game played by two people on a 3 by 3 grid. One person uses the symbol nought (O) and the other person uses the symbol cross (X). Each person takes it in turn to add one of their symbols to the grid. The first person to create a line of three of their symbols either diagonally, vertically or horizontally wins the game. The Tic Tac Toe data was obtained from the UCI Machine Learning Repository. The data contained a representation of the grid for every possible end game, along with the label describing if the person using crosses won the game.

The original data was represented in a fixed length vector, with each element of the vector describing the symbol used at a particular location in the grid. The data was converted into a relational description. Instead of representing the state of every location in the grid only the symbols used in the grid were described along with the spatial relations between them. Figure 6.4 shows the four spatial relations that can exist between symbols on the grid: above, above right, above left and right. The dataset contained 800 possible end games, and was noise free.

6.3.2 Representation

6.3.2.1 STGP

A similar representation described in Section 5.5.2.1 is used for all datasets in this chapter. The CCTV with spatial relations dataset used only one entity definition which describes the detection. There are also relation definitions for the four orientation relations. The aircraft turnaround dataset has entity definitions for the people, and each of the possible vehicles that can appear on the apron. There are also relation definitions for the three RCC-8 spatial relations. The Tic Tac Toe dataset has an entity definition for the symbols used on the grid. This has a property which describes the type of the symbol. It also has relation definitions for the four spatial relations shown in Figure 6.4.

---

2http://archive.ics.uci.edu/ml/datasets/Tic-Tac-Toe+Endgame
Right
Above
Above left
Above right

Figure 6.4: The four spatial relations used in the Tic Tac Toe dataset: above, right, above right, and above left.

All the datasets make use of the RelationExists function to allow the condition section to access relations in the history; and the logical functions: And, Or and Not. The aircraft turnaround and CCTV datasets have functions representing the Allen’s intervals, and temporal state relations described in Chapter 5. Finally, the Tic Tac Toe dataset uses the Get, Equal, and Not-Equal functions to allow the condition section to access and compare the types of different symbols. The dataset also uses the terminals: Cross and Nought.

In both Chapters 4 and 5 the action section of each production rule used a static entity instance, which did not use any variables from the condition section. In this chapter the CCTV dataset requires that the location of the predicted detector is not at a fixed location, but is spatially related to the location of a previous detection. The action section of the production rules therefore needs to contain a relation rather than a static entity instance. The relation contains a variable relating to the previous detector found in the condition section. This illustrates the generalisation ability of the representation.

6.3.2.2 Progol, C4.5, Neural Networks, and Bayesian Networks

The same Progol representation used in Section 5.5.2.2 is used for all datasets in this chapter. The only difference is to add the spatial relations described in Section 6.3.1 along with the temporal relations. Again, the WEKA machine learning system and the same representation described in Section 5.5.2.3 is used to perform the C4.5, Neural Networks, and Bayesian Network learning algorithms. For the datasets in this chapter the binary feature vector not only represents every possible permutation of temporal relations, but spatial relations as well. The approach from Chapter 4 (Section 4.9.3.1) is used to convert
Chapter 6 Learning Predictive Models Using A Qualitative Representation of Space

the clauses learnt by Progol into a SLP.

6.4 Results

This section will firstly show the results of an experiment to see how robust to spatial noise STGP using spatial relations is. Secondly it will show how STGP compares with C4.5, Bayesian Networks, Neural Networks, and Progol on the datasets described previously. It will also explain if estimating the likelihood of the clauses learnt by Progol, using Pe and STGP, improves the results. Finally, the results with experimenting with some of the different parameters for STGP is given. All the experiments used 10 fold cross validation, and the same evaluation criteria from Chapter 4 were used (Section 4.10.1).

6.4.1 Spatial noise robustness of STGP

An experiment was performed to see if the predictive models using spatial relations were robust to spatial noise. The predictive models learnt from the real world CCTV dataset in this chapter, were compared against the predictive models learnt on the same dataset from Chapter 4. Two test sets were used: a handcrafted clean data set, and the similar handcrafted dataset where the locations of two of the detectors were swapped. Figure 6.5 shows the results of the experiment. It can be seen that the predictive models that relied on the detectors occurring in the specific 2D locations were affected when the location of these detectors was changed. The predictive models that used spatial relations were unaffected by the change in detector locations. This is because the predictive models that rely on the detectors being in the specific locations assume the detectors will always occur in a specific sequence. When the location of the detectors is changed, the order of the detectors in the sequence is also changed. This prevents the predictive model from matching the sequence and from making a prediction. The predictive models that use spatial relations look at the spatial change between the location the current detection, and the previous detection. This produces a sequence based on relative spatial change between detectors, rather than the identifiers of the detectors themselves. This will be unaffected by the changes in the actual location of the detectors, which is why the predictive models using spatial relations is still be able to correctly produce a prediction.

6.4.2 A comparison of STGP with current methods

The accuracy results for the different methods on the CCTV dataset is shown in Figure 6.6. The graph shows that STGP produces the most accurate results when compared with
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Figure 6.5: Accuracy and coverage results showing how the movement in the location of the detectors in the CCTV dataset affects the predictive models using and not using spatial relations. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

The other methods, and the difference in accuracy is statistically significant. The optimal result for the CCTV dataset was 100% coverage and 83% accuracy. This is based on the four possible actions on the path occurring in equal proportions. The results for STGP show that it achieved less than this for both coverage and accuracy. The coverage was reduced because STGP did not learn infrequent changes between detectors. The accuracy was reduced because the condition sections of the production rules were not complex enough. Most condition sections only looked at the relations between two previous detections which meant they did not predict well on the more complex patterns that involve the relations between three or more detectors. This is because two or more production rules would match the complex pattern and both produce a prediction reducing the overall accuracy. If a production rule was learnt that could match the complex pattern only it would produce a prediction and the accuracy would be increased.

Some of the clauses learnt by Progol were incorrect because they predict by using data in the future. Figure 6.7 shows one of the clauses learnt by Progol. It can be seen that the east_next, and the north_next clauses base their prediction on the future east or north relations. There is no way to easily prevent Progol from using future data when learning the clauses, which makes it an unsuitable method to learn predictive models of temporal data. The rest of the clauses learnt were too general and made a prediction based on whether a detection had just occurred. This can be seen in Figure 6.7 where the west_next and south_next clauses just contain the enter literal. When the likelihood of the clauses was estimated by Pe there was no improvement in their accuracy. This was because the over general clauses always produce a prediction, which affects the accuracy of clauses that predict correctly. There was, however, an improvement
in the accuracy of the results when the conflict resolver in STGP was used to estimate the likelihood of the clauses. This is because Pe must fire all enabled production rules, and the likelihood of a prediction is based on the likelihood of the other predictions. Incorrectly fired production rules will reduce the accuracy of the correct predictions. The conflict resolver in STGP can probabilistically decide based on a set of enabled production rules, which production rules to fire which is why it gets better accuracy results than Progol and Pe. C4.5, Neural Networks, and Bayesian Networks did not achieve high accuracy. This is because, as explained in Chapter 5, these methods can not generalise, and rely on memorising frequently occurring events. If there is not enough training data to learn the possible events, then the methods will perform poorly on the test data, which can be seen in the results.

Figure 6.6: The accuracy and coverage results for the different methods on the CCTV Spatial dataset. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

```prolog
action(east_next, A, B) :- enter(A, B), east(C, A, D).
action(west_next, A, B) :- enter(A, B).
action(north_next, A, B) :- enter(A, B), north(C, A, D).
action(south_next, A, B) :- enter(A, B).
```

Figure 6.7: An incorrect set of clauses learnt by Progol from the CCTV Spatial dataset.

The accuracy and coverage results for the different methods on the aircraft turnaround dataset is shown in Figure 6.8. The optimal result would be 100% accuracy and 100% coverage, and random chance would on average receive an accuracy of 6% (as there are 16 possible events). The graph shows that the results from the different methods have similar accuracy, and the accuracy for all methods is very low (being below 40% for all methods). Neural Networks did not produce a result as WEKA failed with a Stack size error when
learning from the training data. This indicates the set of possible relations given to WEKA was too large. The confusion matrices for STGP, Progol, Bayesian Networks and C4.5 are shown in Tables 6.2 to 6.5. Figure 6.1 provides a key to relate event numbers to event labels. The graphs show that overall STGP achieved the largest number of correct predictions with a total of 14; C4.5 achieved 11 correct predictions; Bayesian Networks achieved 6 correct predictions and Progol achieved 5.

Some of the events, like catering and loading/unloading from the plane, occur infrequently in the training data which explains why in all methods they are not learnt correctly. STGP produces good coverage results when predicting aircraft arrival, but predicts less well for handler deposits chocks, and the loading and unloading events on the aircraft. Around a third of the time STGP is unable to produce a prediction due to the poor tracking data. Progol typically predicted Ground Power Unit (GPU) positioning for all events, causing it to get poor results. This is due to Progol firstly not learning very specific clauses for the events, and secondly the ordering of the clauses causes Progol to always predict the same event. Bayesian Networks achieved some correct predictions for the aircraft loading and unloading events, but gets confused between aircraft arrival and aircraft departure. Finally, C4.5 achieved some correct predictions for Handler Deposits Chocks and Passenger Boarding Bridge positioning, but failed to correctly predict aircraft arrival and departure. It achieved some good results for aircraft loading events but often confuses unloading events for loading events and vice versa.

![Figure 6.8: The accuracy and coverage results for the different methods on the aircraft turnaround dataset. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.](image)

The coverage and accuracy results for the methods on the Tic Tac Toe dataset is shown in Figure 6.9. The optimal obtainable result is 100% coverage, and 100% accuracy. The results show that all methods except Bayesian Networks got good accuracy, and coverage results that were close to the optimal result. STGP got mean accuracy results that were
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0=Aircraft Arrival  1=Aircraft Departure
2=Catering         3=Handler Deposits Chocks
4=Passenger Boarding Bridge Positioning  5=Passenger Boarding Bridge Removing
6=Suitcase Loading  7=Suitcase Unloading
8=Ground Power Unit Positioning  9=Ground Power Unit Removing
10=Left Refuelling Operation  11=Push Back Positioning
12=Right Aft Container Loading Operation  13=Right Aft Container Unloading Operation
14=Right Forward Container Loading Operation  15=Right Forward Container Unloading Operation
16=No Prediction

Table 6.1: The key for the event types used in the aircraft turnaround dataset.

<table>
<thead>
<tr>
<th>Pred.</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
<th>13</th>
<th>14</th>
<th>15</th>
<th>16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td>0</td>
<td>16</td>
<td>2</td>
<td>5</td>
<td>1</td>
<td>2</td>
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Table 6.2: The confusion matrix for STGP on the aircraft turnaround dataset.

<table>
<thead>
<tr>
<th>Pred.</th>
<th>0</th>
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<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
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<th>9</th>
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<th>11</th>
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<th>13</th>
<th>14</th>
<th>15</th>
<th>16</th>
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<tbody>
<tr>
<td>Total</td>
<td>0</td>
<td>1</td>
<td>3</td>
<td>6</td>
<td>5</td>
<td>1</td>
<td>2</td>
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Table 6.3: The confusion matrix for Progol on the aircraft turnaround dataset.

A large amount of training data was used (800 out of a possible 900 games), which

slightly worse than Progol, C4.5 and Neural Networks. This was because STGP learnt
production rules that in some cases are not specific enough to cover all the different types
of end games. Progol got good results on the dataset because this is the type of data that
Progol has been designed to learn from (non-deterministic, and containing structural rela-
tions). A large amount of training data was used (800 out of a possible 900 games), which
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Table 6.4: The confusion matrix for Bayesian Networks on the aircraft turnaround dataset.

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Table 6.5: The confusion matrix for C4.5 on the aircraft turnaround dataset.

meant that Neural Networks, and C4.5 had enough training data to memorise common examples. This explains why it achieved such good accuracy, and coverage results on the test fold. When the likelihood of the clauses were estimated by using the conflict resolver in STGP, and Pe there was no significant change in the accuracy or coverage results.

### 6.4.3 Parameter experimentation with STGP

In a similar manner to Chapter 5 the STGP experiments in this chapter used the best settings from Section 4.10.3. STGP has an inefficient implementation of the Find Best Substitution algorithm (Figure 3.12). To see if a production rule matches a set of history, all possible combinations of objects, and their relations from the history that might match its condition section are evaluated until one is found that causes the condition section to evaluate true. In the Tic Tac Toe, and CoFriend datasets there can be a large number of combinations to evaluate, which has a large impact on the run-time of STGP (a run for example might take 7 days to complete). To make the runs complete in a more
Figure 6.9: The accuracy results for the different methods on the Tic Tac Toe dataset. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

reasonable time a set of constraints were added to STGP. A limit on the number of combinations that could be searched over was added to the Find Best Substitution algorithm. Any condition section that requires more than this number of combinations is assumed to have evaluated false on the history. All the runs for the Tic Tac Toe dataset also had a reduced population size of 3000, and the maximum number of generations was reduced to 70. A potential solution to this problem is discussed in the Conclusion section at the end of this chapter. The remainder of this section will show experiments with two STGP parameters: Tarpeian value, and History length to see how their values affect the predictive models learnt by STGP.

6.4.3.1 Tarpeian value

An experiment was performed which varied the Tarpeian value for the Tarpeian bloat control method [22] on the three training datasets from this chapter. The results are shown in Figure 6.10. For the CCTV Spatial dataset there was little change in the accuracy by increasing the Tarpeian value when compared to no bloat control. However for all Tarpeian values the size of the predictive models is significantly reduced when compared with the size of the predictive models produced with no bloat control. A Tarpeian value of 4 was the optimal value. Similar results are found for the CoFriend dataset. Again there is little change in the accuracy of the results when using bloat control when compared to not using bloat control. For Tarpeian values below 7 there is a statistical significant reduction in the size of the predictive models when compared to not using bloat control. For the CoFriend dataset a Tarpeian value of 6 was the optimal value. Finally, for the Tic Tac Toe dataset there is no statistical significant difference in both the size and accuracy of the predictive models when using bloat control compared to not using bloat control.
This shows that the limit on the number of combinations affects the size of the production rules produced, and explains why using Tarpeian value control does not reduce the size of the predictive models any further.

Figure 6.10: The mean accuracy and size results for the datasets on different Tarpeian values. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

6.4.3.2 History length

An experiment was performed to see how the length of the history used for the CoFriend, and CCTV Spatial datasets affected the results. For the CCTV Spatial dataset history of
lengths 2 - 10 was used, and for the CoFriend dataset history lengths of: 5, 10, 15, 20, 25, and 30 was used. A longer history length is used for CoFriend, because the temporal length of some of its events is much longer than the events in CCTV Spatial. Figure 6.11 shows the results from the experiments. The CCTV Spatial dataset had no change in the accuracy of the results as the history length was increased. There was a statistically significant decrease in the coverage of the results (p-value between history length 3 to 9 is 0.002). This is because the longer history length produces more complex patterns to learn from, which are harder for STGP to learn predictive models of. For the CoFriend dataset there was no change in the accuracy or coverage of the results for all history values.

![CCTV Spatial](image1)

![CCTV Spatial](image2)

![CoFriend](image3)

![CoFriend](image4)

Figure 6.11: The mean coverage and accuracy results for the CCTV Spatial, and aircraft turnaround datasets on different history length values. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.

### 6.5 Conclusions

This chapter has shown that the use of qualitative spatial relations allows the predictive models to be robust to spatial noise. Section 6.4.1 verified this experimentally by showing that the predictive models learnt from the CCTV data in Chapter 4 (which rely on the
detectors occurring in a specific ordering) fail when the detectors are moved. The predictive models learnt in this chapter are robust to this noise, because they use qualitative spatial relations that look at the spatial change between the location of detections, rather than relying on the detectors occurring in absolute locations. The accuracy results for all methods on the CoFriend dataset was very poor. STGP got the most accurate results on the CCTV Spatial, but got worse accuracy results than Progol, C4.5 and Neural Networks on the Tic Tac Toe dataset. Progol, C4.5 and Neural Networks did not get very accurate results on the CCTV Spatial dataset, but got very accurate results on the Tic Tac Toe dataset.

STGP has an inefficient method to evaluate the condition section of a production rule on a history. It was shown to be an issue (Section 6.4.3) on the CoFriend, and Tic Tac Toe datasets, as large combinations of entities and relations need to be checked. Techniques from databases, or Prolog could be used to fix this problem. These would match parts of the condition section to parts of the history, until an overall match is found. This makes it a more efficient search process than looking over all possible combinations from the history that might match the condition section.

Progol has no temporal constraints during its search to find the most general clause. This can cause it to predict using relations or entities from the future, as was shown in the results from the CCTV Spatial dataset. One way to prevent this from happening is to only allow Progol to see previous spatio-temporal data when it is generalising the most specific clause. This would require changing how the most specific clause is generated, to take into account temporal constraints from the data.
Chapter 7

Automatic Bloat Control in Genetic Programming

7.1 Introduction

In Chapters 4 - 6 experiments were performed using STGP to see what was the best Tarpeian value for different datasets. The experiments had two main conclusions. Firstly, there was no universal optimal Tarpeian value for all datasets. Datasets which require a simpler predictive model typically have a lower optimal Tarpeian value, than datasets which require more complex predictive models. Secondly, having a fixed Tarpeian value may not produce the most accurate and smallest predictive models.

Ekárt and Németh [21] adapt the diversity of the population during the run. In the initial stages of the run a high diversity is maintained, and in the later stages of the run a lower diversity is allowed to force GP to converge on a solution. This chapter investigates a similar technique to vary the Tarpeian value during the run of STGP. It is proposed that during a run a high Tarpeian value (causing high population diversity) is typically required at the start to help STGP find good solutions, and a lower Tarpeian value (causing lower population diversity) is then required once STGP has converged on a solution to reduce the size of the predictive models. This chapter investigates using an adaptive Tarpeian method that varies the Tarpeian value during the run based on the current and initial best fitness values. Section 7.2 presents the method, and Section 7.3 shows the results of the
method applied to the datasets from Chapters 4 - 6.

7.2 Adaptive Tarpeian value

The results from Chapters 4 - 6 showed that there was not a single Tarpeian value that will guarantee both good coverage, and accuracy, and small sized predictive models for all datasets. The problem is that some datasets like Uno and Uno2 require a low Tarpeian value from the start to get a good solution. However, others like PSS, and Uno Temporal need a higher Tarpeian value to get accurate predictive models, but it is not small enough in the later stages of the run to produce very small predictive models.

The Tarpeian bloat control method can be seen as controlling the size of the population. Low Tarpeian values will greatly reduce the size of the population that is sampled from by the genetic operators, and this creates a lower population diversity. Lower diversity allows STGP to find small solutions once it has a correct solution, but can prevent STGP from initially finding a correct solution. High Tarpeian values allow a larger population size to be sampled from by the genetic operators, which leads to a higher diversity. This is good for allowing a more comprehensive initial search of the search space, but can make it hard for STGP to focus on a small correct solution later on in the runs. This chapter proposes (based on the work of [21]) that a high diversity is required at the start of the run to allow a good set of predictive models to be evolved, and low diversity at the end of the run to find compact predictive models.

There has been previous work (Section 2.6.7) in GP on adaptive diversity [21], and adaptive population size [110]. Ekárt and Németh [21] use a gradient based technique that looks at the ratio of the current and previous best fitness values to adapt their diversity controls. Rochat et al. [110] use an absolute method that looks at the ratio of the current best fitness and the initial best fitness to adapt the population size. The same approach has been taken in this chapter to adapt the Tarpeian value. The approach assumes that how close the current best fitness value is to the optimal fitness value (0), relates to how much Tarpeian bloat control should be applied. When the current best fitness value is a long way from the optimal fitness value a high Tarpeian value should be used to allow STGP to investigate a range of possible solutions. However, when the current best fitness value is close to the optimal value a low Tarpeian value can be used to force STGP to converge on a small correct solution. Equation 7.1 shows the method to automatically adapt the Tarpeian value. The new Tarpeian value $t$ is defined as the ratio of the current best fitness $f_b$ to the initial best fitness $f_i$ multiplied by the initial Tarpeian value $t_{initial}$. In all the experiments the initial Tarpeian value is set to 10. To prevent the Tarpeian value from
going to 1 (which would cause all the predictive models that were above the average size to be removed from the population) it is limited to a minimum value of 2. This method was applied to the datasets from Chapters 4 - 6. The results are shown in the next section.

\[
t = \text{Max} \left( \frac{f_c}{f_i} \cdot t_{\text{initial}}, 2 \right)
\]  

(7.1)

7.3 Results

Figures 7.1 - 7.11 show the results for the adaptive Tarpeian method on the datasets from Chapters 4 - 6. The results show that the adaptive Tarpeian method got accuracy results on all the noisy datasets, and most of the clean datasets that were as good as the best results using a fixed Tarpeian value. It also typically produced predictive models of a size equal to or smaller than the most accurate predictive models using a fixed Tarpeian value.

The results on the PSS datasets (Figure 7.1) show that the method does not get very accurate results for the clean dataset. It is too aggressive, causing it to produce small sized predictive models, with accuracy results that are worse than the most accurate results from using a fixed Tarpeian value. The noise results on the Uno2 datasets (Figure 7.3) show that as the level of noise is increased the method produces predictive models that are larger on average than most accurate predictive models produced using a fixed Tarpeian value. The results on the CCTV datasets (Figure 7.4) show that the accuracy of the method on the clean dataset is lower than the best accuracy using the fixed Tarpeian value. The results on the PYCR datasets (Figure 7.5) are similar to the ones for CCTV. On the clean, and 10% noise datasets it gets the smallest size results, but the accuracy results are worse than the best accuracy results using a fixed Tarpeian value. The CCTV dataset using spatial relations (Figure 7.6) gets a similar accuracy result to using a fixed Tarpeian value, but the average size of the predictive model is larger than the best results from using a fixed Tarpeian value.

The results have highlighted two main issues with the method. Firstly, the method assumes that a very small current best fitness (less than 0.10) means that STGP is very close to finding the correct solution, and consequently a high level of bloat control can be used to reduce the size of the predictive model. However, for the clean PSS and PYCR datasets a very low fitness value does not always mean that STGP is close to finding the correct solution. When the adaptive Tarpeian method is applied to these datasets it incorrectly decreases the Tarpeian value causing a decrease in the diversity of the population causing STGP to prematurely converge on an incomplete solution. Secondly, on the noisy datasets, the noise limits the minimum value for the current best fitness that a
predictive model can achieve. This affects the smallest possible Tarpeian value that the adaptive Tarpeian method can produce. In the later stages of the runs the amount of bloat control is reduced which prevents STGP from finding the smallest possible models. This can be seen, for example, in the results for the Uno2 datasets, and the CCTV with spatial relations dataset.

7.4 Conclusions

The previous chapters has shown that there is no universal fixed Tarpeian value that will work well on all datasets. This chapter has shown an adaptive Tarpeian method which computes the Tarpeian value based on the ratio of the current best fitness to the initial best fitness. The results showed that the method got accuracy results that were as good as the best results using a fixed Tarpeian method, for all the noisy datasets, and most of the clean datasets. There are two main problems with the method. Firstly, it reduces the Tarpeian value too quickly for some of the clean datasets, causing STGP to prematurely converge on an incomplete solution. Secondly, the noise in the datasets affects the method making it unable to produce low Tarpeian values. To solve these problems some form of scaling could be used to convert the ratio between the current best fitness and the initial best fitness into a Tarpeian value. An exponential scale could be used for the clean datasets to allow high Tarpeian values to be still used when the current best fitness has a low value. On the noisy datasets a constant noise value (based on the noise level) could be removed from the ratio to allow it to produce low Tarpeian values.
Figure 7.1: The accuracy and size results for the Auto Tarpeian method on the PSS dataset. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.2: The accuracy and size results for the Auto Tarpeian method on the Uno datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.3: The accuracy and size results for the Auto Tarpeian method on the Uno2 datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.4: The accuracy and size results for the Auto Tarpeian method on the CCTV datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.5: The accuracy and size results for the Auto Tarpeian method on the PYCR datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.6: The accuracy and size results for the Auto Tarpeian method on the CCTV dataset using temporal relations, and the CCTV dataset using spatial relations. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.7: The accuracy and size results for Auto Tarpeian method on the Uno Temporal datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.8: The accuracy and size results for Auto Tarpeian method on the CoFriend and Tic Tac Toe datasets. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.9: The accuracy and size results for the Auto Tarpeian method on the PSS dataset, where the predictive models are using a simple conflict resolver. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.10: The accuracy and size results for the Auto Tarpeian method on the Uno datasets, where the predictive models are using a simple conflict resolver. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Figure 7.11: The accuracy and size results for the Auto Tarpeian method on the Uno2 datasets, where the predictive models are using a simple conflict resolver. The error bars show one standard deviation from the mean. All results were produced by 10 fold cross validation.
Chapter 8

Conclusions

8.1 Summary of the work

This thesis has shown a technique to learn predictive models from spatio-temporal data. In Chapter 3 a frame based [78] representation for the spatio-temporal history data was described. The representation enables a set of entities, and relationships between the entities to be described. Relations and entities can also have properties which can also be represented. Each different type of property, entity or relation requires a definition, which is represented by a class frame. This definition is used to create property, entity or relation instances, which are represented by instance frames. A predictive model is represented by a production system, which contains a set of production rules, and conflict resolver. The production rules describe different possible patterns in the history and their possible future outcomes: Each production rule typically models different parts of the activity being modelled. Production rules contain two sections: a condition section that matches a specific subset of the history; and an action section that represents a new entity or relation. The conflict resolver is a conditional probability distribution represented as a Bayesian Network. It takes as its input a set of enabled production rules, and computes the likelihood that a subset of these production rules will be fired to produce a prediction. The chapter concluded by explaining an inference technique which given a predictive model, and a history will produce a prediction.

Chapter 4 described how a predictive model is learnt from the spatio-temporal history
Chapter 8

Conclusions

data using Spatio-Temporal Genetic Programming (STGP). The chapter described how the predictive models were initially generated, the fitness function, and the genetic operators used. It also explained how the parameters of the conflict resolver are computed. A bloat control technique is used (the Tarpeian method [22]) to control the size of the predictive models. Five datasets were used to evaluate the system. Four were based on the card games: Uno, Papers Scissors Stone and Play your cards right; and one based on people walking along a path.

The method presented in this thesis (STGP) achieved the most accurate results on all the datasets in this chapter in comparison to a set of existing machine learning methods: Progol, Neural Networks, Bayesian Networks, C4.5 and Pe. Progol managed to learn the correct clauses for many of the datasets, but it was unable to apply them in the correct order, which affected both its coverage and accuracy results. When Progol was combined with Pe (a technique to estimate the probability of the clauses when used as a stochastic logic program) it managed to improve Progol’s coverage, but due to clashing clauses it did not often improve its accuracy. Pe must fire all enabled production rules, and the likelihood of a prediction is based on the likelihood of the other predictions. Sometimes an enabled production rule will produce an incorrect prediction when it is fired, which affects Pe’s accuracy. The conflict resolver used by STGP can probabilistically decide which of the enabled production rules to fire. This prevents enabled production rules that produce incorrect predictions from being fired. It was shown that when the clauses learnt by Progol were estimated by the conflict resolver in STGP it improved both their coverage, and accuracy results. Bayesian Networks and C4.5 performed fairly well on the datasets in this chapter, but were limited due to their inability to learn generalised rules from the data. It was shown that STGP produces the best results with: some form of size control on the predictive models; the tournament selection sampling technique using a tournament selection value that favours the better scoring predictive models; and an increased amount of adding and replacement of production rules in the initial 10 generations of the run.

Chapter 5 showed the use of qualitative temporal relations in the predictive models. A novel temporal state relation to relate the time range of an entity or relation instance to the current time was presented. Handcrafted Uno datasets; and real-world and handcrafted CCTV datasets were used for the experiments. Again, STGP produced the most accurate predictive models for all datasets. Progol did not manage to learn clauses complex enough to correctly predict from the training data. Estimating the likelihood of the clauses using Pe did not improve the accuracy of the results. When the likelihood of the clauses were estimated by STGP the coverage, and accuracy of the results were improved except for the noise free CCTV dataset. Again, the inability for Neural Networks, Bayesian Networks,
and C4.5 to generalise from data affected the accuracy of their results. It was shown experimentally that using temporal relations in the predictive models when compared to not using them allowed STGP to be robust to injection noise, and to be slightly more accurate when predicting from scenes containing multiple people. Finally, it was shown that increasing history length used by the predictive models reduced their coverage and accuracy results.

Chapter 6 demonstrated the use of spatio-temporal relations in the condition section of the production rules, and the ability to use relations in the action section of the production rules. The temporal relations were the same as the ones used in Chapter 5. The chapter verified experimentally that predictive models that use spatial relations between objects are robust to spatial noise when compared to predictive models that do not use spatial relations. Three datasets were used for the experiments: CCTV, aircraft turnarounds, and Tic Tac Toe. STGP was shown to have an inefficient technique to evaluate the condition section of the production rules on the history, which had a large impact on its run-time on the Tic Tac Toe and aircraft turnaround datasets. Section 8.4 explains a possible solution to this problem. Progol learnt overly general clauses on the CCTV datasets, and sometimes the clauses it learnt based their predictions on relations occurring in the future. There is no easy way to prevent this from happening, which makes Progol unsuitable for learning from temporal data.

Chapter 7 firstly described an adaptive Tarpeian method which computes the Tarpeian value based on the ratio of the current best fitness to the initial best fitness. The method was evaluated using all the datasets from the previous chapters. The results showed that the method got accuracy results that were as good as the best results using a fixed Tarpeian method, for all the noisy datasets, and most of the clean datasets. The results showed two main problems with the method. Firstly, it reduces the Tarpeian value too quickly for some of the clean datasets, causing STGP to prematurely converge on an incomplete solution. Secondly, the noise in the datasets affects the method making it unable to produce low Tarpeian values. Section 8.4 explains possible solutions to these problems.

8.2 Contributions

The main contributions from this thesis are:

1. A novel predictive model architecture represented as a production system. Each production rule models a separate part of the spatio-temporal data. The conflict resolver (represented as a Bayesian Network) allows the architecture to model non-deterministic data, and to use a set of production rules to make a prediction.
2. A novel temporal relation that relates the time range of an entity or relation instance in the history to the current prediction time.

3. A technique to learn predictive models by Genetic Programming.

4. The use of spatial relations within the condition section of the production rule.

5. Initial work on a technique to adapt the Tarpean bloat value during the run of STGP.

### 8.3 Discussion

Chapter 1 introduced six questions that this thesis has attempted to investigate. This section will show to what extent this thesis has managed to answer them.

**Question 1: Does representing the components of the predictive models using first-order logic, produce more accurate results on non-deterministic spatio-temporal data than using standard machine learning representations?**

In Chapters 4 - 6 experiments were performed on two techniques using first order logic: STGP, and Progol; along with three techniques using standard machine learning representations: Neural Networks, Bayesian Networks, and C4.5. The results showed that STGP, and Progol produced more generalised results than Neural Networks, Bayesian Networks, or C4.5. These can not generalise in many situations and effectively rely on storing common examples and their outcomes. The accuracy results for STGP and Progol (when combined with STGP) were shown to be as good as or better than the accuracy results for Neural Networks, Bayesian Networks and C4.5.

**Question 2: Does using a probabilistic conflict resolver produce more accurate predictive models on non-deterministic spatio-temporal data than other conflict resolution approaches?**

The results from the datasets in Chapters 4 - 6 showed that the simple conflict resolver used by Progol did not produce such good coverage and accuracy results as the probabilistic conflict resolvers used by STGP, and Pe. The clauses learnt by Progol are evaluated in the default manner used in Prolog. This applies the clauses in order until one entails the unseen example. If the clauses are placed in the wrong order Progol will predict incorrectly and the accuracy of its results will be affected (Section 4.10.2). These results can be improved by using Pe and STGP. On all datasets Pe improved the coverage results of
Progol, but did not always improve its accuracy results. This is because Pe must fire all enabled production rules, and the likelihood of a prediction is based on the likelihood of the other predictions. Incorrectly fired production rules will reduce the accuracy of the correct predictions. The probabilistic conflict resolver presented in this thesis can decide, based on a set of enabled production rules, which production rules to fire. This in some cases, significantly improves the accuracy results when compared against the accuracy results from Progol and Pe.

**Question 3: Does using evolutionary search techniques to learn production rules produce more accurate results on non-deterministic spatio-temporal data than using a deterministic (greedy) search?**

STGP uses a genetic programming based approach to learn the production rules. It was shown that for all datasets (except Tic Tac Toe) that STGP produced predictive models which had an accuracy that was the same as, or better than the accuracy for all other methods. Progol is an alternative technique to learn the production rules. It uses a greedy search, but did not get accuracy results (even when combined with the probabilistic conflict resolver presented in this thesis) that were better than STGP. The results on the datasets from Chapters 5 and 6 were often too general, and it shows that Progol did not fully search for good clauses.

**Question 4: Does learning the production rules and the parameters of the conflict resolver simultaneously produce more accurate results on non-deterministic spatio-temporal data than learning them sequentially?**

The results from Chapters 4 - 6 showed that (apart for Tic Tac Toe) STGP was as accurate or more accurate than all other methods. This shows that the combined approach to learning the production rules and the conflict resolver parameters used by STGP was more accurate than the sequential approach of using Progol to learn the production rules, and then using Pe or STGP to estimate the parameters for the conflict resolver. The combined approach allows the learner to use the properties of the conflict resolver as part of the predictive model learning process. This allows the learner to allow different production rules to be enabled at the same time to produce simpler and smaller predictive models as shown in Section 3.3.
Question 5: Does use of qualitative temporal relations within the components of the predictive models make them robust to changes in the temporal structure of the non-deterministic spatio-temporal data?

Section 5.6.1 presented the results of an experiment where predictive models using temporal relations and predictive models not using temporal relations were tested on datasets containing injection noise, and multiple people. Overall the predictive models using temporal relations were not affected by the injection noise; and were more accurate when predicting from the dataset containing multiple people than the predictive models not using temporal relations. This shows that using temporal relations in the predictive models makes them robust to some changes in the temporal structure of the spatio-temporal data.

Question 6: Does use of qualitative spatial relations within the components of the predictive models make them robust to changes in the spatial structure of the non-deterministic spatio-temporal data?

Section 6.4.1 showed results of an experiment where predictive models using, and not using qualitative spatial orientation relations were firstly tested on a clean dataset, and secondly on a dataset where the location of some of the objects was changed. The predictive models that used spatial relations were unaffected by the change in the location of the objects, but the predictive models that did not use spatial relations were affected by this change. This shows that spatial relations are robust to some changes in the spatial structure of the spatio-temporal data. Further work could be done using different spatial relations, and different test datasets containing different forms of spatial noise. The spatial noise could take the form of different types of camera movement like horizontal, vertical, or zooming. It could also take the form of occlusion where parts of the image are hidden.

8.4 Future work

This thesis has highlighted a variety of problems that are potential avenues of future work:

1. Methods could be investigated for improving the speed of STGP in finding a solution and improving the accuracy of the solution. A simplistic method is currently used to vary the type, and probability of genetic operators used during the run. This only allows the genetic operators that operate on the predictive model for the initial \( n \) generations, and then uses genetic operators that operate on both the predictive model and the production rules for the rest of the run. Another approach is to adapt
the operator type, and probabilities during the run. This idea has been successfully applied in the context of GP [91]. Using these techniques within STGP would allow it to use the optimal set of operators during the different stages of the run. This should allow STGP to find more accurate solutions in a reduced amount of generations. This is an easy project and could be done as an undergraduate dissertation.

2. Chapter 7 described a method to automatically adjust the Tarpeian value based on the ratio of the current best fitness to the initial best fitness. The results showed that it did not work for all datasets. The method was affected by noise in the data, and can often reduce the Tarpeian value too quickly on clean datasets. To fix these problems the ratio between the current best fitness and the initial best fitness could be applied to a scaling function to convert it into a Tarpeian value. Work could be performed to see which scaling functions produced the best results on the clean, and noisy datasets. This is an easy project and could be done as an undergraduate dissertation.

3. Currently the condition section of a production rule is created randomly. However, Progol initialises its search for the most general clause by generating and using the most specific clause. This is then used to bound the search. Allowing the condition section to be some variant on the most specific clause could reduce the search space, and make finding a solution faster. This is a harder project and could be done as a masters thesis.

4. It was assumed in this thesis that all the predictions made by the predictive models were for the next time step. In noisy datasets it may not always be the case that the current prediction will happen at the next time step. For example with multiple people in a scene the system might predict that a person will perform a particular action, but before it happens a different person might have already performed an action. Techniques could be investigated that allow STGP to take a series of predictions from a predictive model and decide when each prediction should be applied. This could be used to more accurately predict when future actions might occur. This is a hard project and could be done as a PhD thesis.

5. In all the datasets used in this thesis the entities, relations and their properties have a probability of 1. In the real world the probability of entities, relations and their properties can be less than 1, representing uncertainty in information received the world. For example, a tracking algorithm might use a probability less than 1 for the type of an object when it is unsure of the type it could be classified as. There
has been previous work to learn models based on first order logic where the data is uncertain, for example Markov Logic Networks [106], Stochastic Logic Programs [18], and Bayesian Logic Programs [53]. The ideas from this research could be incorporated into STGP to allow it to learn and predict from uncertain data. This is also a harder project and could be done as a masters thesis.

6. Chapter 6 showed how relations could be used in the action section of the production rule. The relations could use variables from the condition section to represent entities. Section 3.3.1.2 showed in theory how the properties of entities from the history could be used in the action section. This has not been implemented, or experimented on in this thesis. Further work could be done to implement and experiment with this. This would create more generalised production rules, which should help STGP to find a solution faster. It would also allow the predictive models to contain less production rules. This is a harder project and could be done as a masters thesis.

7. Work could be done to apply STGP to more complex domains that have a larger number of objects, and more complex behaviour patterns to learn. This is an open problem and might require a team of researchers to work on it.

8. Work could be done to investigate extra genetic operators that could be used in STGP. This would allow it to find solutions faster, and to better investigate the search space. This is a harder project and could be done as a masters thesis.

9. Chapter 6 highlighted problems with the algorithm to see if the condition section of a production rule was enabled on some history. It was shown to be inefficient when there are large numbers of combinations of relations and entities in the history to check against. Work could be done to investigate alternative algorithms. One potential approach could be to use a Prolog or database search style approach where instead of matching the whole tree against the history sub-trees are matched on the history in turn until an overall match is found. This is an easy project and could be done as an undergraduate dissertation.
Bibliography


