Electrokinetic Migration of Nitrate Through Heterogeneous Granular Porous Media

by Richard T. Gill, Steven F. Thornton, Michael J. Harbottle, and Jonathan W.N. Smith

Abstract

This study investigates and quantifies the influence of physical heterogeneity in granular porous media, represented by materials with different hydraulic conductivity, on the migration of nitrate, used as an amendment to enhance bioremediation, under an electric field. Laboratory experiments were conducted in a bench-scale test cell under a low applied direct current using glass bead and clay mixes and synthetic groundwater to represent ideal conditions. The experiments included bromide tracer tests in homogeneous settings to deduce controls on electrokinetic transport of inorganic solutes in the different materials, and comparison of nitrate migration under homogeneous and heterogeneous scenarios. The results indicate that physical heterogeneity of subsurface materials, represented by a contrast between a higher-hydraulic conductivity and lower-hydraulic conductivity material normal to the direction of the applied electric field exerts the following controls on nitrate migration: (1) a spatial change in nitrate migration rate due to changes in effective ionic mobility and subsequent accumulation of nitrate at the interface between these materials; and (2) a spatial change in the voltage gradient distribution across the hydraulic conductivity contrast, due to the inverse relationship with effective ionic mobility. These factors will contribute to higher mass transport of nitrate through low hydraulic conductivity zones in heterogeneous porous media, relative to homogeneous host materials. Overall electrokinetic migration of amendments such as nitrate can be increased in heterogeneous granular porous media to enhance the in situ bioremediation of organic contaminants present in low hydraulic conductivity zones.

Introduction

The effectiveness of groundwater remediation using hydraulic-based techniques is limited in aquifers and sediments with a hydraulic conductivity ($K$) less than about $10^{-7}$ m/s (Saichek and Reddy 2005a). In low $K$ porous media solute transport may be influenced more by diffusion than advection. This can result in the sequestration of contaminants within low $K$ zones (e.g., clays and silts) in settings characterised by physical heterogeneity (e.g., $K$ contrasts), making them inaccessible to treatments delivered by hydraulic methods, such as amendment injection (Li et al. 2010), or those involving fluid extraction, such as pump and treatment (Lee et al. 2000). The low $K$ zones then function as secondary sources of contaminants, which diffuse back into more permeable zones, prolonging remediation measures (Reynolds and Kueper 2002). Electrokinetics (EK) can initiate different transport phenomena (electroosmosis, electromigration, and electrophoresis) in porous media with hydraulic conductivities as low as $10^{-10}$ m/s (Acar and Alshawabkeh 1993; Reddy and Saichek 2003). Coupling these processes to the delivery of suitable amendments may therefore enhance the treatment of contaminants within low $K$ strata, using techniques such as bioremediation. This can be achieved by overcoming technical barriers for bioremediation (Gill et al. 2014), for example: (1) electromigration or electroosmotic delivery of electron acceptors and nutrients to the contaminant and/or microorganisms to overcome mass transfer limitations (Lohner et al. 2008); (2) increasing the bioaccessible contaminant fraction by enhancing desorption by electroosmotic pore fluid flux (Niqui-Arroyo et al. 2006); and (3) augmenting the indigenous microbial community to enhance species diversity and increase the biodegradation capacity (Mao et al. 2012).

Most studies of EK applications have been conducted in homogeneous rather than heterogeneous materials, although the latter more appropriately represent the subsurface environment. In many cases physical heterogeneity, represented by spatial variability in the distribution and form of materials with different $K$, exerts a significant control on solute transport (Song et al. 2014), contaminant distribution (Rahman et al. 2005) and options for remediation strategies in soils and aquifers (McCray et al. 2011). EK-moderated transport of substances into, and out of, low $K$ zones in a heterogeneous setting can be significantly more effective than advection (Saichek and Reddy 2005b; Reynolds et al. 2008). However, to date there are no empirical studies of the influence of physical heterogeneity on EK transport. Nitrate is often used as an amendment to support the in
Electrokinetic Theory

Electromigration is the most effective transport mechanism to deliver a charged amendment through an electrolyte in an EK-dominated system. Theoretically electromigration can be influenced by the type of host material, insofar as this affects the spatial variation in properties of the porous media which control the applied EK phenomena. For homogeneous conditions the 1-D electromigration solute mass transport equation is given by Equation 1 (Acar and Alshawabkeh 1993):

\[ J_i = C_i (u_i^* - k_e) \frac{\partial E}{\partial x} \]  

(1)

where \( J_i \) is the electromigration solute mass flux (kg/m²/s); \( C_i \) is the solute concentration (kg/m³); \( u_i^* \) is the effective ionic mobility (m²/V/s); \( k_e \) is the electrophoretic permeability (m²/V/s); \( E \) is the electrical potential (V); and \( x \) is distance (m). The effective ionic mobility is analogous to the effective diffusion coefficient (Equation 2):

\[ u_i^* = u_i n \tau = \frac{D_i^* z_i F}{RT} \]  

(2)

where \( n \) is porosity (—); \( \tau \) is tortuosity (—); \( F \) is the Faraday’s constant (C/mol); \( z_i \) is ion valence; \( D_i^* \) is the effective diffusion coefficient (m²/s); \( R \) is the universal gas constant \((J/K/mol)\); and \( T \) is absolute temperature (K). The effective solute diffusion coefficient has been shown to decrease with decreasing \( K \) due to a decrease in the tortuosity factor associated with the migration path length (Rowe and Badv 1996). From this relationship effective ionic mobility should also vary between sand, silts and clays, that is, decreasing with decreasing \( K \). It is also likely that the counter pore fluid flux created by electroosmosis will increase with decreasing \( K \), due to the presence of more fine grained particles with an associated larger surface charge, represented by the zeta potential (\( \zeta \)) (Acar and Alshawabkeh 1993):

\[ q_w = k_e \frac{\partial E}{\partial x} \]  

(3)

\[ k_e = \frac{\zeta n}{\eta} \]  

(4)

where \( q_w \) is the pore fluid flux (m/s); \( \epsilon \) is the permittivity of the porous medium (C²/J/m²); \( \zeta \) is the zeta potential (V); and \( \eta \) is the fluid viscosity (Pa/s). For example, electroosmosis is about five times higher in clays than fine-grained sands with hydraulic conductivities of 1 to 2 × 10⁻⁸ m/s and 3.5 × 10⁻⁸ m/s, respectively (Wu et al. 2007). The electroosmotic flux is generally an order of magnitude lower than electromigration, and therefore electromigration is typically the dominant transport mechanism (Acar and Alshawabkeh 1993).

Under 1-D physically heterogeneous conditions where the porosity and tortuosity of the material vary and therefore the effective mobility varies, there will be step changes in the electromigration velocity. Moreover, there should also be an associated variation in the voltage gradient due to the relationship between effective ionic mobility and effective electrical conductivity (Alshawabkeh and Acar 1996):

\[ \frac{\partial E}{\partial x} = -\frac{I + F \sum_{i=1}^{N} z_i D_i^* \frac{\partial C_i}{\partial x}}{\sigma^*} \]  

(5)

\[ \sigma^* = \sum_{i=1}^{N} F z_i u_i^* C_i \]  

(6)

where \( I \) is current density (C/s/m²); and \( \sigma^* \) is the effective fluid electrical conductivity (S/m).

Thus, in a physically heterogeneous setting where the concentration of chemical species is uniform, the voltage gradient should increase in material with a low effective ionic mobility relative to material with a high effective ionic mobility. This is in contrast to homogeneous systems where, if the effective ionic mobility and chemical species concentration are uniform, the voltage gradient is also uniform.

Materials and Methods

Material Properties

The porous medium was created using soda-lime silica glass beads (Potters Ballotini Ltd, Barnsley, South Yorkshire, UK) and Speswhite kaolin (Imerys Performance Materials Ltd, Par, Cornwall, UK) to represent a model system composed of two materials with consistent properties.
The physical heterogeneity in these experiments is a contrast between high and low $K$, created by positioning layers of appropriate material in the test cell as shown in Figure 1. High hydraulic conductivity (HK) sections were consistently produced using 1.4 mm diameter glass beads, whereas low hydraulic conductivity (LK) sections were produced using a 90/10 mix of 0.25 and 0.5 mm glass beads. Between experiments the glass beads were cleaned with deionised water and autoclaved to minimise biological activity in the tests. Additional $K$ contrasts were achieved by blending the small glass bead mix with different proportions by weight of kaolinite. The clay grain size distribution is 76% to 83% ≤2 µm and introduced a small amount of surface-adherent dissolvable salts (approximately 0.2% by mass of sodium and sulphate ions based on dissolution tests) into the test fluids.

Consolidation of glass beads in preparation for tests was achieved using a small shaker table at a frequency of 31 Hz and calibrated using a hand-held accelerometer. The test cells were filled with material in layers up to 3 cm and placed on the shaker table for intervals of 20 s. This was repeated until the test cell was full, excess material removed and the lid secured. The glass bead mix and clay was added together and combined with sterilised synthetic groundwater to give a mass equivalent to the clay’s plastic limit (approximately 30% by weight of the clay). This was to facilitate mixing and aid compaction. The mixture was then wet packed into the sediment chamber in the test cell (Figure 1) and tamped on the shaker table for intervals of 20 s. This was repeated that at each time point the total fluid extracted was <1%.

Samples of the pore fluid for chemical analysis were taken every 2 to 4 days during the experiment via a narrow bore (ID = 0.5 mm) PEEK tubes located along the length of the test chamber. The sampling tubes extended normal from the edge into the centre of the sediment mass within the test chamber and were offset to each other on either side of chamber. This ensured that any edge effects from the chamber panels on fluid sampling were avoided and that the centreline of the fluid flow path could be sampled in detail. Sample tube blockages were prevented by fitting a small cube of porous sintered glass to the end of each tube. At each time point seven samples of the pore fluid in the sediment chamber and one sample from each electrode chamber were taken. Each pore fluid sample was 1 mL to ensure that at each time point the total fluid extracted was <1% of the total pore fluid volume, with minimal disturbance.

Figure 1. Schematic of experimental set-up used in tests. Sediment chamber volume: 7.5 L; and electrode chamber 2 L. HK and LK represent the high and low $K$ contrasts in the sediment, X and O represent sampling and voltage probe ports.
Five voltage probes consisting of 4 mm diameter grade 316 stainless steel rods housed in HDPE piping were fitted within the chamber. Voltages and current were logged every 24 h or after sampling during the tests. The dimensions of the HK and LK sections were H:125 × W:125 × L:280 mm and H:125 × W:125 × L:210 mm, respectively; the difference accommodates the distribution of sample and voltage probe ports (Figure 1).

Nitrate was selected as it is a representative amendment used extensively in electrokinetic-bioremediation studies (Gill et al. 2014). Bromide was used as a tracer under an electric field because it is chemically conservative and has similar electromigration transport properties to nitrate. Amendments were added to the cathode at a rate 1.5 mL/min from a 10-L reservoir tank maintained at a constant concentration of either nitrate or bromide solutions. The reservoir tank was topped up at regular intervals.

Electrokinetic Apparatus and Test Conditions

A direct current was applied at a constant current strength of 25 mA (1.6 A/m<sup>2</sup>) to allow more effective control of pH changes at the electrodes. Electrodes were made from a 125 × 125 × 10 mm graphite block perforated with 8 mm diameter holes to allow passage of water, using the method described by Harbottle et al. (2009). The connection between the graphite electrodes and copper wires to the DC power source was housed inside the electrodes and secured in place with a threaded seal and silicone sealant to give a water-tight seal. This also reduced the risk of contaminating the electrode chambers by metal corrosion.

A peristaltic pump (Ismatec, Mondfeld, Wertheim, Germany, Ecoline VC-MS/CA 8-6) was used to circulate acid and base solutions (1 M HCl and NaOH) to the cathode and anode, respectively, to neutralise electrolysis reactions as follows:

\[ 2\text{H}_2\text{O} - 4e^- \rightarrow 4\text{H}^+ + \text{O}_2 \]  \hspace{1cm} (7)

\[ 4\text{H}_2\text{O} + 4e^- \rightarrow 4\text{OH}^- + 2\text{H}_2 \]  \hspace{1cm} (8)

The rate of acid (H<sup>+</sup>) and base (OH<sup>−</sup>) generation can be estimated assuming steady-state electrolysis and 100% Faradaic efficiency at the electrode (Kim and Han 2003):

\[ \text{Rate} = \frac{\text{Current}}{2.2 	imes 10^4 (\text{±} 2.1 	imes 10^4)} \]  \hspace{1cm} (9)

where \( R_{\text{H}^+} \) is the rate of H<sup>+</sup> (or OH<sup>−</sup>) generated (mol/s). These values were used to determine the volume of acid or base that would be required over a certain time period to neutralise electrolysis reactions, dosing being controlled by a timer and applied every 3 h. In experiments where electroosmotic flow was evident a Mariotte bottle was used to ensure that the anode compartment was not depleted of water and no hydraulic gradient developed.

Experimental Design

Two types of experiments were undertaken: (1) bromide tracer tests to determine the effective ionic mobility of the materials used in the HK and LK sections; and (2) nitrate migration experiments under homogeneous and heterogeneous conditions, based on the arrangement of materials used in the respective tests. Bromide tracer experiments were run under homogeneous conditions using the same material specifications used in the nitrate migration experiments (Table 1). Bromide was added at 1 g-Br/L concentration in the reservoir tanks, with fluid samples and voltage readings taken every 24 h. Nitrate migration experiments

**Table 1**

<table>
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<th>Name</th>
<th>EK Properties</th>
<th>Reservoir Tank Properties</th>
<th>HK Properties</th>
<th>LK Properties/HOM Properties</th>
<th>Clay (%)</th>
<th>( K^2 ) (m/s)</th>
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<td>2.2 × 10&lt;sup&gt;4&lt;/sup&gt; (± 2.1 × 10&lt;sup&gt;4&lt;/sup&gt;)</td>
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<td>2.2 × 10&lt;sup&gt;4&lt;/sup&gt; (± 2.1 × 10&lt;sup&gt;4&lt;/sup&gt;)</td>
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<td>4.5 × 10&lt;sup&gt;9&lt;/sup&gt; (1.1 × 10&lt;sup&gt;9&lt;/sup&gt;)</td>
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<sup>1</sup>Averaged value.

<sup>2</sup>Falling head permeameter tests.
were run at low- and high-nitrate inlet concentrations of 0.1 and 1 g-NO₃/L, respectively. At low concentration nitrate migration was compared under heterogeneous and homogeneous conditions, whereas at high concentration nitrate migration was evaluated for increasing K contrasts (Table 1). Two control experiments with no nitrate and no direct current (Control_1 and Control_2, respectively) were also performed. The experimental results were interpreted according to theoretical predictions using numerical analysis of nitrate breakthrough at the anode (Equation 1) and proportion of the voltage gradient distributed across HK and LK sections based on major ion analysis (Equations 5 and 6). Replicates were run for experiments with low nitrate inlet concentration, HET_1, HOM, and high inlet concentration, HET_2. Experimental reproducibility is inferred from tests with one or more replicates. All experiments were run with pH control to eliminate the influence of acid and base fronts on the voltage gradient (Lohner et al. 2008).

### Results and Discussion

#### Bromide Electromigration under Homogeneous Conditions

Tracer experiments were conducted using bromide to determine the effective ionic mobility of nitrate for the different materials evaluated in the nitrate migration experiments. This is justified as bromide has similar transport properties to nitrate under an electric field, for example both have similar ionic mobility at infinite dilution (bromide: 8.1 × 10⁻⁸ m²/s/V; nitrate: 7.4 × 10⁻⁸ m²/s/V; CRC 2002). A tortuosity factor for the host material was estimated from the effective ionic mobility of bromide to deduce the effective ionic mobility of nitrate (Equation 2).

Results from the bromide tracer experiments at steady-state are shown in Table 2. Steady-state in these experiments is the point at which nitrate breaks through to the anode and the mass transport normalised to the voltage gradient stops increasing. Mass transport is defined as the mass of bromide that passed through the sediment over time, normalised to the voltage gradient. The mass flux and effective ionic mobility can be determined from this value by re-arranging Equation 1. The tortuosity factor reflects the path length that ions must take through the sediment, in porous media it is always less than one and decreases as the tortuosity of the flow path increases (Fetter 1993); it is calculated by rearranging Equation 2. The migration velocity is the distance across the sediment chamber divided by the time bromide is first observed in the anode chamber and is normalised to the voltage gradient.

Values for mass transport, effective ionic mobility and migration velocity all decrease with decreasing K (Table 2), with the exception of values for Tracer_1 which are slightly lower than Tracer_2. K and the effective ionic mobility have no direct relationship, as both reflect the porous material used. Results from these experiments demonstrate that these two parameters can be indirectly related by the tortuosity factor, which decreases in fine grained sediments (Rowe and Badv 1996). Thus, as K decreases the effective ionic mobility also decreases. For example, as clay content increases between Tracer_2 and Tracer_5 there is greater occlusion of the pore spaces between the larger glass beads, which impedes solute migration. The effective ionic mobility estimated for nitrate in the different materials is similar in trend to, but slightly lower than, the bromide results due to the differences in ionic mobility value at infinite dilution (Table 2). This range of values is lower than those reported for pure kaolinite (1.55 to 1.65 × 10⁻⁸ m²/V/s), which has high porosity and tortuosity values (0.6 and 0.35, respectively) (Acar and Alshawabkeh 1993; Thevanayagam & Rishindran 1998).

Electromigration of negative species such as bromide and nitrate towards the anode can be hindered by a counter electroosmotic flow in fine-grained material with a high

### Table 2

#### Bromide Transport Properties at Steady-State Estimated from Tracer Tests

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Bromide Mass Transport [m/s/(V/m)]</th>
<th>Bromide Effective Ionic Mobility [m²/V/s]</th>
<th>Tortuosity Factor (−)</th>
<th>Migration Velocity [m/s/(V/m)]</th>
<th>Nitrate Effective Ionic Mobility [m²/V/s]</th>
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<tr>
<td>Tracer_1</td>
<td>7.0 × 10⁻⁶ (± 3.5 × 10⁻⁶)</td>
<td>1.4 × 10⁻⁴ (± 1.1 × 10⁻⁴)</td>
<td>0.56 (± 0.04)</td>
<td>6.3 × 10⁻⁴</td>
<td>1.3 × 10⁻⁸ (± 1.0 × 10⁻⁸)</td>
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<tr>
<td>Tracer_2</td>
<td>7.9 × 10⁻⁶ (± 7.5 × 10⁻⁶)</td>
<td>1.5 × 10⁻⁴ (± 1.6 × 10⁻⁴)</td>
<td>0.55 (± 0.06)</td>
<td>5.0 × 10⁻⁴</td>
<td>1.4 × 10⁻⁸ (± 1.5 × 10⁻⁸)</td>
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<td>1.1 × 10⁻⁴ (± 1.5 × 10⁻⁴)</td>
<td>0.47 (± 0.06)</td>
<td>4.1 × 10⁻⁴</td>
<td>1.0 × 10⁻⁸ (± 1.3 × 10⁻⁸)</td>
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<td>4.5 × 10⁻⁵ (± 4.4 × 10⁻⁶)</td>
<td>8.2 × 10⁻⁹ (± 7.5 × 10⁻¹⁰)</td>
<td>0.30 (± 0.03)</td>
<td>4.4 × 10⁻⁴</td>
<td>7.5 × 10⁻⁸ (± 6.9 × 10⁻¹⁰)</td>
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<td>Tracer_5</td>
<td>2.5 × 10⁻⁵ (± 1.2 × 10⁻⁷)</td>
<td>7.2 × 10⁻⁹ (± 5.4 × 10⁻¹¹)</td>
<td>0.22 (± 0.002)</td>
<td>1.5 × 10⁻⁴</td>
<td>6.5 × 10⁻⁸ (± 4.9 × 10⁻¹¹)</td>
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</table>

Mass transport and migration velocity are normalised against the voltage gradient. The error represents one standard deviation from the mean of values obtained once the experiment has reached steady-state.
surface charge (Acar and Alshawabkeh 1993). Other authors have noted this phenomena, whereby a negatively charged ion migrates faster through sands than clays due to the presence of counter electroosmotic flow (Acar et al. 1997; Wu et al. 2007). In these experiments electroosmotic flow was only observed in Tracer_5, with a 20% clay content (electroosmotic permeability: $2.7 \times 10^{-9} \pm (3.6 \times 10^{-10})$ m²/V/s) because all systems are run at constant current where the voltage gradient decreases over time. Under these conditions the ratio between electromigration and electroosmosis increases over time and the influence of electroosmotic flow decreases (Acar and Alshawabkeh 1993).

Nitrate Electromigration under Heterogeneous Conditions

Observed and calculated values for nitrate breakthrough at the anode in experiments HET_1, HOM and HET_2 are shown in Figure 2. HET_1 and HOM experiments were run at an inlet concentration of 0.1 g/L under heterogeneous and homogeneous configurations, whereas HET_2 is the same heterogeneous configuration to HET_1 but with an inlet concentration of 1 g/L. Results in Figure 2 are normalised to the starting inlet concentration and the voltage gradient across the length of the sediment section. Calculated values for the HOM experiment were obtained using Equation 1 for 1-D electromigration, whereas values for heterogeneous experiments can be calculated by modifying this equation to account for migration through the HK and LK sections:

$$J_{HK} = C_{Cathode}^* u_{HK}^* \frac{\partial E_{HK}}{\partial x_{HK}}$$ (10)

$$J_{LK} = C_{HK}^* u_{LK}^* \frac{\partial E_{LK}}{\partial x_{LK}}$$ (11)

where $J_{HK}$ and $J_{LK}$ are the mass flux across the HK and LK sections, $C_{Cathode}$ and $C_{HK}$ are the concentrations in the cathode compartment and HK section; $x_{HK}$ and $x_{LK}$ are the distances across the sections; and $E_{HK}$ and $E_{LK}$ are the electrical potentials across the different sections. Equation 10 represents the mass flux of nitrate from the cathode into the HK section accounting for the effective ionic mobility of the material and voltage gradient across that section. Equation 11 incorporates the same variables for the LK section but uses the nitrate concentration within the HK section calculated from the mass flux in Equation 10. Calculated values are derived from the effective ionic mobility determined in the bromide tracer experiments, observed voltage gradient and inlet nitrate concentration values (either 0.1 or 1 g/L). This method was used to calculate the nitrate concentration at the anode over time. Good agreement between the observed and calculated values shows that the observed experimental values conform to applicable EK theory (Figure 2).

The observed nitrate breakthrough for HET_1 is higher than HOM and HET_2 after 100 h, relative to the inlet concentration and voltage gradient (Figure 2). A good match between observed and calculated datasets shows that this is due to a higher voltage gradient across the HK section in HET_1 (Figure 3A). This allows more nitrate to enter the sediment section from the cathode and increase the proportion passed through the LK section, relative to HOM and HET_2.

![Figure 2](image2.png)

Figure 2. Nitrate breakthrough at the anode normalised to inlet concentration and voltage gradient across the sediment section for experiments HET_1, HOM and HET_2. Dots and dashed lines represent the observed and calculated values, respectively. Error bars represent one standard deviation from the mean; error associated with the calculated values is within the same range for observed values.

![Figure 3A](image3A.png)

(b) Effective Electrical Conductivity (S/m)

![Figure 3B](image3B.png)

Figure 3. (A) Proportion of voltage gradient across the HK section for HET_1, Control_1 and HET_2 and the equivalent section in the HOM experiment. (B) Effective electrical conductivity for the HK and LK sections in HET_1 and Control_1 calculated using Equation 6 and the ionic composition of the pore fluid from sample ports in the respective sections. Error bars for values from experiments HET_1 and HET_2 represent one standard deviation from the mean between replicates.
The increased voltage gradient across the HK section in HET_1 can be attributed to several factors. Firstly, the effective ionic mobility has an inverse relationship with the voltage gradient (Equations 5 and 6). In these experiments the effective ionic mobility is slightly lower in the HK section compared with the LK section (Table 2). Therefore, there should be an elevated voltage gradient across the HK section, which is evident for both HET_1 and Control_1 in Figure 3A. This phenomena is the likely cause for the divergence in effective electrical conductivity between the HK and LK sections of HET_1 and Control_1 in Figure 3B. Ions will move faster through the HK section where the voltage gradient is highest but accumulate in the LK section where it decreases and electromigration rate subsequently falls. Li et al. (2013) noted similar phenomena when investigating the influence of bands with a high associated electrical conductivity within a homogeneous soil. They found that the associated decrease in the voltage gradient caused the electromigration rate to fall. Over time these bands dissipated due to chemical diffusion, but in physically heterogeneous settings the contrast in migration rates could establish a permanent change in the voltage gradient.

Secondly, between HET_1 and HET_2 nitrate accounts for different proportions of the total electrolyte. Based on Equation 6 and accounting for the major ions in the electrolyte, nitrate in HET_1 is 3.4% (± 0.4%) when added at 0.1 g/L compared with HET_2, where it accounts for 22.8% (± 2.3%) when added at 1 g/L. Therefore nitrate should have a greater effect on the voltage gradient in HET_2 compared with HET_1. This is observed in Figure 3A, where the voltage gradient across the HK system dips for HET_2 over the first 100 h due to nitrate entering the system and increasing the electrical conductivity of the electrolyte in that zone. This phenomena is noted by Wu et al. (2012a), who found that increasing the concentration of the amendment in homogeneous settings increased the depression in the voltage gradient adjacent to the cathode and thus reduced the relative amount of amendment that migrated into the material.

Nitrate Electromigration under an Increasing Hydraulic Conductivity Contrast

Experiments HET_2 to HET_5 quantify the effect of an increasing contrast in the $K$ between two host materials on the electromigration of nitrate through them. The transport properties of nitrate through HK and LK sections of the sediment are in broad agreement with the bromide tracer results from homogeneous settings (Table 3). For example, the range in HK mass transport and migration velocity values (except HET_5) are equivalent to Tracer_1 and the trend in decreasing mass transport and migration velocity between Tracer_2 to Tracer_5 is repeated in the LK results. In addition, electroosmotic flow is observed in HET_5 that originates in the LK section and transfers through the HK section, contributing to the relatively low mass transport value; migration velocity is not restricted because nitrate was detected in the LK section after 24 h. However mass transport estimates are either equivalent to, or higher in, the LK section compared with the relevant bromide tracer experiment. This results from the influence of the voltage gradient on the heterogeneous setting.

Furthermore, nitrate concentration in the HK section increases as the ratio between HK/LK sections increases (Figure 4). This is due to a reduction in electromigration rates from the HK to LK sections. The range of values for steady-state concentrations under homogeneous conditions are shown as dotted lines and show the expected conditions without the associated influences of a heterogeneous system. These are calculated using the method in Wu et al. (2012a), applying the bromide mass transport values from experiment Tracer_1 (Table 2). Results for HET_2 are closest to the steady-state nitrate concentration because the HK and LK effective ionic mobility values are closest. Conversely, HET_5 values are furthest from steady-state due to the combined effect of a low associated effective ionic mobility in the HK section and counter electroosmotic flow, which hinders nitrate migration.

Influence of Increasing Hydraulic Conductivity Contrasts on the Voltage Gradient

EK-driven mass transport increases in heterogeneous relative to homogeneous systems (Tables 2 and 3), for example the mass transport for HET_4 is $7.4 \times 10^{-5}$ (± 1.1 $\times 10^{-5}$) compared with $4.5 \times 10^{-5}$ (± 4.4 $\times 10^{-6}$) (mg/s)/(V/m) in equivalent material for Tracer_4. This is because in heterogeneous settings the voltage gradient is higher across the zone with a low effective ionic mobility compared with a homogeneous setting where the voltage gradient is more

Table 3

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Mass Transport [(m/s)/(V/m)]</th>
<th>Migration Velocity [(m/s)/(V/m)]</th>
<th>HK Transport Properties</th>
<th>Mass Transport [(m/s)/(V/m)]</th>
<th>Migration Velocity [(m/s)/(V/m)]</th>
<th>Mass Transport [(m/s)/(V/m)]</th>
<th>Migration Velocity [(m/s)/(V/m)]</th>
<th>Electroosmotic Permeability (m²/V/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HET_2A</td>
<td>$8.4 \times 10^{-5}$ (± 1.4 $\times 10^{-5}$)</td>
<td>$4.6 \times 10^{-4}$</td>
<td></td>
<td>HET_5</td>
<td>$3.8 \times 10^{-5}$ (± 7.3 $\times 10^{-5}$)</td>
<td>$5.3 \times 10^{-4}$</td>
<td>$1.3 \times 10^{-4}$</td>
<td>$3.8 \times 10^{-5}$ (± 6.4 $\times 10^{-11}$)</td>
</tr>
<tr>
<td>HET_2B</td>
<td>$8.6 \times 10^{-5}$ (± 1.9 $\times 10^{-5}$)</td>
<td>$6.4 \times 10^{-4}$</td>
<td></td>
<td></td>
<td>$9.3 \times 10^{-5}$ (± 2.0 $\times 10^{-5}$)</td>
<td>$4.6 \times 10^{-4}$</td>
<td>$8.6 \times 10^{-5}$ (± 1.3 $\times 10^{-5}$)</td>
<td>$3.0 \times 10^{-4}$</td>
</tr>
<tr>
<td>HET_3</td>
<td>$9.3 \times 10^{-5}$ (± 2.0 $\times 10^{-5}$)</td>
<td>$4.6 \times 10^{-4}$</td>
<td></td>
<td></td>
<td>$4.7 \times 10^{-4}$</td>
<td>$7.4 \times 10^{-5}$ (± 1.1 $\times 10^{-5}$)</td>
<td>$3.8 \times 10^{-5}$ (± 3.4 $\times 10^{-5}$)</td>
<td>$3.8 \times 10^{-5}$ (± 6.4 $\times 10^{-11}$)</td>
</tr>
<tr>
<td>HET_4</td>
<td>$1.0 \times 10^{-4}$ (± 1.4 $\times 10^{-4}$)</td>
<td>$4.7 \times 10^{-4}$</td>
<td></td>
<td></td>
<td>$3.8 \times 10^{-5}$ (± 7.3 $\times 10^{-5}$)</td>
<td>$5.3 \times 10^{-4}$</td>
<td>$1.3 \times 10^{-4}$</td>
<td>$3.8 \times 10^{-5}$ (± 6.4 $\times 10^{-11}$)</td>
</tr>
<tr>
<td>HET_5</td>
<td>$5.8 \times 10^{-5}$ (± 2.5 $\times 10^{-5}$)</td>
<td>$5.3 \times 10^{-4}$</td>
<td></td>
<td></td>
<td>$3.8 \times 10^{-5}$ (± 7.3 $\times 10^{-5}$)</td>
<td>$3.8 \times 10^{-5}$ (± 7.3 $\times 10^{-5}$)</td>
<td>$3.8 \times 10^{-5}$ (± 10^{-5})</td>
<td>$3.8 \times 10^{-5}$ (± 6.4 $\times 10^{-11}$)</td>
</tr>
</tbody>
</table>

The error represents one standard deviation from the mean of values obtained once the experiment has reached steady-state. Both replicates for HET_2 are shown.
These experiments show that increasing the $K$ and associated effective ionic mobility contrast increases the difference in voltage gradient between the HK and LK sections (Table 4). In experiments with a low effective ionic mobility contrast (HET_2) the observed voltage gradient is distributed evenly, that is, there is little change in the voltage gradient across the HK and LK zones relative to a uniform voltage gradient. At higher $K$ contrasts there is a difference of up to 30% relative to a fixed voltage gradient (HET_5).

The factors controlling this difference can be identified from Equations 5 and 6 as the spatial change in effective ionic mobility and subsequent spatial change in the effective electrical conductivity. Additionally, the spatial change in migration rates resulting from changes in the effective ionic mobility will influence the distribution of ions within the system.

A comparison of the major ion concentrations in the electrolyte (nitrate, chloride, sulphate, sodium and potassium) across two different $K$ contrasts highlights the complex interactions between the effective ionic mobility and the voltage gradient in heterogeneous settings (Figure 5). In experiment HET_2 there is minimal difference between the total ion concentration and voltage gradient (Figure 5A). However, in HET_4 there is a higher total ion concentration in the LK zone compared with the HK zone (Figure 5B). Assuming uniform effective ionic mobility (and according to Equation 5) this should be reflected by a higher voltage gradient across the HK section relative to the LK section because there is a lower concentration and therefore a lower electrical conductivity. However, the opposite is observed due to the difference in effective ionic mobility. This demonstrates that under heterogeneous conditions where ionic mobility varies spatially there will be associated changes in the voltage gradient.

**Experiment Mass Balance**

As a quality control check on the operation of the experiments a mass balance for nitrate was undertaken, by comparing the mass of nitrate recovered at the end of the experiment with the known input (Table 5). The amount of amendment recovered (80% to 90%) is similar to that found in other electrokinetic transport experiments (73% to 106%) (Wu et al. 2007; Lohner et al. 2008). Every effort was made to minimise the loss of nitrate via biological processes.
Implications for Field-Scale Application

This study demonstrates that electrokinetic phenomena can enhance the transfer of amendments across a permeability boundary. The important implication for field applications is the observation that LK zones cause an increase in the voltage gradient across that zone. Scaling up these findings requires consideration of several factors shown in Figure 6. This scenario assumes that the contamination is localised within the LK zone and an amendment is added at the cathode and migrated towards the anode. It is representative of scenarios where EK is applied to a heterogeneous subsurface.

Physical heterogeneity will directly affect the choice of electrode configuration, as this influences the electric field. There are numerous types of electrode configuration, the two considered here are unidirectional (shown in Figure 6) and radial arrangements. Under a unidirectional configuration with a simple K contrast at the field-scale, similar phenomena to those observed in these experiments will occur.

However, if the variety and orientation of LK zones varies there will be corresponding perturbations to the applied electric field. A nonlinear electric field results in nonlinear ion flow paths, decreasing migration rates between electrodes (Segall and Bruell 1992). A radial configuration consists of a central electrode surrounded by electrodes of the opposite polarity. In these settings the voltage gradient tends to be highest adjacent to the central electrode (Alshawabkeh et al. 1999). This could be enhanced in heterogeneous settings by placing this central electrode within a LK zone and the surrounding electrodes within the HK host material. An increase in the spacing between the anode and cathode results in higher predicted energy expenditure and remediation times (Alshawabkeh et al. 1999). In the experiments in this paper, heterogeneity affected the voltage gradient in a consistent manner, indicating that the influence of heterogeneity will be independent of the spacing between electrodes.

Selecting the right amendment concentration for a treatment requires consideration of several factors and the trade-offs between them. If amendment concentration is too high, migration will stall adjacent to the electrode (Wu et al. 2012a), however, if it is too low insufficient amendment mass will be delivered to the contaminated zone (Rabbi et al. 2000). Experiments in this paper demonstrate that, under heterogeneous conditions, the voltage gradient is highest across the LK zone in a system with a high K contrast. If amendments were added into these LK zones via electrode or amendment wells, the higher voltage gradient would counter the effect of the voltage gradient drop associated with adding high amendment concentrations. Thus, a higher amendment mass flux into the sediment could be maintained compared to a homogenous setting. For example, in clay an amendment concentration equivalent to 0.2 S/m at an electrode spacing of 1 m results in a 60% drop in the voltage gradient next to the cathode compared to a system where the voltage gradient is fixed (Wu et al. 2012a). Assuming a system where 100 V is applied between electrodes 1 m apart and homogeneous conditions where voltage is distributed uniformly the inlet voltage gradient decreases from 100 V/m to 40 V/m. In a heterogeneous setting where an increase of 30% relative to a fixed voltage gradient is observed across a LK zone equivalent to half the sediment section (Table 4), the voltage gradient would drop from 130 V/m to 52 V/m.

The type of K contrast will influence the effect on the voltage gradient. For example, a graduated contrast from LK to HK could cause a step-like increase in the voltage gradient. Alternatively a HK-LK-HK contrast as in Figure 6 would create an increase in the voltage gradient specifically over the LK zone. Furthermore, it is important to maximise current density against the surface area of the LK zone to enhance mass flux perpendicular to the electric field and increase treatment efficiency. For example, in Figure 6 the LK zone is normal to the direction of the electric field, exposing a large surface area to the amendment flux. However, in scenarios with multiple, narrow, LK (e.g., clay) lenses the treatment efficiency may drop because less amendment reaches the target location, with implications for treatment costs (Wu et al. 2012b).

### Table 5
Nitrate Mass Balance at the End of the Experiment Run for HET_2 to HET_5

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Mass In (mg)</th>
<th>Mass Recovered (mg)</th>
<th>Recovery (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HET_2A</td>
<td>4984</td>
<td>4422</td>
<td>89</td>
</tr>
<tr>
<td>HET_2B</td>
<td>4582</td>
<td>4119</td>
<td>90</td>
</tr>
<tr>
<td>HET_3</td>
<td>5907</td>
<td>5271</td>
<td>89</td>
</tr>
<tr>
<td>HET_4</td>
<td>6536</td>
<td>5215</td>
<td>80</td>
</tr>
<tr>
<td>HET_5</td>
<td>4644</td>
<td>4067</td>
<td>88</td>
</tr>
</tbody>
</table>

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An advective flow field will also have an important control on the configuration of an EK field setup. Advection will be more dominant in HK material, whereas EK will be more important in LK material. For example, calculated advective bromide mass flux (hydraulic gradient: 0.1; concentration: 1 g/L) in HK and LK materials is $2.2 \times 10^{-2}$ and $4.5 \times 10^{-7}$ g/m²/s, respectively, compared with an observed bromide electromigration mass flux in HK and LK material of $1.2 \times 10^{-4}$ and $7.4 \times 10^{-7}$ g/m²/s, respectively. In HK material solute transport by EK cannot easily override advection in the opposite direction (Eid et al. 1999). However, for treatments to be effective in scenarios such as Figure 6, an amendment must first migrate through the HK section to reach the target LK zone. The solution is to position the electric field so that it complements the existing advective flow field (as shown in Figure 6), or place the amendment injection well/ electrode within the LK zone, thus eliminating the influence of the advective flow field.

Conclusions

Physical heterogeneity in granular porous media, represented by a $K$ contrast, exerts an important influence on the migration, under an electric field, of nitrate used as an amendment for bioremediation. In heterogeneous settings $K$ contrasts reflect a spatial change in the effective ionic mobility, with subsequent control on the migration rate of an amendment and the distribution of the voltage gradient. The spatial change in migration rate leads to an accumulation of the amendment at the interface between high- and low-$K$ zones, relative to the steady-state concentration. Moreover, in heterogeneous settings the voltage gradient is highest in zones where the effective ionic mobility is lowest. This leads to higher mass transport in LK zones within a heterogeneous setting relative to the same material in a homogeneous setting.

Overall these results show that EK application in heterogeneous settings is controlled by the same mechanisms in homogeneous settings, but that the distribution in amendment migration rates and voltage gradient vary relative to the change in the effective ionic mobility. These phenomena can be manipulated at the field-scale to either establish a high voltage gradient across the inlet zone, to increase the mass of amendment that enters the system, or ensure that a high voltage gradient is established across the zone targeted for bioremediation, to enhance biodegradation in situ. Thus, EK is not restricted in the heterogeneous configurations investigated in this study. Further work on the effectiveness of EK in heterogeneous systems should consider more complex heterogeneous configurations and attempt to quantify the effect of resulting non-uniform electric fields on amendment migration. In addition, EK experiments examining physical heterogeneity should be extended to include other variables, such as microorganisms for contaminant biodegradation, to determine their mobility under EK.

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References


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